

Luminosity measurement at muon collider

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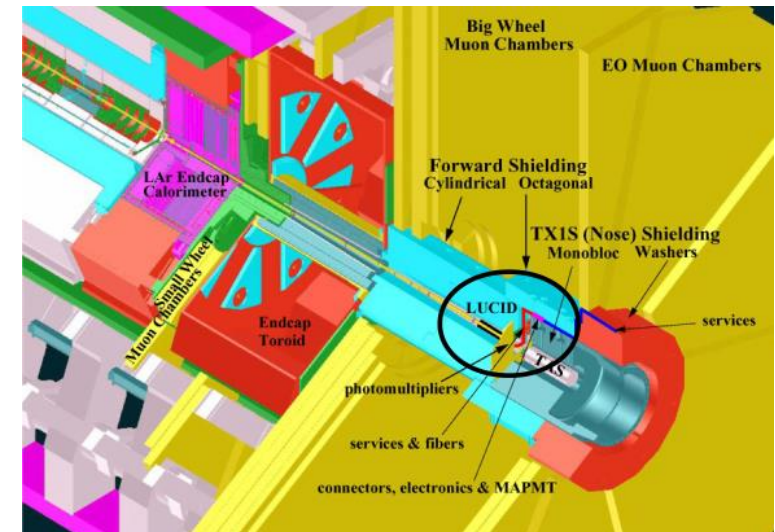
Luminosity Measurements: method 1

- Precise determination of the integrated luminosity target uncertainty is of crucial importance for any physics cross section measurement. In a two beams collider

$$L = \frac{N_1 \cdot N_2 \cdot f \cdot n_b}{A_{eff}}$$

n_b : number of colliding bunches, f : revolution frequency in the collider → known by the machine
 N_1, N_2 : average number of particle per bunch, A_{eff} : effective area of the luminous region → to be measured

- Dedicated detectors, luminometers, are used in combination to “van der Meer” scan method to determine N_1, N_2 and A_{eff} . For example ATLAS

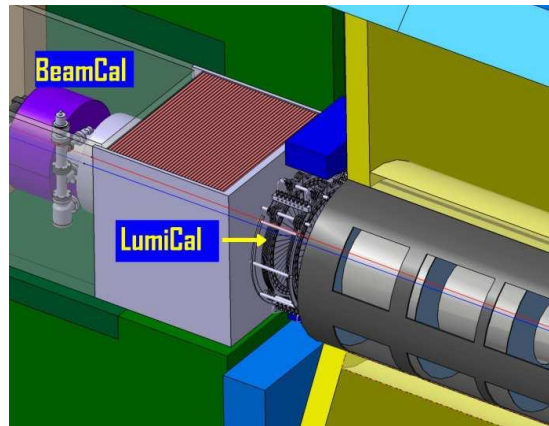


Luminosity Measurements: method 2 at e^+e^-

Experiments like KLOE, Babar, Belle, BES and, recently, Belle2 and BESIII, measure the integrated luminosity by counting the number of events, N , of a process whose cross-section is theoretically known with high precision, σ_{th} exploiting: $N=L\cdot\sigma_{th}$

The mostly used process: Bhabha scattering, $e^+e^- \rightarrow e^+e^-$ mainly in the forward region.

ILC and CLIC have dedicated detector in the forward regions to reconstruct e^+e^- pairs



Source of uncertainty	DL/L (500 GeV)	DL/L (1 TeV)
Bhabha cross-section S_B	$5.4 \cdot 10^{-4}$	$5.4 \cdot 10^{-4}$
Polar angle resolution S_q	$1.6 \cdot 10^{-4}$	$1.6 \cdot 10^{-4}$
Bias of polar angle D_q	$1.6 \cdot 10^{-4}$	$1.6 \cdot 10^{-4}$
IP lateral position uncertainty	$1 \cdot 10^{-4}$	$1 \cdot 10^{-4}$
Energy resolution a_{res}	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$
Energy scale	$1.0 \cdot 10^{-3}$	$1.0 \cdot 10^{-3}$
Beam polarization	$1.9 \cdot 10^{-4}$	$1.9 \cdot 10^{-4}$
Physics background B/S	$2.2 \cdot 10^{-3}$	$0.8 \cdot 10^{-3}$
Beamstrahlung + ISR ¹	$-1.1 \cdot 10^{-3}$	$-0.7 \cdot 10^{-3}$
Beamstrahlung + ISR ²	$0.4 \cdot 10^{-3}$	$0.7 \cdot 10^{-3}$
EMD ¹	$-2.4 \cdot 10^{-3}$	$-1.1 \cdot 10^{-3}$
EMD ²	$0.5 \cdot 10^{-3}$	$0.2 \cdot 10^{-3}$
$(DL/L)^1$	$4.3 \cdot 10^{-3}$	$2.3 \cdot 10^{-3}$
$(DL/L)^2$	$2.6 \cdot 10^{-3}$	$1.6 \cdot 10^{-3}$

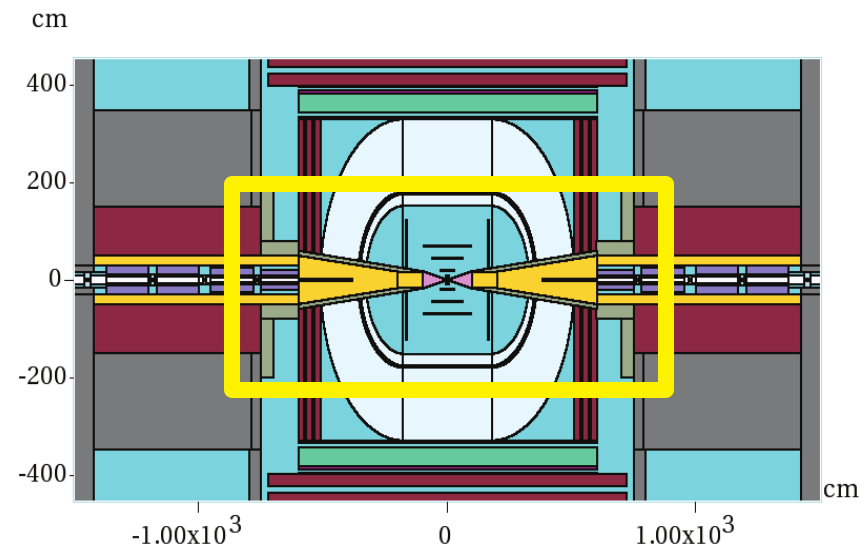
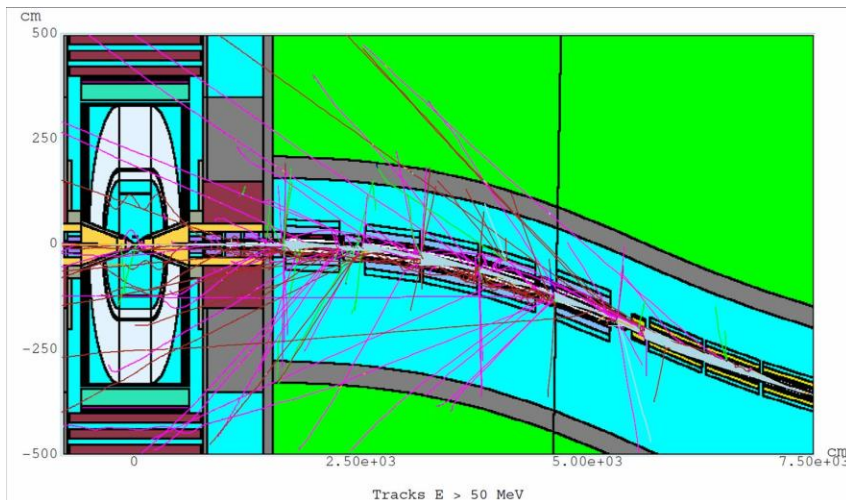
Physics background and beamstrahlung are among the dominant sources of systematic errors

Muon Collider: Beam-Induced Background

At muon collider the two mentioned methods can not be used because of the detector configuration.

Detector performance at a Muon Collider could be strongly limited by the rate of background particles arriving at each subdetector due to muon decays.

Nozzles have been designed to mitigate the effect of a such background.



Luminosity measurement at Muon Collider

Proposal: reconstruct $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ events at large angle with respect to the beam line to obtain

$$L = \frac{N}{\sigma_{th}}$$

Questions:

1. do we have enough μ -Bhabha events at large angle?
2. Is the precision of the theoretical cross section enough to measure L ?

Plan:

- a. Produce a sample of events $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ at $\sqrt{s}=1.5\text{TeV}$, $\sqrt{s}=3.0\text{TeV}$ and $\sqrt{s}=10\text{TeV}$ by using a tree-level Monte Carlo generator and study the reconstruction efficiency at large angle by using the full detector simulation and identify additional kinematical requirements that can help to obtain a more precise theoretical prediction.
- b. Perform the same studies with Mu-BabaYaga event generator.
- c. Evaluate the theoretical precision on the Bhabha cross section.
- d. Determine the expected precision on the luminosity.

Status of the activities: preparation of the dataset

A sample of $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ at $\sqrt{s}=1.5\text{TeV}$ has been produced with Pythia and analyzed at Monte Carlo level to understand how many events we have in the “central” region.

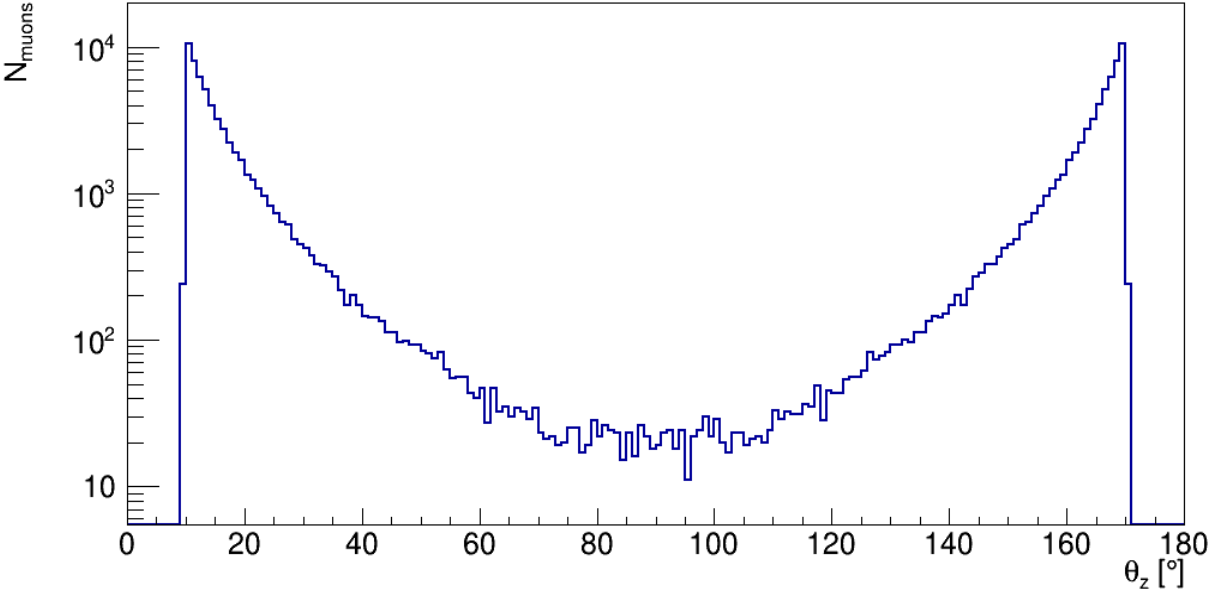
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*----- PYTHIA Event and Cross Section Statistics -----*
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Subprocess	Code	Number of events			sigma +- delta (estimated) (mb)	
		Tried	Selected	Accepted		
f fbar -> gamma gamma	204	6331	2788	0	0.000e+00	0.000e+00
f f' -> f f' (t-channel gamma*/Z0)	211	1531041922	885384204	99669	3.085e-08	9.771e-11
f_1 f_2 -> f_3 f_4 (t-channel W+-)	212	1385941	169276	0	0.000e+00	0.000e+00
f fbar -> gamma*/Z0	221	1704	1623	158	4.925e-11	3.723e-12
f fbar -> gamma*/Z0 gamma*/Z0	231	7548	358	22	7.268e-12	1.512e-12
f fbar -> W+ W-	233	46301	5162	28	8.702e-12	1.641e-12
f fbar -> gamma*/Z0 gamma	243	24073	2768	88	2.783e-11	2.930e-12
f fbar -> H (SM)	901	0	0	0	0.000e+00	0.000e+00
f fbar -> H0 Z0 (SM)	904	99	26	3	6.897e-13	3.837e-13
f f' -> H0 f f' (Z0 Z0 fusion) (SM)	906	331	113	27	7.090e-12	1.237e-12
f_1 f_2 -> H0 f_3 f_4 (W+ W- fusion) (SM)	907	2697	977	5	1.599e-12	7.138e-13
sum		1532516947	885567295	100000	3.095e-08	9.786e-11

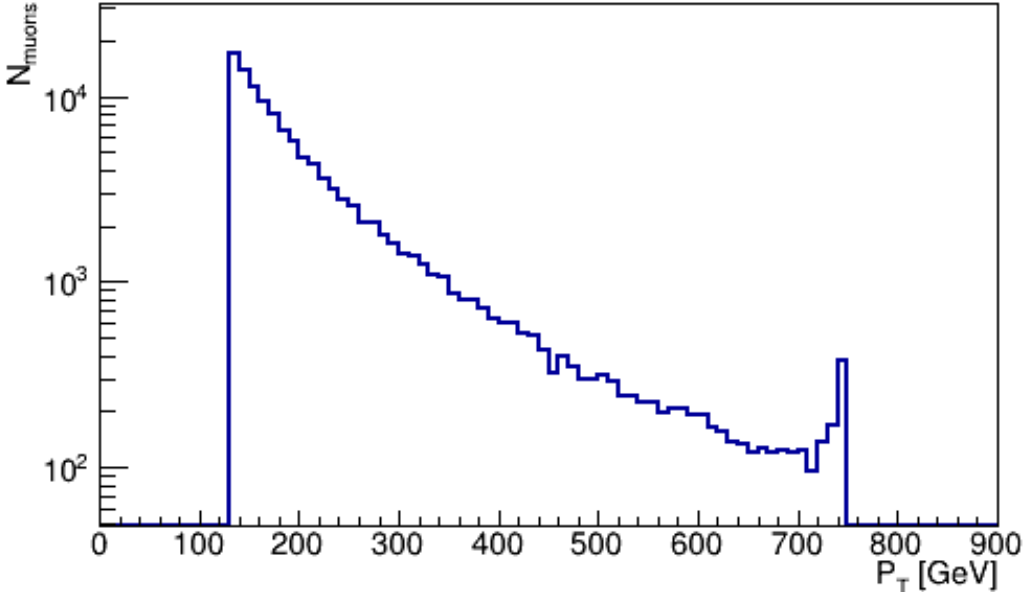
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*----- End PYTHIA Event and Cross Section Statistics -----*
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Status of the activities: first look at data

Accepting all muons in the detector acceptance with $P_t > 130 \text{ GeV}$



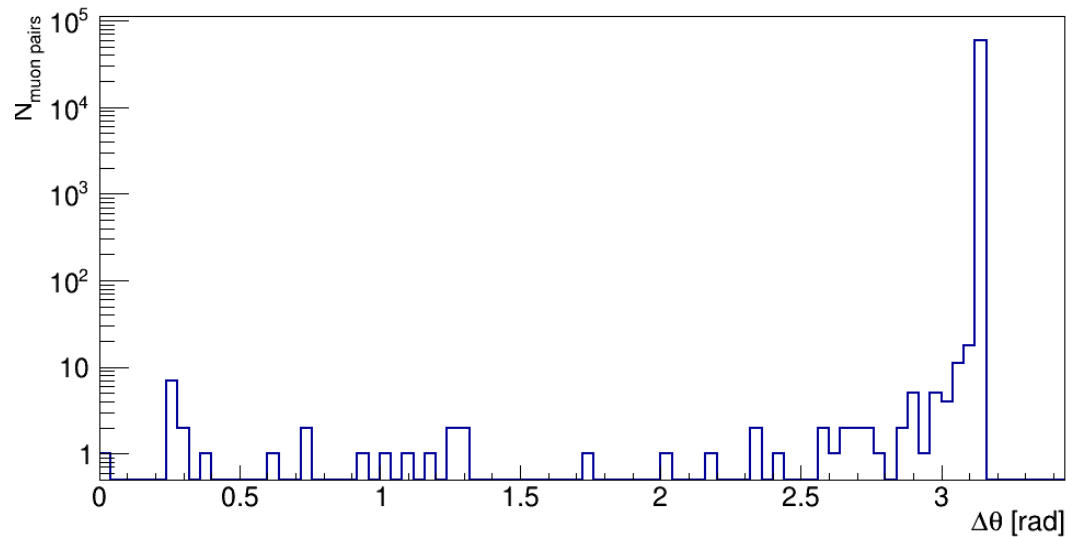
θ angle of muons with respect to the z axis in the detector acceptance



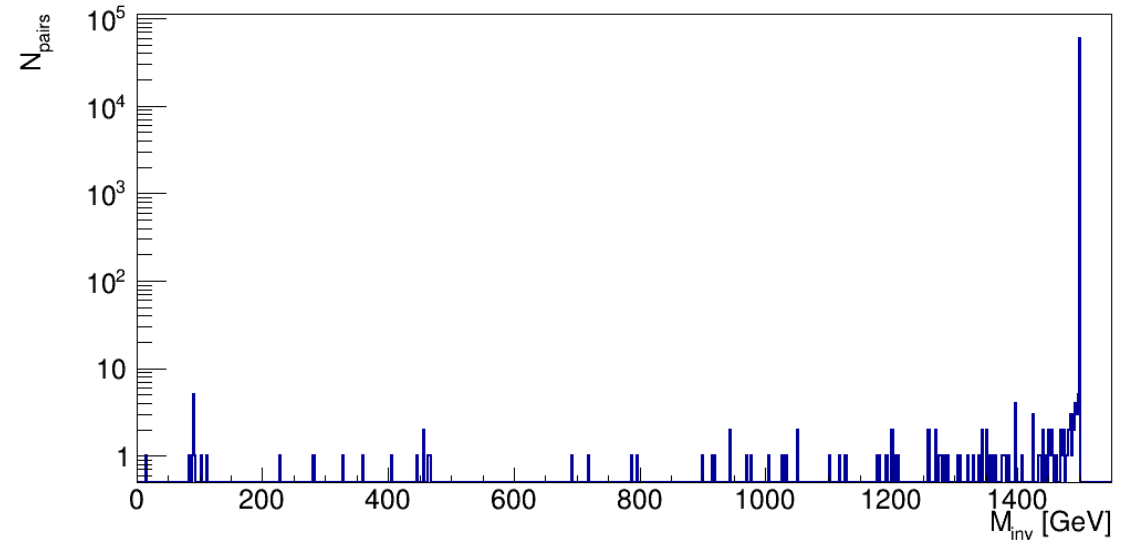
Transverse momentum of muons in the detector acceptance

Status of the activities: first look at data

Analysis on the muons's pairs in the detector acceptance with $P_t > 130 \text{ GeV}$



$\Delta\theta$ between the muons in the detector acceptance



Invariant mass of the muons

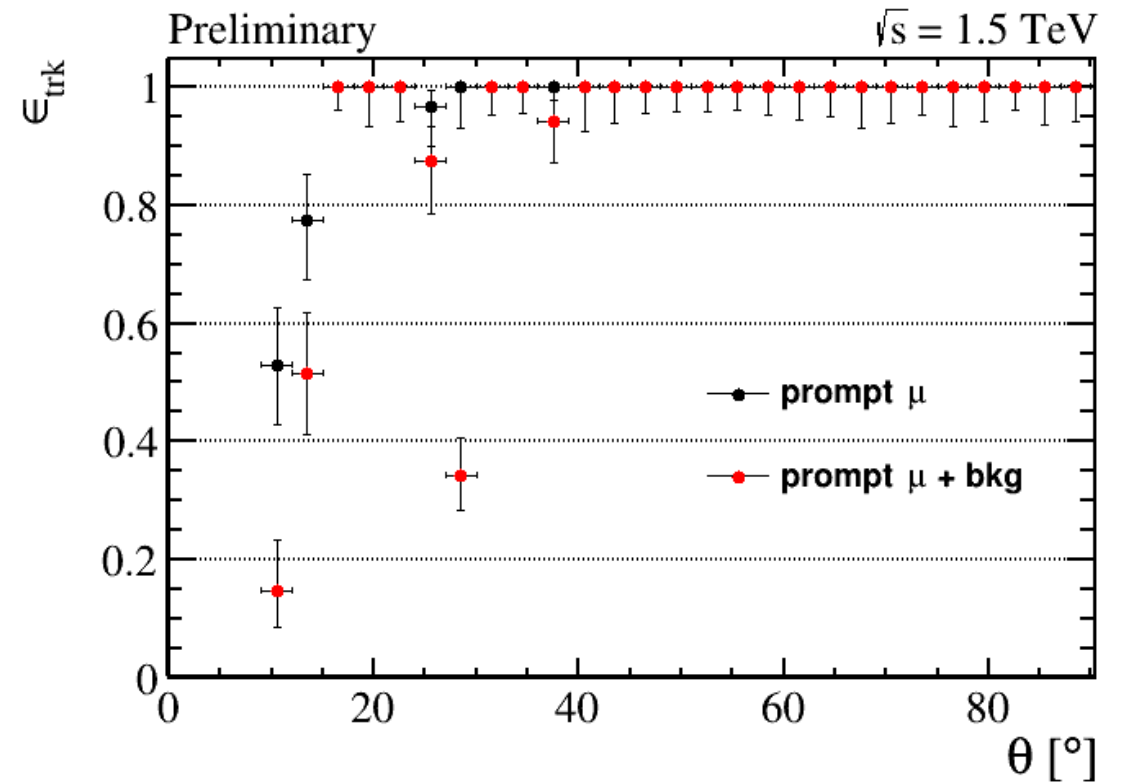
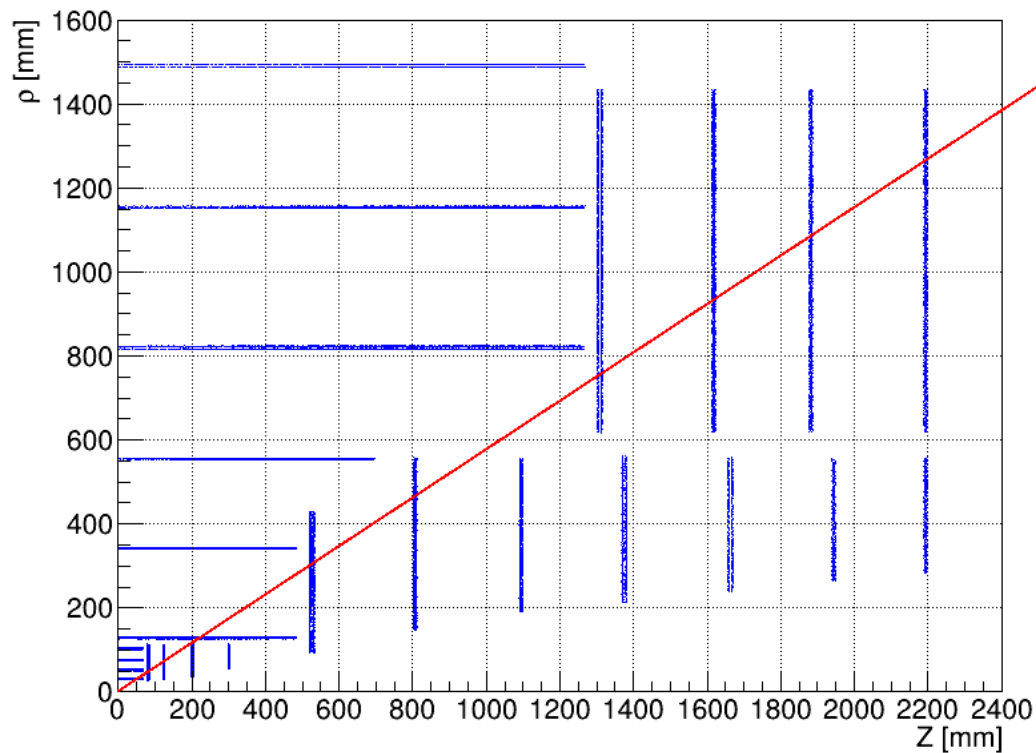
Assuming a Snowmass year = 10^7 seconds

$$\mathcal{L} = 1.25 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

Total events: 2.3 M

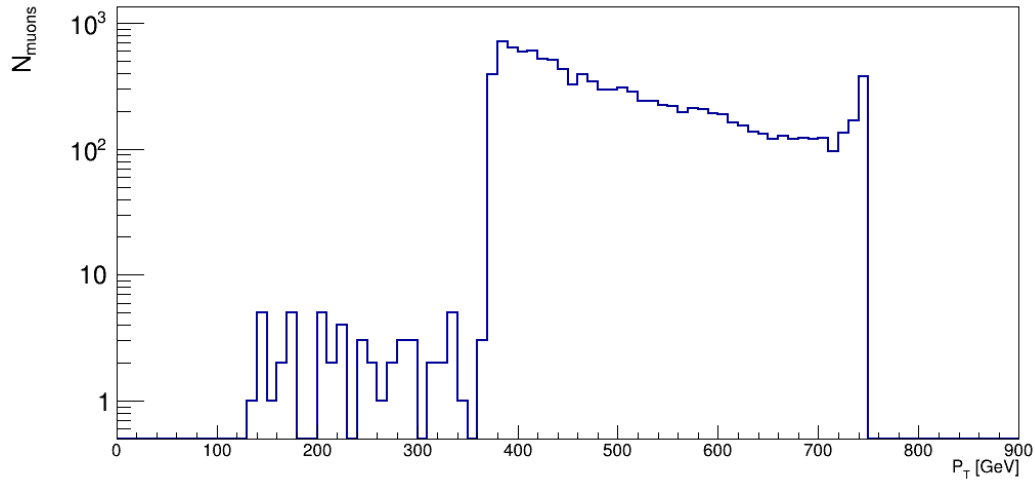
Status of the activities: Identify “safe” detector regions

In order to avoid the crowded regions affected by beam-induced background muons $30^\circ < \theta < 150^\circ$ are selected in addition to $P_t > 130$ GeV



Status of the activities count useful events

Muons with $30^\circ < \theta < 150^\circ$ are selected and $P_t > 130 \text{ GeV}$



Transverse momentum of muons in the detector acceptance

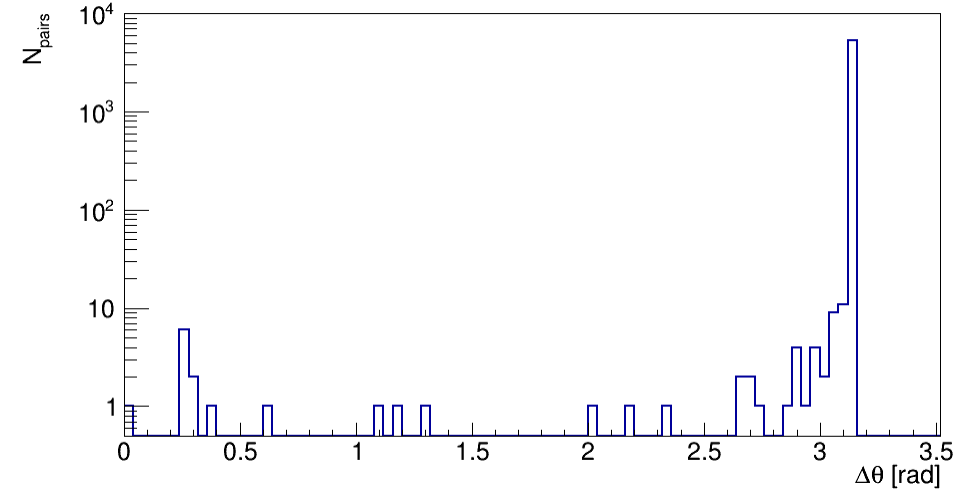
Assuming a Snowmass year = 10^7 seconds

$$\mathcal{L} = 1.25 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

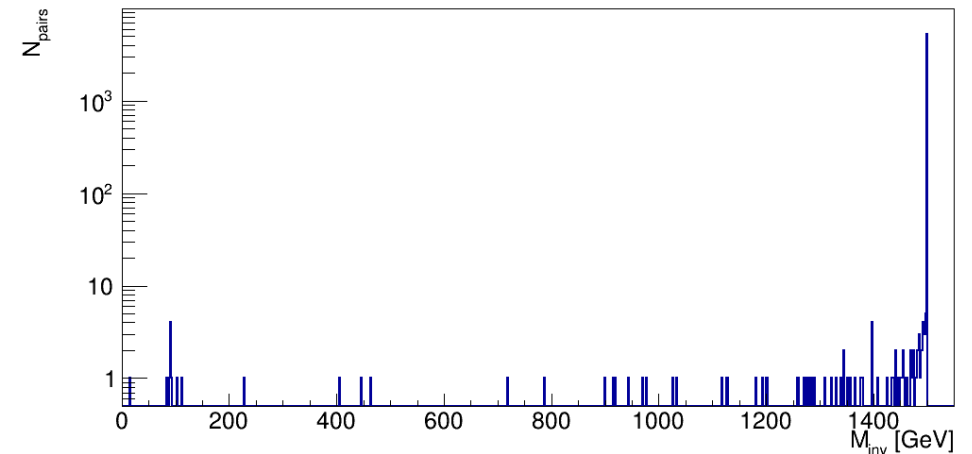
Total events: 213 K

$$\frac{\Delta \mathcal{L}}{\mathcal{L}} \sim \frac{1}{\sqrt{N}} = 0.002$$

$\Delta\theta$ between the muons



Invariant mass of the muons



Summary

- A method to measure the luminosity at Muon Collider is proposed based on μ -Bhabha at large angle.
- By looking at the number of events produced by using Pythia it seems the number of events is enough to determine the luminosity with a reasonable precision (usually $\sim 1\%$) at least at $\sqrt{s}=1.5\text{TeV}$.
- The next steps:
 - Re-do the exercise with the full detector simulation.
 - Perform the same analysis at $\sqrt{s}=3.0\text{TeV}$ and $\sqrt{s}=10\text{TeV}$.
 - Use mu-BabaYaga to generate $\mu^+ \mu^- \rightarrow \mu^+ \mu^-$ samples and identify the best kinematic cuts to select Bhabha events.
 - Determine the theoretical precision on the cross section at the different center of mass energies.