

# WIMPy Inelastic Dark Matter In Light Of Low-Background Experiments

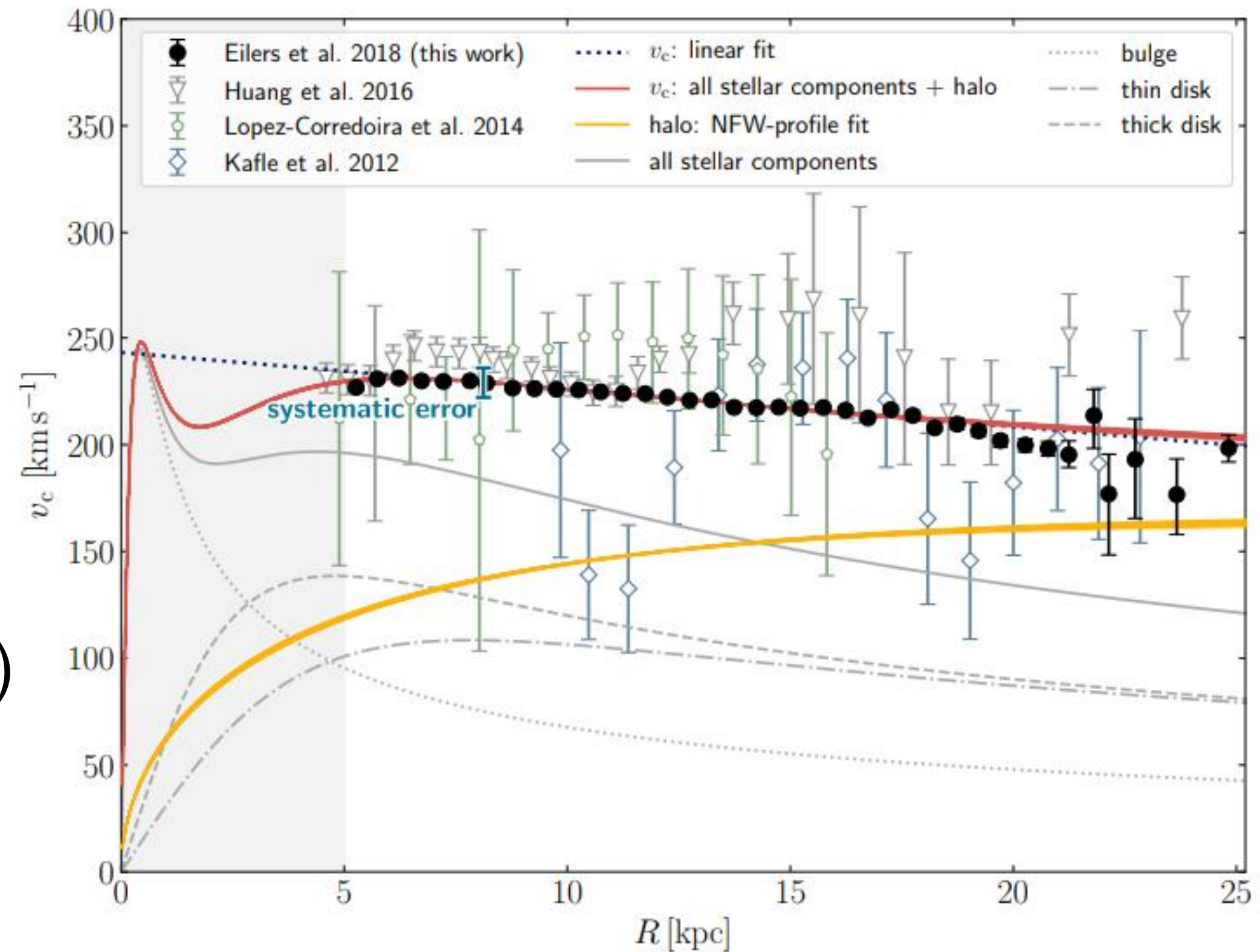
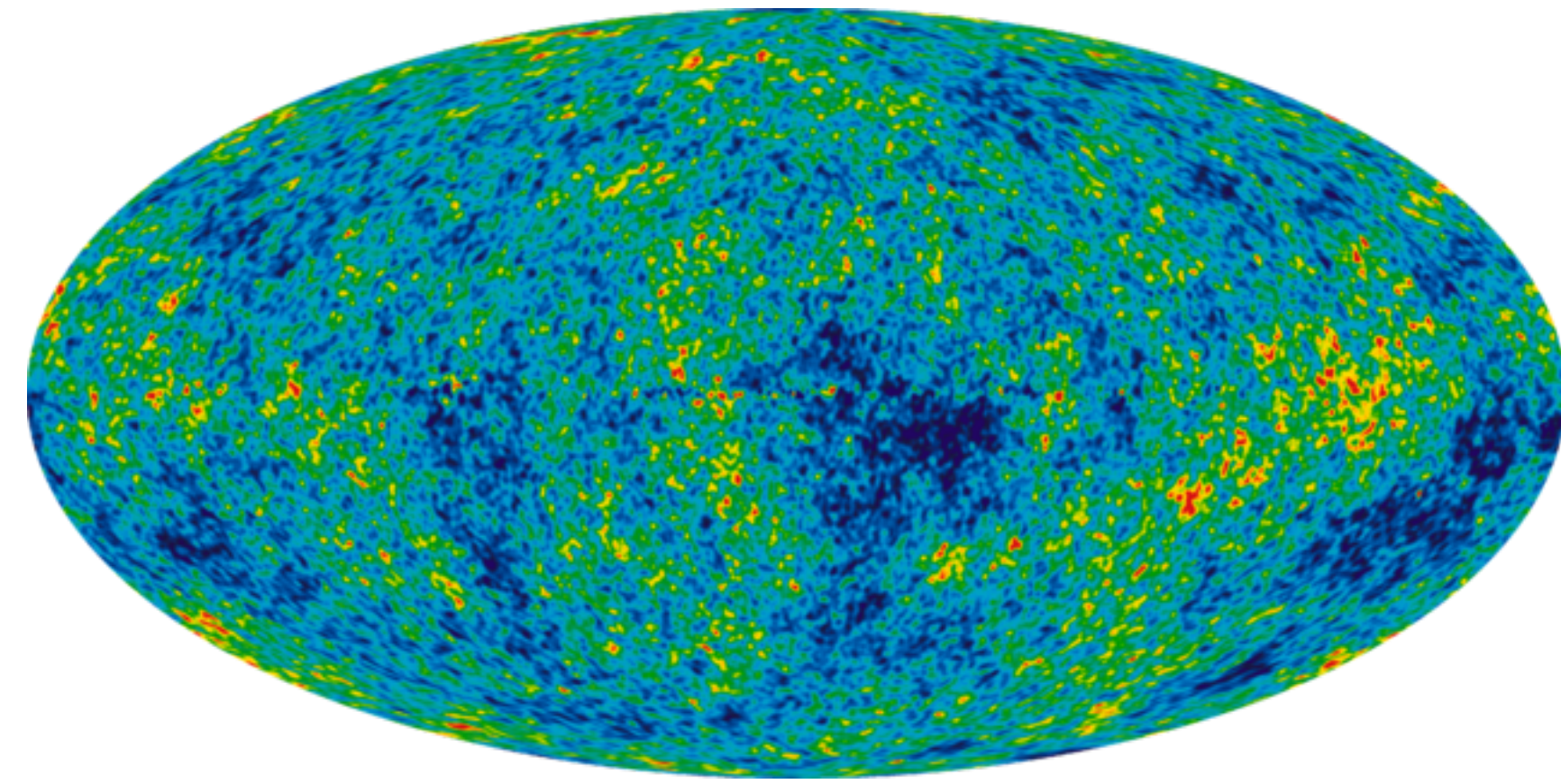
**Ningqiang Song**

with Ben Broerman, Serge Nagorny and Aaron Vincent

**Queen's University, McDonal Institute, Perimeter Institute**

**June 9, 2021**





Dark matter is virialized in Milky Way

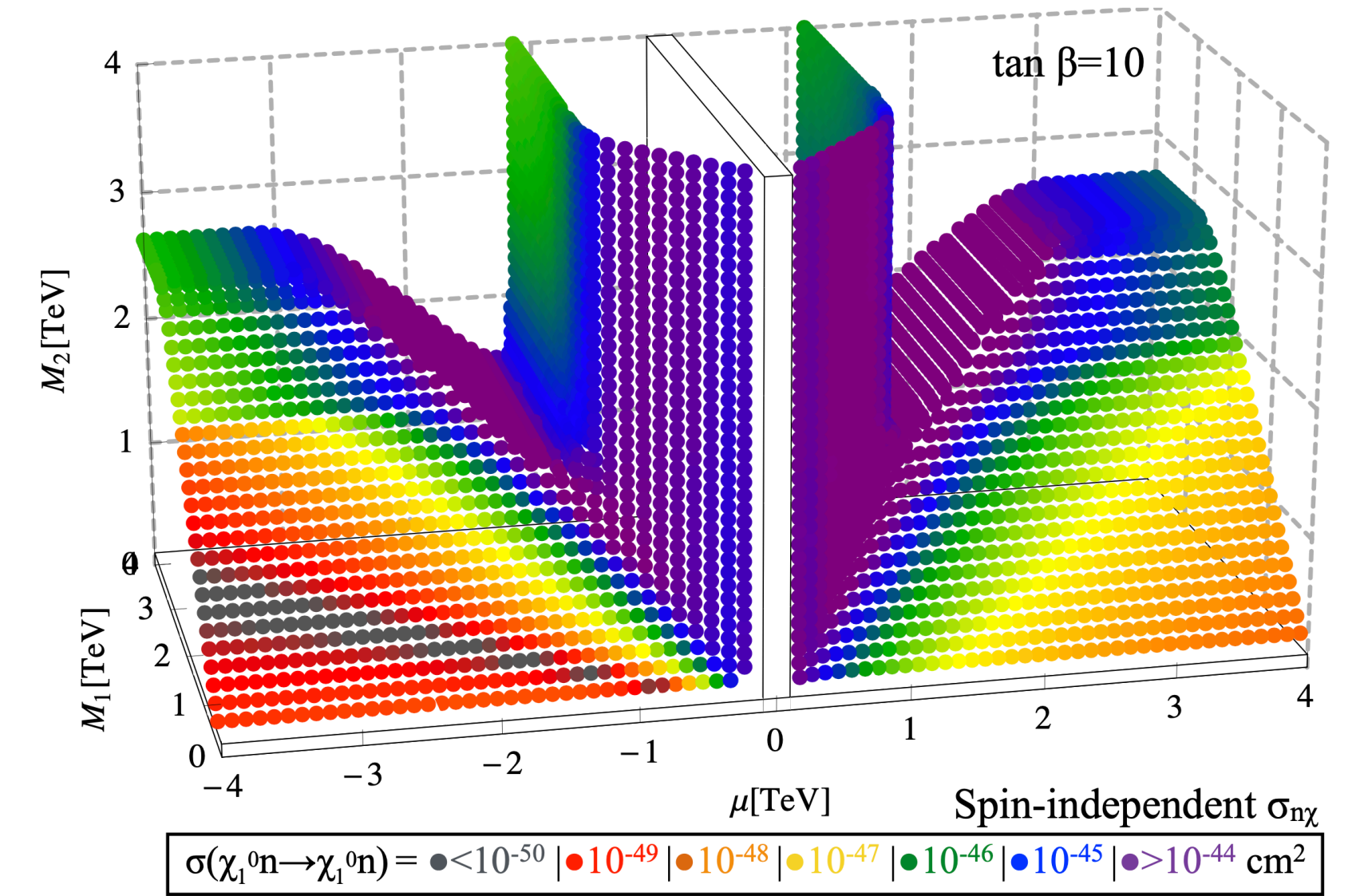
- Maxwellian distribution  $v \sim 10^{-3}c$  (220 km/s)
- Escape velocity  $v_{esc} \sim 500 - 600$  km/s (Gaia)
- Mass?
- Interactions?

# Inelastic Dark Matter

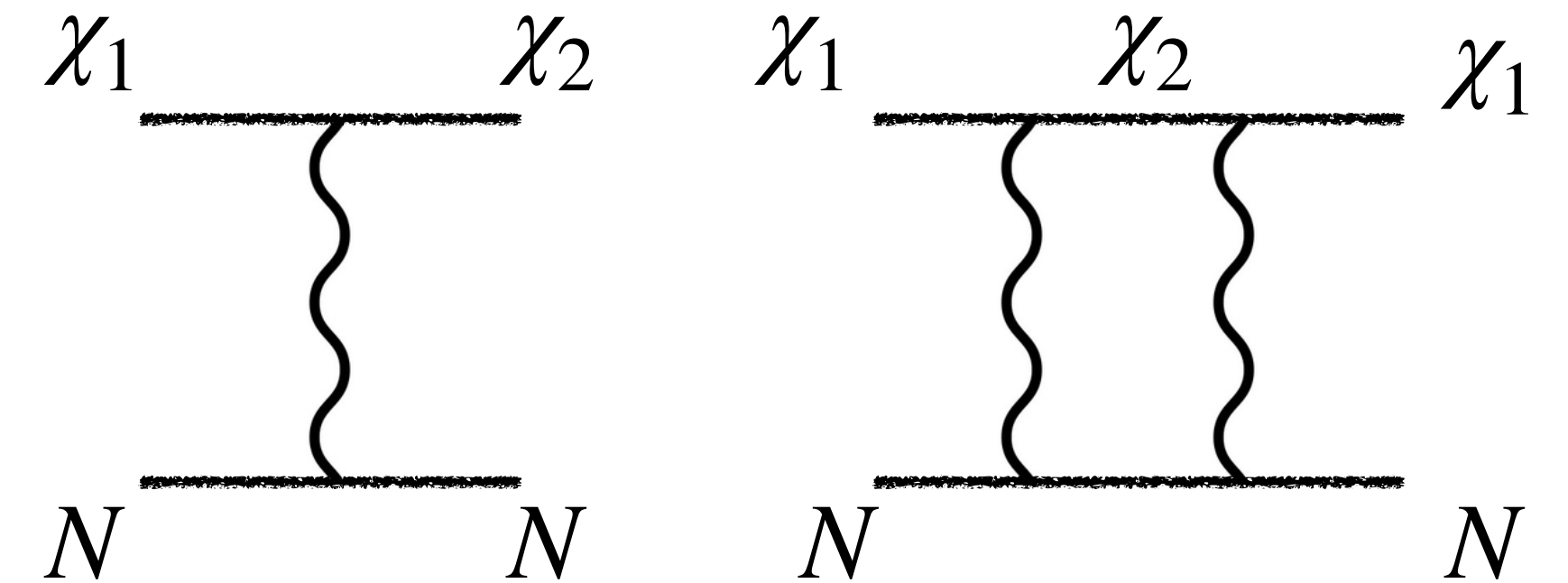
- Off-diagonal mass term  $\begin{pmatrix} M & \nu \\ \nu & M \end{pmatrix}$
- After diagonalization  $M_{\chi_1} = M + \nu$ ,  $M_{\chi_2} = M - \nu$
- $\delta \equiv M_{\chi_2} - M_{\chi_1} \ll M_\chi$
- Example: dark photon-mediated DM

$$\mathcal{L} \supset \bar{\psi}(iD_\mu \gamma^\mu - m_\psi)\psi + (y\phi\bar{\psi}^T C^{-1}\psi + h.c.)$$

Bramante, **NS**, PRL/2006.14089  
 Batell, Pospelov, Ritz, 0903.3396



Neutralino DM, see Bramante et al,  
 1510.03460, 1412.4789



kinematically suppressed

loop suppressed

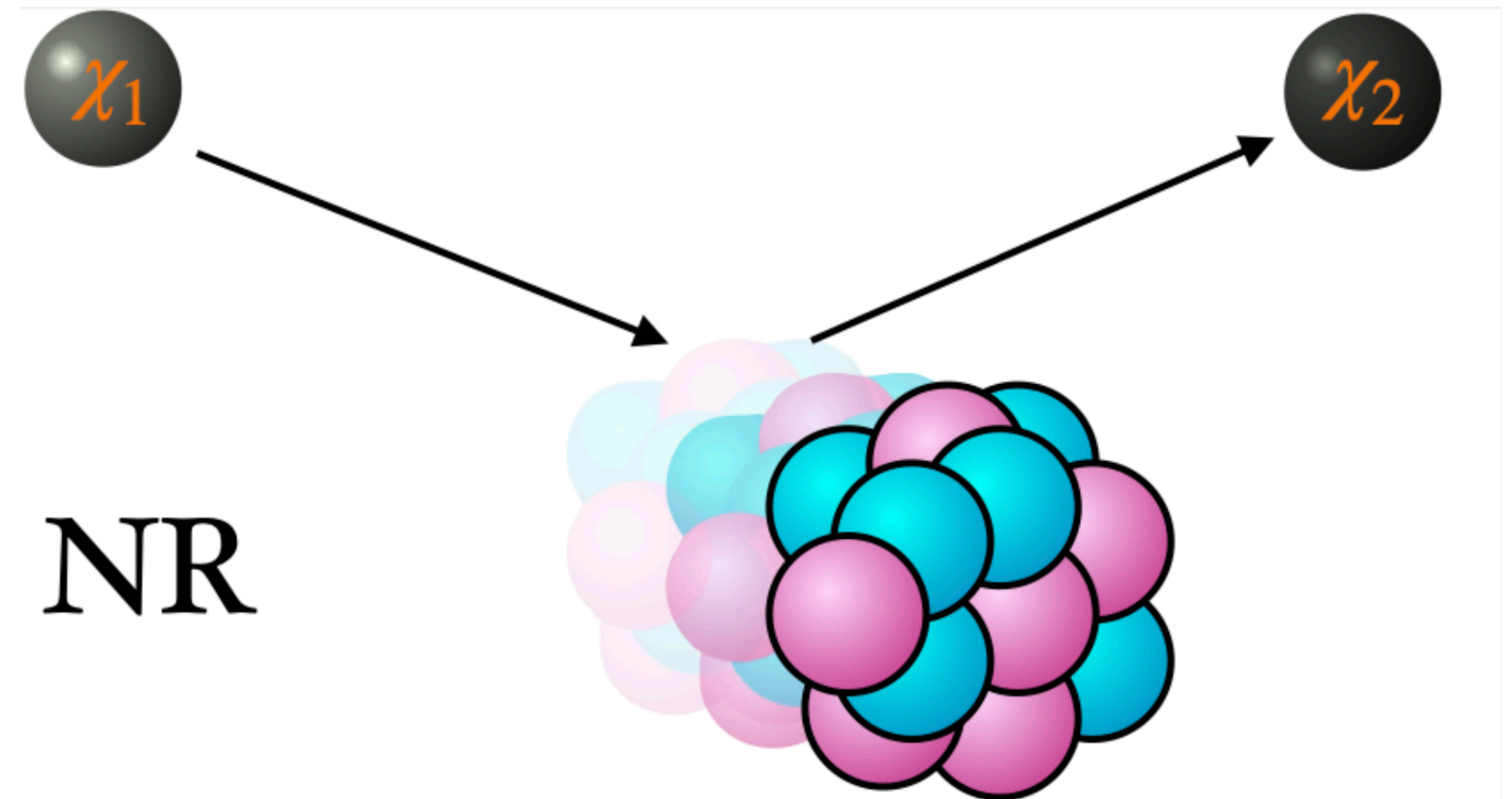
# Kinematics in Nuclear Recoil

- $$\frac{\vec{q}_i^2}{2M_{\chi_1}} = \frac{\vec{q}_f^2}{2M_{\chi_2}} + \frac{\vec{q}^2}{2M_A} + \delta$$

- $$q_{\min/\max} = \mu_{\chi A} v \left[ 1 \mp \sqrt{1 - 2 \frac{\delta}{\mu_{\chi A} v^2}} \right]$$

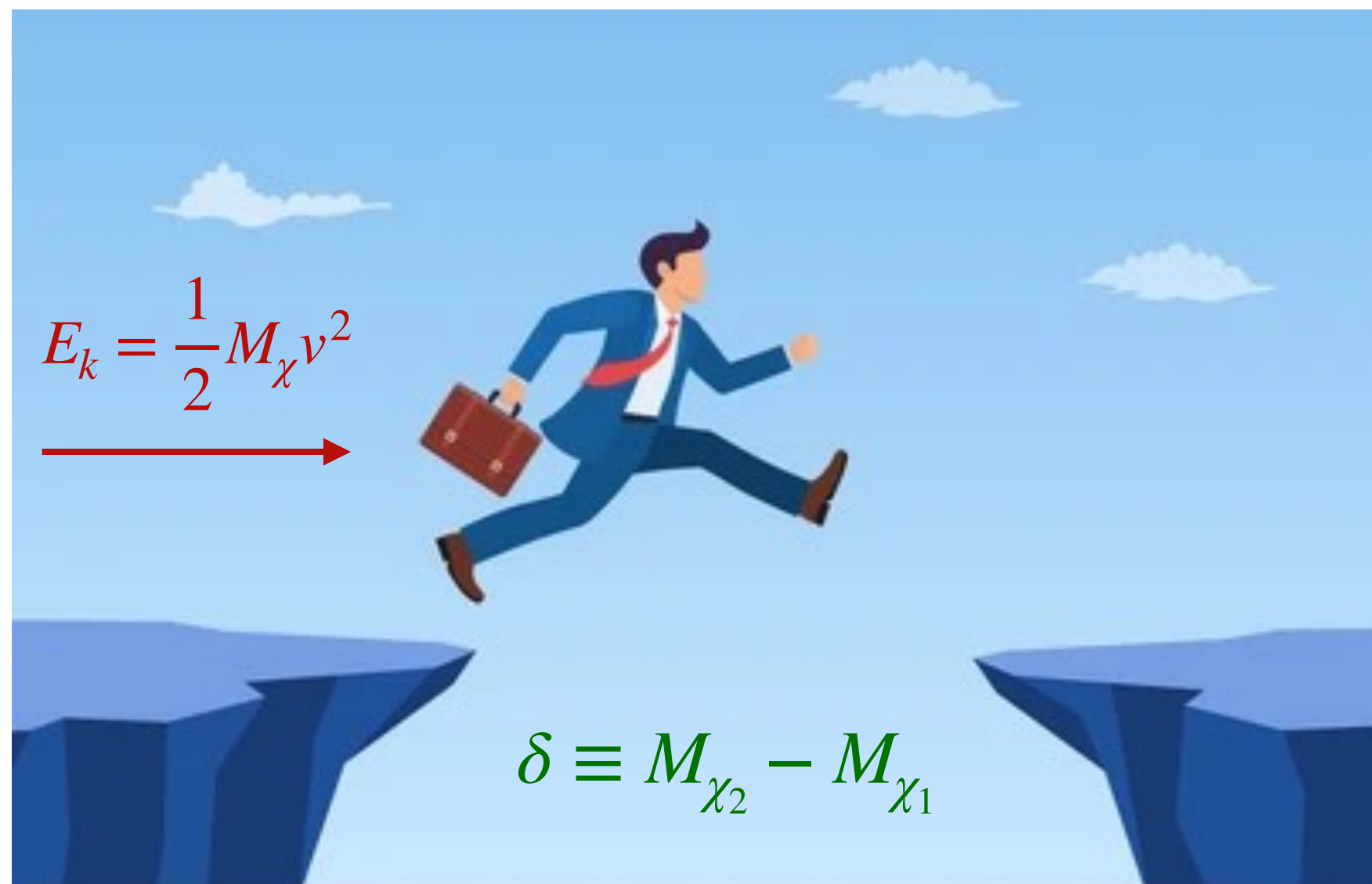
- $$\text{Minimum velocity } v_{\min} = \sqrt{2 \frac{\delta}{\mu_{\chi A}}}$$

$$\delta \equiv M_{\chi_2} - M_{\chi_1}$$

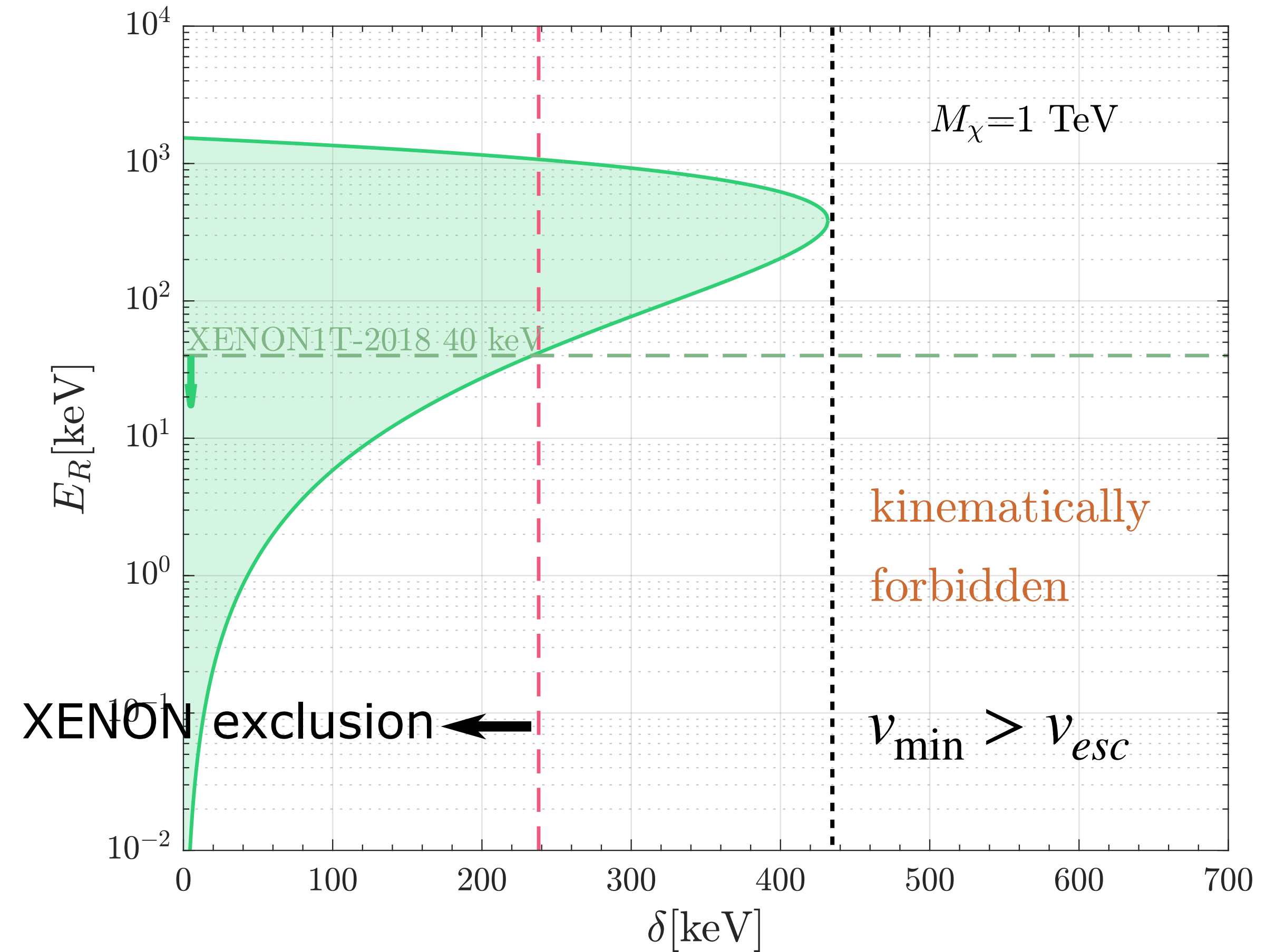


# Why not XENON

- Xenon not heavy enough
- Xenon experiments only sensitive to low energy deposition ( $E_R \lesssim 40$  keV)



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# Two Criteria

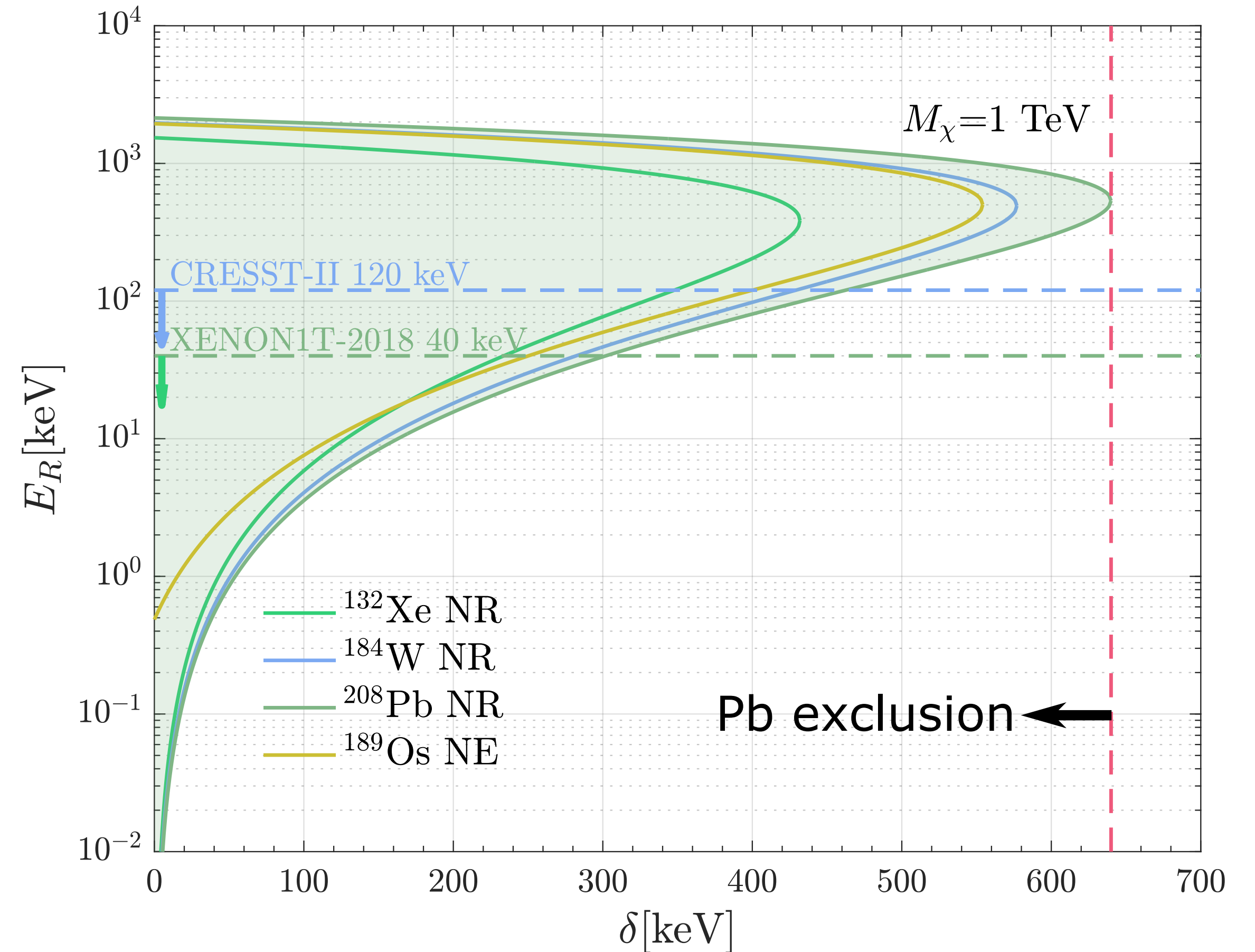
- Heavy nuclear target

$$\delta_{\max} = \frac{1}{2} \mu_{\chi A} (v_e + v_{\text{esc}})^2$$

- High energy deposition acceptance

$$E_{\text{accept}} > E_R^{\min} \sim \text{MeV}$$

Target nuclei with  $A \sim 200$



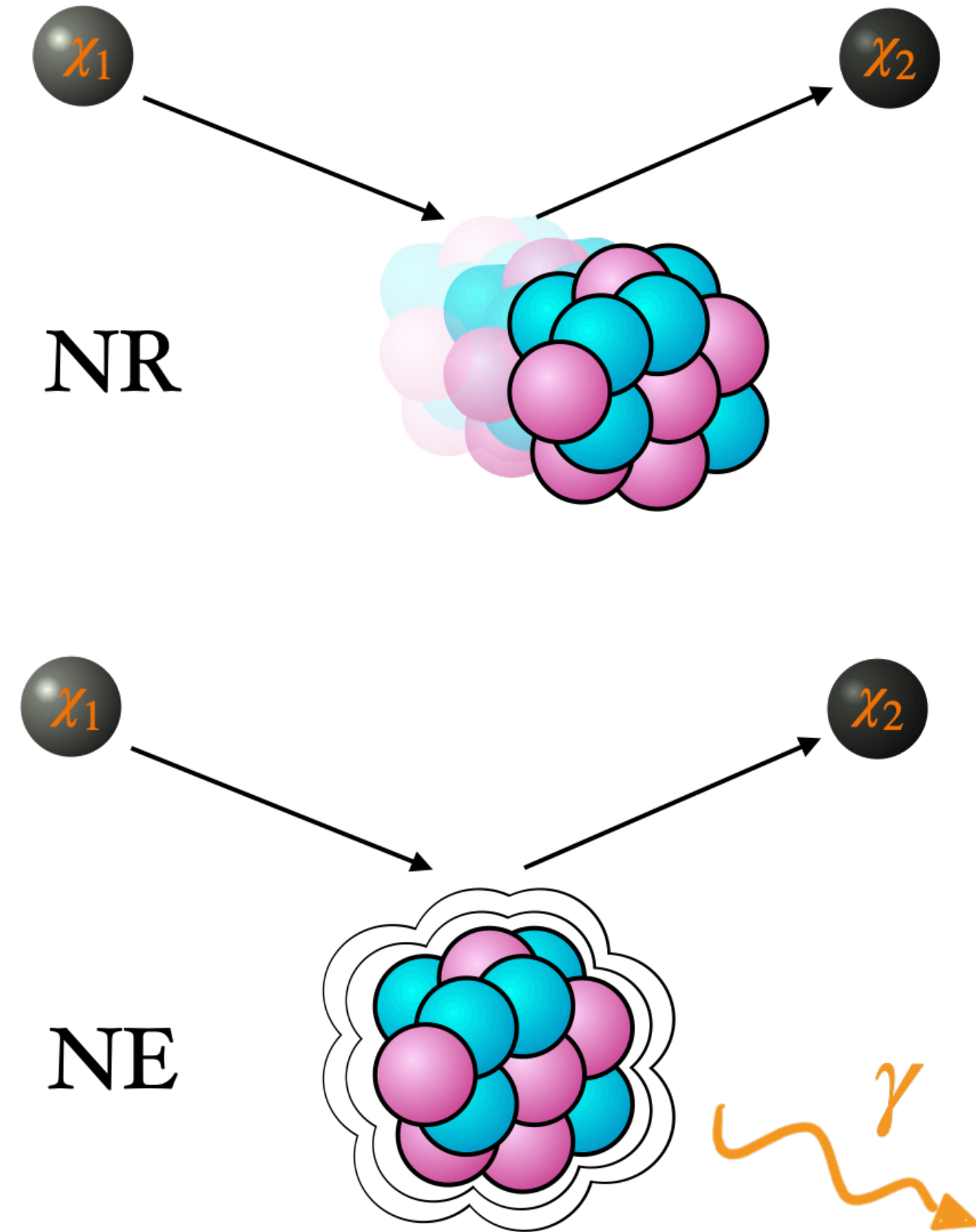
# Nuclear Excitation (NE)

$$\Delta \equiv \delta + E_{\text{excitation}}$$

$$\frac{\vec{q}_i^2}{2M_{\chi_1}} = \frac{\vec{q}_f^2}{2M_{\chi_2}} + \frac{\vec{q}^2}{2M_A} + \Delta$$

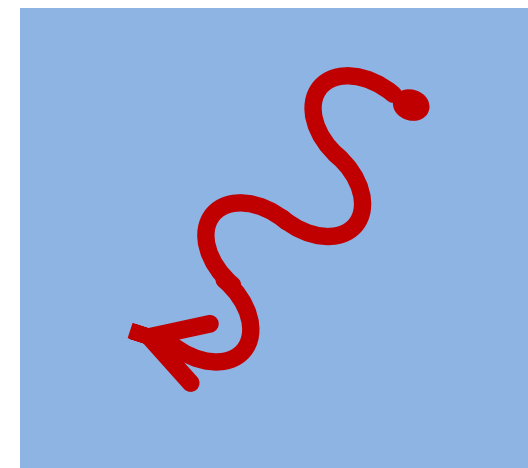
$$q_{\text{min/max}} = \mu_{\chi A} v \left[ 1 \mp \sqrt{1 - 2 \frac{\Delta}{\mu_{\chi A} v^2}} \right]$$

$$\text{Minimum velocity } v_{\text{min}} = \sqrt{2 \frac{\Delta}{\mu_{\chi A}}}$$

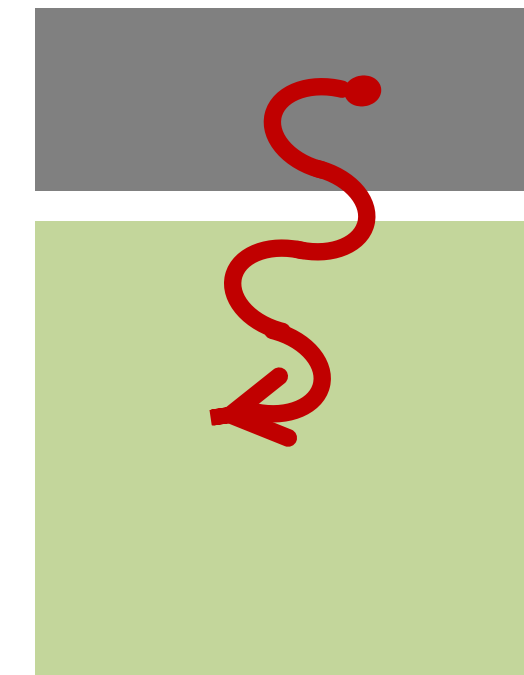


# Nuclear Recoil vs Nuclear Excitation

*detector = source*



*detector ≠ source*



Nuclear Recoil	Type	Nuclear Excitation
Nuclear recoil	<i>Signal</i>	Deexcitation gamma
Scintillating bolometer	<i>Detection</i>	Gamma detector
Coherent $\propto A^2$	<i>Scattering</i>	Incoherent $\propto \cancel{A^2}$
Helm form factor	<i>Form factor</i>	$S(\vec{q}) = \sum_L  \langle J_f    j_L(qr) Y_{LM}(\hat{r})    J_i \rangle ^2$
Mass splitting	<i>Kinematical suppression</i>	Mass splitting+excitation

Engel, Vogel, hep-ph/9910409

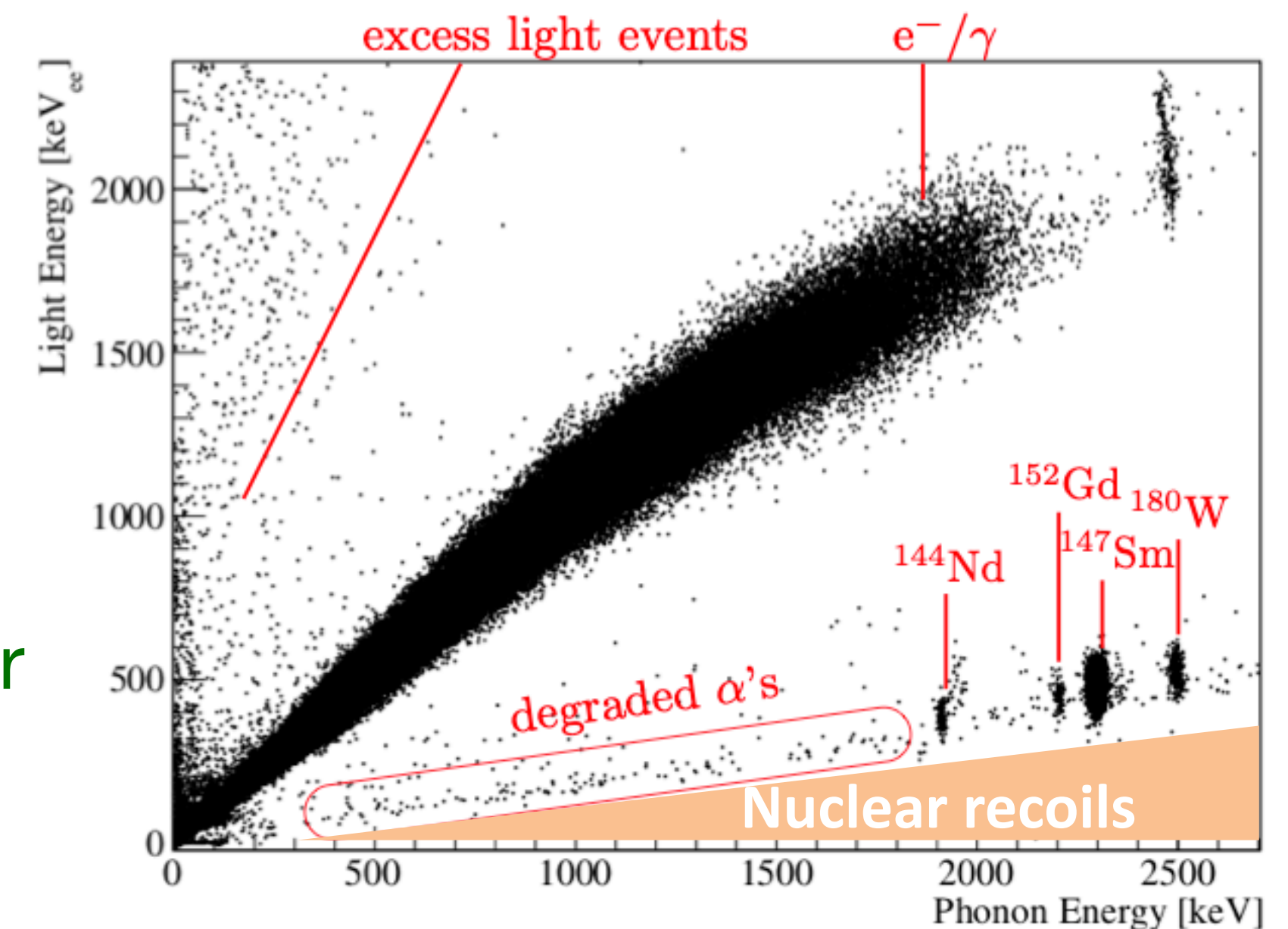
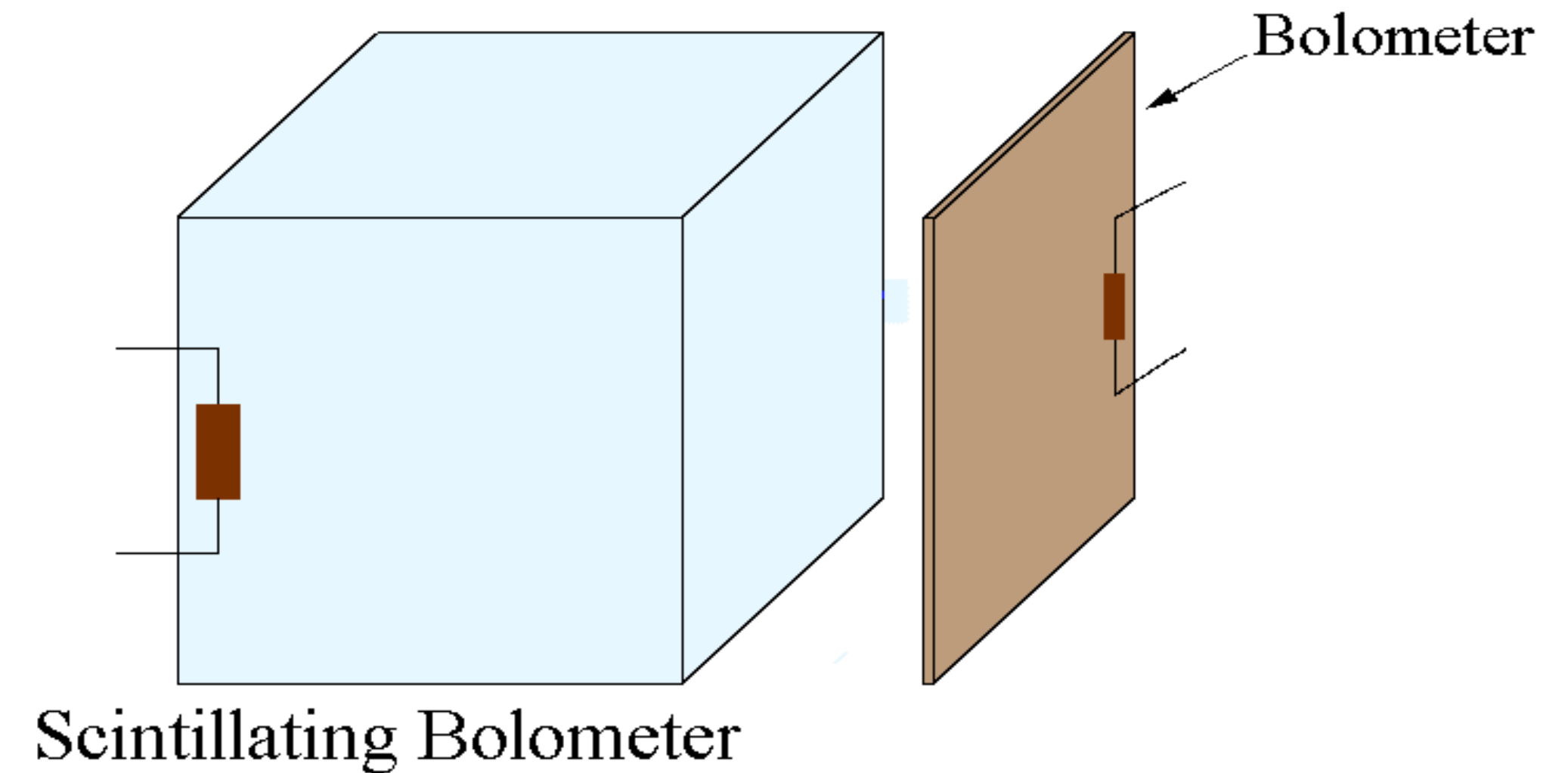


# Scintillating Bolometers

- Simultaneous double readout of **heat (H)** and **scintillation light (L)**
- Fraction of the deposited energy is converted into a scintillation (up to 25%)
- effective discrimination of  $e/\gamma$  from  $\alpha$  events/DM by the difference in L/H ratio

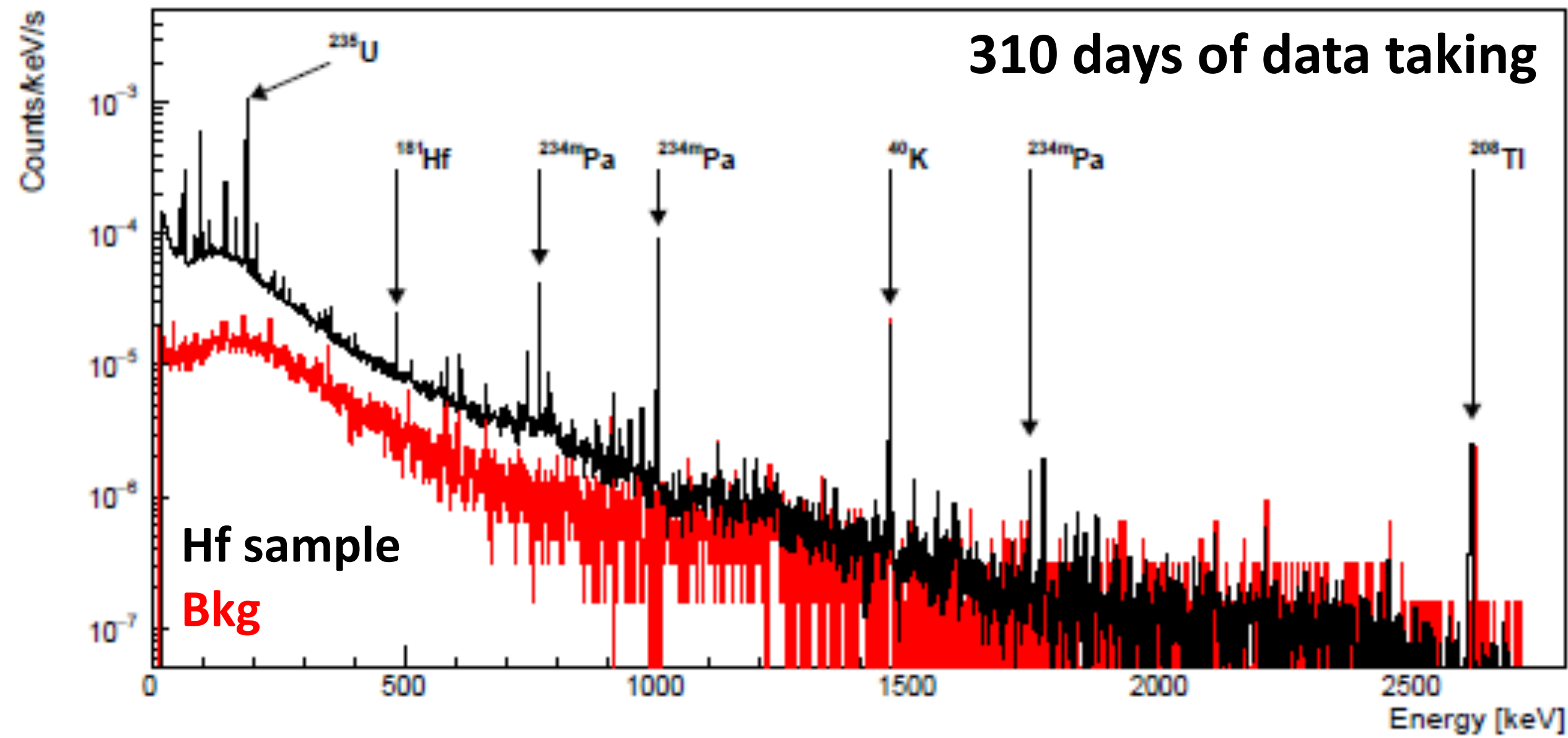
CaWO<sub>4</sub> scintillating bolometer

Munster *et al.*, arXiv:1403.5114

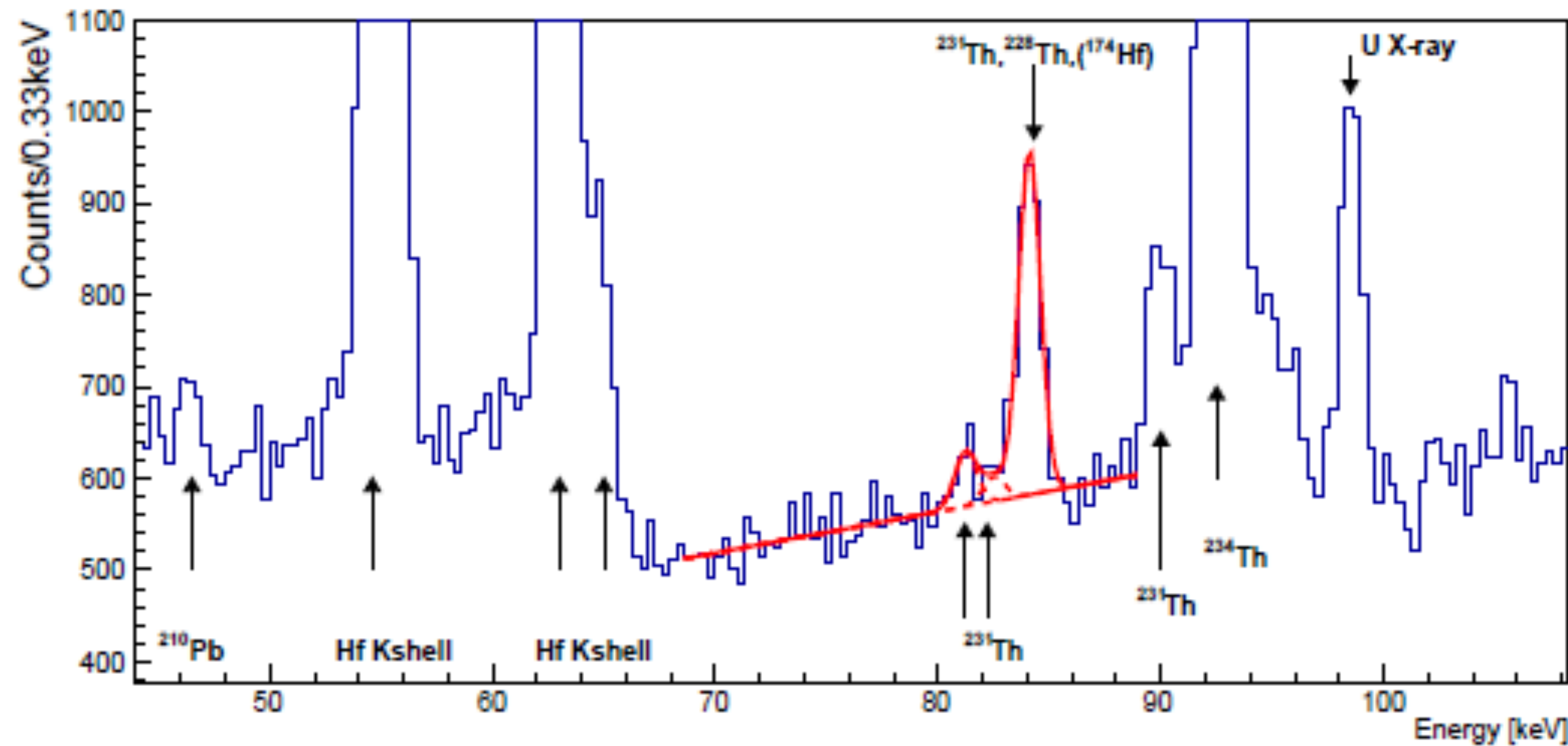


# Gamma Detection

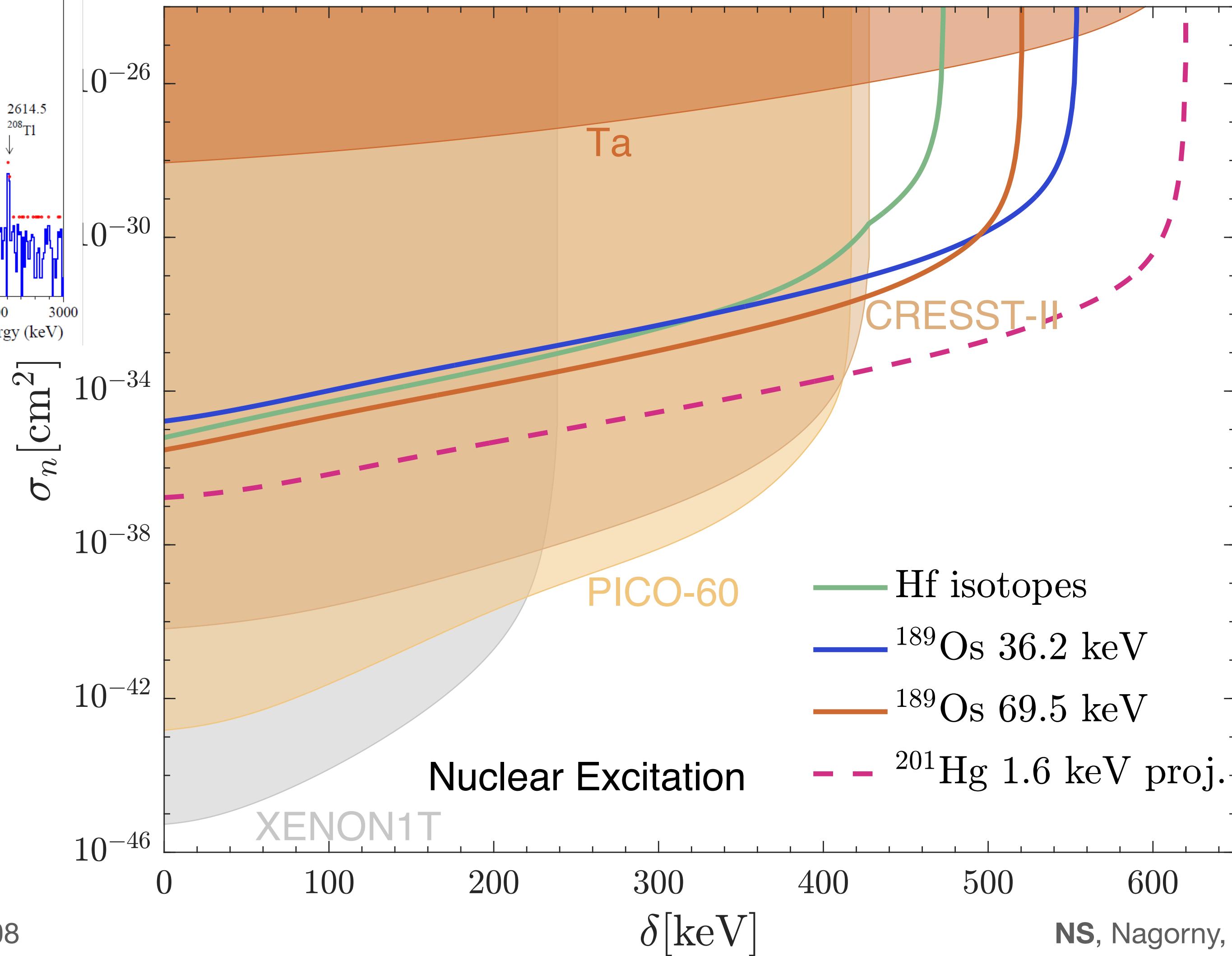
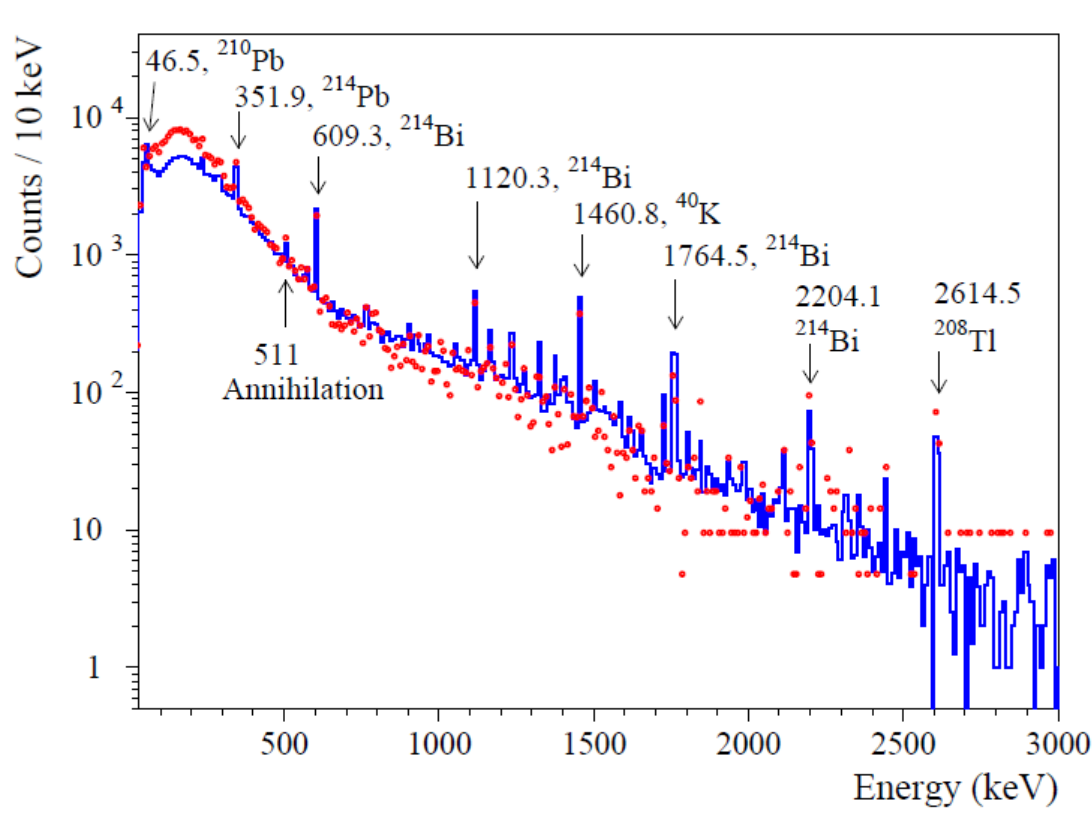
Broerman, Laubenstein, SN, NS, Vincent, 2012.08339



**A(238U chain) = 11 Bq/kg**  
**A(235U chain) = 0.5 Bq/kg**  
**A(232Th chain) = 0.01 Bq/kg**



# Nuclear Excitation with Gamma Measurement



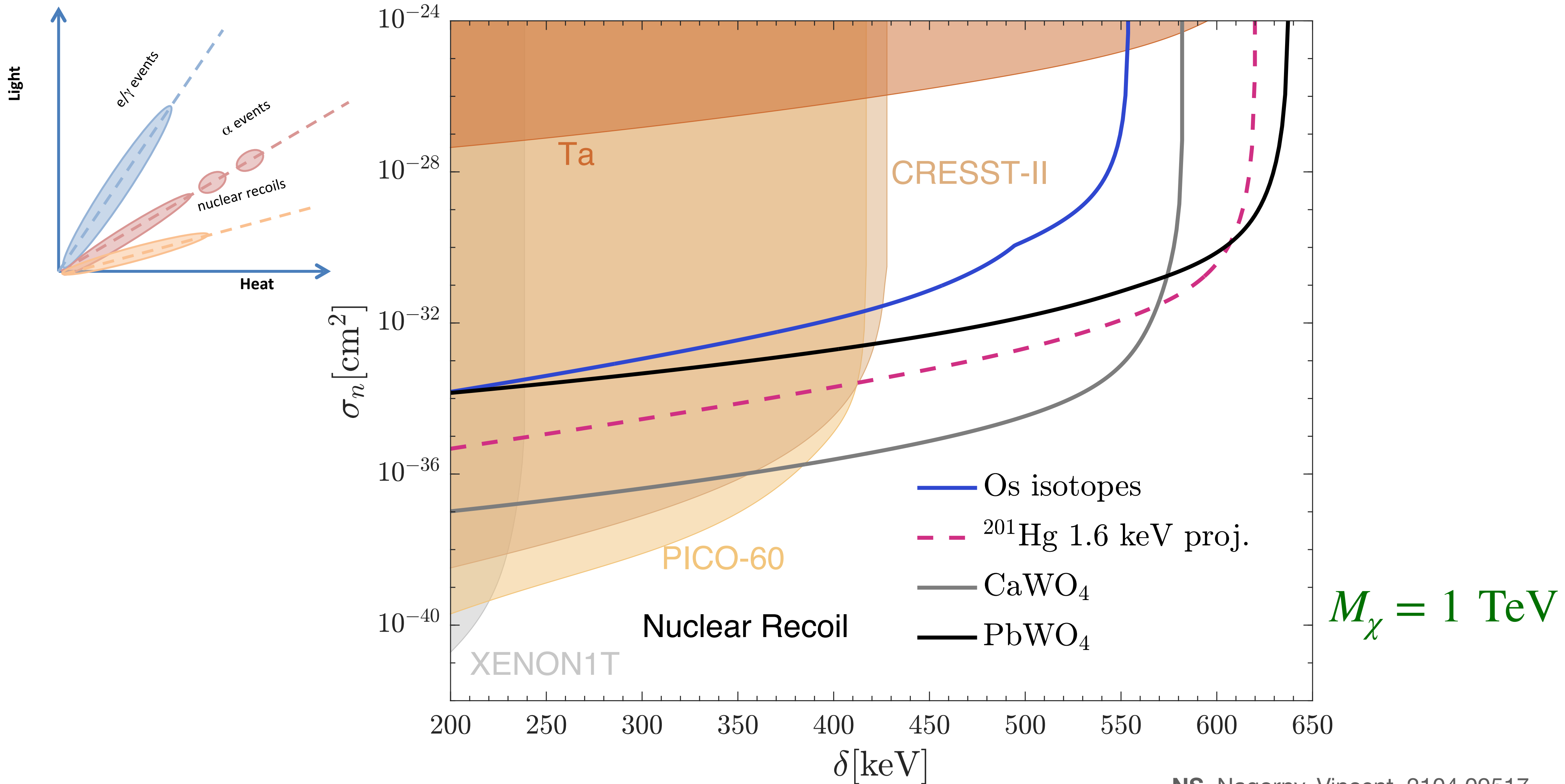
$M_\chi = 1 \text{ TeV}$

Belli *et al.*, 2009.01508

**NS**, Nagorny, Vincent, 2104.09517

Broerman, Laubenstein, **NS**, Nagorny, Vincent, 2012.08339

# Nuclear Recoil with Scintillating Bolometer

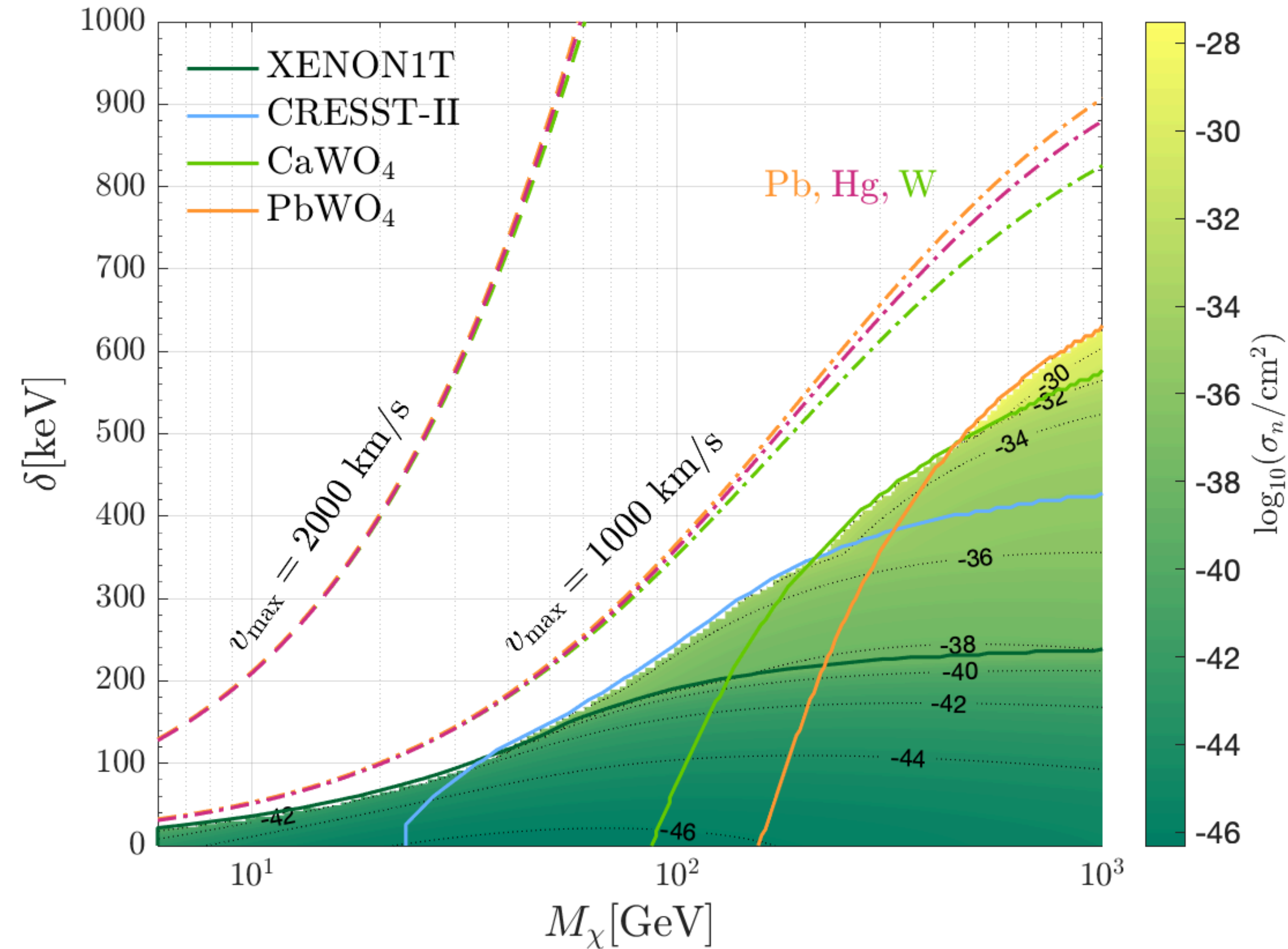


NS, Nagorny, Vincent, 2104.09517

# Conclusions

- Inelastic dark matter detection challenged by kinematics
- **Nuclear recoil** search with  $\text{CaWO}_4$ ,  $\text{PbWO}_4$
- **Nuclear excitation** search with Hf, Os
- Boosted dark matter

$$\delta_{\max} = \frac{1}{2} \mu_{\chi A} (v_e + v_{\text{esc}})^2$$



# Backup Slides

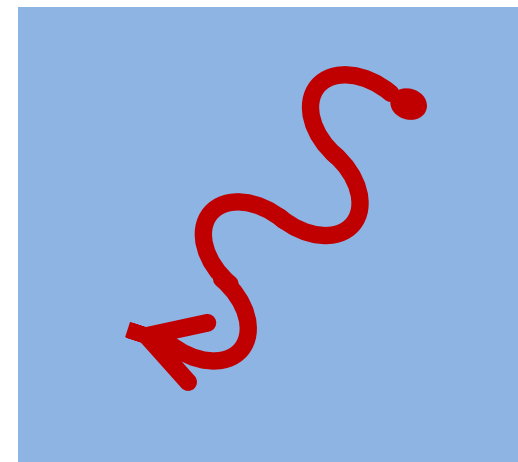
# Nuclear Transition Table

Isotope	Abund.[%]	$J_{g.s.}^p$	$J_{e.s.}^p$	$\Delta E$ [keV]	B(E2)[ <i>W.u.</i> ]	$E_\gamma$ [keV]	$I_\gamma$ [%]	Bkg.[mBq/kg]
$^{174}\text{Hf}$	0.16	$0^+$	$2^+$	90.985	152(8) [105]	91.00	100	3.8
$^{176}\text{Hf}$	5.26	$0^+$	$2^+$	88.349	183(7) [106]	88.34	100	3.1
$^{177}\text{Hf}$	18.60	$7/2^-$	$9/2^-$	112.9500	282(8) [64]	112.9498	100	0.9
$^{178}\text{Hf}$	27.28	$0^+$	$2^+$	93.1803	160(3) [65]	93.1803	100	2.2
$^{179}\text{Hf}$	13.62	$9/2^+$	$11/2^+$	122.7904	245(14) [107]	122.793	100	0.9
$^{180}\text{Hf}$	35.08	$0^+$	$2^+$	93.3240	154.8(21) [66]	93.324	100	2.2
$^{187}\text{Os}$	1.8794	$1/2^-$	$3/2^-$	74.356	$50_{-50}^{+60}$ [108]	74.30	100	0.25
		$1/2^-$	$5/2^-$	75.016	38(10) [108]	64.31	54.3	0.31
$^{189}\text{Os}$	16.152	$3/2^-$	$1/2^-$	36.17	27(7) [67]	36.17	100	0.40
		$3/2^-$	$5/2^-$	69.54	100(10) [67]	69.53	99.8	0.16
		$3/2^-$	$3/2^-$	95.27	14(3) [67]	59.06	75.5	0.20
$^{201}\text{Hg}$	13.17	$3/2^-$	$1/2^-$	1.5648	$\sim 34$ [68]	1.5648	100	0.0056 (proj.)
		$3/2^-$	$5/2^-$	26.272	2.4(8) [68]	26.34	100	0.0060 (proj.)
		$3/2^-$	$3/2^-$	32.145	20(9) [68]	32.19	50.5	0.012 (proj.)

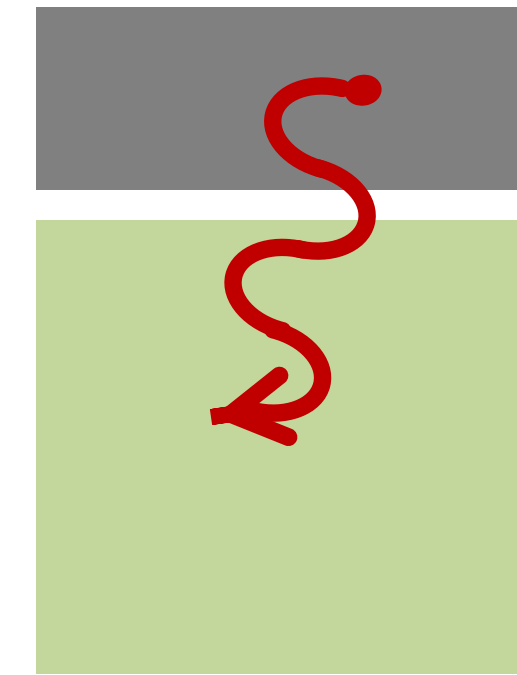
NS, Nagorny, Vincent, 2104.09517

# Two different experimental approaches

*detector = source*



*detector ≠ source*



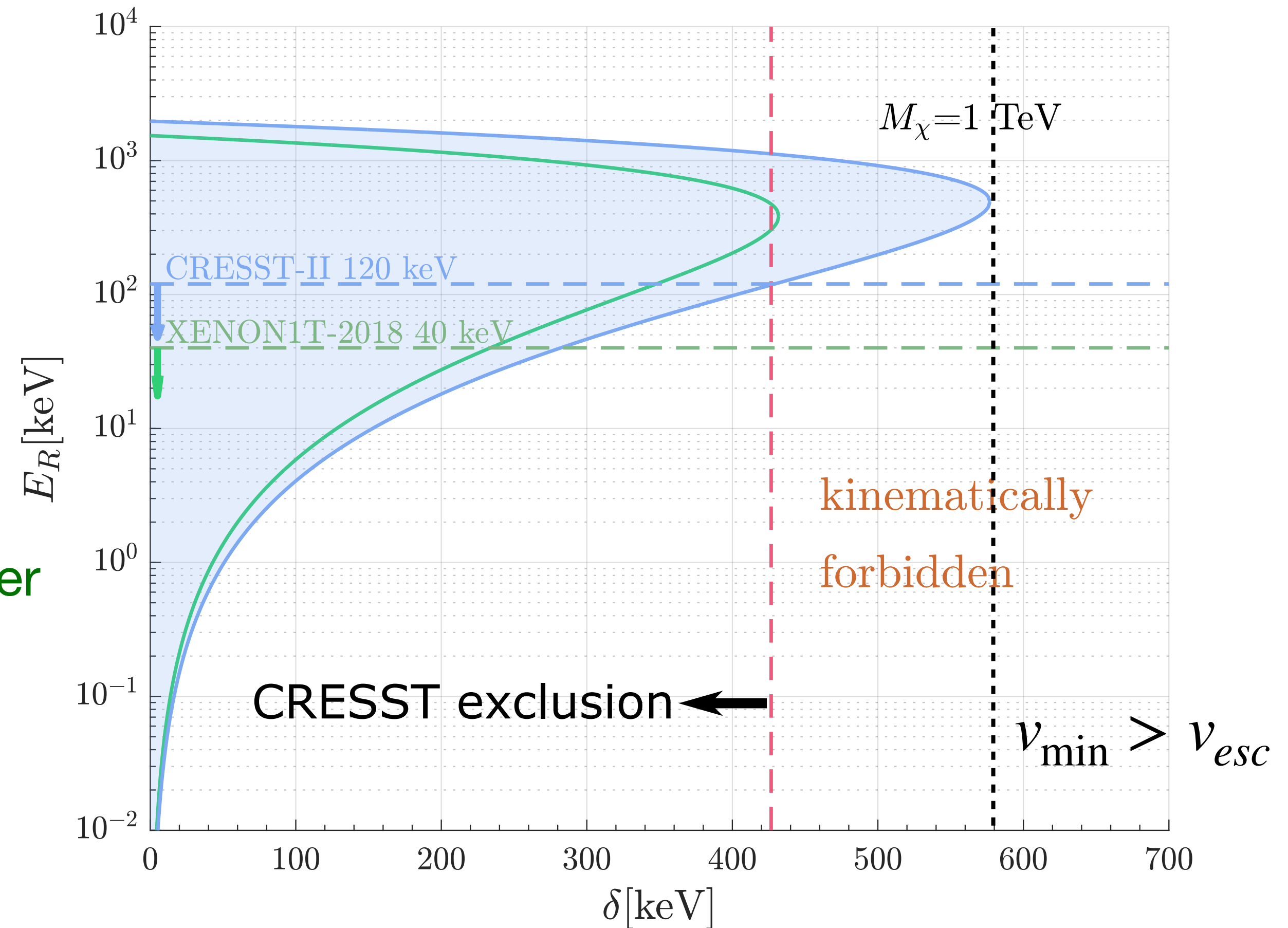
<b>Light/Heat</b>	<i>Possible channel/s</i>	<b>Charge</b>
<b>Scintillating bolometer</b>	<i>Detector type</i>	<b>HPGe</b>
<b>Partially</b>	<i>Material flexibility</i>	<b>Yes</b>
<b>No limitation</b>	<i>Energy limitation</i>	<b>&gt; 300 keV (gamma)</b>
<b>High (up to 100%)</b>	<i>Detection efficiency</i>	<b>Low (few %)</b>
<b>High (1/1000)</b>	<i>Energy resolution</i>	<b>High (1/1000)</b>
<b>Yes</b>	<i>Particle discrimination</i>	<b>No</b>
<b><math>\leq 10^{24}</math> y</b>	<i>Sensitivity</i>	<b><math>\leq 10^{22}</math> y</b>



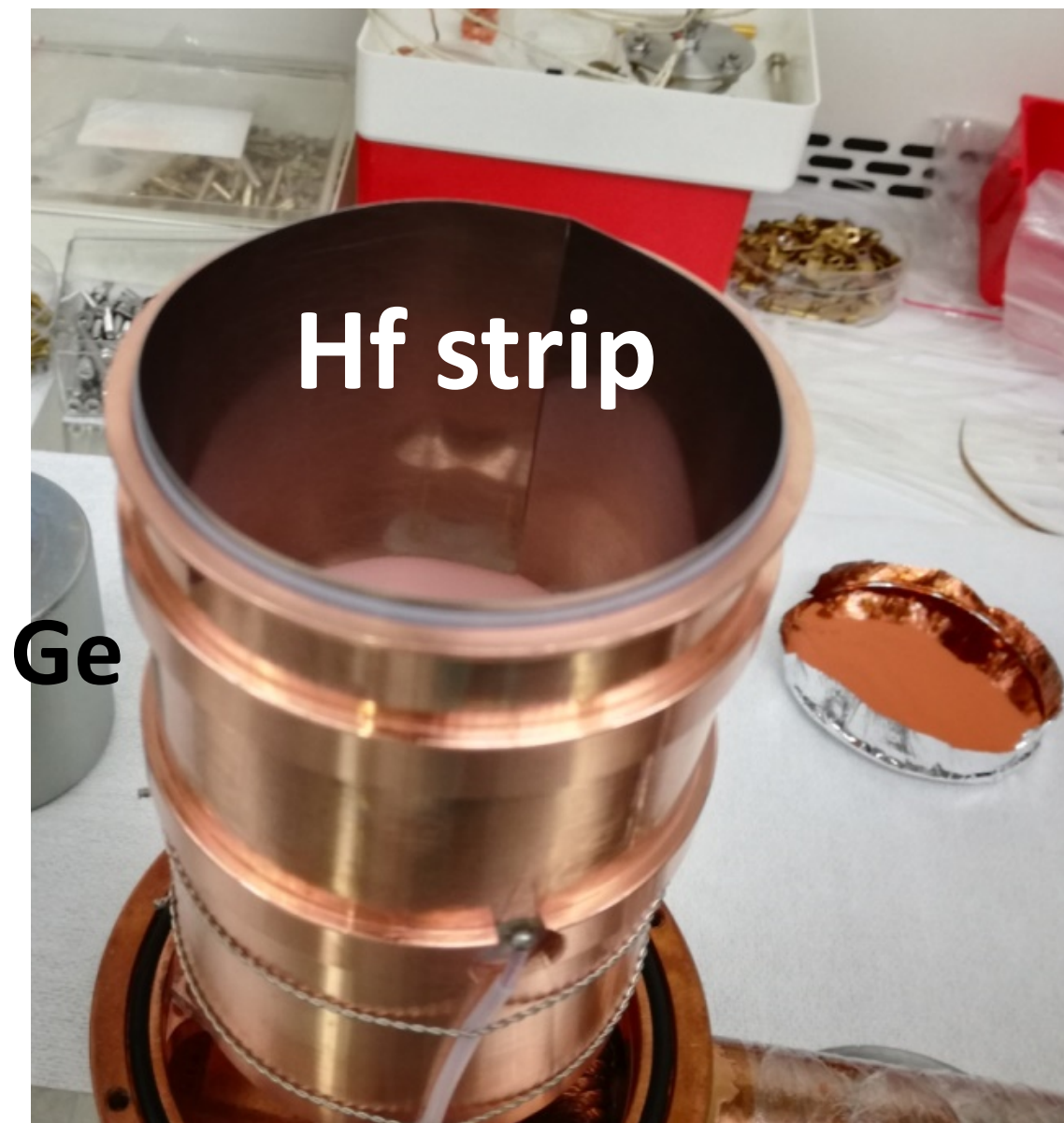
# Why Not CRESST

- CRESST experiments sensitive to low energy deposition ( $E_R < 120$  keV)

CaWO<sub>4</sub> scintillating bolometer



# Hf-metal sample

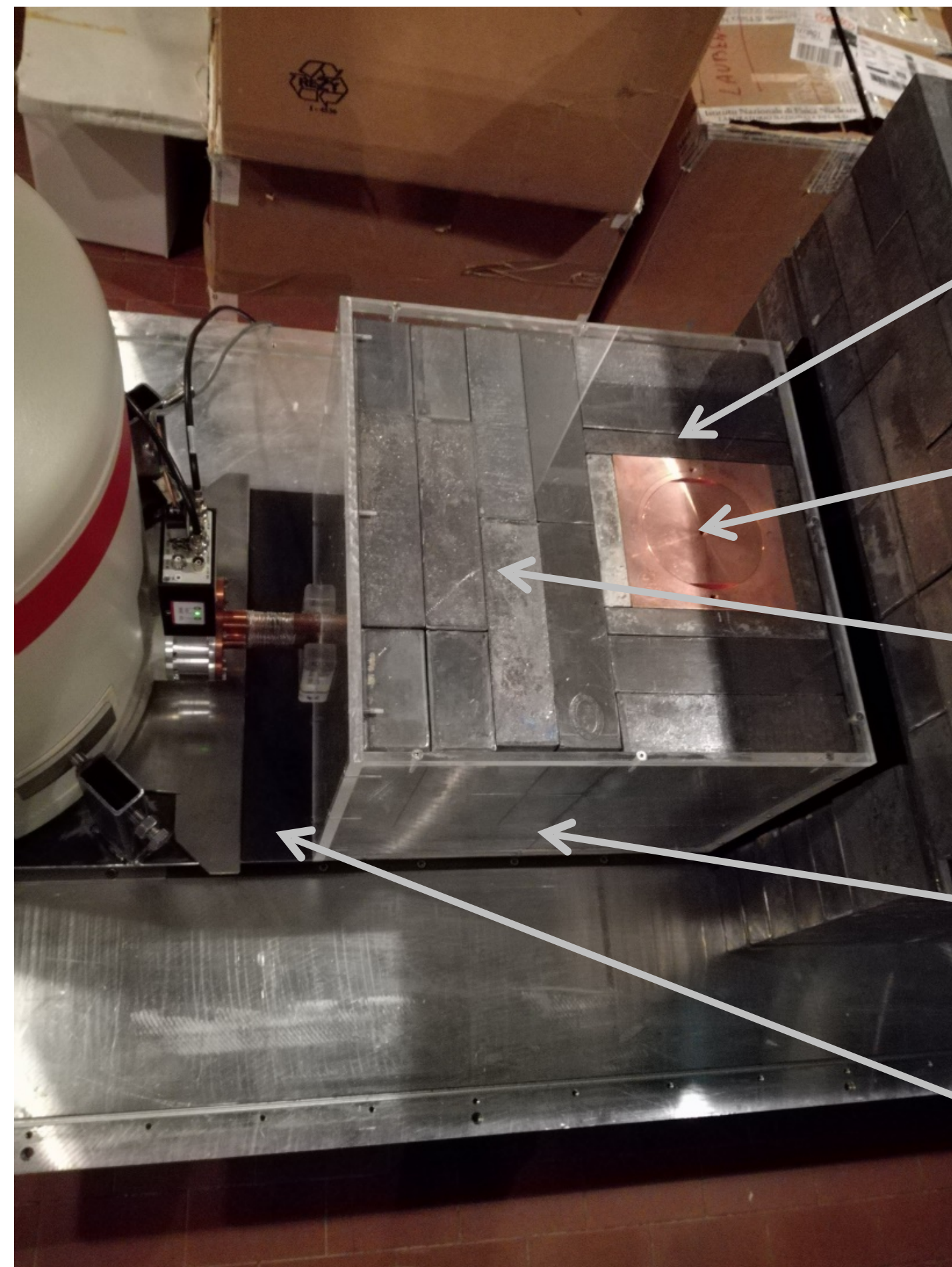


Total mass : **55.38 g** (99.5% grade)

Strip: 65 × 220 mm<sup>2</sup>  
thickness 0.25 mm

Disk: Ø65 mm  
thickness 0.25 mm

# Fast-movable part of passive shield



Roman lead (7 cm)

OFHC Copper shield (5 cm min)

Low-radioactivity lead (15 cm)

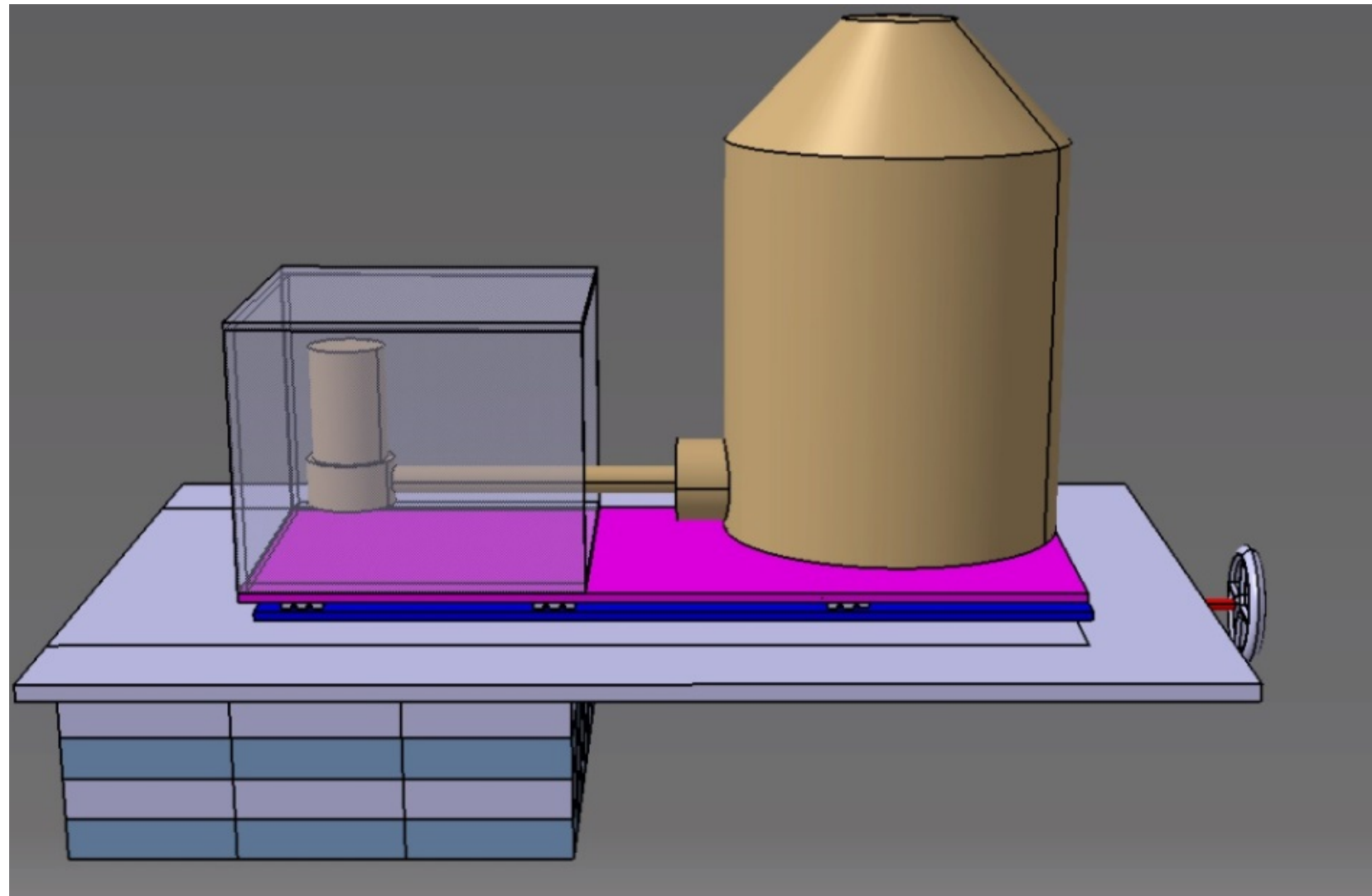
Plexiglas box 40×40×40 cm  
continuously flushed by N<sub>2</sub>

Stainless steel movable plate (1 cm)

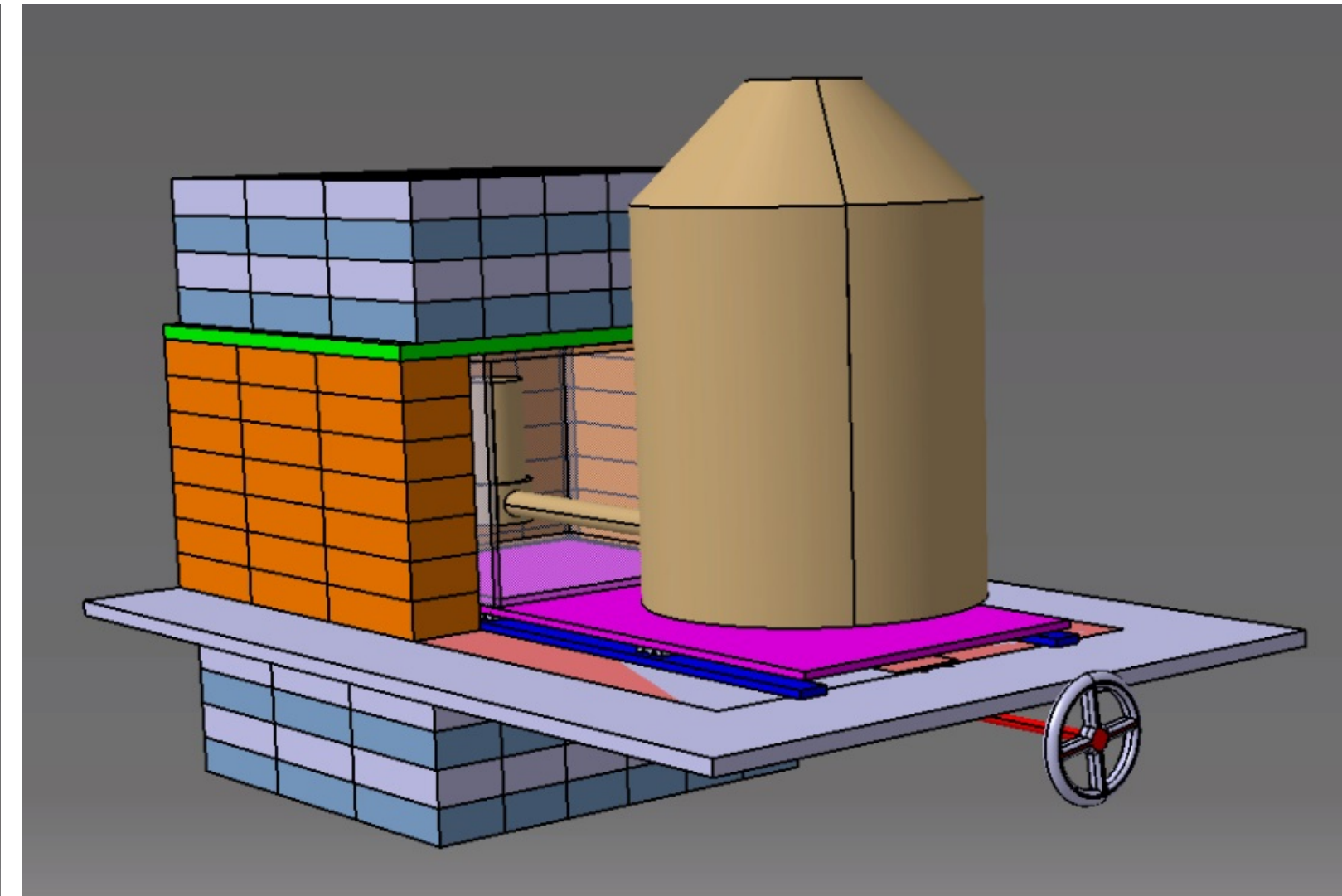
*S. Nagorny et al., JINST 16 (2021) 03, P03027*

# Fast-movable passive shield

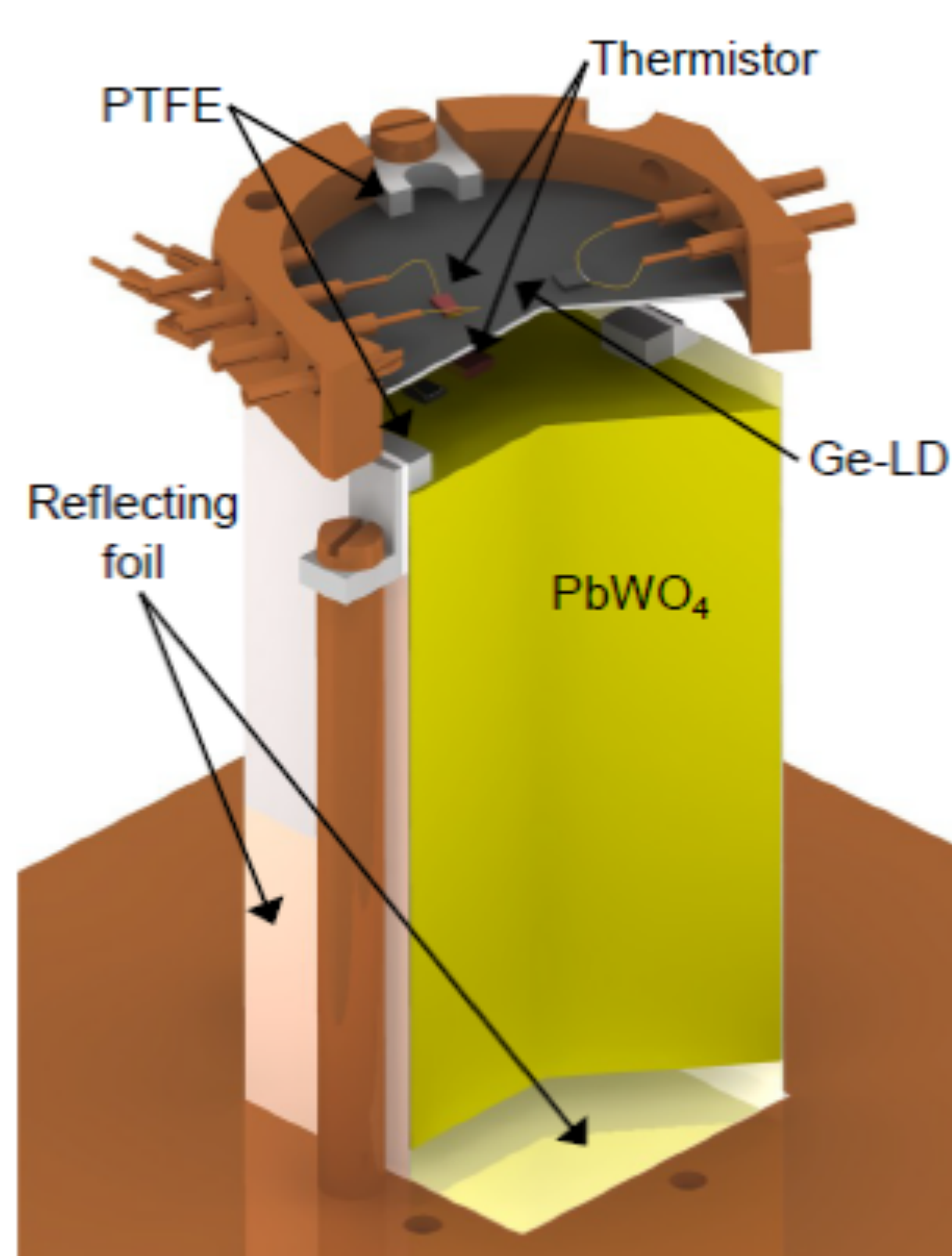
View of movable part



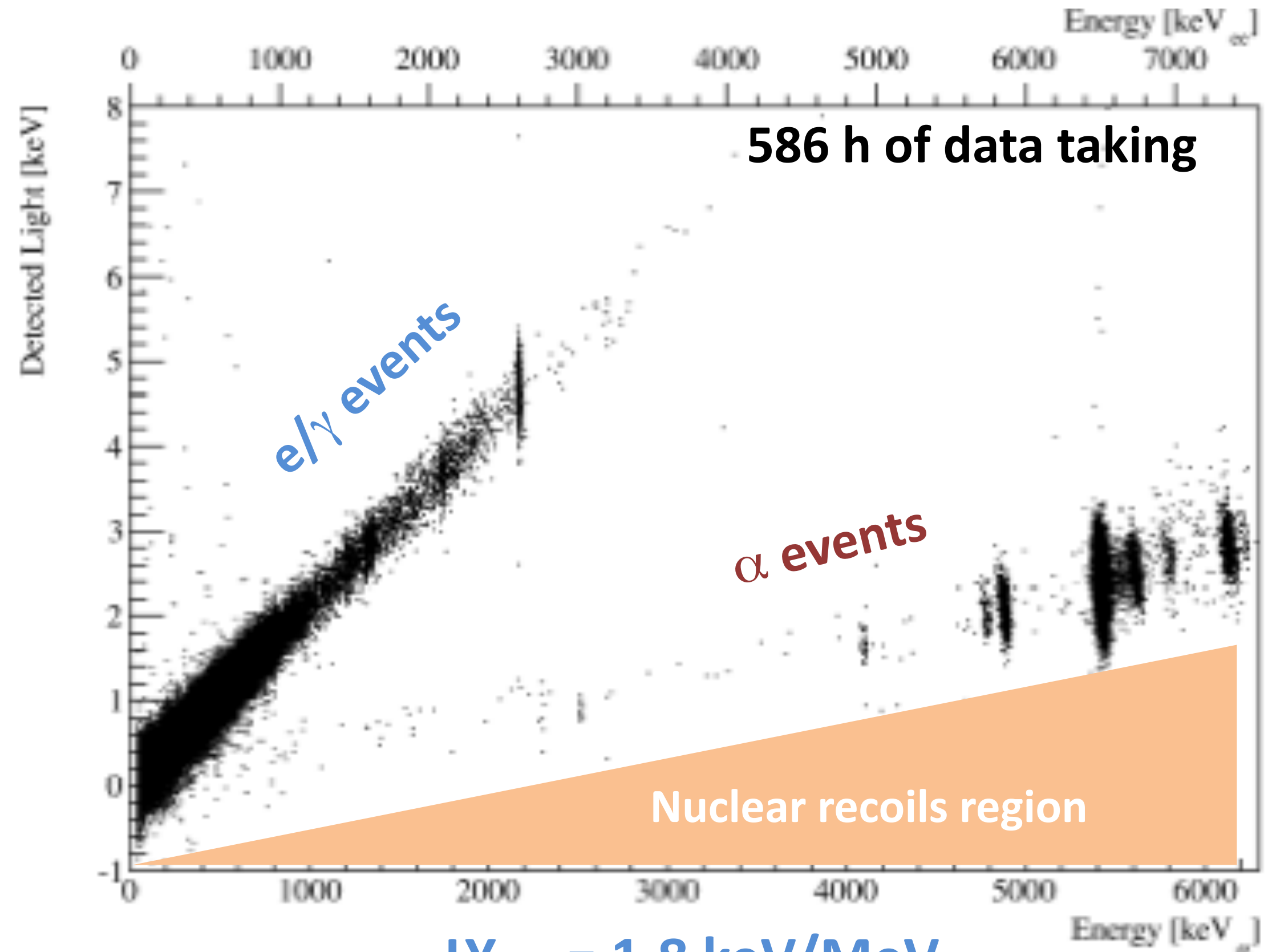
View of completed shield



# Experiment with $^{\text{arch}}\text{PbWO}_4$ scintillating bolometer to search for alpha decay of natural lead isotopes



**$\text{PbWO}_4$  crystal**  
**from archaeological lead**  
**454.1 g,  $3.0 \times 3.0 \times 6.1 \text{ cm}^3$**



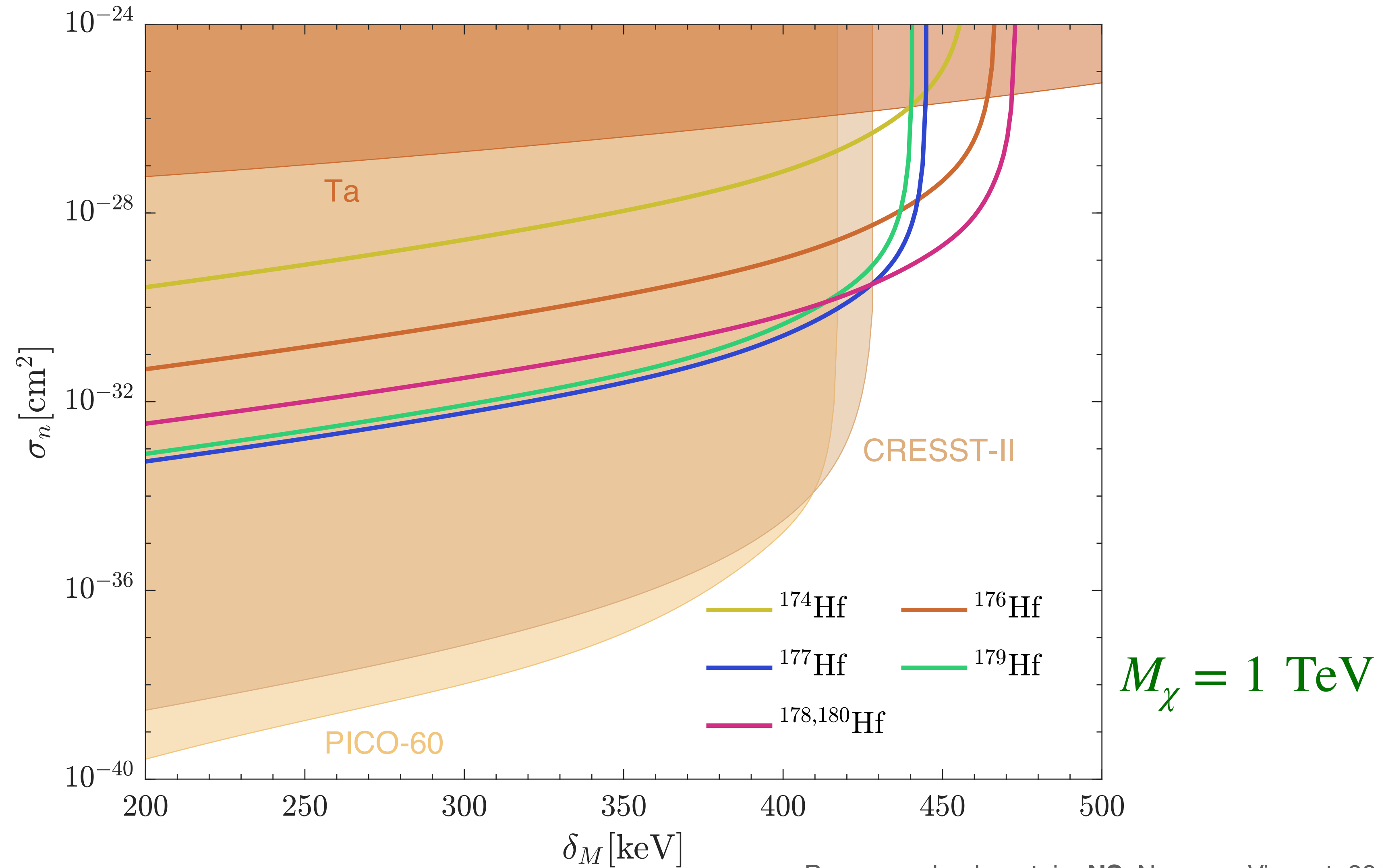
$$LY_{\gamma/\beta} = 1.8 \text{ keV/MeV}$$

$$LY_{\alpha} = 0.3 + 2.9 \times 10^{-5} E_{\alpha} \text{ keV/MeV}$$

**7 events with  $LY_{\text{n.r.}} < LY_{\alpha}$**

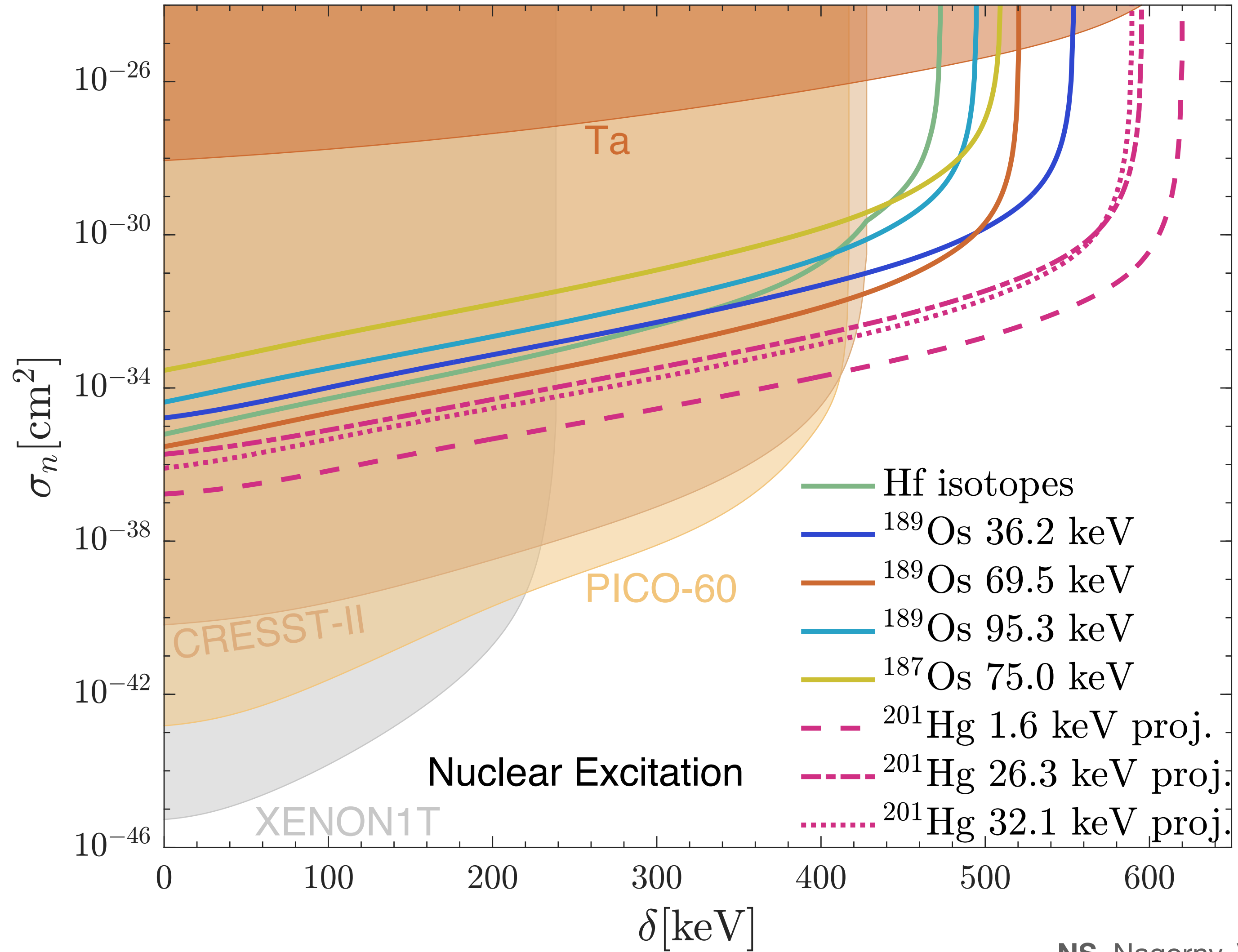
*J.W. Beeman et al., Eur. Phys. J. A 49 (2013) 50*

# Hf Bounds



Broerman, Laubenstein, **NS**, Nagorny, Vincent, 2012.08339

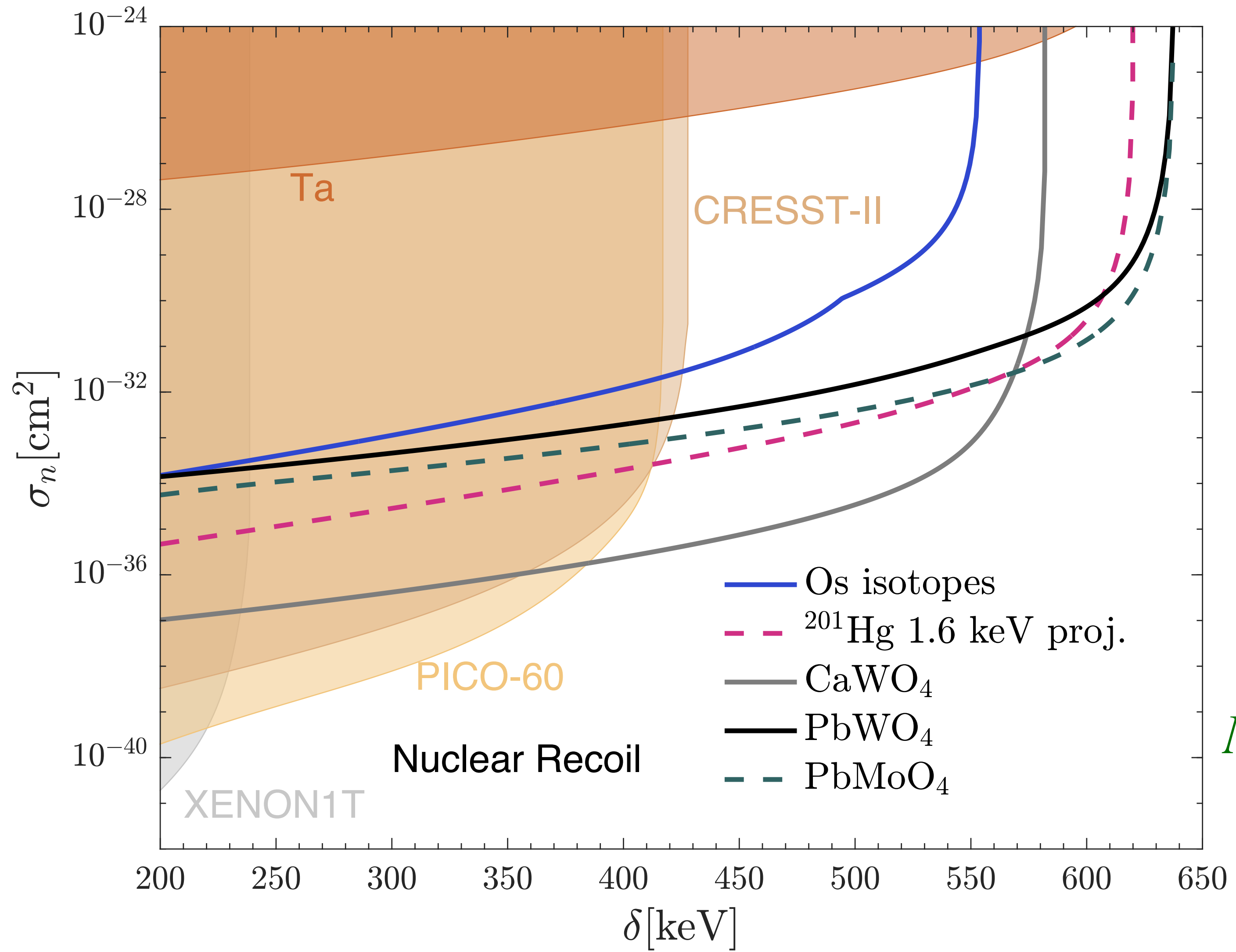
# More Nuclear Transitions



$M_\chi = 1$  TeV

NS, Nagorny, Vincent, 2104.09517

# PbMoO<sub>4</sub>



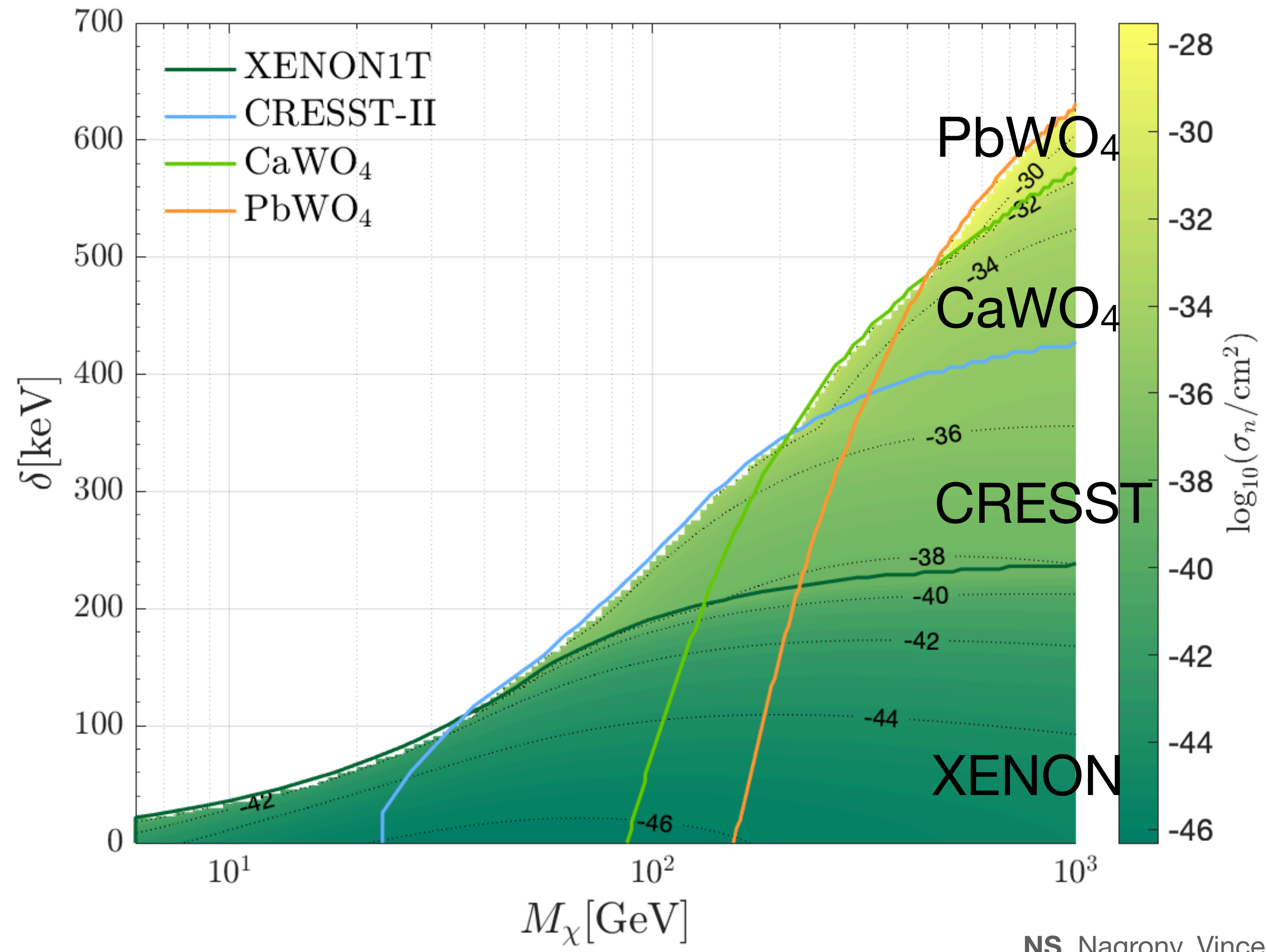


# Event Rate for Nuclear Excitation

- $$R = \sum_i N_{T_i} \frac{\rho_\chi}{M_\chi} \int_{v_{\min}}^{v_{\max}} dv v f(v) \int_{E_{R,\min}}^{E_{R,\max}} \frac{d\sigma_{\chi N}}{dE_R} dE_R$$
- $$S(\vec{q}) = \sum_L |\langle J_f || j_L(qr) Y_{LM}(\hat{r}) || J_i \rangle|^2$$
- $$B(E2) = \frac{1}{2J_i + 1} |\langle J_f || er^2 Y_2 || J_i \rangle|^2$$
- $$S(\vec{q}) = \frac{A^2}{Z^2} (2J_i + 1) j_2(qR)^2 \frac{B(E2)}{e^2 R^4}$$

$$\frac{d\sigma_{\chi N}}{dE_R} = \frac{\sigma_n M_N}{2v^2 \mu_{\chi n}^2} S(E_R)$$

# WIMPy Inelastic Dark Matter Window

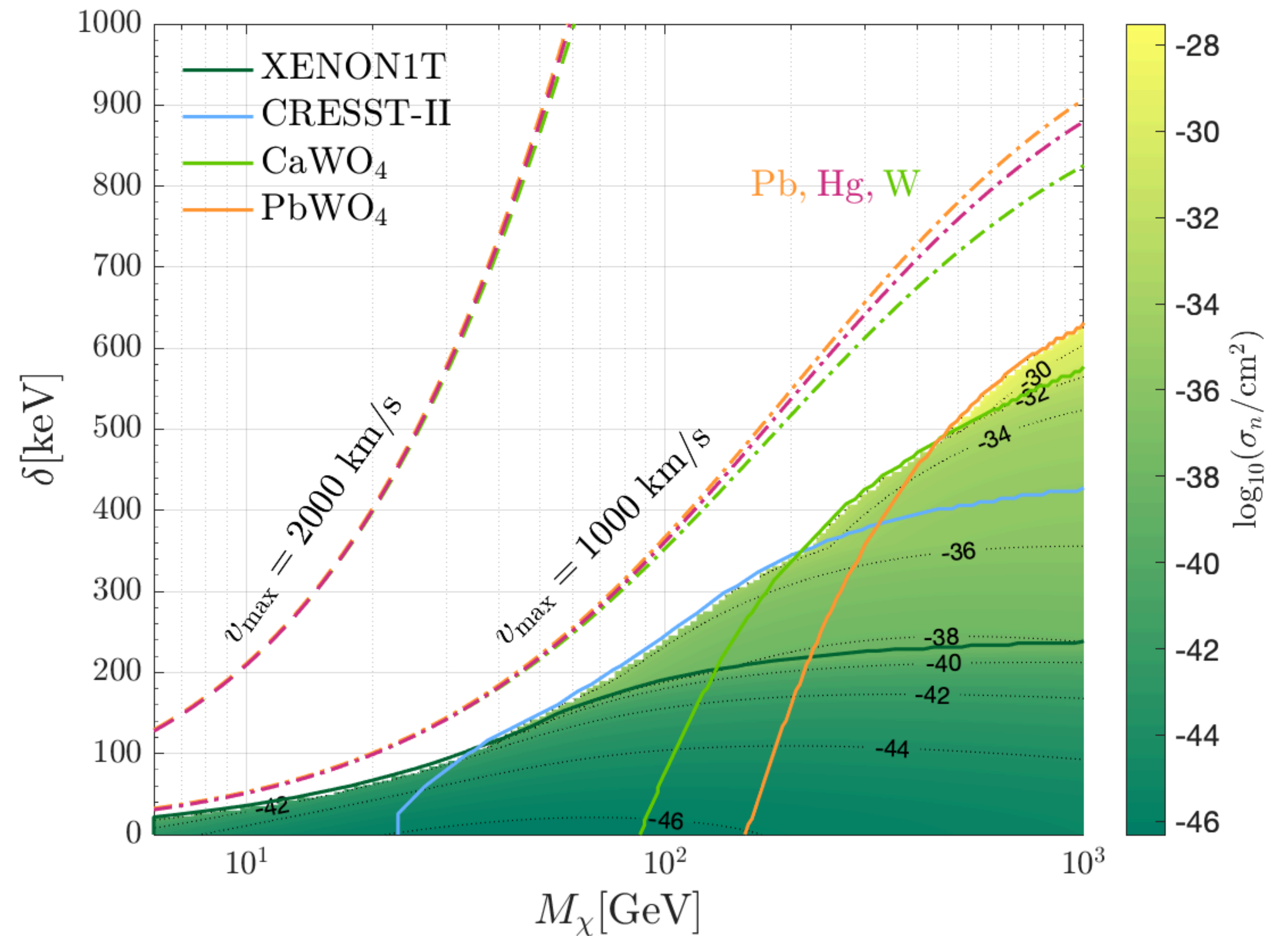


NS, Nagrony, Vincent, 2104.09517

# Boosted Dark Matter

- Cosmic-ray, neutrino up-scattering
- Stellar acceleration
- Annihilation, semi-annihilation
- Heavy DM decay

$$\delta_{\max} = \frac{1}{2} \mu_{\chi A} (v_e + v_{\text{esc}})^2$$



NS, Nagorny, Vincent, 2104.09517

# Loop Elastic Scattering

- Dark photon mediated DM

- $$\sigma_{n,\text{tree}} = \frac{16\pi\alpha\alpha_D\epsilon^2\mu_{\chi n}^2}{m_V^4}$$

- $$\sigma_{n,1\text{loop}} \sim \frac{\alpha^2\alpha_D^2\epsilon^4\mu_{\chi n}^4}{\pi m_V^6}$$

