

Off Equilibrium Effects on Kurtosis Along Strangeness-Neutral Trajectories

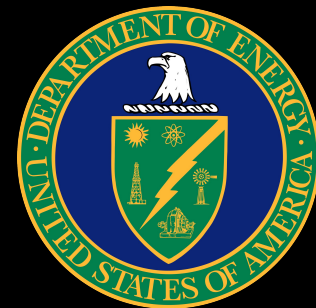
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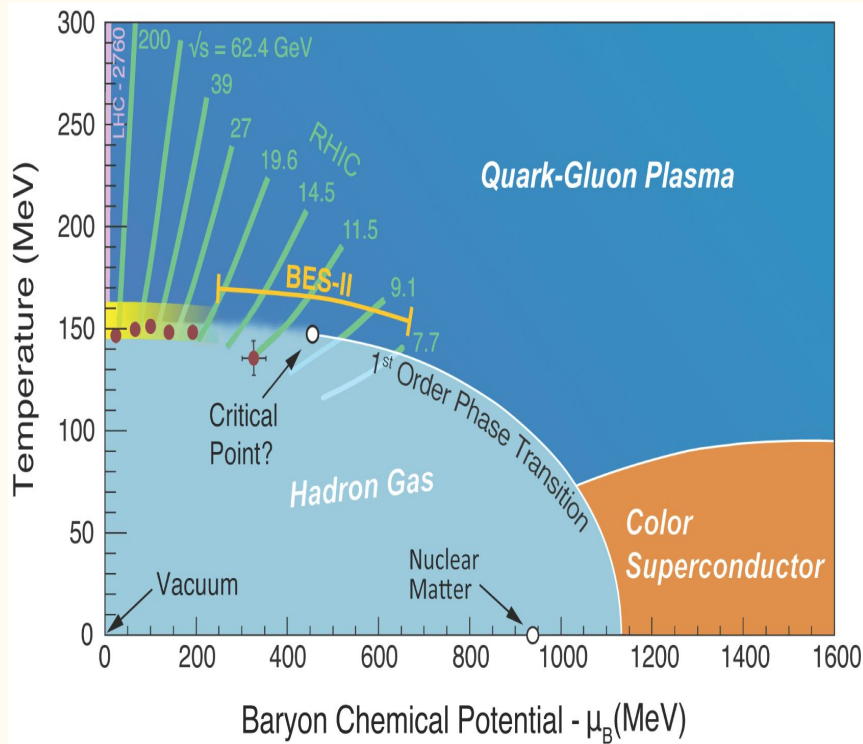


Work done with:

Jaki Noronha-Hostler, Jamie Karthein, Debora Mroczek,
Paolo Parotto, Claudia Ratti



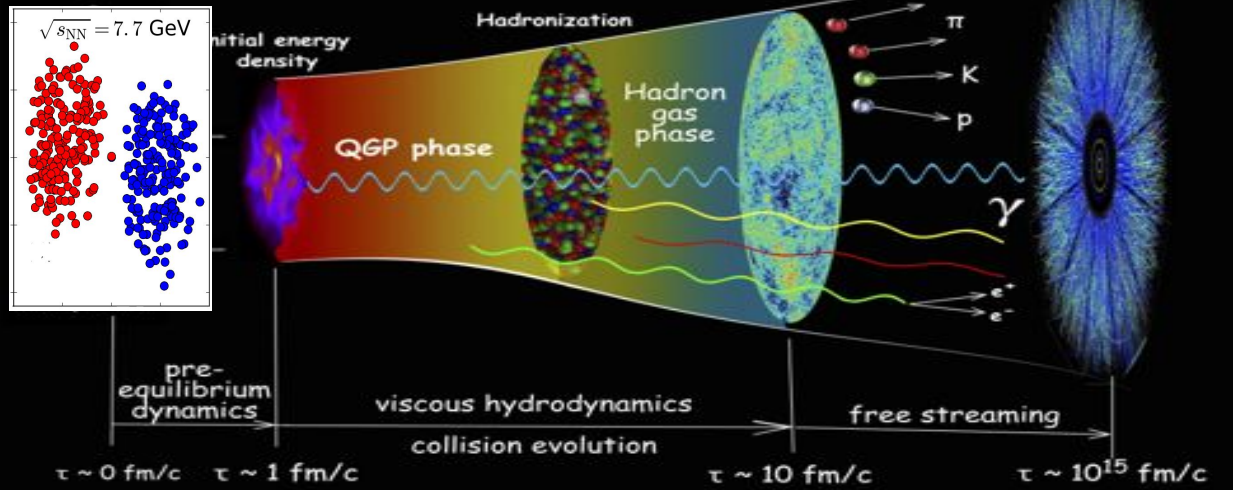
The Beam Energy Scan (BES)



- Main Objective:
Probe thermal behavior of QCD in Baryon rich regime
- Onset of criticality?
- Complicated by lower energies, finite lifetime, **out of equilibrium effects**

Relativistic Heavy-Ion Collisions

made by Chun Shen



Initial State

- Baryon Stopping (some work has been done)
C. Shen, B. Schenke *Phys.Rev. C* **97**
- Initializing full $T^{\mu\nu}$
 - Also problem at $\mu_B = 0$

Equation of State

- QCD EoS and Fermi Sign Problem

Freeze-out

- Need to conserve locally, not just on average
D. Oliinychenko, et al., *Phys. Rev.C* **102** (2020)
3
- Out of equilibrium corrections
 - Also problem at $\mu_B = 0$

Hydro Implementation

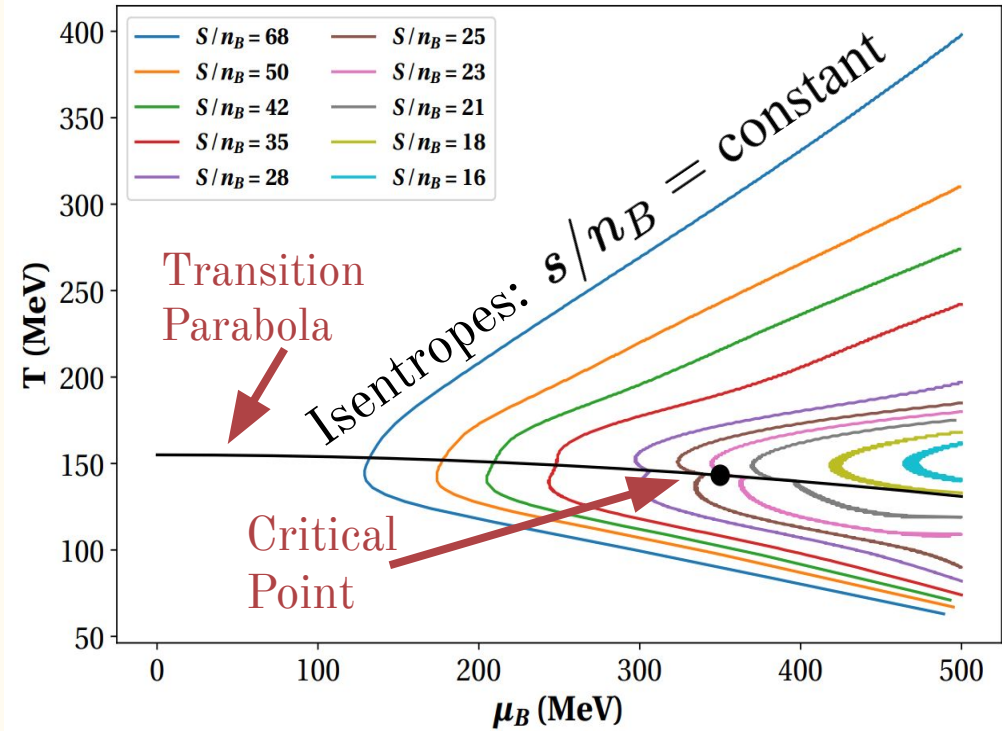
- (3+1)D with finite BSQ
- Transport Coefficients?
- Critical Fluctuations
- Correct Formulation?

This talk touches on these different areas of needed research

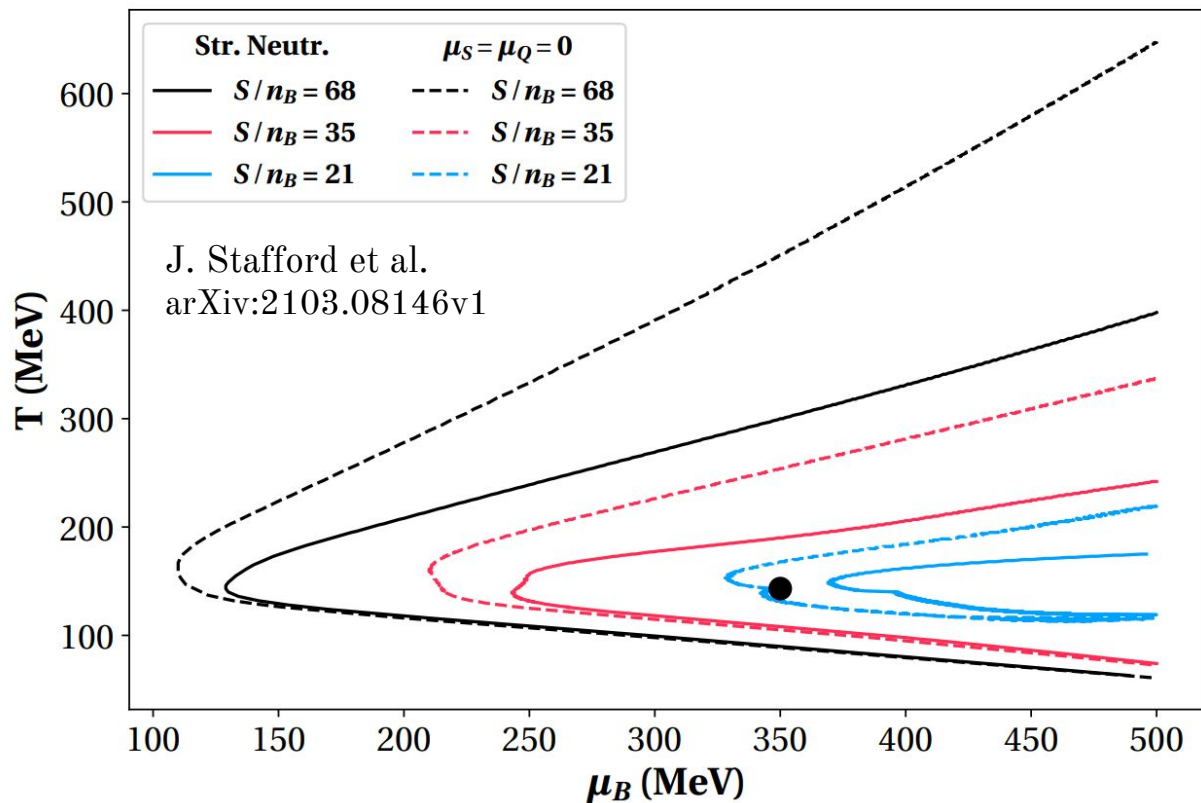
Phenomenological Tool:

Lattice QCD EoS with Parameterized CP (3D Ising University Class)

- Ideal hydrodynamics evolves along isentropic trajectories
- How do out of equilibrium effects influence trajectories?
- Interplay of EoS, Hydro and observables?



Enforcement Of Strangeness Neutrality:

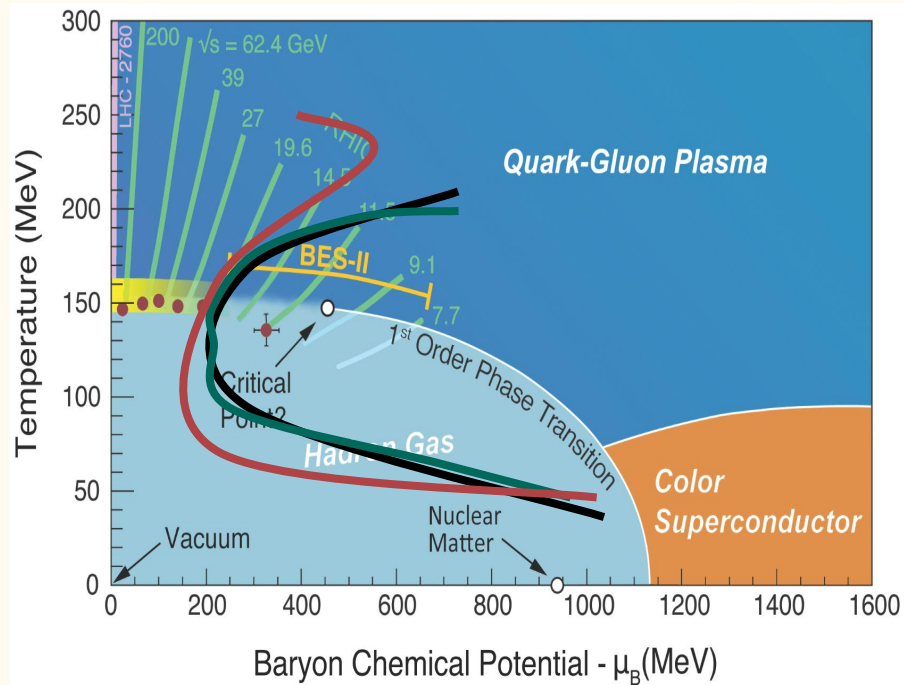


Enforcing the
condition (solid)
 $n_S = 0, n_Q = .4$

Leads to very
different
behavior
compared to
(dashed)

$\mu_S = 0, \mu_Q = 0$

An Evolving Hydrodynamic Picture



- Without viscous effects there is no entropy production. System evolves isentropically
- Close to equilibrium scenario may not alter trajectories dramatically
- Far from equilibrium effects may significantly affect trajectories.

Main Question:

For a given beam energy, how might the probed kurtosis change with an off equilibrium initial state?

This Work:

Qualitative study on kurtosis using a simplified hydrodynamic scenario

DNMR Equations of Motion

- ★ Independent and dynamic viscous currents that *relax* to Navier-Stokes values before equilibrium

Independent of initial energy distribution and flow!!

- ★ Energy conservation *requires* knowledge of EoS

Relaxation equations with boost invariance and polar symmetry:

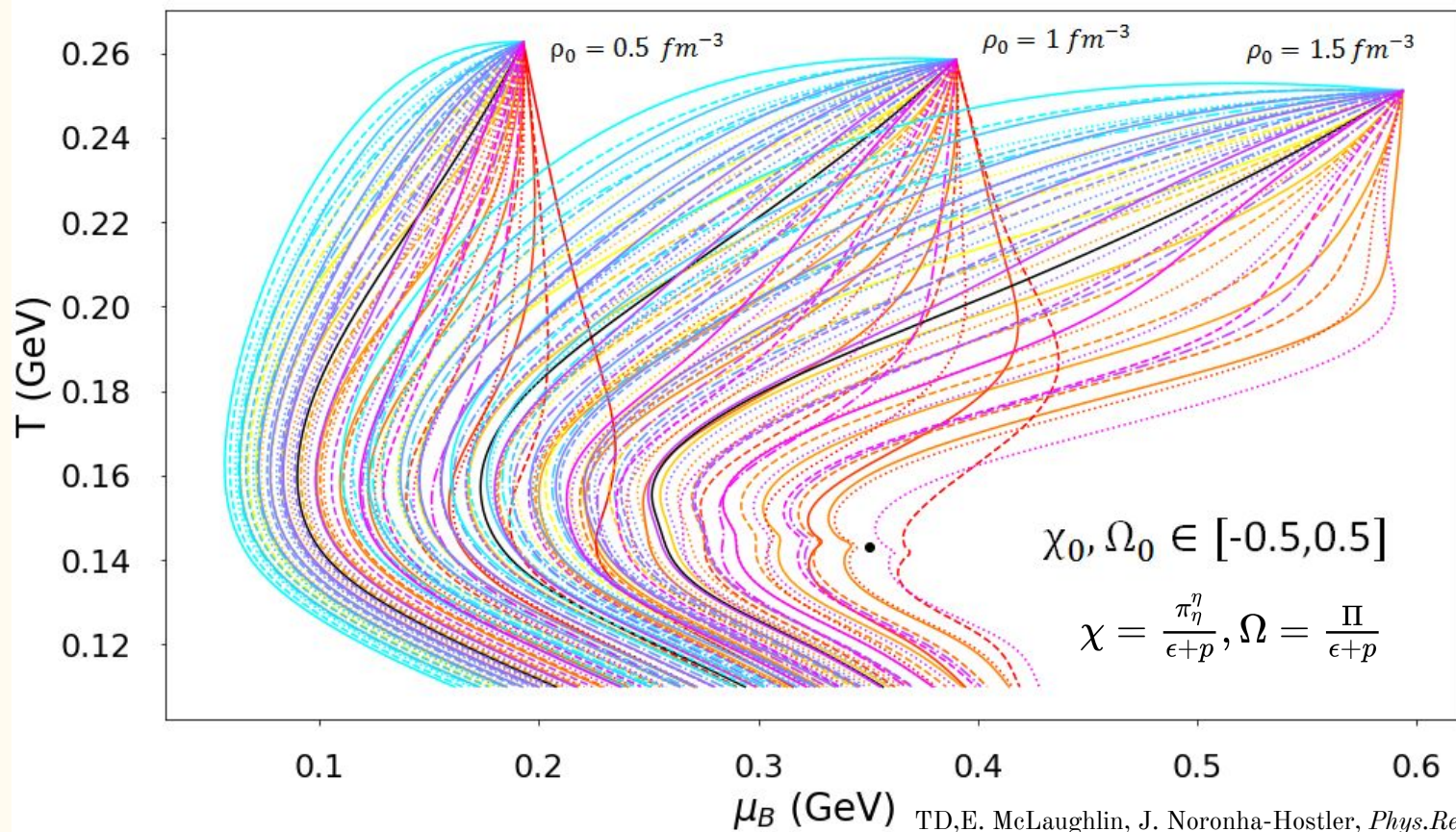
$$\tau_{\pi} \dot{\pi}_{\eta}^{\eta} + \pi_{\eta}^{\eta} = \frac{1}{\tau} \left[\frac{4\eta}{3} - \pi_{\eta}^{\eta} (\delta_{\pi\pi} + \tau_{\pi\pi}) + \lambda_{\pi\Pi} \Pi \right]$$

$$\tau_{\Pi} \dot{\Pi} + \Pi = -\frac{1}{\tau} \left(\zeta + \delta_{\Pi\Pi} \Pi + \frac{2}{3} \lambda_{\Pi\pi} \pi_{\eta}^{\eta} \right)$$

G. Denicol, et al, *Eur.Phys. J.A* 48 (2012)

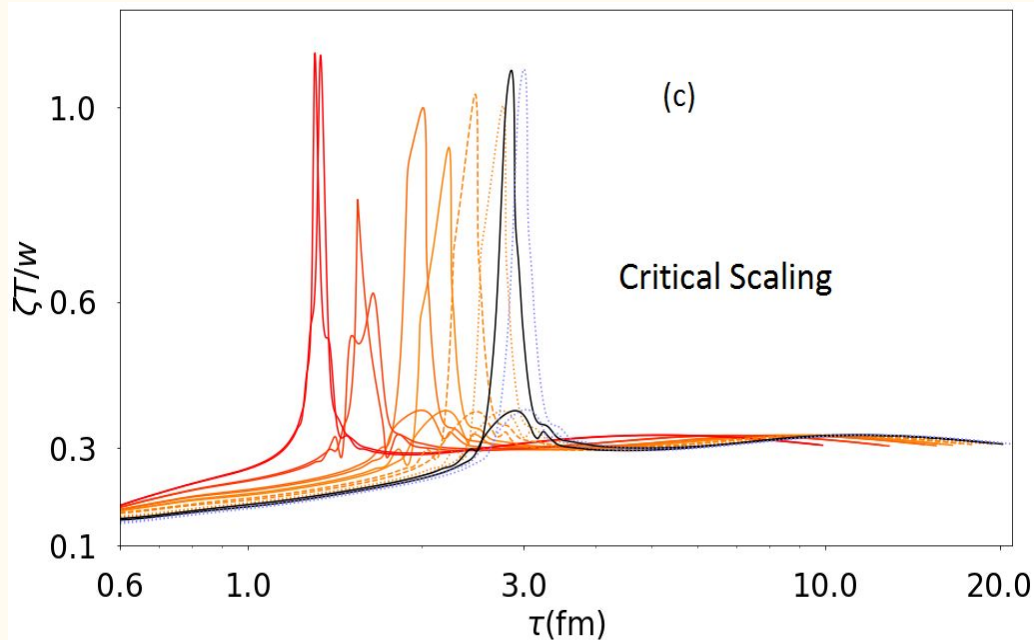
$$\dot{\epsilon} = -\frac{\epsilon + p + \Pi - \pi_{\eta}^{\eta}}{\tau} \quad \text{Where } p \text{ is the thermodynamic pressure}$$

Out Of Equilibrium Effects Are Important



Influence of Criticality on Bulk Viscosity

TD,E. McLaughlin, J. Noronha-Hostler, *Phys.Rev.D* 102 (2020) 7



Monnai, Akihiko et al,
Nucl. Phys.
,A967,2017

Critically Scaled Bulk:

$$\left(\frac{\zeta T}{w}\right)_{CS} = \frac{\zeta T}{w} \left[1 + \left(\frac{\xi}{\xi_0}\right)^3\right]$$

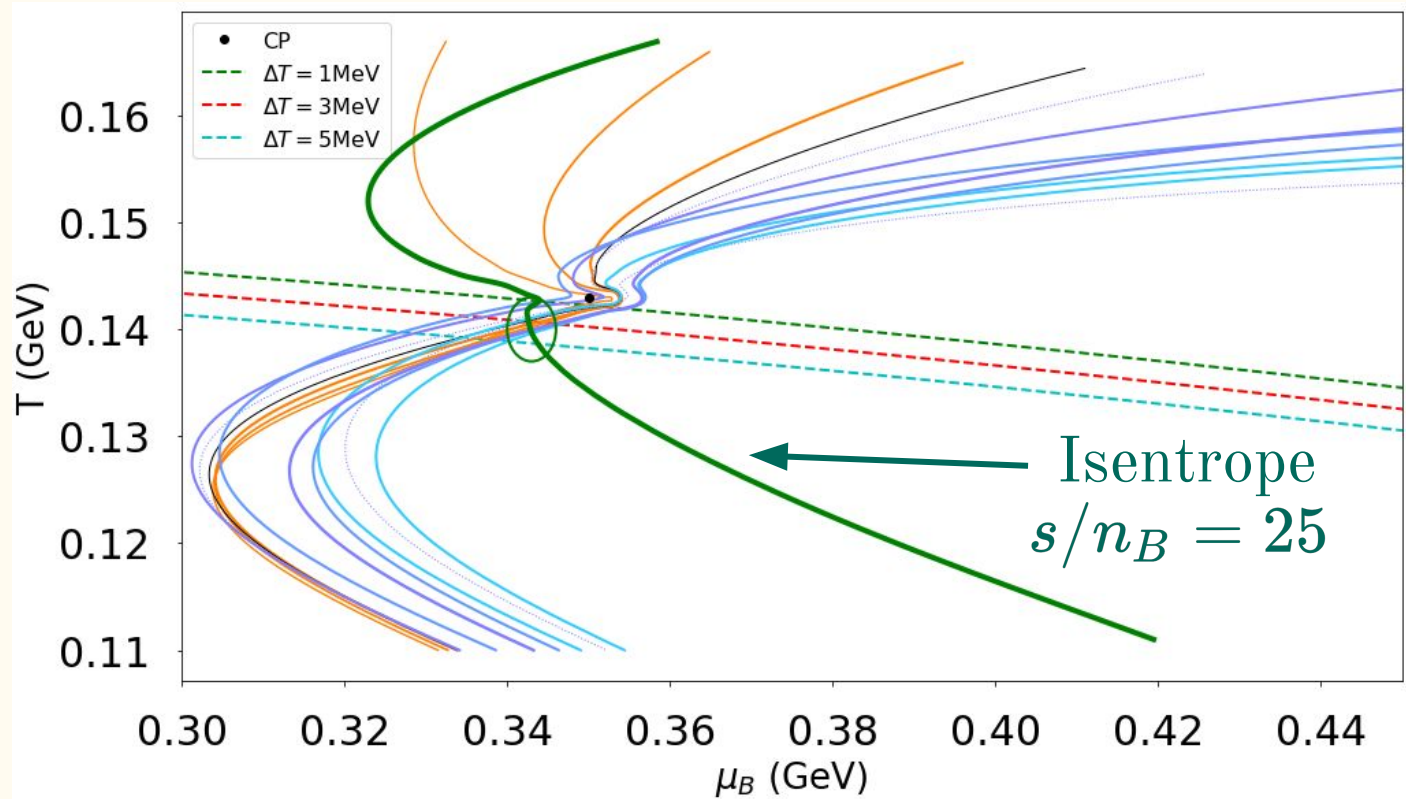
Correlation length ξ
diverges at the critical
point

Correlation length calculated in linear parametrization model

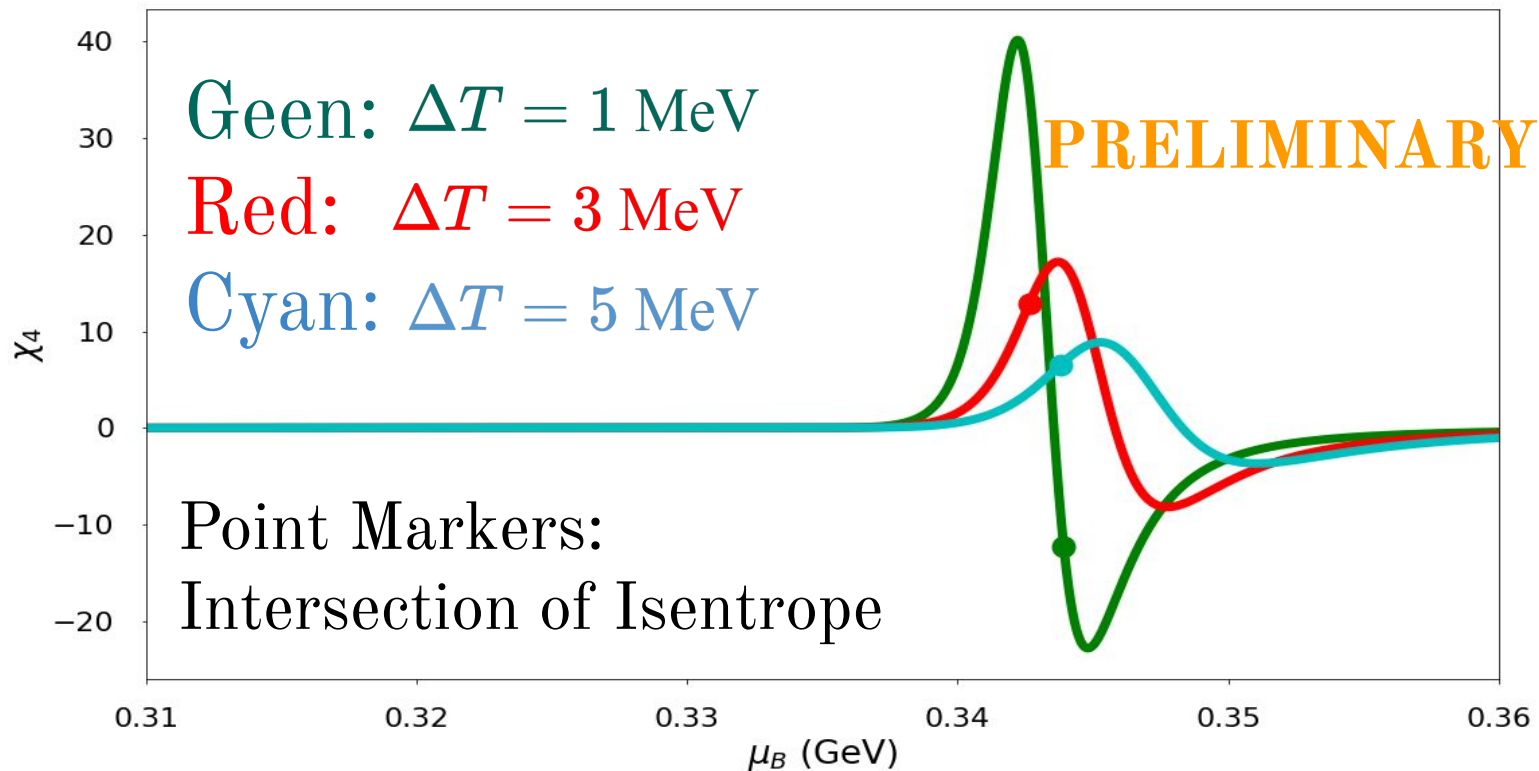
For more on transport coefficients see talk: E. McLaughlin, Bulk Correlations

Trajectories For Same Initial Energy

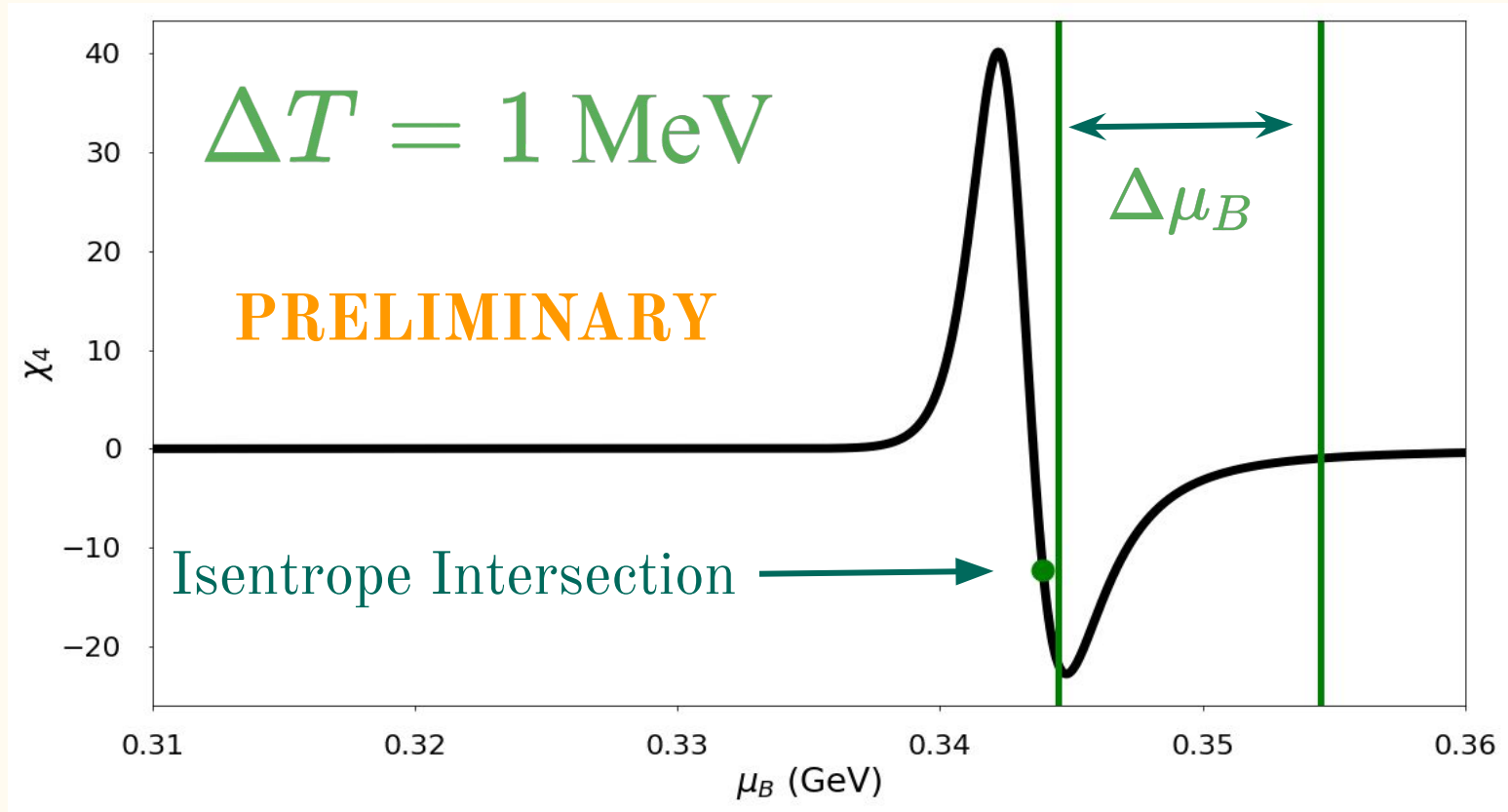
Shifted
Chiral
Transition
Lines
(by 1, 3,
and 5 MeV)
Are Plotted
As Dashed
Lines



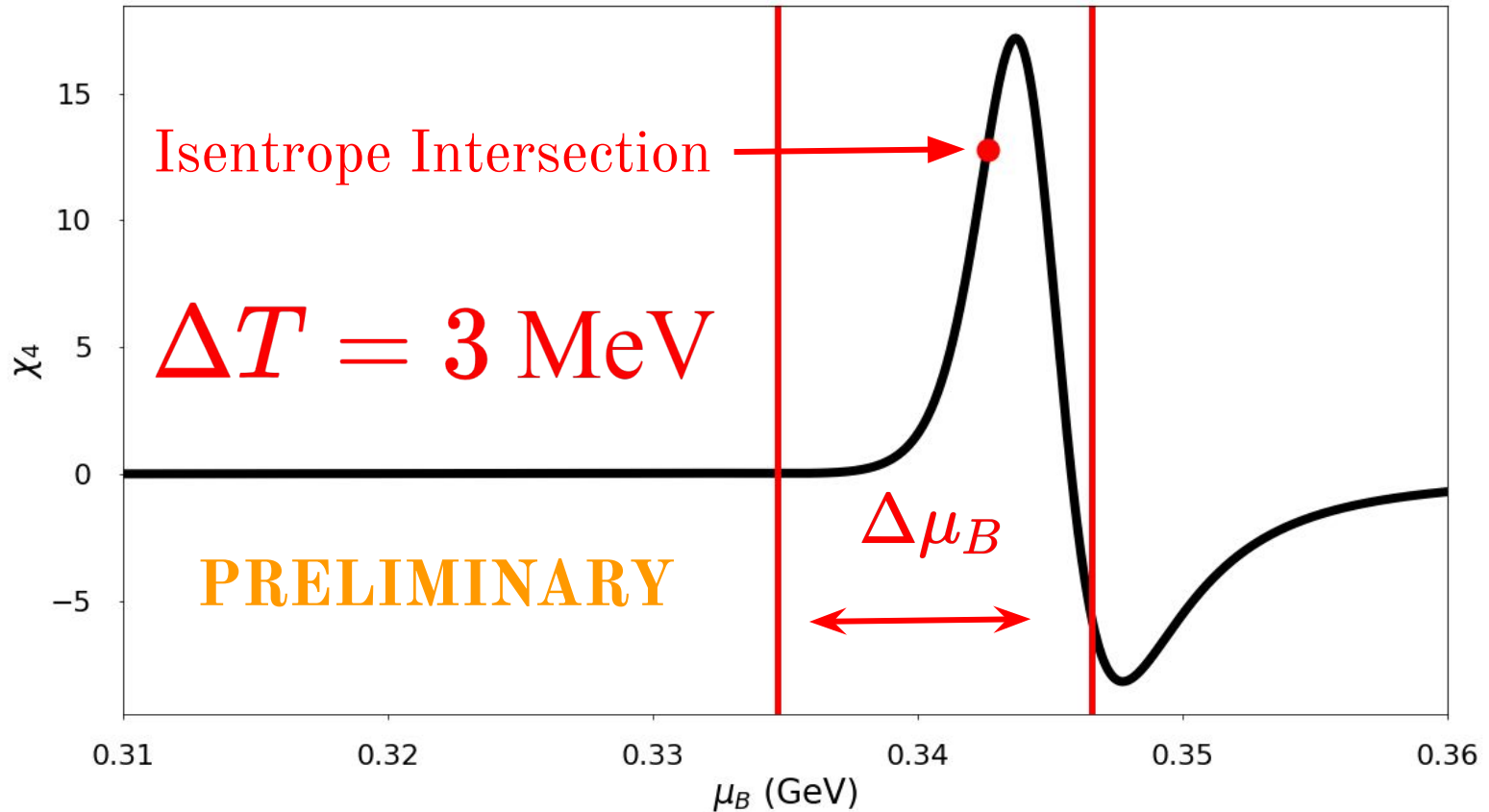
χ_4 Along Transition Parabola



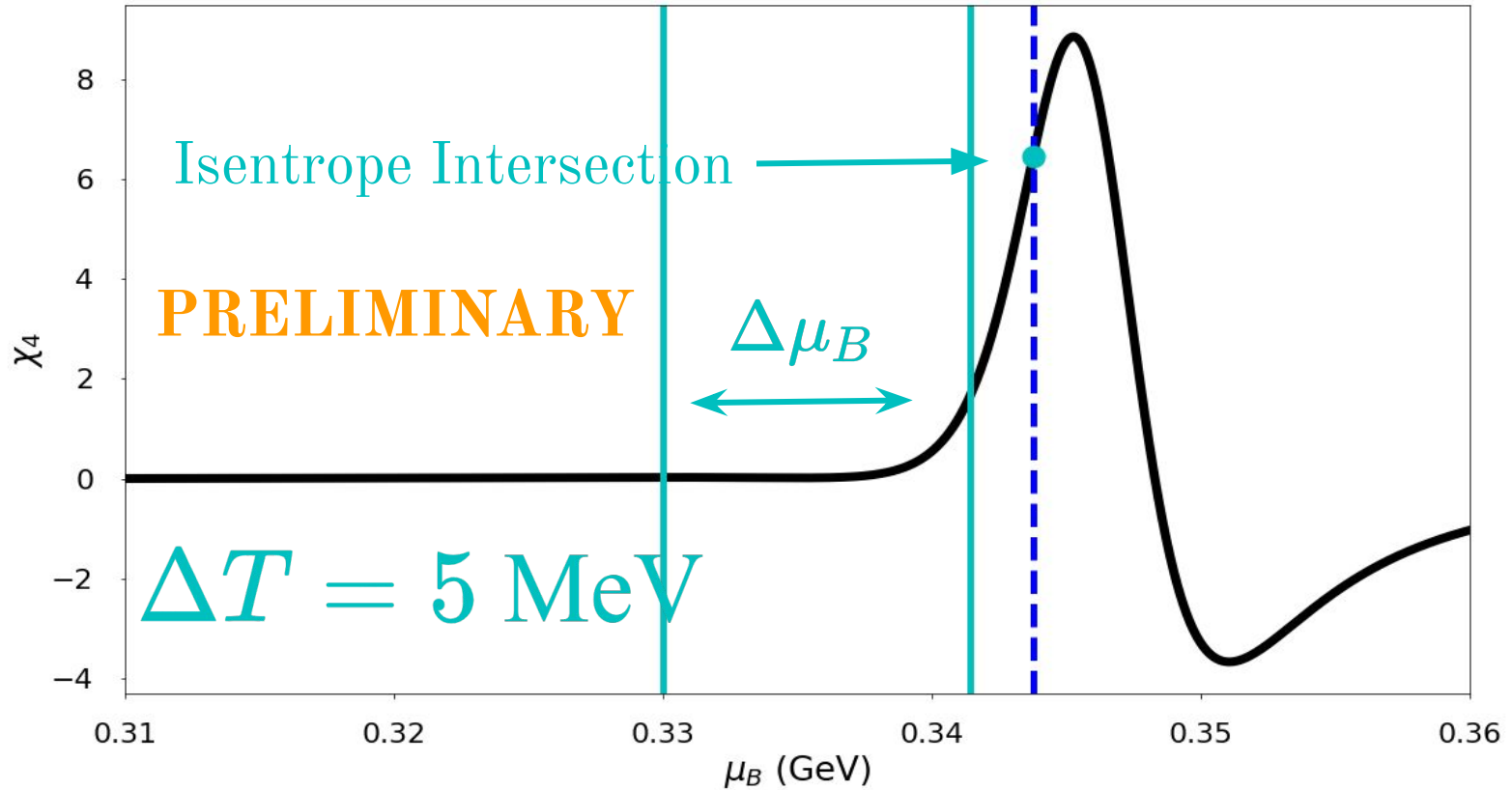
Range of χ_4 Given Off Equilibrium Initial State



Range of χ_4 Given Off Equilibrium Initial State

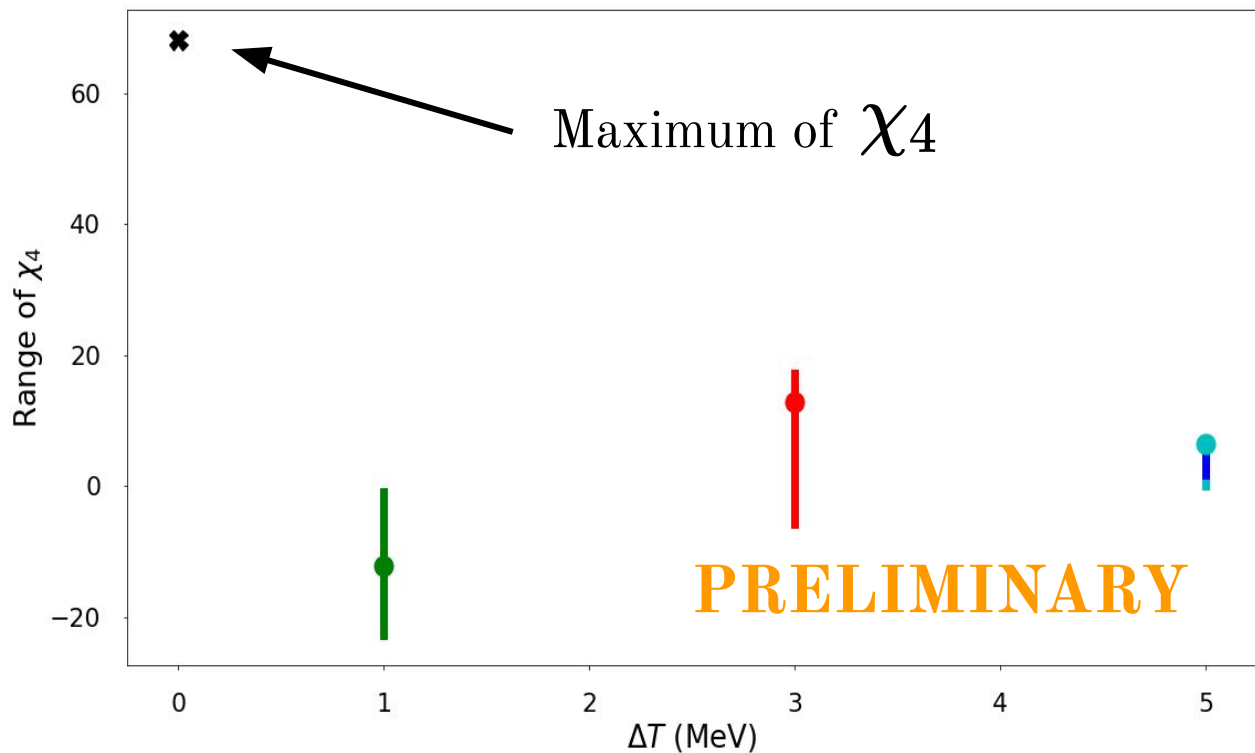


Range of χ_4 Given Off Equilibrium Initial State



Max and Min of Probed Off Equilibrium χ_4

Takeaway:
Out of equilibrium effects lead to spread in χ_4 probed on event-by-event basis



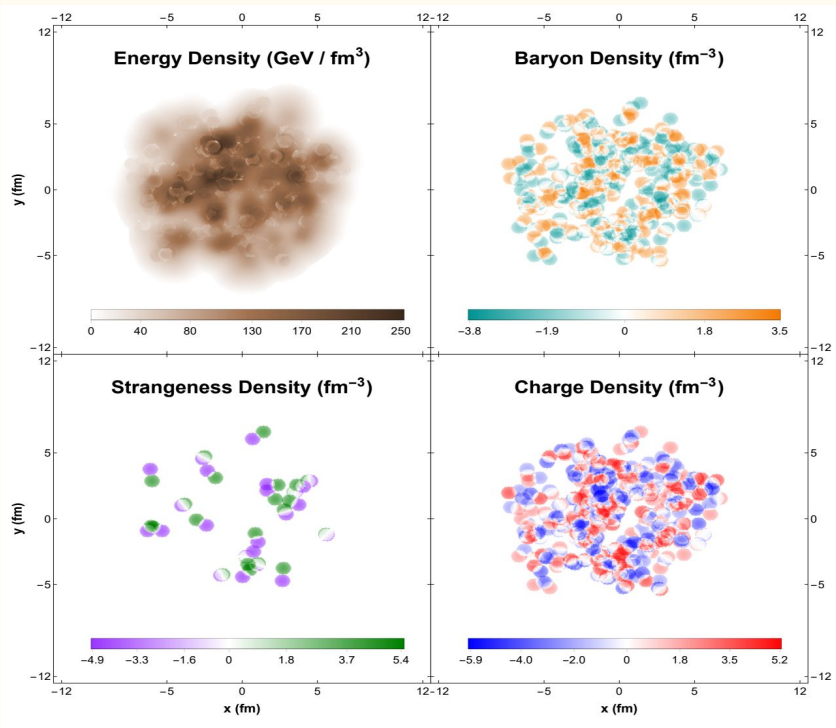
Conclusions

- Initial state effects have important consequences on hydro evolution, and thus probed observables
- Out of equilibrium effects leads to EbE spread at freeze out
- Much more dynamic modeling needs to be done
 - See talk V. Vovchenko (earlier this session)

Backup Slides

Next Steps towards BES Hydrodynamics

Start with what we know: LHC energies and **ICING** **Initializing**
Conserved
Charges
in Nuclear
Geometries



Initializing charges at 0
net density allows study
of diffusion in a better
controlled environment

M. Martinez, et al., arXiv:1911.12454

M. Martinez, et al., arXiv:1911.10272

Requirements:

- (2+1) dimensional Hydro
 - V-USPhydro
- 4D EoS Noronha-Hostler, et al. *Phys.Rev.C 100* (2019)
 - $\{\epsilon, \rho_B, \rho_Q, \rho_S\} \rightarrow \{T, \mu_B, \mu_Q, \mu_S\}$

For more on ICING, see poster: Carzon (session 0)

$$\tau_\pi \dot{\pi}_\eta^\eta + \pi_\eta^\eta = \frac{4\eta}{3\tau} - \frac{\eta T \pi_\eta^\eta}{2} \left(\frac{\beta_\pi}{\tau} + \dot{\beta}_\pi \right)$$

$$\tau_\Pi \dot{\Pi} + \Pi = -\frac{\zeta}{\tau} - \frac{\zeta T \Pi}{2} \left(\frac{\beta_\Pi}{\tau} + \dot{\beta}_\Pi \right)$$

$$\beta_\pi = \frac{\tau_\pi}{2\eta T}$$

$$\beta_\Pi = \frac{\tau_\Pi}{\zeta T}$$

$$\dot{\epsilon} = -\frac{1}{\tau} [\epsilon + p + \Pi - \pi_\eta^\eta]$$

$$\tau_\pi \dot{\pi}_\eta^\eta + \pi_\eta^\eta = \frac{1}{\tau} \left[\frac{4\eta}{3} - \pi_\eta^\eta (\delta_{\pi\pi} + \tau_{\pi\pi}) + \lambda_{\pi\Pi} \Pi \right]$$

$$\tau_\Pi \dot{\Pi} + \Pi = -\frac{1}{\tau} \left(\zeta + \delta_{\Pi\Pi} \Pi + \frac{2}{3} \lambda_{\Pi\pi} \pi_\eta^\eta \right)$$

$$\dot{\rho} = -\frac{\rho}{\tau}$$

$$\tau_\pi = \frac{5\eta}{\epsilon + p}$$

$$\tau_\Pi = \frac{\zeta}{15(\epsilon + p) \left(\frac{1}{3} - c_s^2 \right)^2}$$

$$\lambda_{\pi\Pi} = \frac{6}{5} \tau_\pi$$

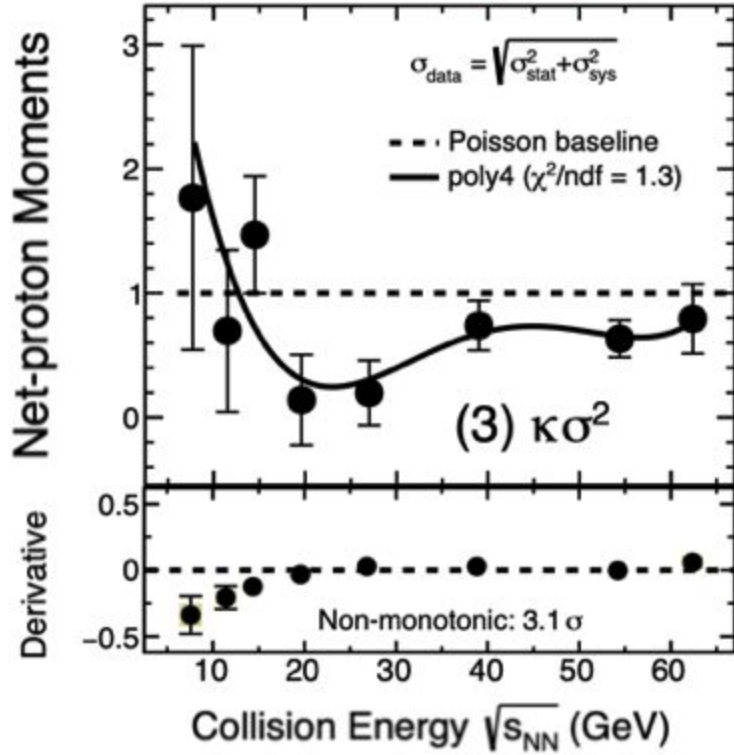
$$\delta_{\pi\pi} = \frac{4}{3} \tau_\pi$$

$$\tau_{\pi\pi} = \frac{10}{7} \tau_\pi$$

$$\lambda_{\Pi\pi} = \tau_\Pi \frac{8}{5} \left(\frac{1}{3} - c_s^2 \right) \tau_\Pi$$

$$\delta_{\Pi\Pi} = \frac{2}{3} \tau_\Pi$$

Central Au+Au - STAR (2021): 2101.12413



Keeping Track of Reference Density: Example

$$\Pi + \tau_{\Pi} \frac{d}{d\tau} \Pi + = -\zeta \theta \implies \frac{\Pi}{\sigma} + \tau_{\Pi} \frac{d}{d\tau} \left(\frac{\Pi}{\sigma} \right) = -\frac{\zeta}{\sigma} \theta$$

$$\frac{\Pi}{\sigma} + \tau_{\Pi} \frac{1}{\sigma} \frac{d}{d\tau} \Pi + \tau_{\Pi} \Pi \frac{d}{d\tau} \frac{1}{\sigma} = -\frac{\zeta}{\sigma} \theta$$

$$\Pi + \tau_{\Pi} \frac{d}{d\tau} \Pi + \tau_{\Pi} \Pi \sigma \frac{d}{d\tau} \frac{1}{\sigma} = -\zeta \theta$$

Use relation

$$\sigma \frac{d}{d\tau} \frac{1}{\sigma} = \theta$$

$$\Pi + \tau_{\Pi} \frac{d}{d\tau} \Pi + = -(\zeta + \tau_{\Pi} \Pi) \theta$$

Extra
term
unique to
SPH

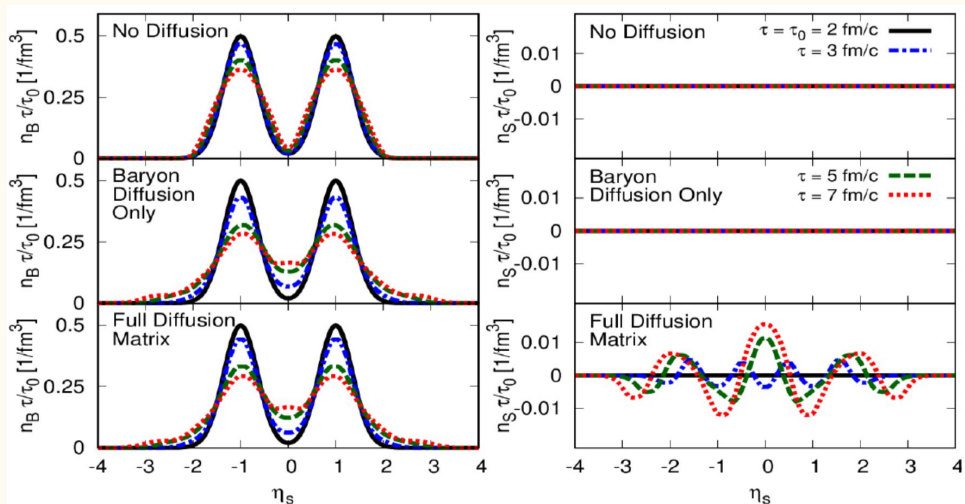
Relativistic Coupled Diffusion

Generalization: *for* $q, l \in \{B, S, Q\}$

Greif, Fotakis et al., PRL 120, 242301 (2018)

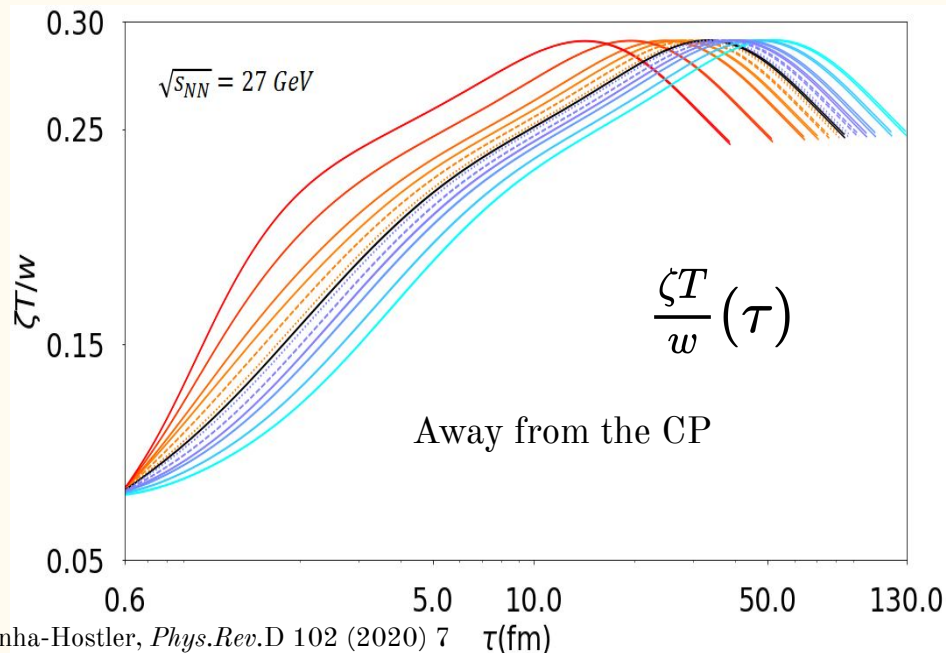
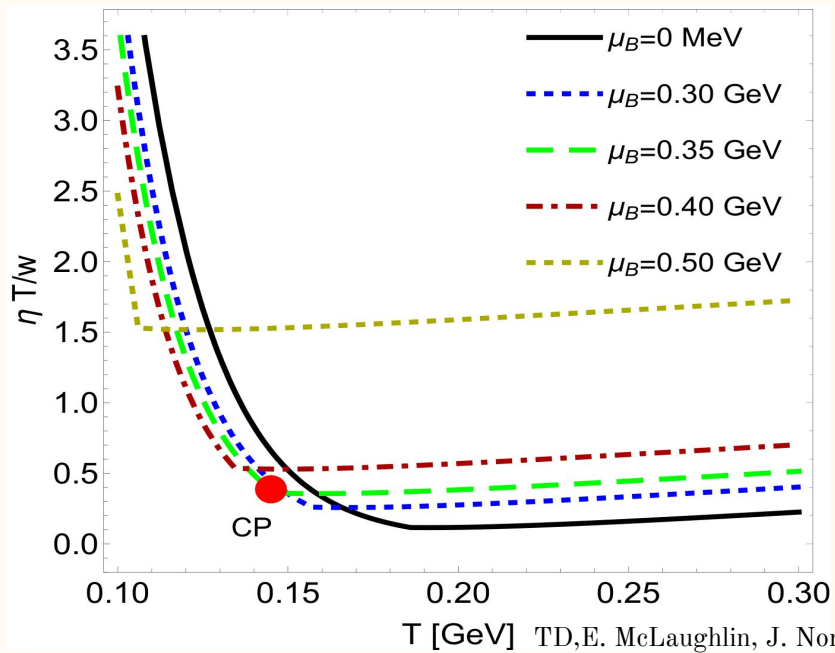
Fotakis, Greif et al., PRD 101, 076007 (2020)

$$\tau_q \dot{n}_q^\mu + n_q^\mu = \kappa_q \nabla^\mu \alpha_q \Rightarrow \sum_l \tau_{ql} \dot{n}_l^\mu + n_q^\mu = \sum_l \kappa_{ql} \nabla^\mu \alpha_l$$



(2+1) SPH equations
for Israel-Stewart
currently being derived
and implemented into
existing v-USPhydro
code

Transport Coefficient Behavior



Shear viscosity not sensitive to criticality explicitly

Bulk viscosity away from CP shows similar behavior