



Muon Track Reconstruction: Likelihood Analysis

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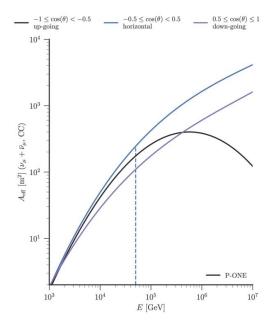


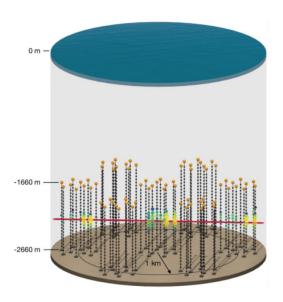






- Produce Effective Area/Volume Plots of P-ONE.
 - Need a reconstruction method.





Simulation







- ICECUBE Software on Illume
- NuGen
- Clsim
- Pentagon Geometry:
 - 100 meters between strings
 - 40 meters between DOMs
 - 19 DOMs per string
 - 10 strings
- 400,000 Events ranging from 100 GeV 10,000 GeV

Reconstruction







- LineFit
 - -Simple Chi-squared fit of a line to position-time of hits.

- Likelihood Fit
 - -Statistical fit on hits of DOMs.

Likelihood Reconstruction







$$p(\vec{x}|\vec{\theta})$$

$$t_{\rm res} = t_{\rm hit} - t_{\rm geo}$$

$$\mathcal{L}(\vec{\theta}) = \prod_{i} p(\vec{x}_i | \vec{\theta})$$

$$\mathcal{L}(\vec{\theta}) = \prod p(\vec{x}_i | \vec{\theta}) \quad \ell(\vec{\theta}) = -\log(\mathcal{L}(\vec{\theta}))$$

Likelihood Reconstruction







- Will be minimizing to find result.
- Minuit
 - -Give initial guess of LineFit
 - Loops over track parameters

Muon Track





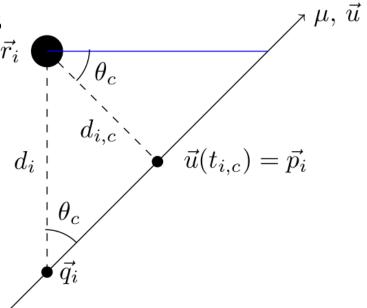


• Simple geometric derivations

 Rests on finding distance of closest approach

$$d_{i} = \frac{d_{i,c}}{\sin \theta_{c}}$$

$$t_{i,\text{geo}} = \frac{d_{i,c}}{\sin \theta_{x} \cdot c} + \frac{|\vec{q}_{i} - \vec{q}_{0}|}{c}$$



Muon Track



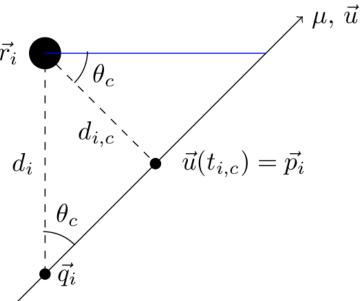




• Simple geometric derivations

 Rests on finding distance of closest approach

$$d_{i,c} = |(\vec{r} - \vec{x}) - ((\vec{r} - \vec{x}) \cdot \hat{v})\hat{v}|$$

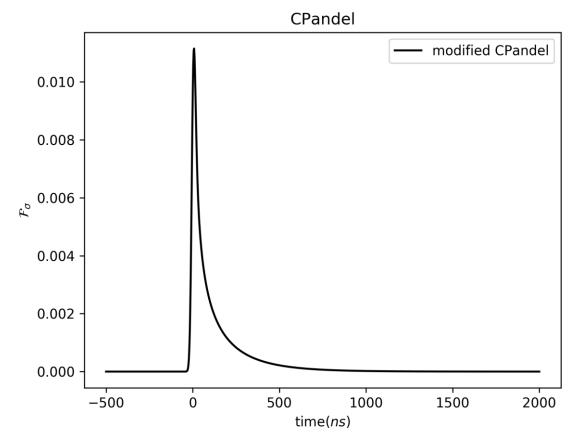


Likelihood Distribution







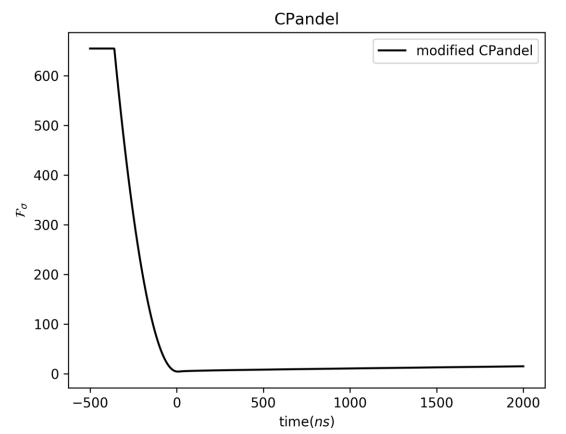


Likelihood Distribution







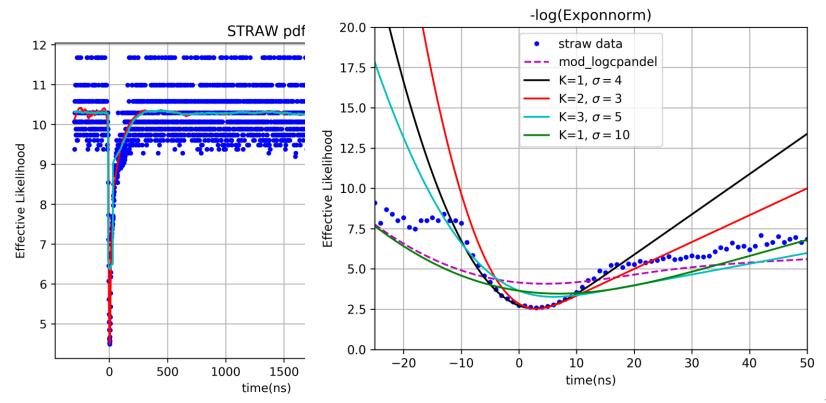


Likelihood Distribution







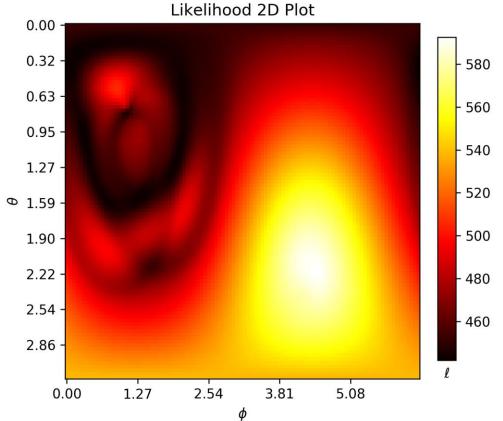


Testing Likelihood









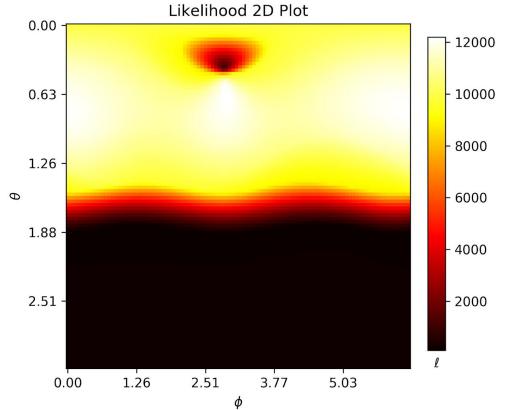
- ~60 hit DOMs
- Fixed at True Vertex
- True direction (phi, theta) = (1.10, 0.81)

Testing Likelihood









- <10 hit DOMs
- Fixed at True Vertex
- True direction
 (phi, theta) = (2.84, 0.31)

Testing Likelihood







- Minuit Misbehaves
 - -Gets pulled by other minima
- Likelihood Distribution needs some fine-tuning
- Finnicky, but looks hopeful!

Future Goals







Account for charge of hits

- Thomas McElroy has written some code for this
- Uses charge and acceptance angle
- Should help with lower hit counts

Fine tune Likelihood Distribution

- Need to account for emission point distance
- Something more accurate for water (fit to POCAM data)