
 x05



 51

000151730

 233



Higgs in the Swampland

Nathaniel Craig
UC Santa Barbara



 x05

○○○

51

000151730

233



The Naturalness Strategy

Param	UV sensitivity	Natural if	NP	Scale	Natural?
" m_e "	$e^2 \Lambda$	$\Lambda \lesssim 5 \text{ MeV}$	Positron	511 keV	✓
$m_{\pi^\pm}^2 - m_{\pi^0}^2$	$\frac{3\alpha}{4\pi} \Lambda^2$	$\Lambda \lesssim 850 \text{ MeV}$	Rho	770 MeV	✓
$m_{K_L} - m_{K_S}$	$\frac{s_c^2 f_K^2 m_{K_L^0}}{24\pi^2 v^4} \Lambda^2$	$\Lambda \lesssim 2 \text{ GeV}$	Charm	1.2 GeV	✓
m_H^2	$-\frac{6y_t^2}{16\pi^2} \Lambda^2 + \dots$	$\Lambda \lesssim 500 \text{ GeV}$?	?	?

From the “naturalness strategy” to new physics

At this level, we expect

- New physics below the TeV scale...
- ...coupling to the Higgs

Strong motivation for BSM Higgs physics!

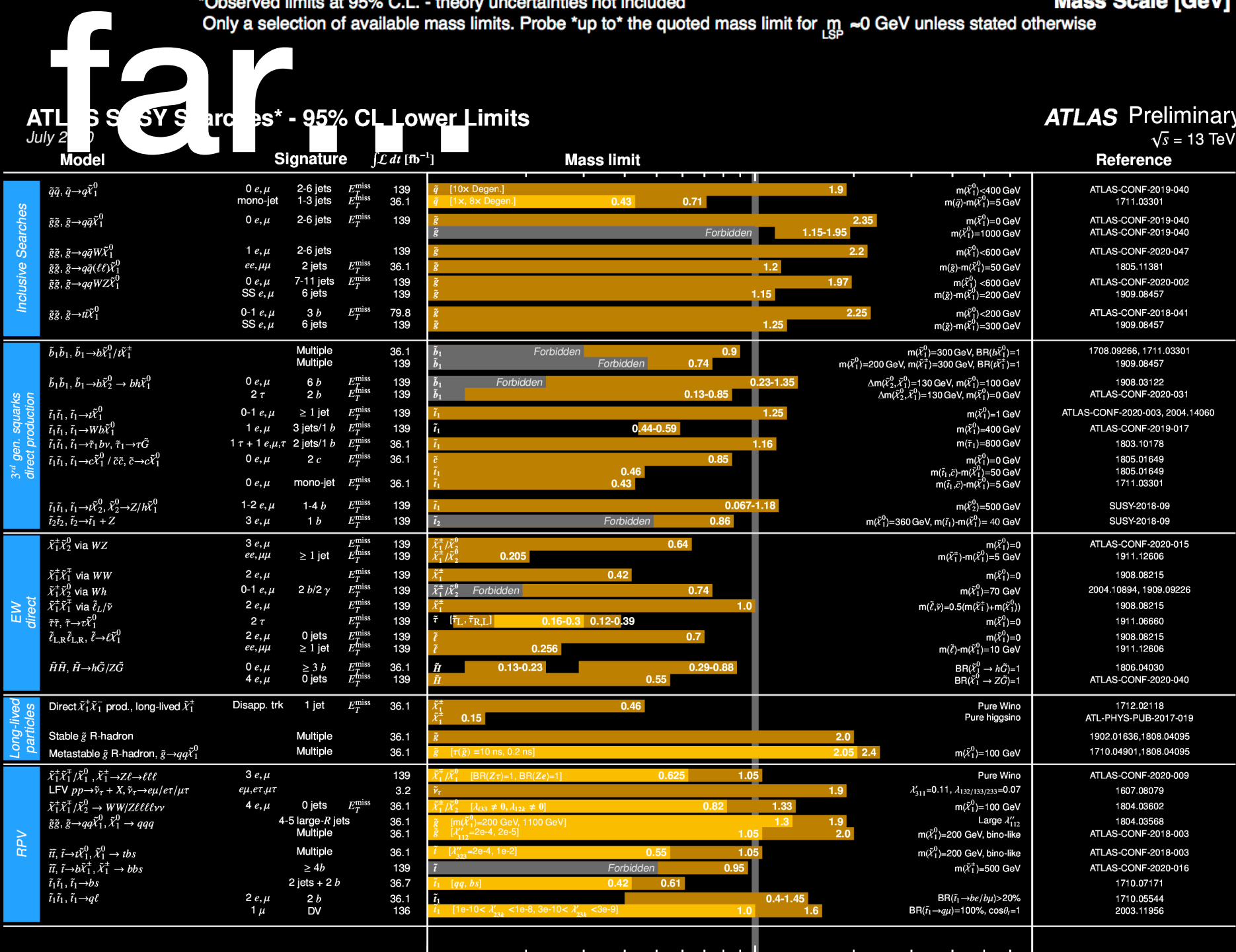
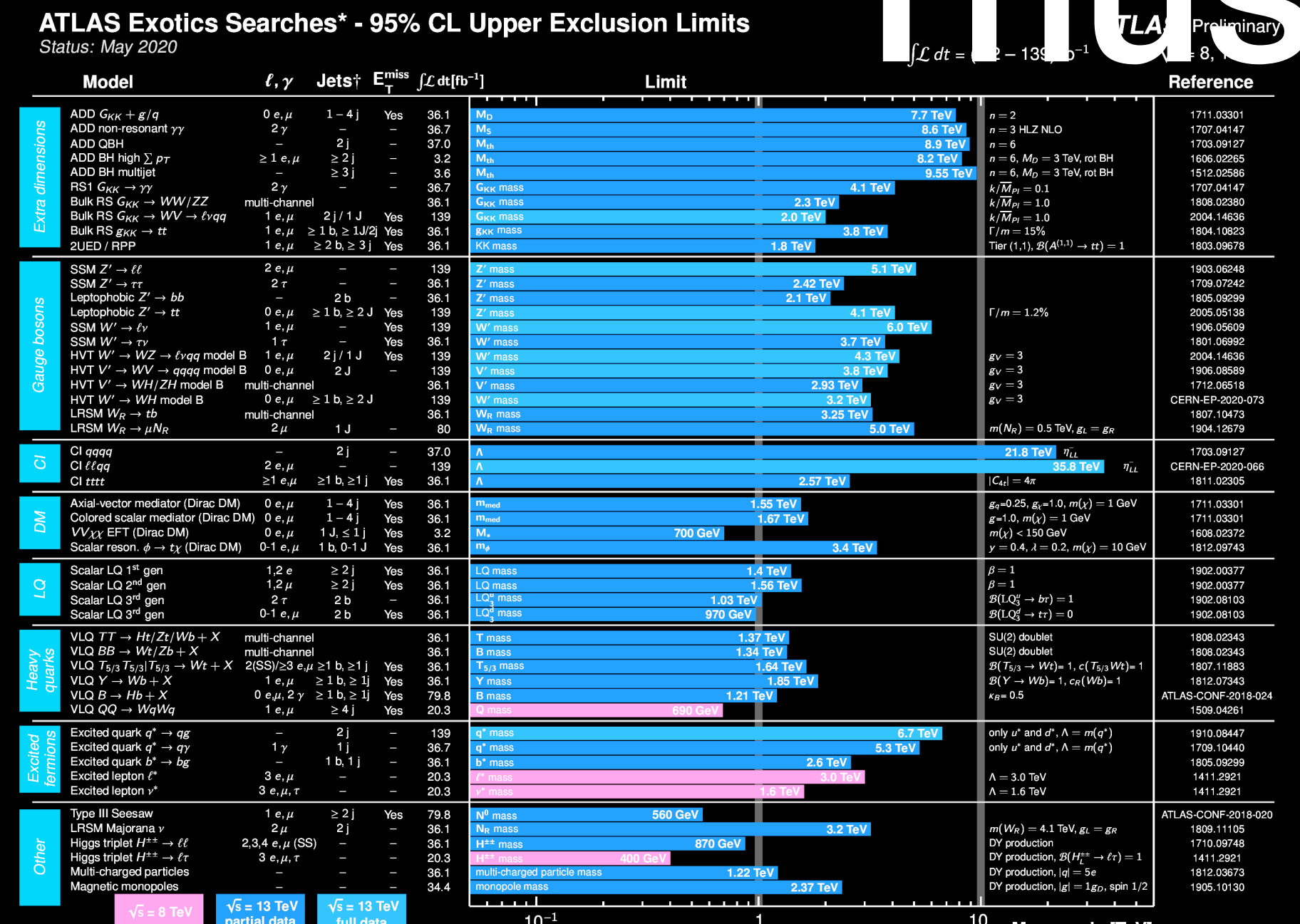
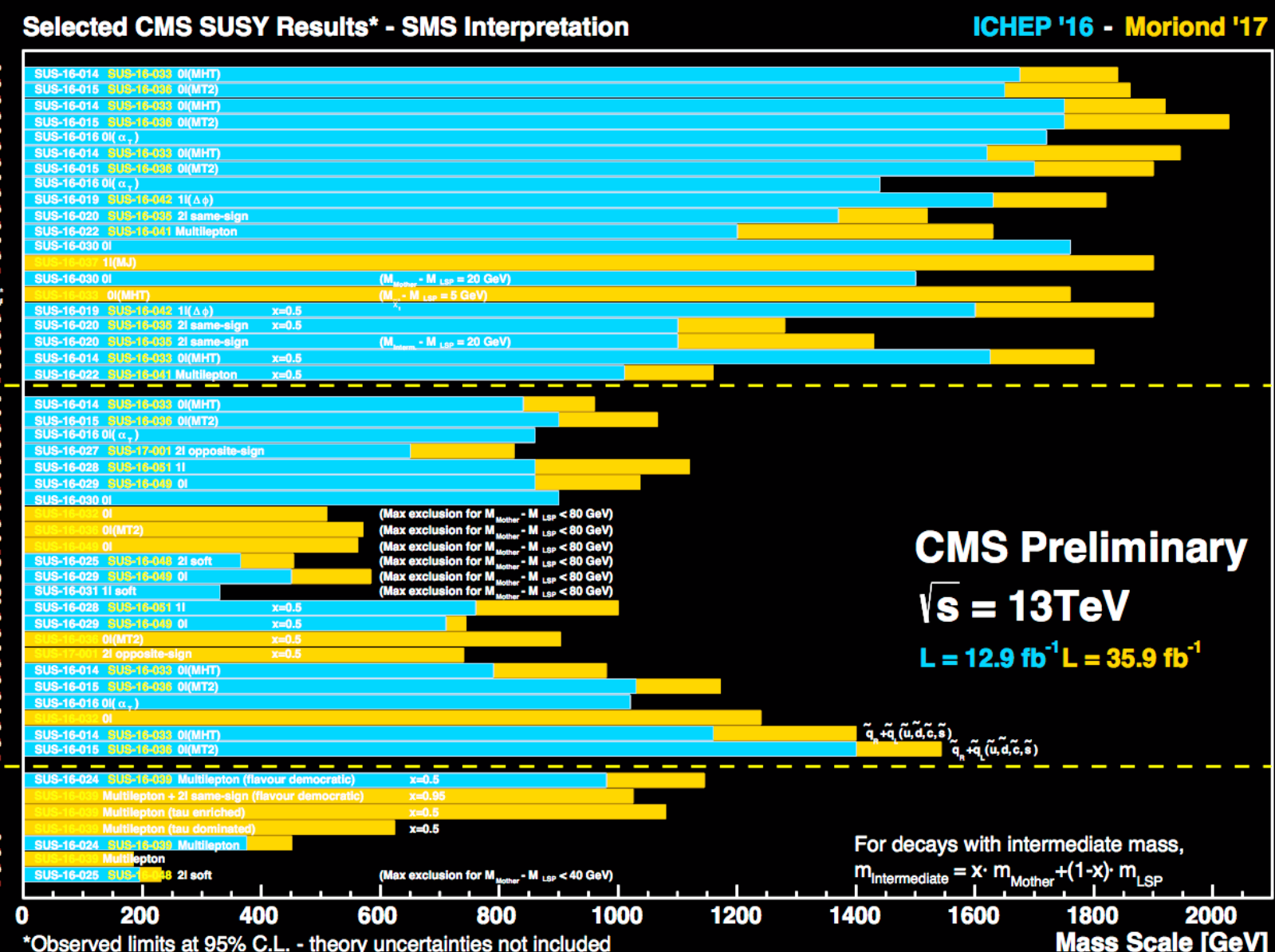
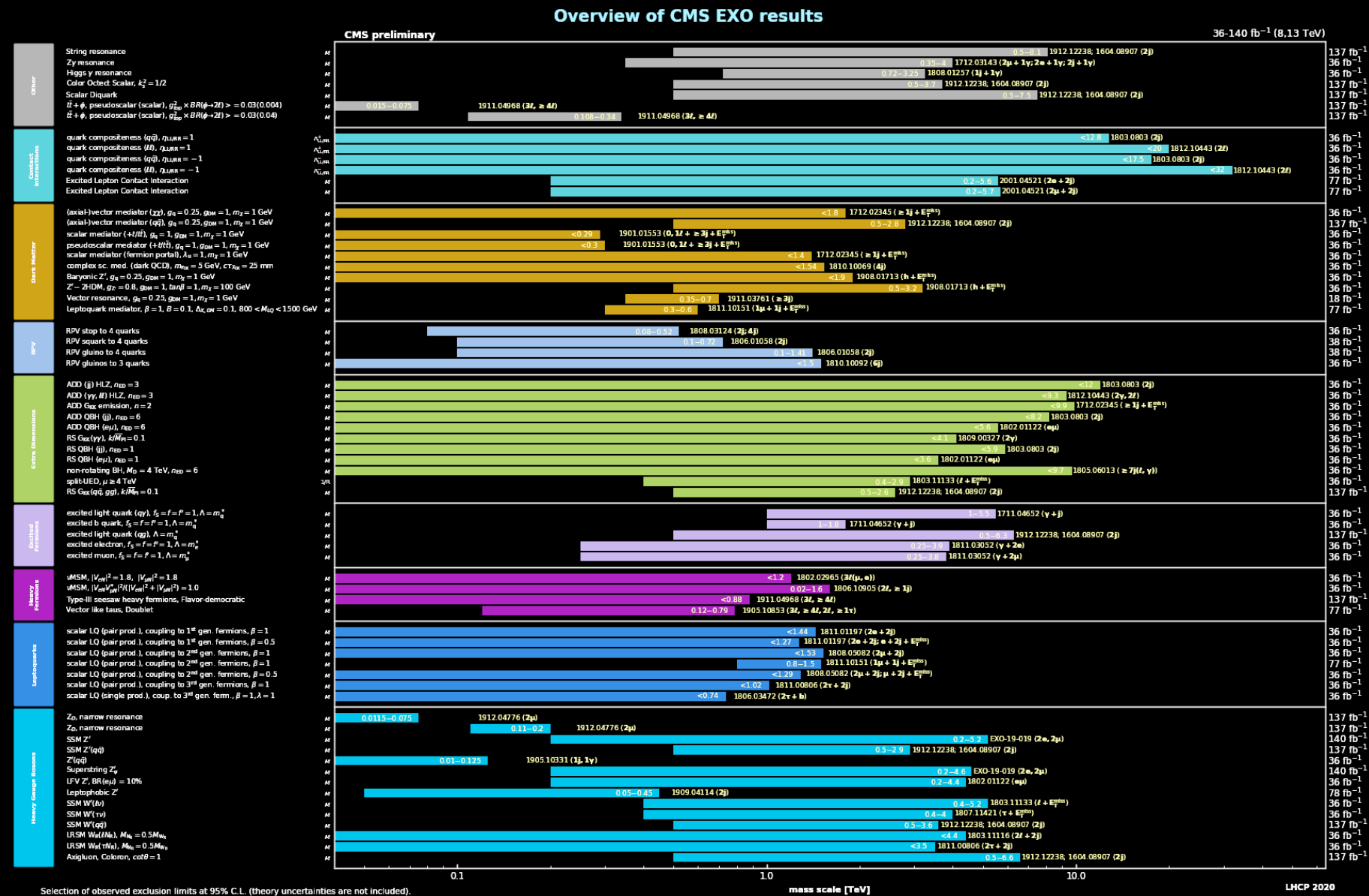
But maybe too broad to be useful...

Implementation is up to us

We've refined this strategy using some rules of thumb, for example...

- 1. The Standard Model coupled to gravity is a generic EFT.**
- 2. The solutions to the hierarchy problem involve symmetries, low cutoffs, or anthropics.**
- 3. Symmetries imply new particles charged under the SM.**

In turn, this tells us what kind of NP to expect: SUSY, CHM,...



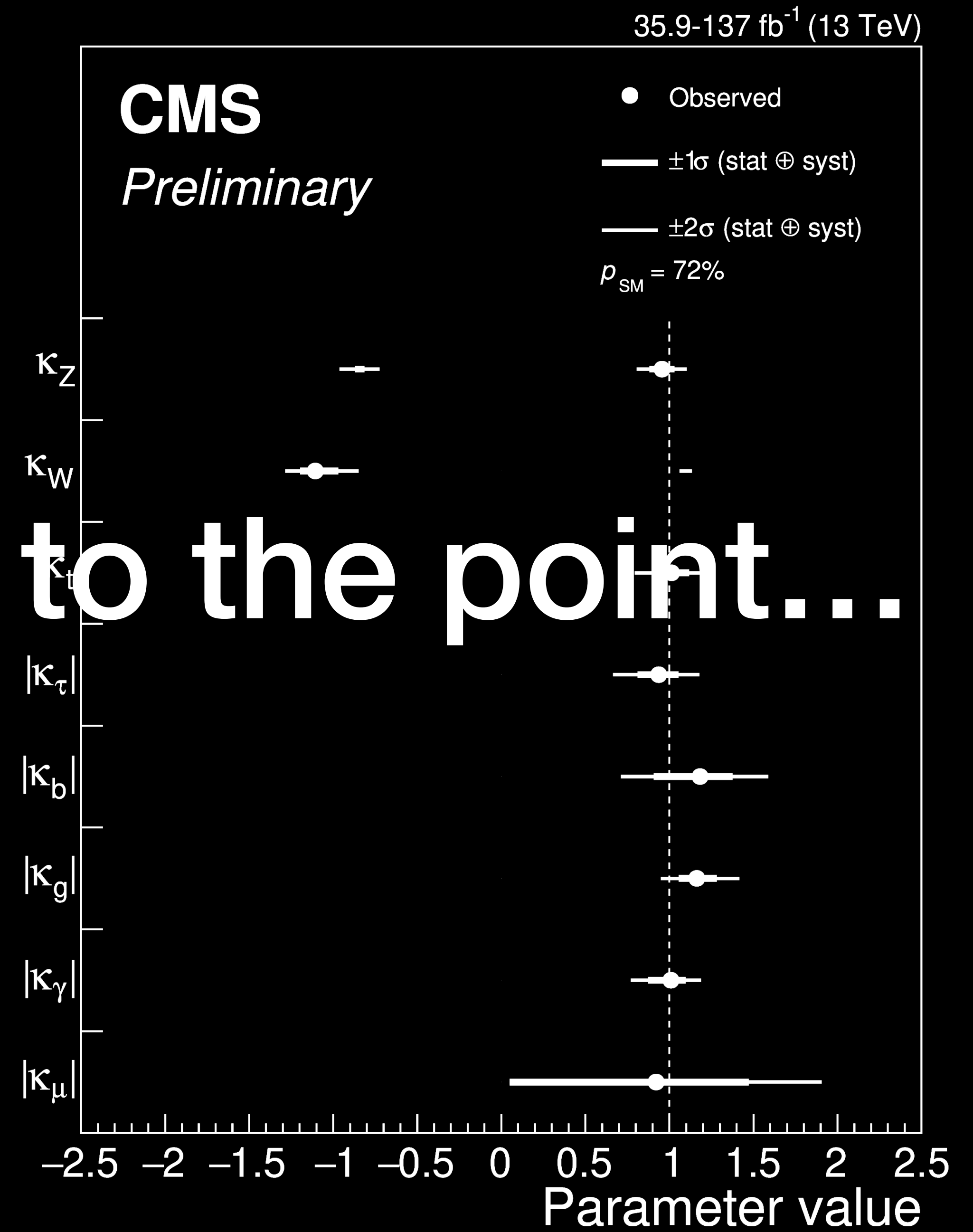
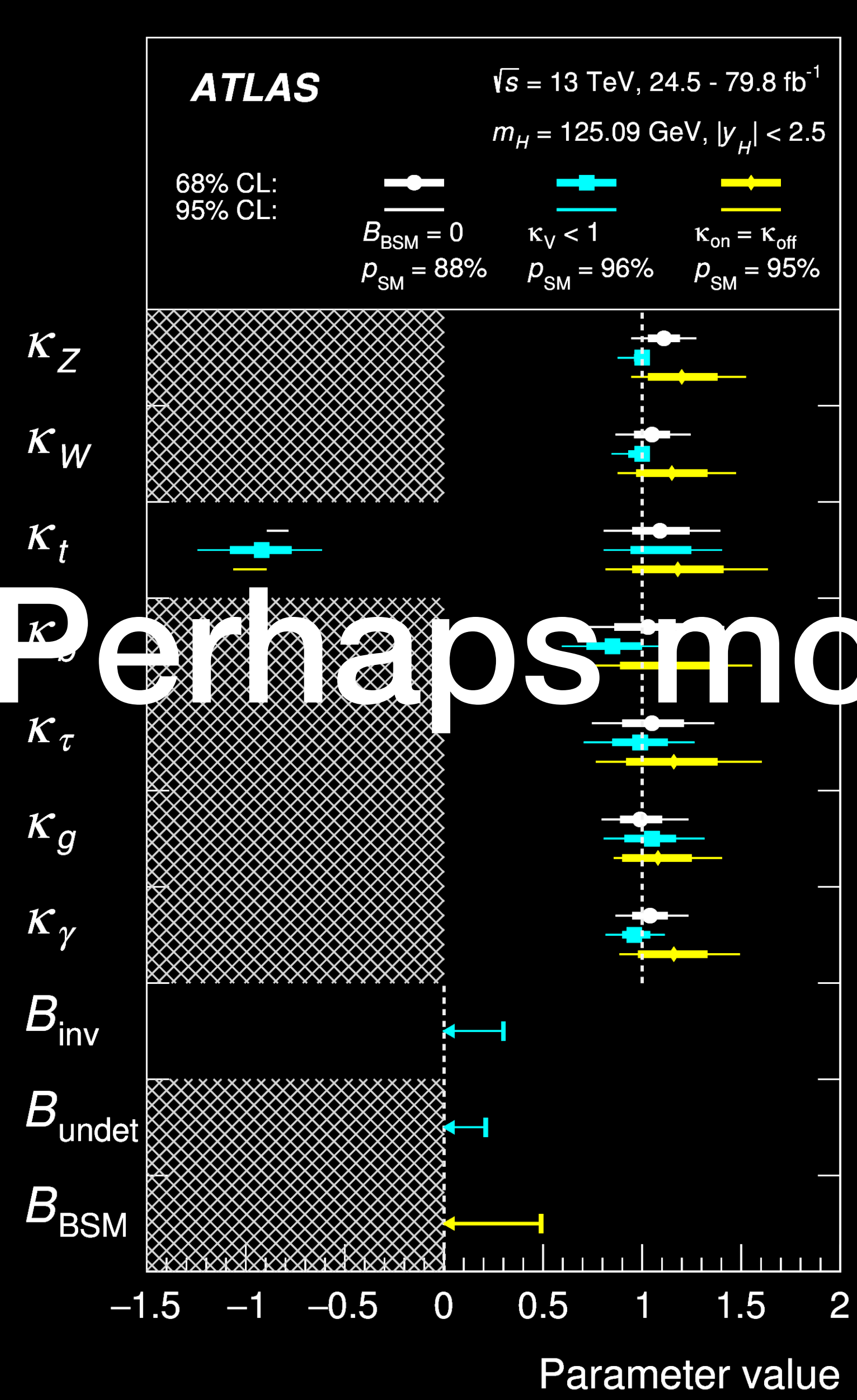
Thus far...

ICHEP '16 - Moriond '17

*Only a selection of the available mass limits on new states or phenomena is shown.
 †Small-radius (large-radius) jets are denoted by the letter J (J).

*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on simplified models, c.f. refs. for the assumptions made.

Perhaps more to the point...



On the wrong track?

What if some of the rules of thumb are wrong?

1. ~~The Standard Model coupled to gravity is a generic EFT.~~ → **TODAY**
 2. ~~The solutions to the hierarchy problem involve symmetries, low cutoffs, or anthropics.~~
 3. ~~Symmetries imply new particles charged under the SM.~~
- Relaxion**
- Twin Higgs, discrete symmetries,
“neutral naturalness”, ...**
-

The End of EFT?

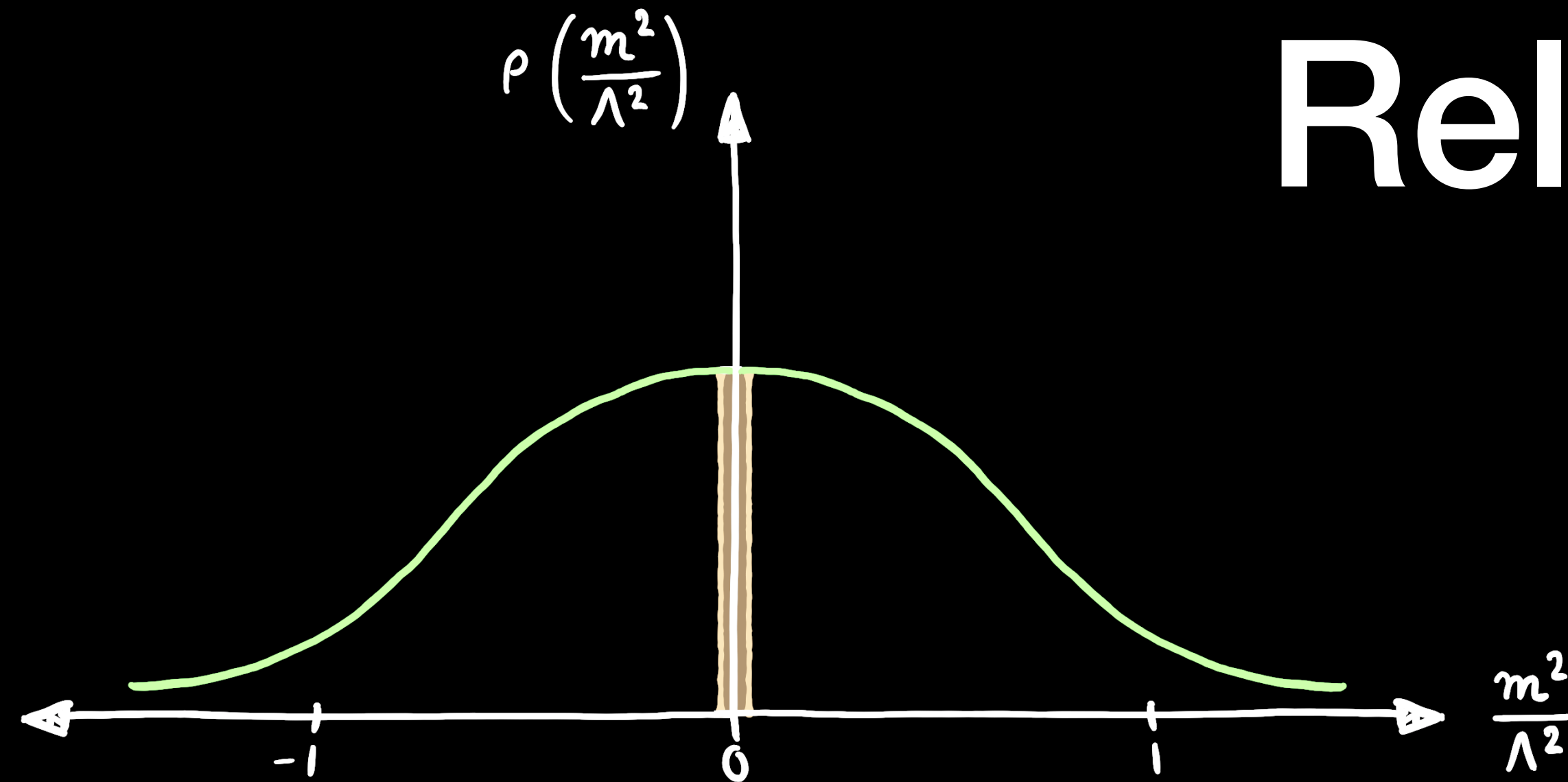
Parameter space of EFTs shaped by consistent coupling to gravity



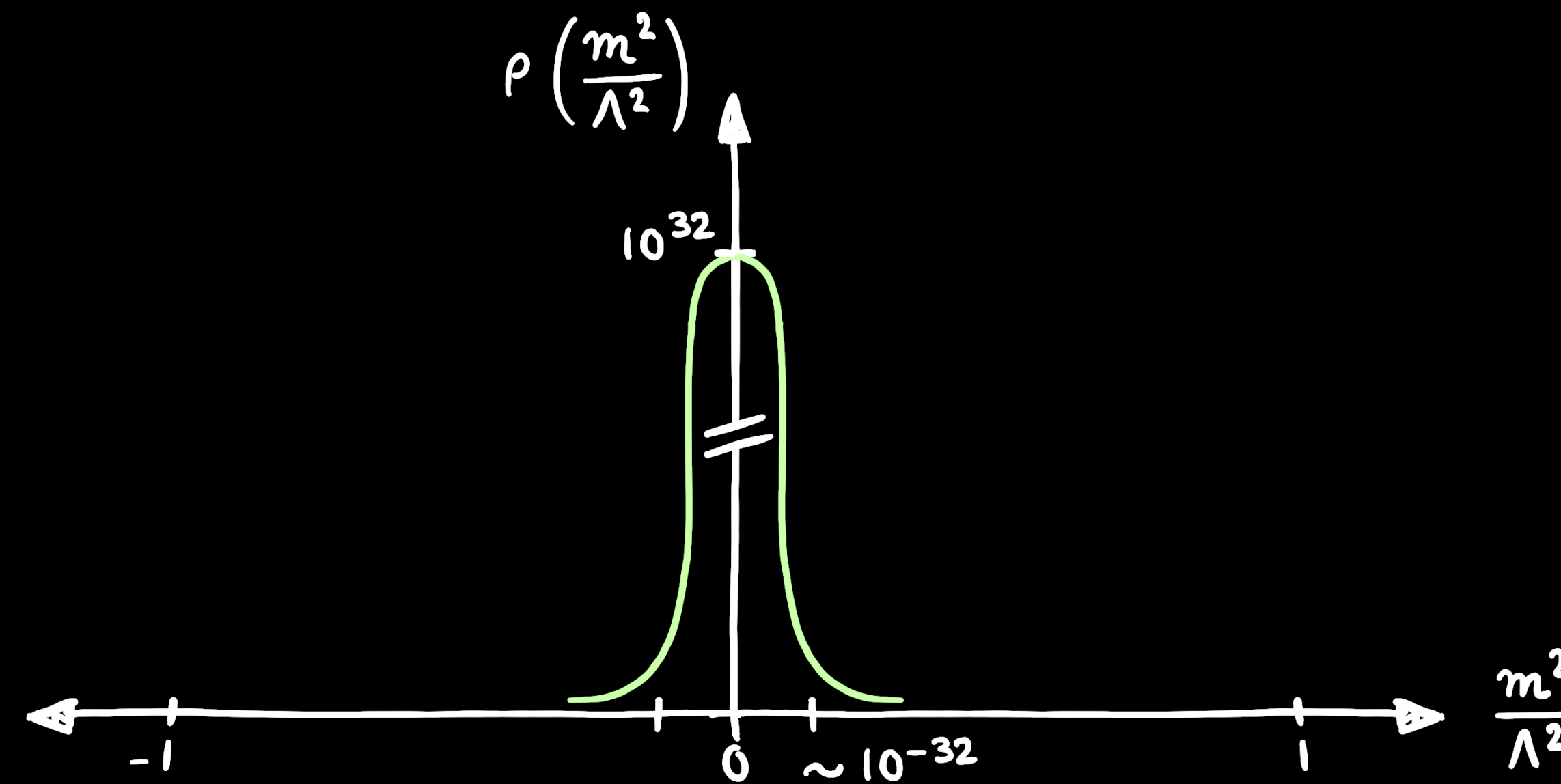
Various (conjectured) consequences:

- No global symmetries
- Charge quantization
- Completeness hypothesis
- No (meta)stable dS vacua
- Infinite states @ infinite distances
- “Gravity is the weakest force”

Relevance to BSM?



Usual (EFT) logic of hierarchy problem: uncorrelated UV contributions give broad distribution of possible values of m_h up to cutoff; m_h well below cutoff “unlikely”



Usual (EFT) logic of hierarchy solution: lower the cutoff.

Alternately: consistency with gravity orchestrates correlations among UV parameters to satisfy bounds, changing the distribution.

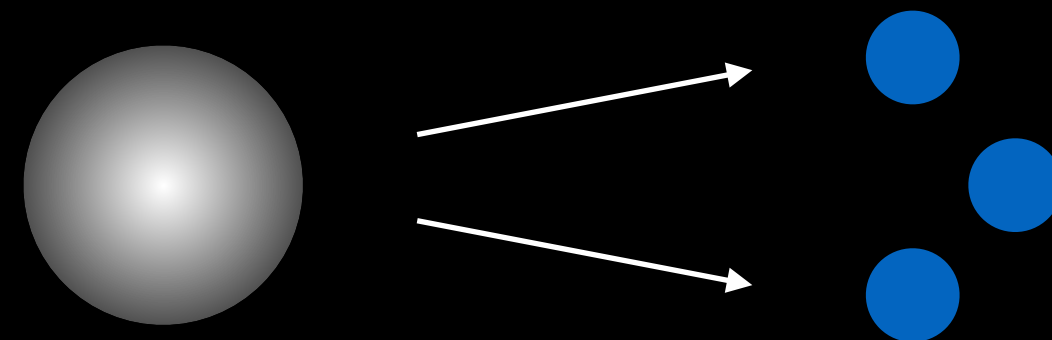
The Weak Gravity Conjecture

(Electric) weak gravity conjecture: an abelian gauge theory must contain a state of charge q and mass m satisfying

$$qg > \frac{m}{M_{\text{Pl}}}$$

[Arkani-Hamed, Motl, Nicolis, Vafa '07]

“Justification”: consider BH of charge Q , mass M decaying to this particle



particles produced = Q/q

Energy conservation: $mQ/q < M$

Then BH satisfies

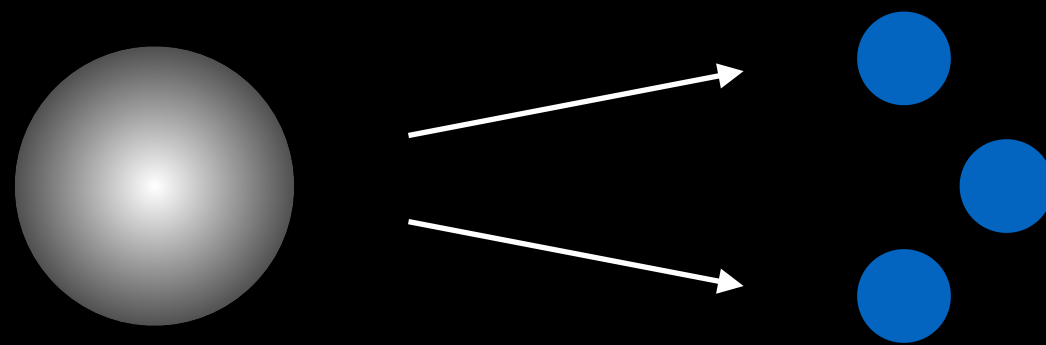
$$Z = Q M_{\text{Pl}}/M < z = q M_{\text{Pl}}/m$$

Extremal BH ($Z=1$) stable unless there exists a state with $z > 1$

$\Rightarrow q > m/M_{\text{Pl}}$ to avoid stable black holes, remnants, in conflict w/ holography

Magnetic Weak Gravity Conjecture

Analogous argument for BHs carrying magnetic charge:



For monopole of size L ,
decay of extremal BH implies

$$m_{\text{mon}} \sim \frac{(2\pi/g)^2}{L} \lesssim \frac{2\pi}{g} M_{\text{Pl}}$$

$$\Rightarrow \Lambda \equiv L^{-1} \lesssim g M_{\text{Pl}}$$

*Note: cutoff need not imply appearance of quantum gravity,
only physics underlying monopole structure*

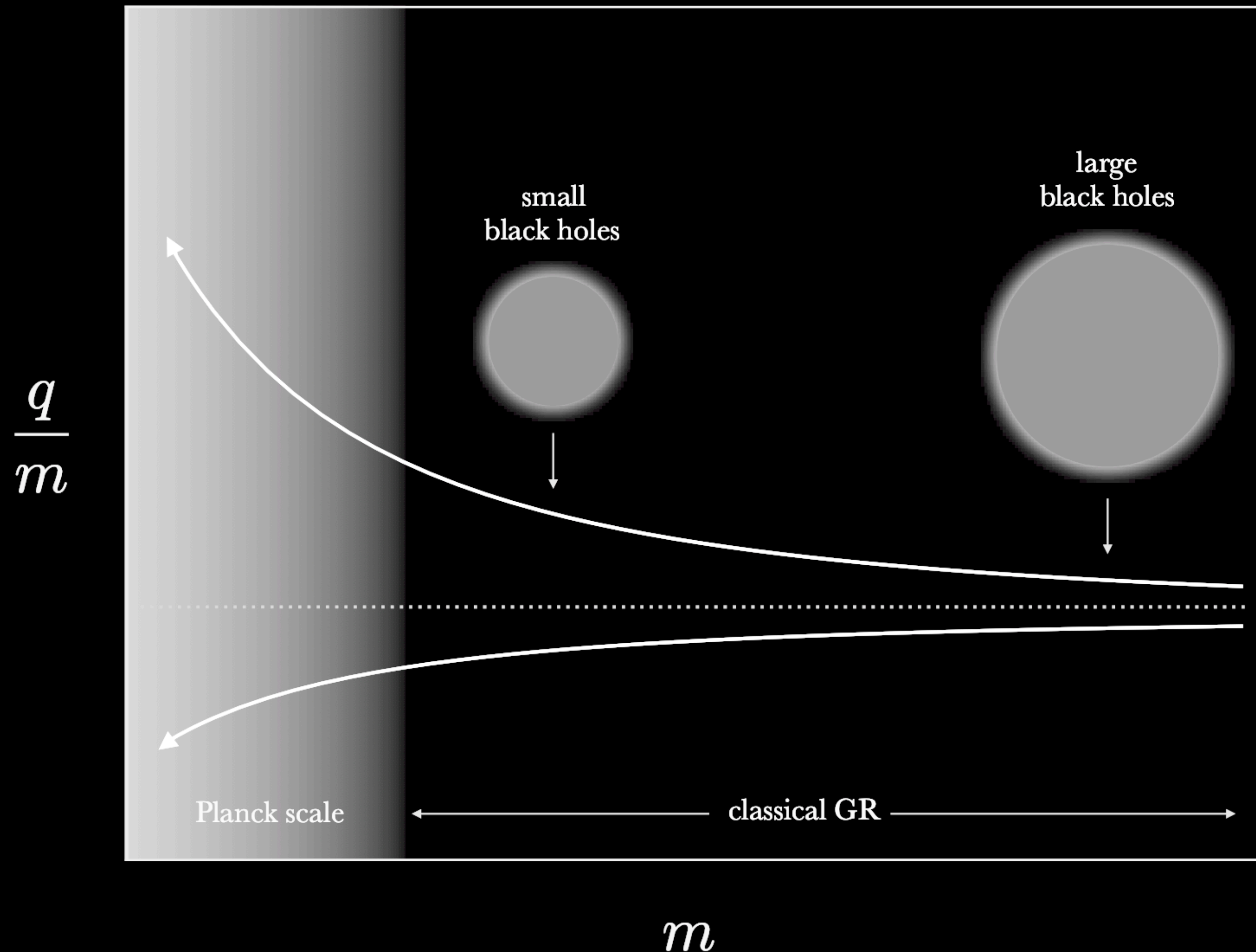
A Family of Conjectures

Electric WGC: [Arkani-Hamed, Motl, Nicolis, Vafa '07]	$m \leq (gq)M_{\text{Pl}}$
Magnetic WGC: [Arkani-Hamed, Motl, Nicolis, Vafa '07]	$\Lambda \lesssim gM_{\text{Pl}}$
+Scalar WGC: [Palti '17]	$m \leq \sqrt{g^2q^2 - \mu^2}M_{\text{Pl}}$
dS WGC: [Montero, Van Riet, Venken '19]	$m^2 \gtrsim gqM_{\text{Pl}}H$
Axion WGC: [Arkani-Hamed, Motl, Nicolis, Vafa '07]	$f \leq (1/S)M_{\text{Pl}}$

New hierarchies from EFT + gravity.

Irrelevance to BSM?

[Cheung, Liu, Remmen '18]



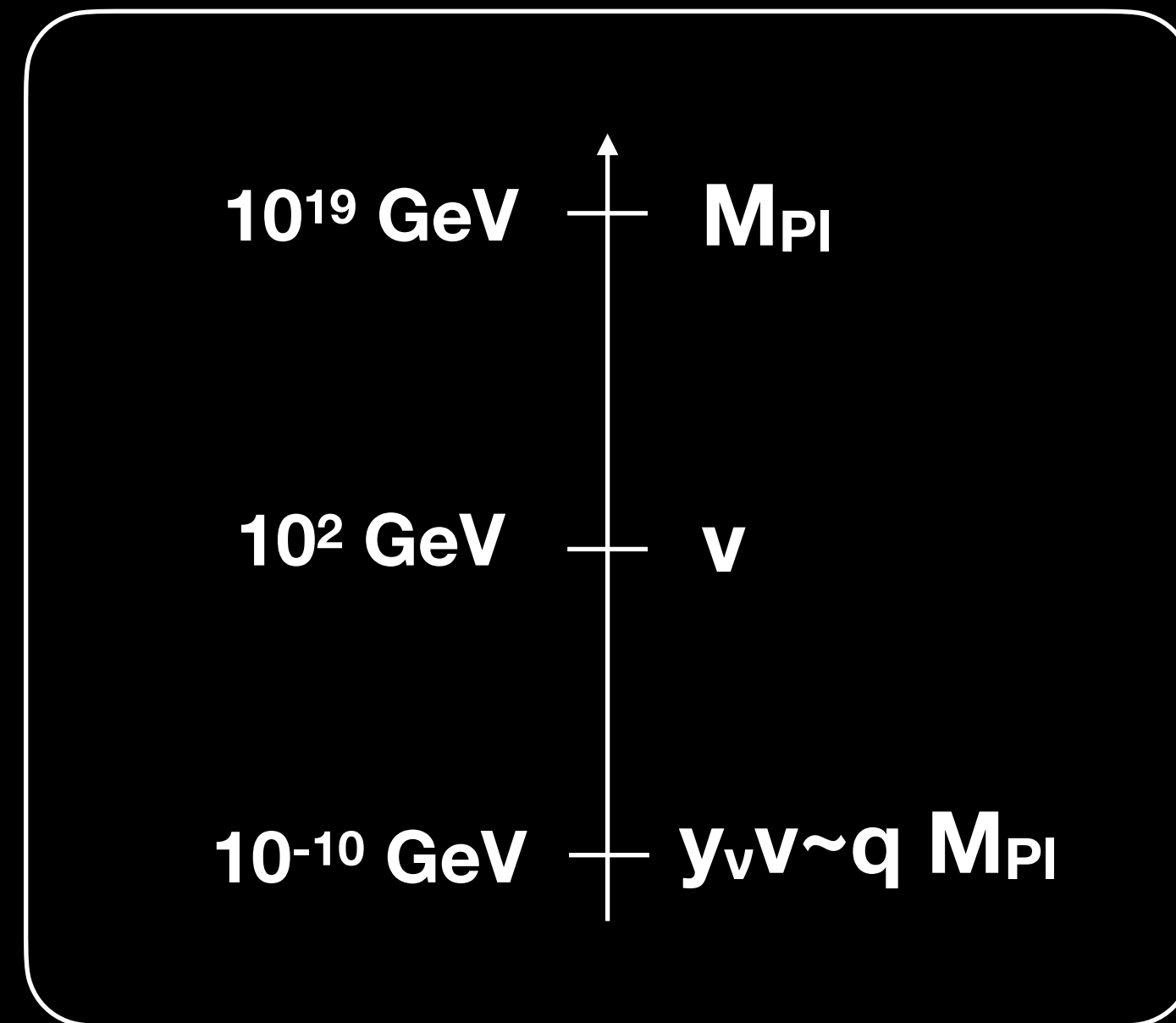
Higher-dimensional operators deform extremality curve in direction that allows larger extremal black holes to decay into smaller extremal black holes, “self-satisfying” WGC.

Could still expect arguments to hold for sub-Planckian states, in which case WGC still relevant to particle physics; status unclear.

Weak Gravity, Weak Scale?

[Cheung, Remmen '14]: If mass of WGC particle is UV sensitive, then for fixed UV-insensitive parameters, satisfying the WGC enforces fine-tuning. (*Or: would orchestrate correlations among UV contributions*)

Application to SM: charge SM fermions under weakly gauged (unbroken) $U(1)_{B-L}$ (bounds currently $q \lesssim 10^{-24}$).
Cancel anomalies with RHN ν_R



Neutrino mass from EWSB

$$y_\nu H \bar{L} \nu_R \rightarrow m_\nu \sim y_\nu v$$

If lightest neutrino is WGC particle,

$$m_\nu \sim 0.1 \text{ eV}, q \gtrsim 10^{-29}$$

For fixed y, q , satisfying WGC places an upper bound on ν

Weak Gravity, Weak Scale?

Things that could go wrong:

- WGC could be satisfied by states outside EFT
- Satisfying WGC could compel the appearance of a new light state that enforces apparent UV correlations (e.g. relaxion)
- Apparently UV-sensitive parameters might control apparently UV-insensitive ones (e.g. emergent gauge fields)

Thing that certainly goes wrong:

- Magnetic WGC implies cutoff of U(1) at $\Lambda \lesssim gM_{Pl}$

Weak Gravity, Weak Scale?

First order of business: can m, Λ be raised to the weak scale?

New $U(1)_X$ plus matter acquiring some mass from the Higgs. E.g...

[NC, Garcia Garcia, Koren '19]

	$SU(2)_L$	$U(1)_Y$	$U(1)_X$
L	\square	$+1/2$	$+1$
L^c	\square	$-1/2$	-1
N	$-$	0	$+1$
N^c	$-$	0	-1

$$-\mathcal{L} \supset \{m_L L L^c + m_N N N^c + y H^\dagger L N^c + \tilde{y} H L^c N\} + \text{h.c.}$$

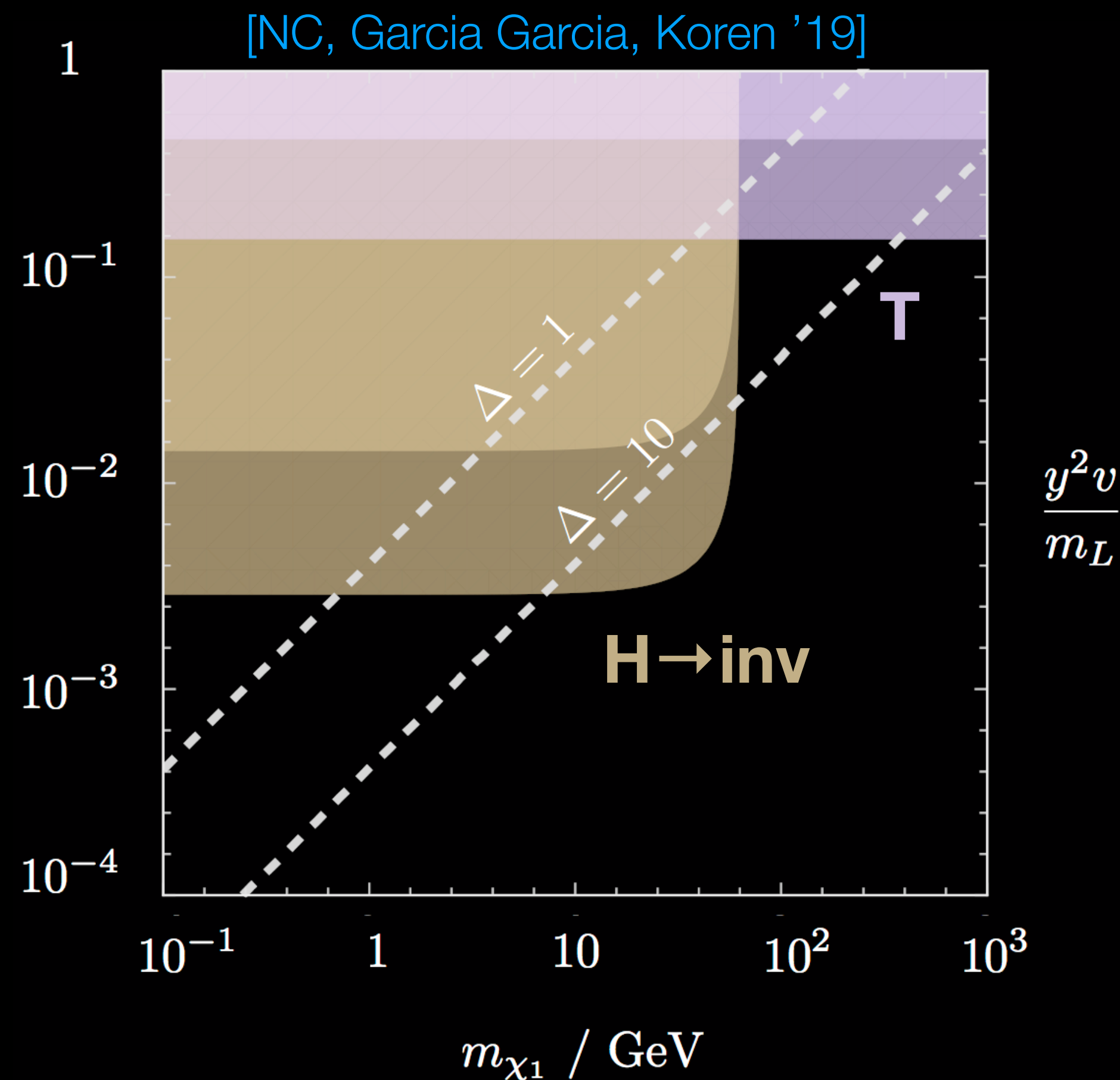
Best option: $m_N < m_L$, lightest mass eigenstate χ_1 is WGC particle

Then for fixed
(technically natural)
 $g, m_L, m_N, y,$

$$v^2 \lesssim \frac{2}{y^2} (m_{\chi_1}^2 + m_{\chi_1} (m_L - m_N) - m_L m_N)$$

Weak Gravity, Weak Scale?

Still have a notion of sensitivity of the weak scale
to parameters involved in the bound



**Quantify
with e.g.**

$$\Delta_x \equiv \left| \frac{\partial \log v^2}{\partial \log x} \right|$$

Here

$$\Delta_{\text{max}} \sim \frac{m_N m_L}{y^2 v^2}$$

Not surprising: WGC particle should
get “most of” its mass from EWSB.

Surprisingly predictive: look for new
singlet fermions coupled to the
Higgs at/below the weak scale.

DM story interesting...

Weak Gravity, Weak Scale?

Lightest particle charged under $U(1)_X$ is stable \Rightarrow **dark matter** candidate

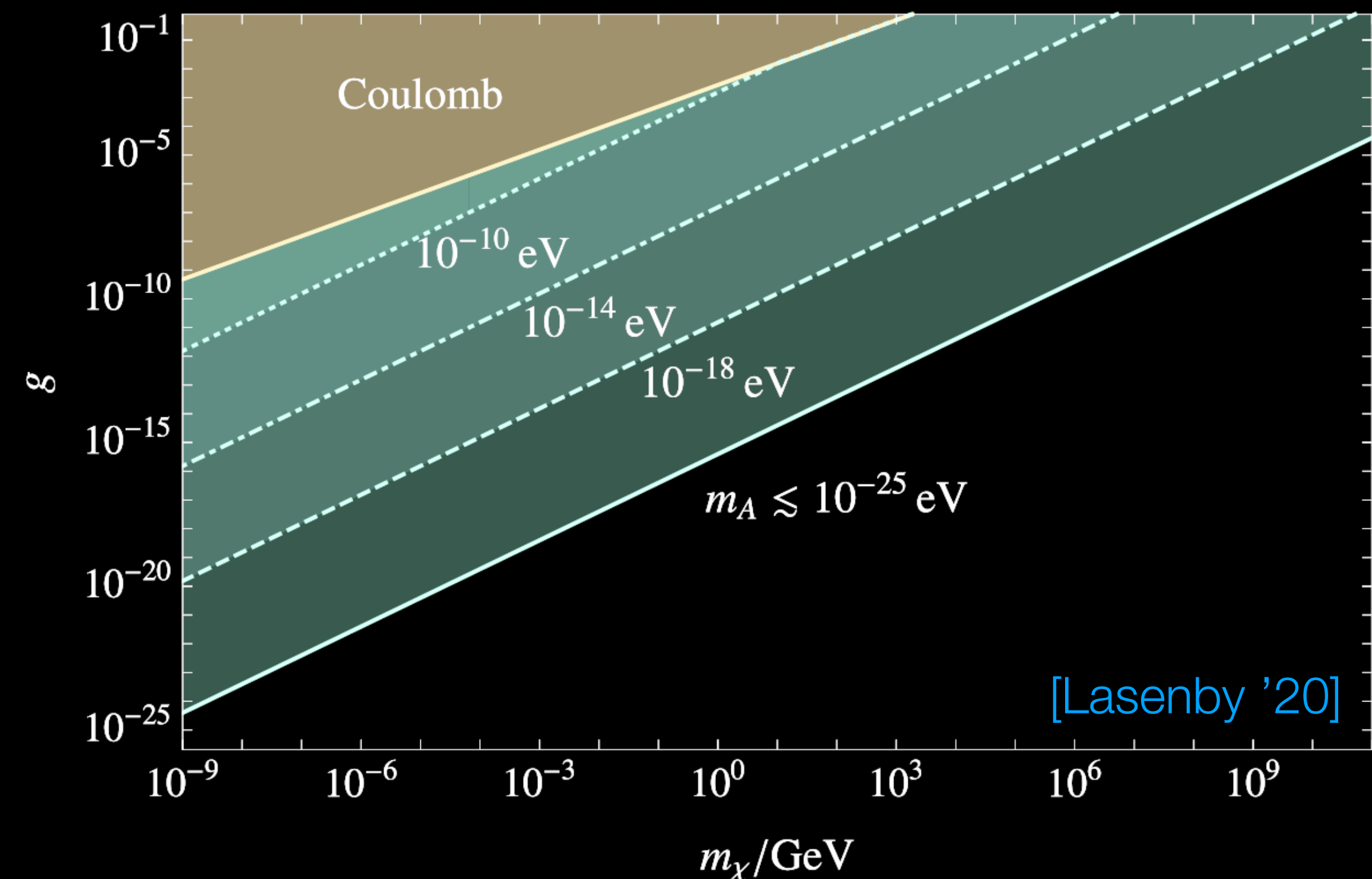
$U(1)_X$ gives a very weak, long-range force, too weak to influence individual collisions but relevant on scale of galaxy clusters

Galaxy cluster collisions can trigger plasma instabilities, making DM collisional on large scales
 [Ackerman, Buckley, Carroll, Kamionkowski '08; Heikinheimo, Raidal et al '15; Spethmann et al '16]

Timescale of plasma fluctuations set by plasma frequency,

$$\omega_p = \sqrt{\frac{g^2 \rho}{m^2}} \geq \frac{\sqrt{\rho}}{M_{\text{Pl}}} \quad \omega_p^{-1} \lesssim 10^{15} \text{ s} \times \left(\frac{0.04 \text{ GeV cm}^{-3}}{\rho} \right)^{1/2}$$

C.f. $\tau \sim 1 \text{ Gyr} \sim 10^{16} \text{ s}$ for galaxy cluster collisions



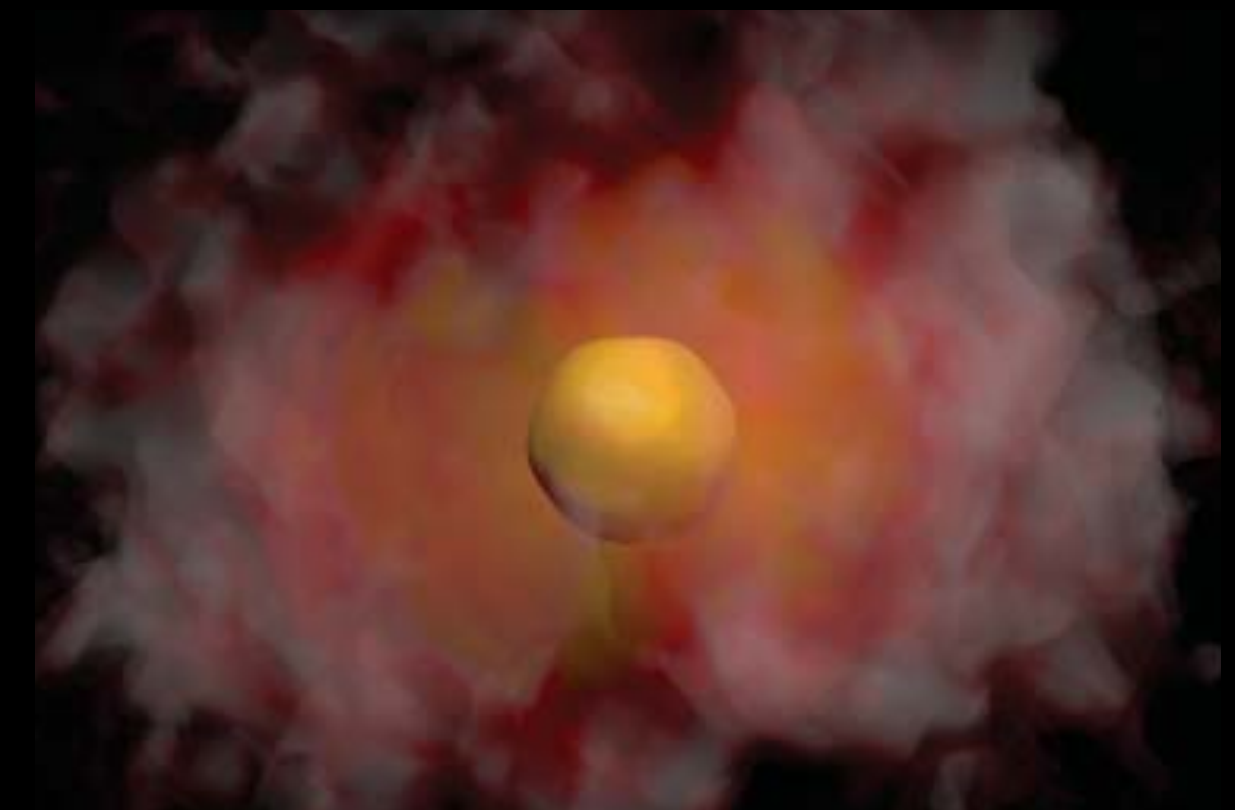
Weak Gravity, Weak Scale?

Second order of business: can the magnetic WGC scale be something less severe than the SM cutoff? Only confident that $\Lambda \sim$ scale associated w/ structure of magnetic monopoles

E.g. t' Hooft-Polyakov monopoles $SU(2)_X \xrightarrow{\langle \text{Adj} \rangle} U(1)_X$

$$“\Lambda” = m_W = g_2 f = 2g f \lesssim 2g M_{\text{Pl}}$$

W's would trivialize bound from vanilla electric WGC, but not e.g. unit charge version (charge ± 2 under $U(1)_X$)



Resolution of physics at $\Lambda \sim$ weak scale implies additional exotic physics coupling directly or indirectly to the Higgs.

The de Sitter Conjecture

de Sitter Conjecture: Low energy effective scalar potential in any consistent theory of quantum gravity must satisfy

$$|\nabla V| \geq c \frac{V}{M_{\text{Pl}}}$$

[Obied, Ooguri, Spodyneiko, Vafa '18]

Arguments from string theory examples, entropy of dS + distance conjecture
Challenging for inflation, suggests dark energy should be dynamical

[Denef, Hebecker, Wrase '18]: **Badly violated by SM Higgs boson + dynamical DE**

$$\frac{|\nabla V|}{V} \simeq \frac{|\nabla V_{\text{quintessence}}|}{\Delta V_H} \sim \frac{10^{-120}}{10^{-65}} \frac{1}{M_{\text{Pl}}} \sim \frac{10^{-55}}{M_{\text{Pl}}}$$

Either quintessence field couples nontrivially to Higgs, or conjecture too strong...

The Refined dS Conjecture

Refined dS Conjecture: Low energy effective scalar potential in any consistent theory of quantum gravity must satisfy either the dS Conjecture or

$$\min(\nabla_i \nabla_j V) \leq -c' \frac{V}{M_{\text{Pl}}^2}$$

[Ooguri, Palti, Shiu, Vafa '18]

Consistent with SM Higgs,

$$\frac{\min(\nabla_i \nabla_j V)}{V} \sim -\frac{10^{35}}{M_{\text{Pl}}^2}$$

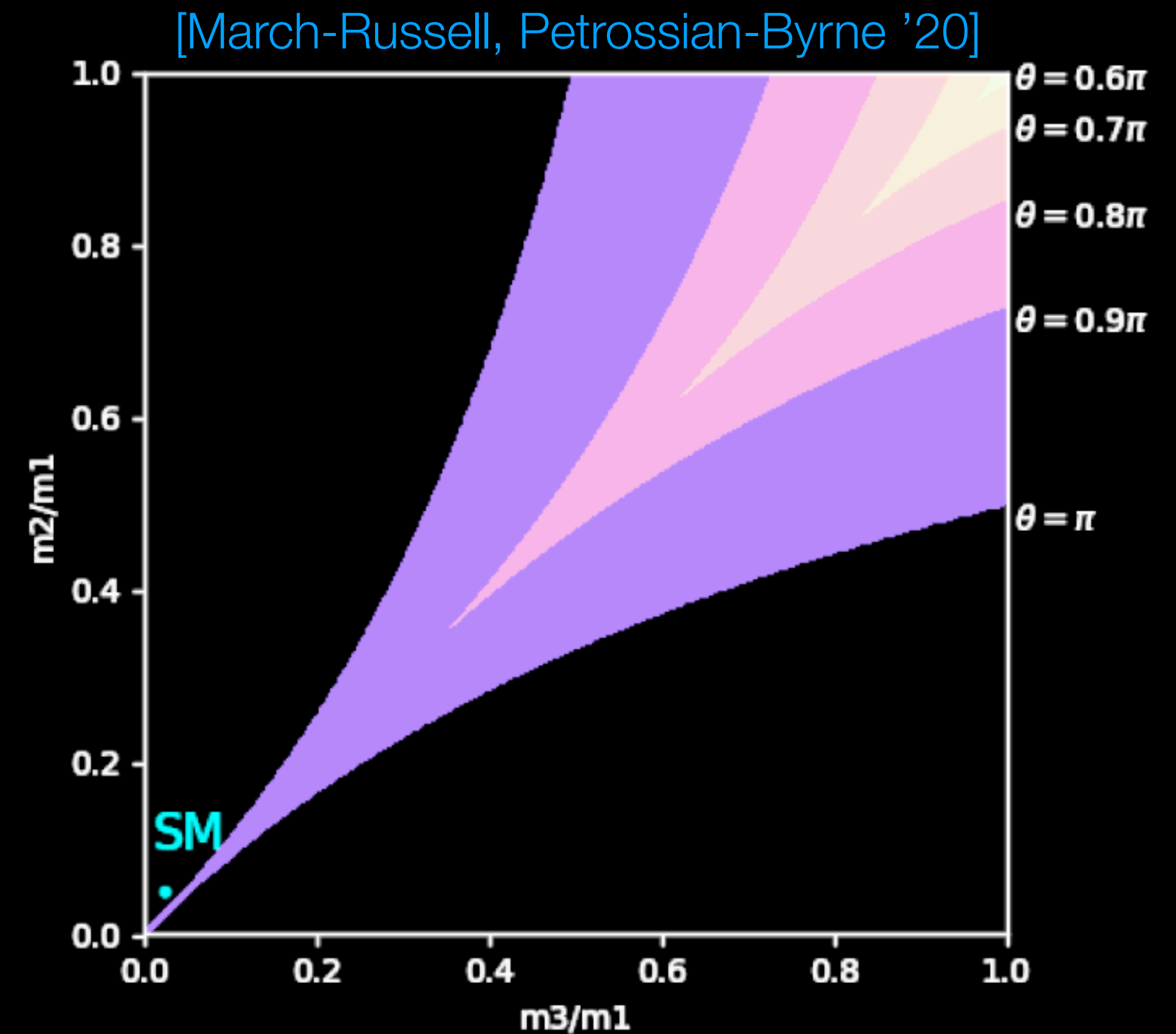
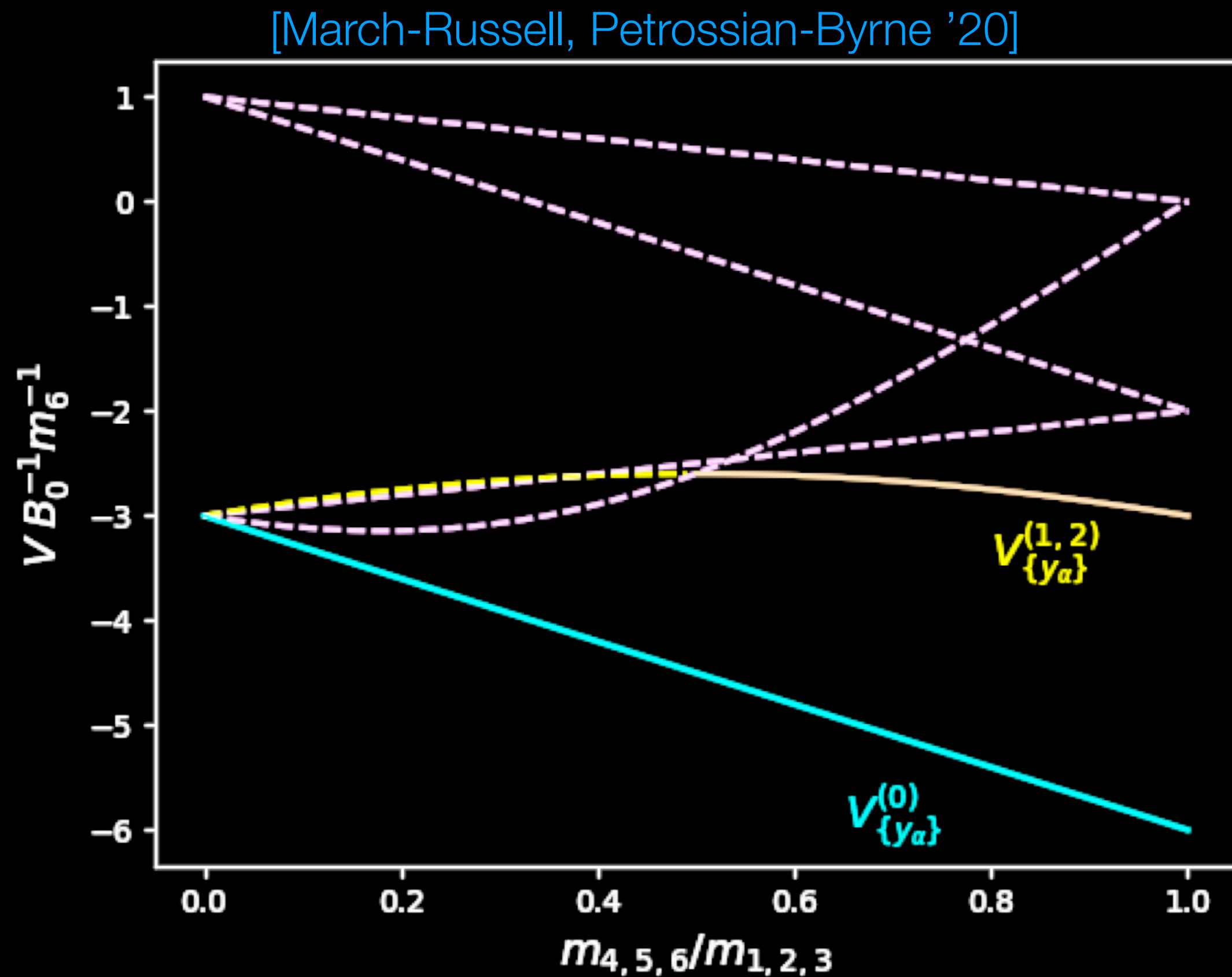
New wrinkle: **essentially forbids metastable vacua**, since satisfying RdSC in metastable minimum implies quintessence evolving too rapidly in our vacuum, reaching deep AdS state (“big crunch”) within ~fraction of a Hubble time

See also: [Ibañez, Martin-Lozano, Valenzuela '17,...]

The SM and the RdSC

[March-Russell, Petrossian-Byrne '20] RdSC relevant to SM flavor!

QCD has metastable vacua for certain values of yukawas, $\bar{\theta}$;
measured values consistent w/ RdSC

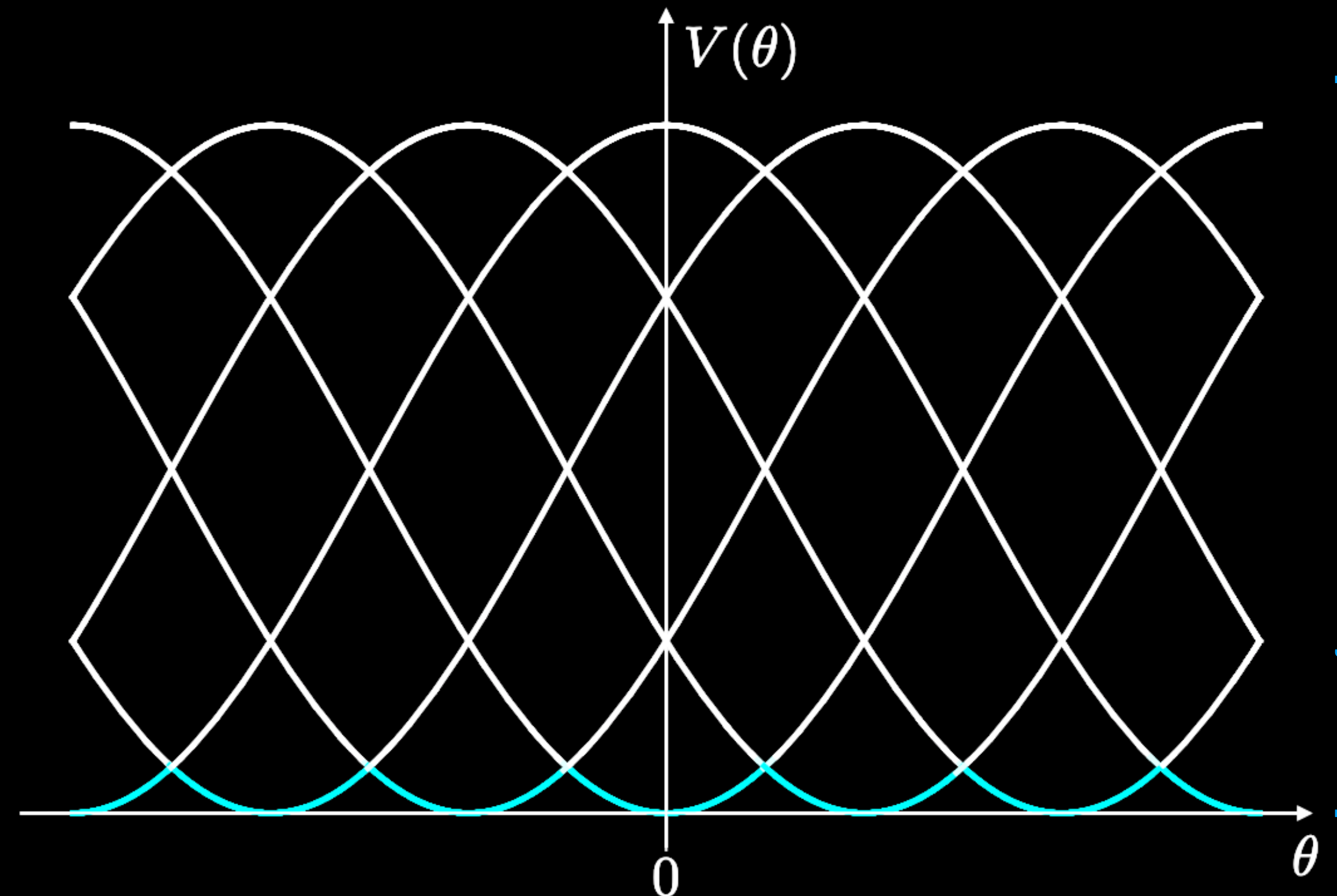


The Weak Scale & the RdSC

[March-Russell, Petrossian-Byrne '20] If pure SU(3) YM has metastable vacua, then for fixed yukawas the RdSC would bound the weak scale from above, $v \lesssim 50$ TeV.

[Witten '98, Shifman '98] Large-N YM should possess $N-1$ metastable vacua: reconciles 2π periodicity $V(\theta + 2\pi) = V(\theta)$ and large-N scaling $V(\theta) = N^2 f(\theta/N)$ for 2π periodic $f(x)$: potential is multi-branched, with each branch $2\pi N$ periodic, ground state 2π periodic due to level crossings

Status at small N unknown, no lattice studies or reliable semiclassics, would be lovely to find out!



Conclusions

- Not sure (personally) how much more there is to say about Higgs & hierarchy problem following traditional EFT logic.
- If the naturalness strategy fails, it should be for good reason. Failure of EFT logic due to gravitational effects is compelling, albeit hard to quantify. Swampland conjectures provide tools applicable to low-energy theory.
- Surprising relevance to Higgs, SM, and its extensions, and visa versa.
- Applications to hierarchy problem convolve conjecture & supposition (e.g. applying WGC to EFT landscape at fixed dimensionless couplings), but follow familiar reasoning (anthropics) and have testable consequences.
- Early days, but stand to learn much more about BSM from Swampland Conjectures and visa versa...

Thank you!