

Sec 2.7 Grossman-Nir violating models

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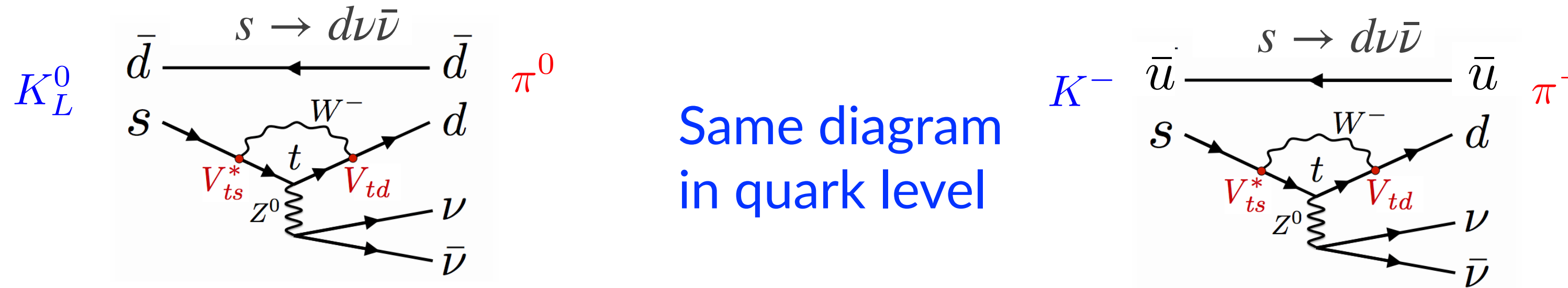
Zoom meeting “Searches for Hidden Sectors at Kaon and Hyperon Factories,”
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Grossman-Nir bound



$$\frac{\Gamma(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\Gamma(K^+ \rightarrow \pi^+ \nu \bar{\nu})} = \frac{(\text{Im } M)^2}{|M|^2} \leq 1 \quad (\text{Isospin relation } \Delta I = 1/2)$$

- ◆ **Grossman-Nir bound** for general NP models (including $\nu_i \bar{\nu}_j$) [Grossman, Nir '97; Grossman, Isidori, Murayama '04]

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \left(\frac{\tau_L}{\tau^+} + \Delta_{\text{IB, EM}} \right) \sin^2 \theta \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \leq 4.32 \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

- ◆ e.g., **Grossman-Nir bound** can be applied for scalars channel $\theta = \text{Arg} \left(\frac{q \langle \pi^0 \nu \bar{\nu} | \mathcal{H} | \bar{K}^0 \rangle}{p \langle \pi^0 \nu \bar{\nu} | \mathcal{H} | \bar{K} \rangle} \right) / 2$

$$\mathcal{B}(K_L \rightarrow \pi^0 X) \leq 4.32 \mathcal{B}(K^+ \rightarrow \pi^+ X) \quad \text{The bound is saturated when } X \text{ is CP-even scalar [Leutwyler, Shifman '90]}$$

Grossman-Nir bound



- ◆ Is the Grossman-Nir bound strict one on general new physics scenario?

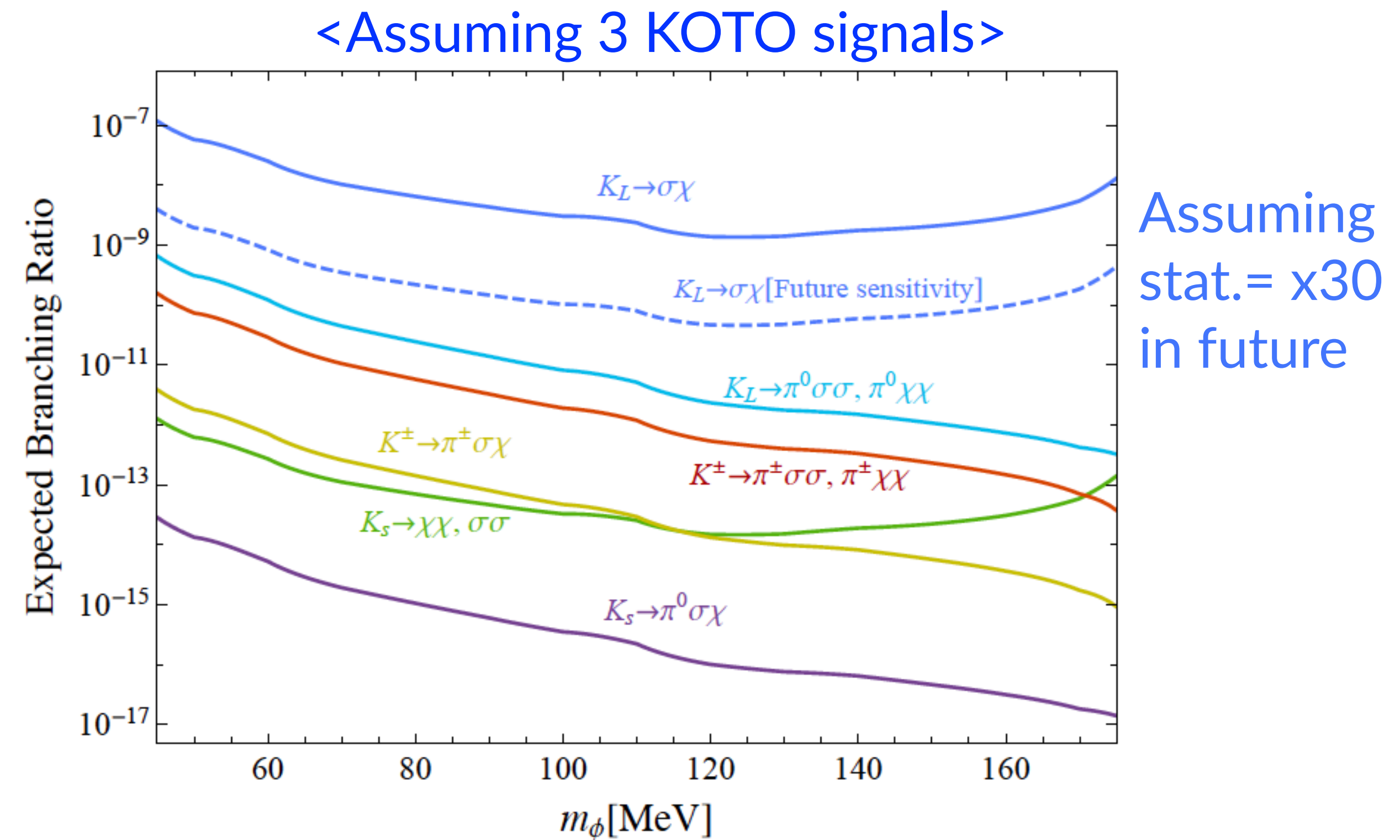
◆ **No!** But, it is strict on many new physics cases.

Violation of Grossman-Nir bound

- ◆ $\gamma\gamma$ (in K_L mode) comes from not π^0 but other sources
- ◆ Two dark particles; $X_2 \rightarrow X_1 + \pi^0$ [Section 2.8]
- ◆ Isospin-violating operator by dimension-seven interaction
- ◆ Kinematics (phase space difference; $m(K_L - \pi^0) = 362$, $m(K^+ - \pi^+) = 354\text{MeV}$) [backup slide]
- ◆ **Effective violation** of the Grossman-Nir bound (GN bound is satisfied in the parton level)
 - ◆ Detector size difference (“lifetime gap”)
 - ◆ Pion-mass new physics (“ π^0 blind spot”) [backup slide]

$\gamma\gamma$ comes from not π^0

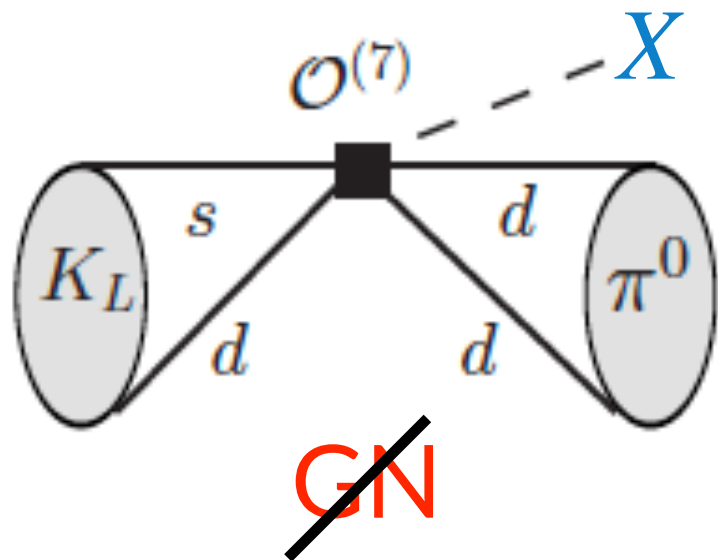
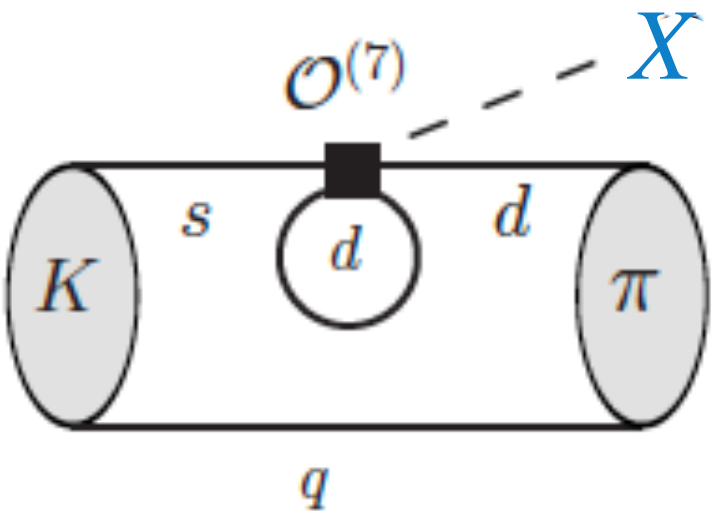
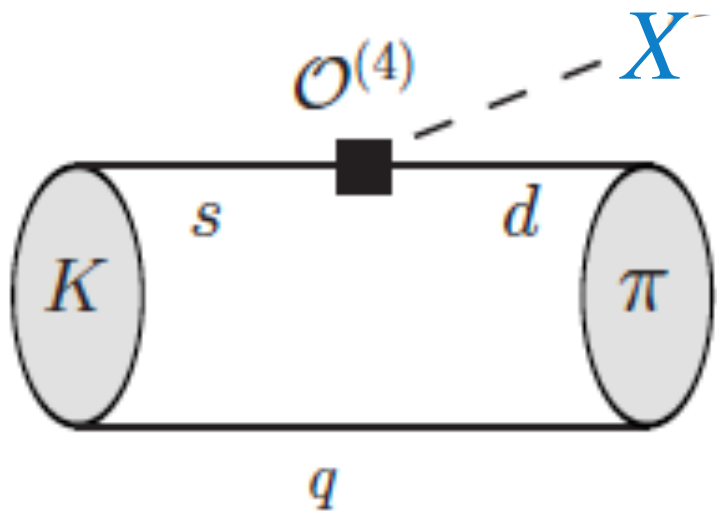
- ◆ $K_L \rightarrow \sigma^0 \chi^0$, $\chi \rightarrow \gamma\gamma$ in strange flavor symmetry with ChPT (SM + ϕ ; $\phi = \sigma + i\chi$; σ is stable within detectors) [Gori, Perez, Tobioka '20]
- ◆ This is annihilation of quark lines, and there is no counterpart in K^+ decay
- ◆ Note: there is also $K_L \rightarrow \pi^0 \sigma\sigma$ and $K^+ \rightarrow \pi^+ \sigma\sigma$ with the same small ratios
- ◆ Only $K_L \rightarrow \sigma^0 \chi^0$ can be probed by KOTO



Isospin-violating operator

- The following isospin-violating operators can violate the Grossman-Nir bound [Ziegler,Zupan, Zwicky '20]

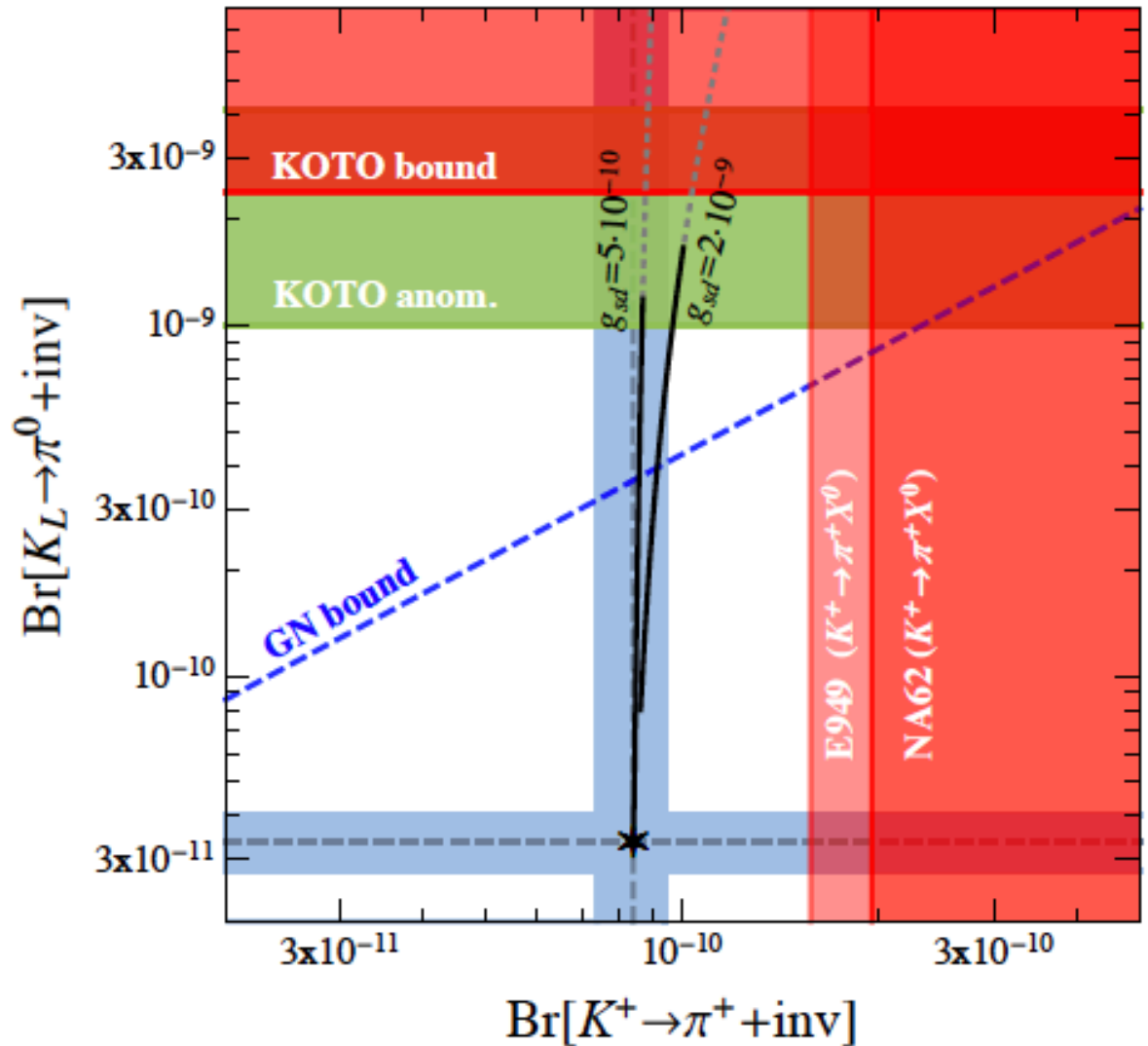
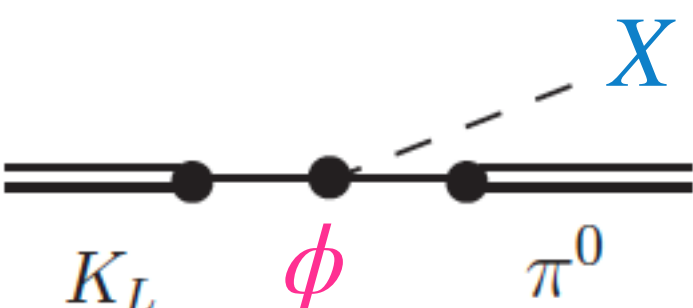
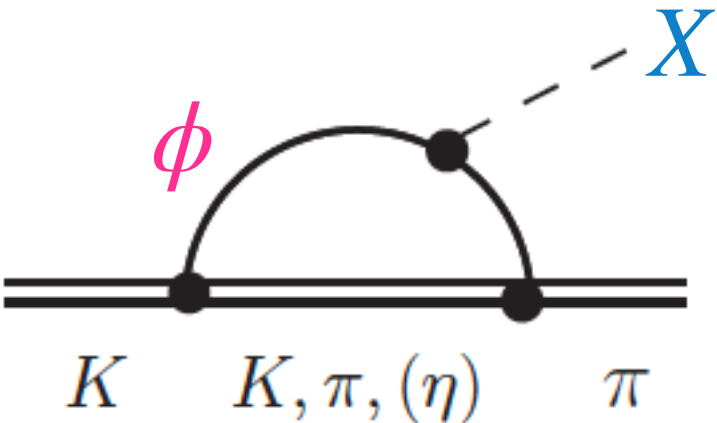
$$\mathcal{L} = c^{(4)}(\bar{s}d)X + \frac{c_i^{(7)}}{\Lambda^3}(\bar{s}\Gamma_i d)(\bar{d}\Gamma'_i d)X$$



$c^{(4)} \ll c^{(7)}$ is required for large violation of the GN bound

- This structure is realized by additional $\mathcal{O}(1)$ GeV mediator ϕ

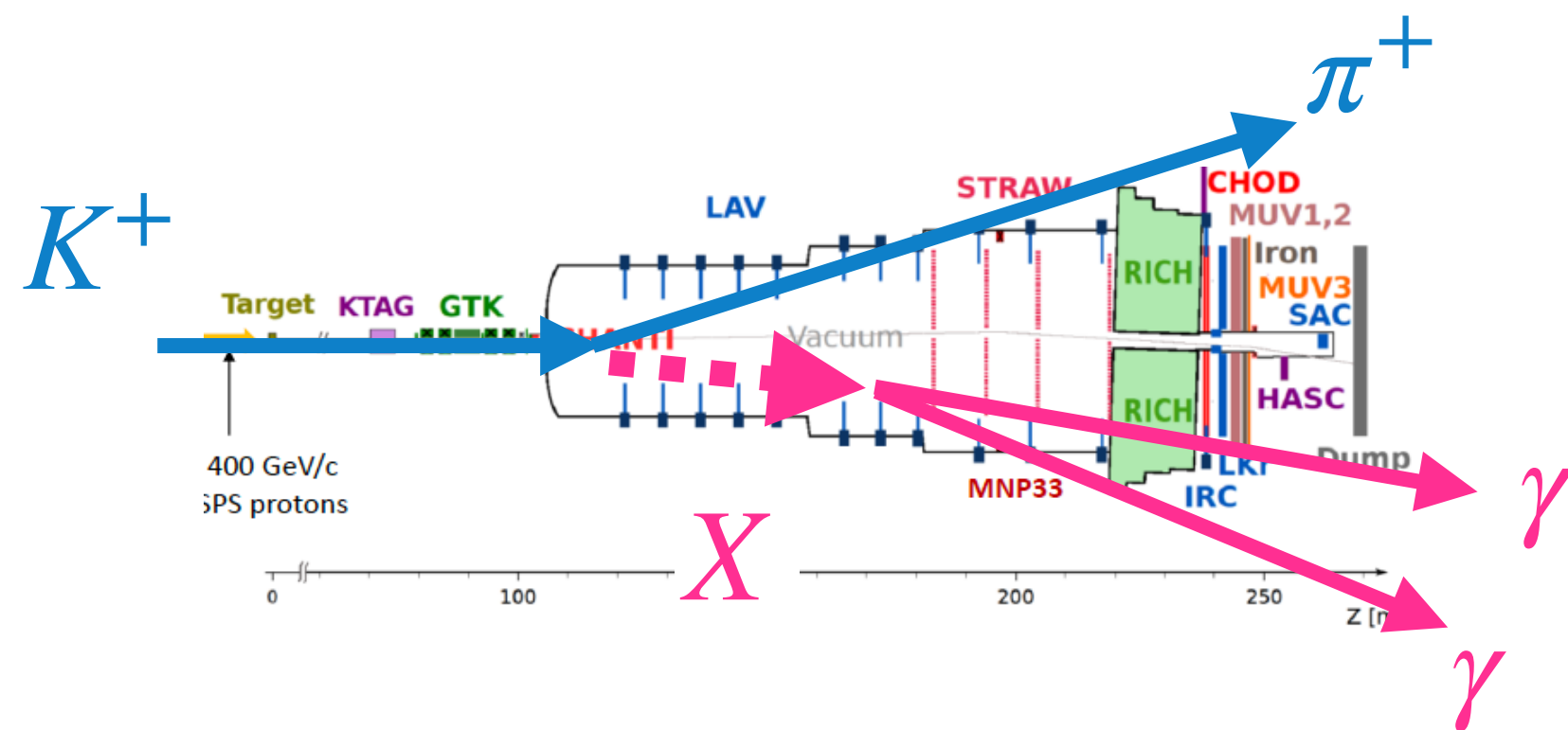
$$\mathcal{L} = g_{sd}(\bar{s}_L d_R)\phi + g_{dd}(\bar{d}_L d_R)\phi + \lambda m\phi^2 X$$



Effective violation of GN bound “lifetime gap”

- ◆ New particle X (CP even) decays into $\gamma\gamma$ (or e^+e^-) with **finite lifetime**

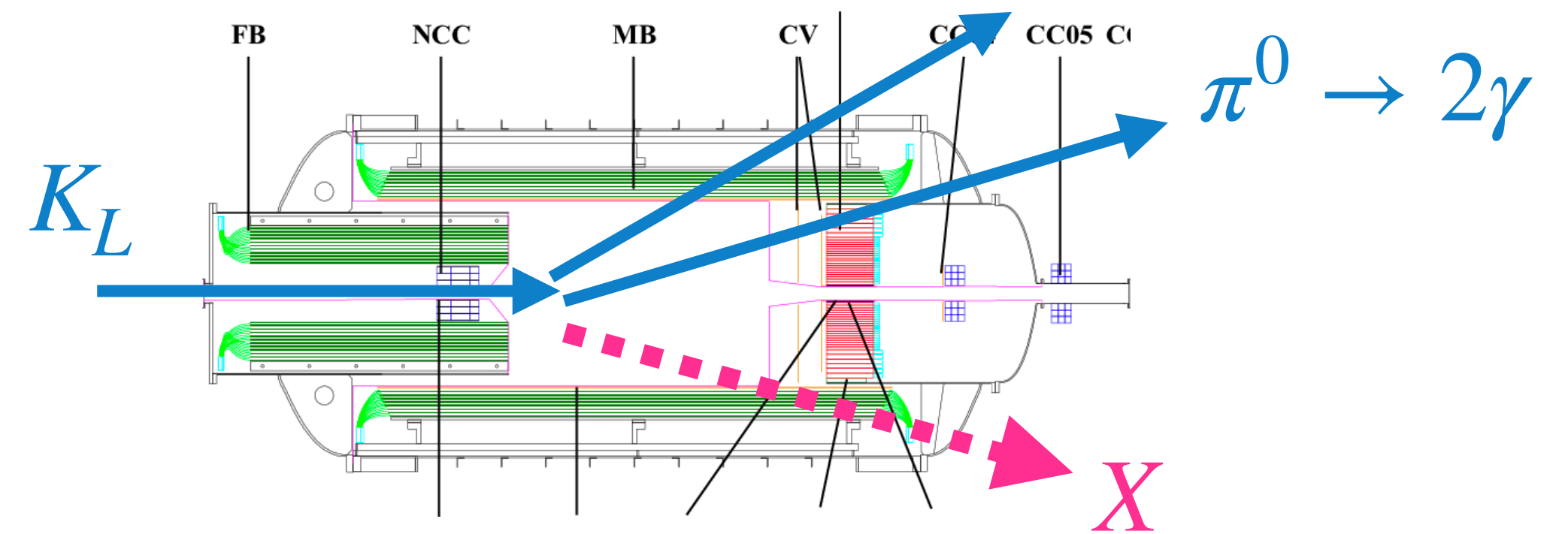
[TK, Okui, Perez, Soreq, Tobioka '20; Liu, McGinnis, Wagner, Wang '20; Liao, Wang, Yao, Zhang '20]



$K^+ \rightarrow \pi^+ X, X \rightarrow \gamma\gamma$ is **rejected** in the NA62 detector



L = 150 m, E = 37 GeV



X seems long-lived in the KOTO detector



L = 3 m, E ~ 1.5 GeV

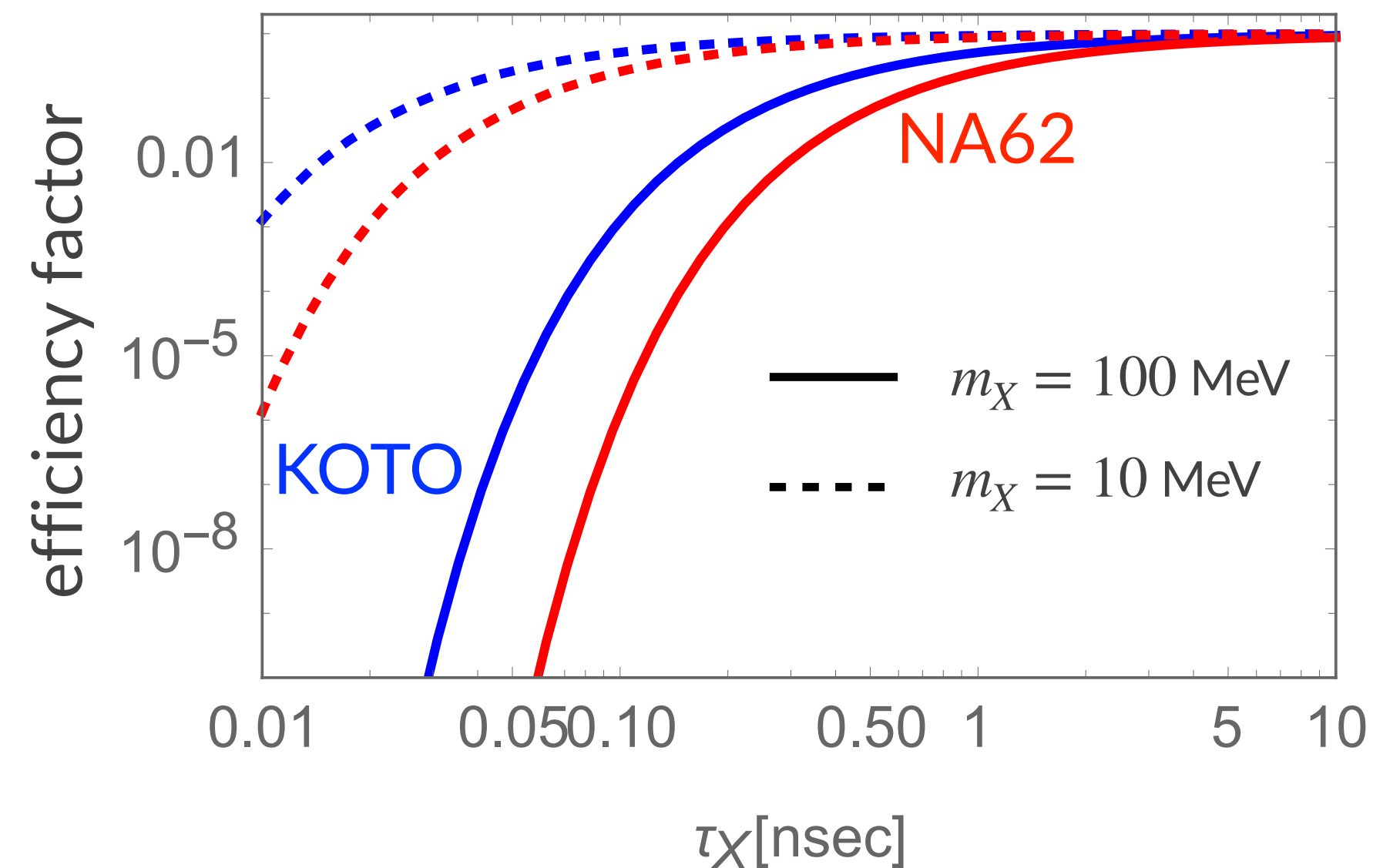
Effective violation of GN bound “lifetime gap”

- ◆ Probability that X does not decay in the detector volume
= efficiency factor that X looks missing neutrinos

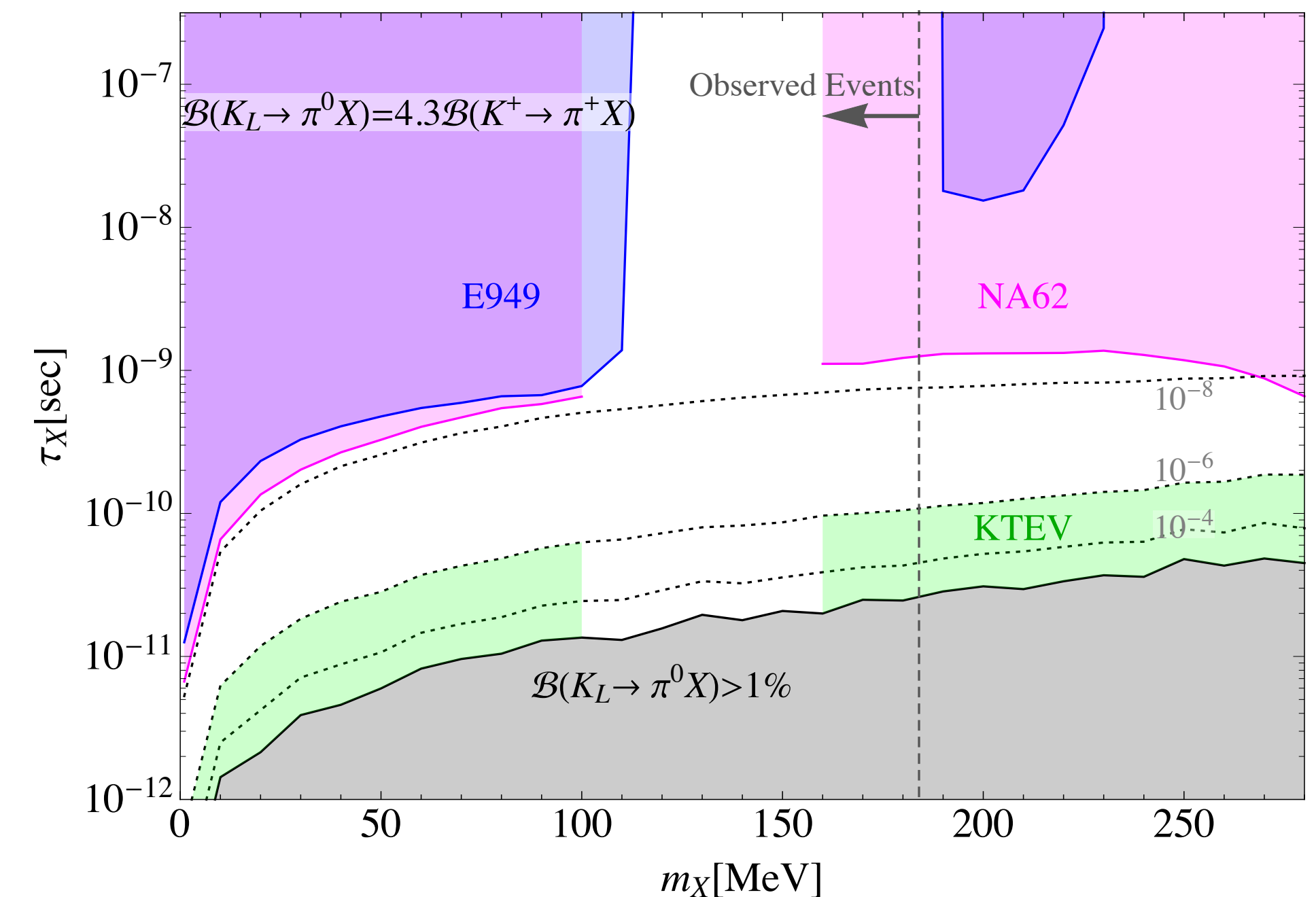
$$P = \exp\left(-\frac{L}{\gamma\beta\tau_X}\right) = \exp\left(-\frac{L}{(E_X/m_X)\beta\tau_X}\right) \simeq \exp\left(-\frac{Lm_X}{p_X\tau_X}\right)$$

(Energy scale)² $\gg m_X^2$

Efficiency difference
=
Effective violation of
the GN bound



<Assuming 3 KOTO signals>



Comments

- ◆ <3 KOTO signals> are assumed in many plots. Now, this assumption should be changed.
- ◆ We should take special care to the KTeV/NA48 data of $\text{BR}(K_L \rightarrow \pi^0 \gamma \gamma)$ which are consistent with SM prediction and new particle X must decay there [Liao, Wang, Yao, Zhang '20]
- ◆ FASER could probe the finite lifetime particle X via $pp \rightarrow K_L \rightarrow X \rightarrow \gamma \gamma$ [Kling, Trojanowski '20].
But, it is unclear that FASER can detect the diphoton signals
- ◆ Connection to muon $g-2$ anomaly is possible [Liu, McGinnis, Wagner, Wang '20]

Backup slide

Violation of Grossman-Nir bound by isospin-violating operators

Violation of Grossman-Nir bound by kinematics

Effective violation of Grossman-Nir bound by pion-mass new physics

Isospin-violating operators; other examples

- ◆ Isospin-violating axion operator = dimension 8

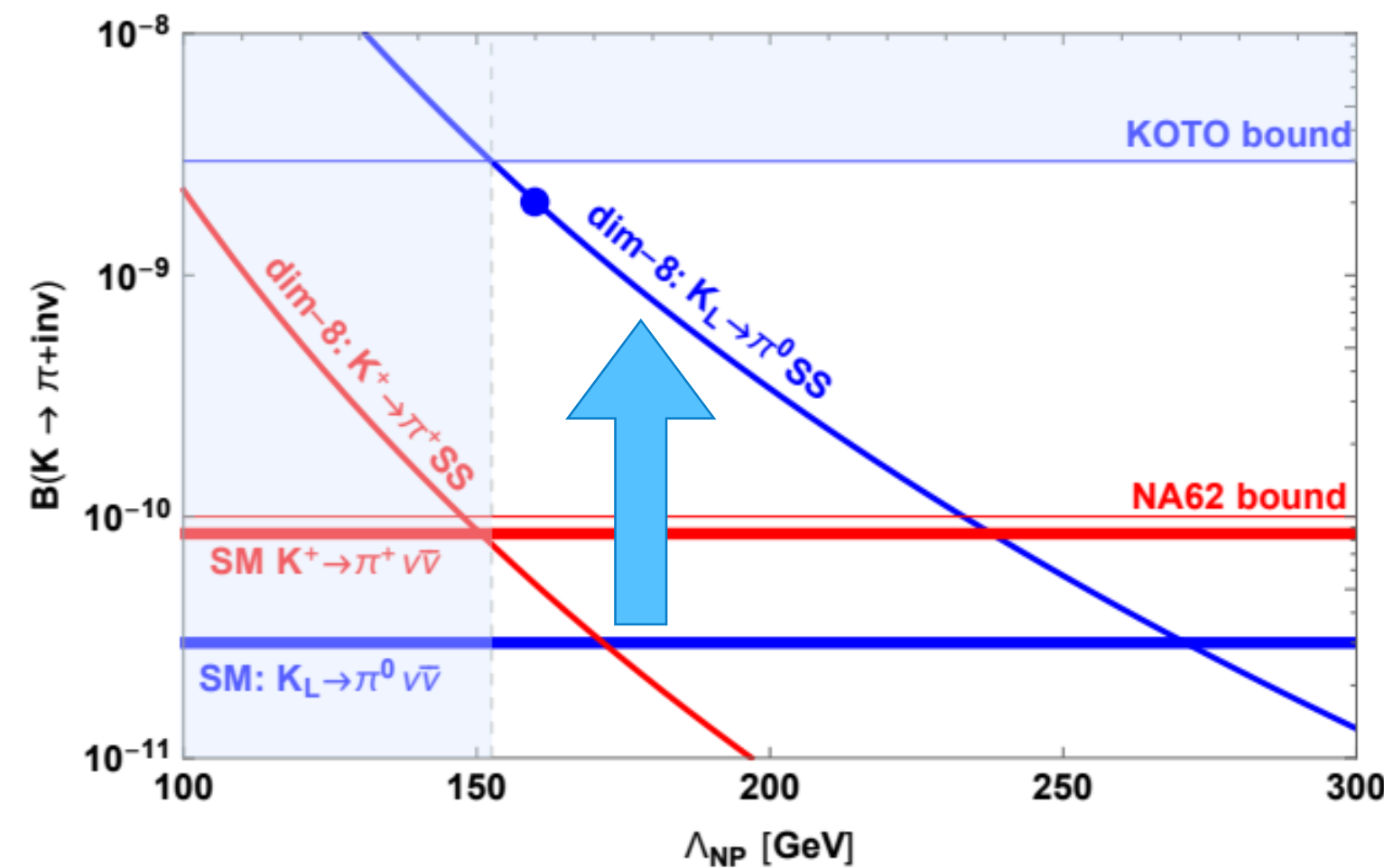
$$\mathcal{L} = \frac{1}{\Lambda^4} \partial_\mu a (\bar{s} \gamma^\mu d) (\bar{u} u - \bar{d} d)$$

[TK, Okui, Perez, Soreq, Tobioka '20]

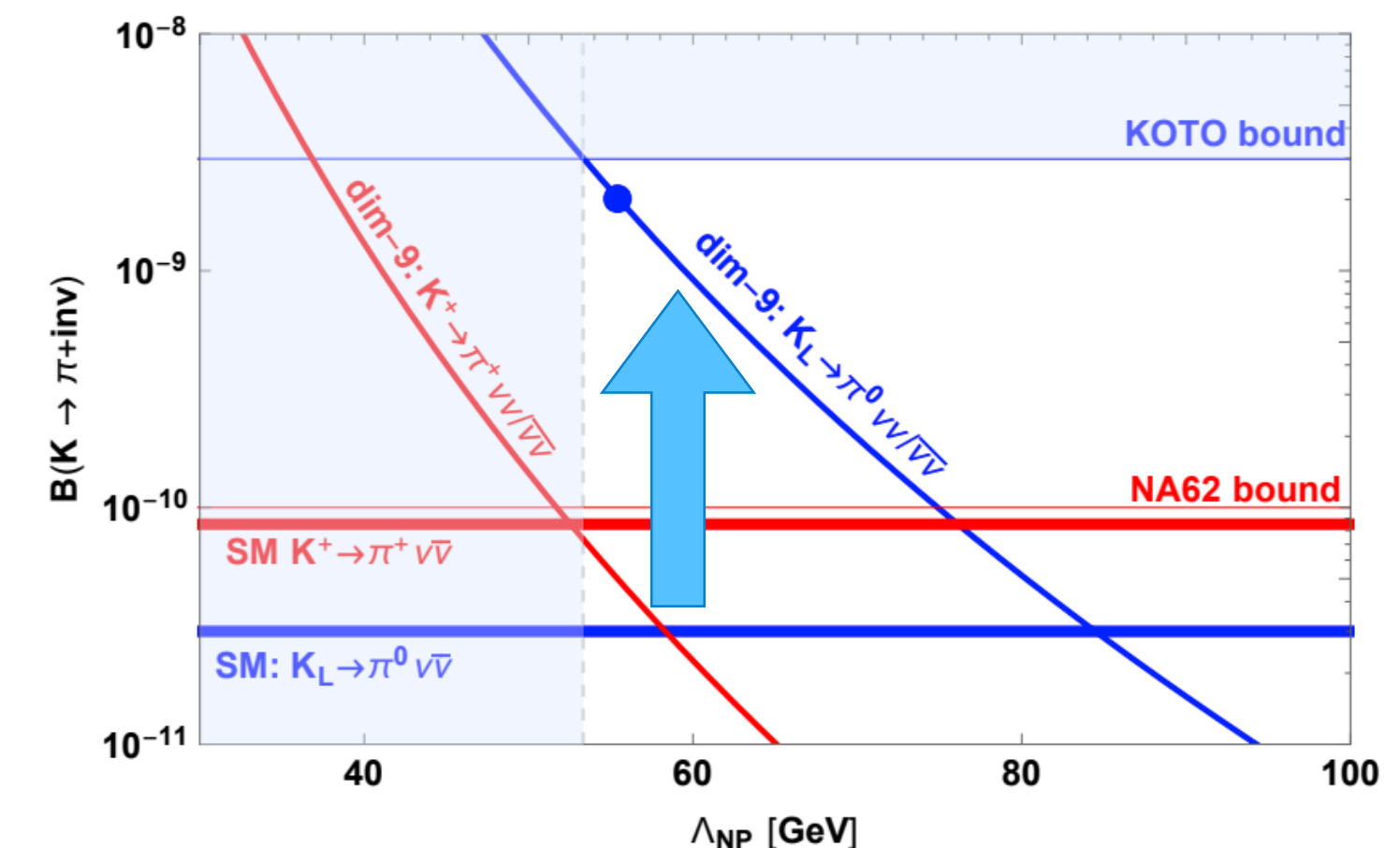
No study. But, dimension-5 axion operator is already severely constrained

- ◆ Other operators [He, Ma, Tandean, Valencia '20, '20]

$(\bar{s}d)(\bar{q}q) S^2$: dimension-8



$(\bar{s}d)(\bar{q}q)(\bar{\nu}^c \nu)$: LNV dimension-9



Note: $(\bar{s}d)(\bar{q}q)(\bar{\nu}\nu)$ enters from dimension-10

By kinematics

- ◆ Simple idea: violating the Grossman-Nir bound is just kinematics:

$$m_{K_L} = 497.6 \text{ MeV}$$

$$m_{\pi^0} = 134.9 \text{ MeV}$$

$$\Delta m = 362.7 \text{ MeV}$$

$$m_{K^\pm} = 493.6 \text{ MeV}$$

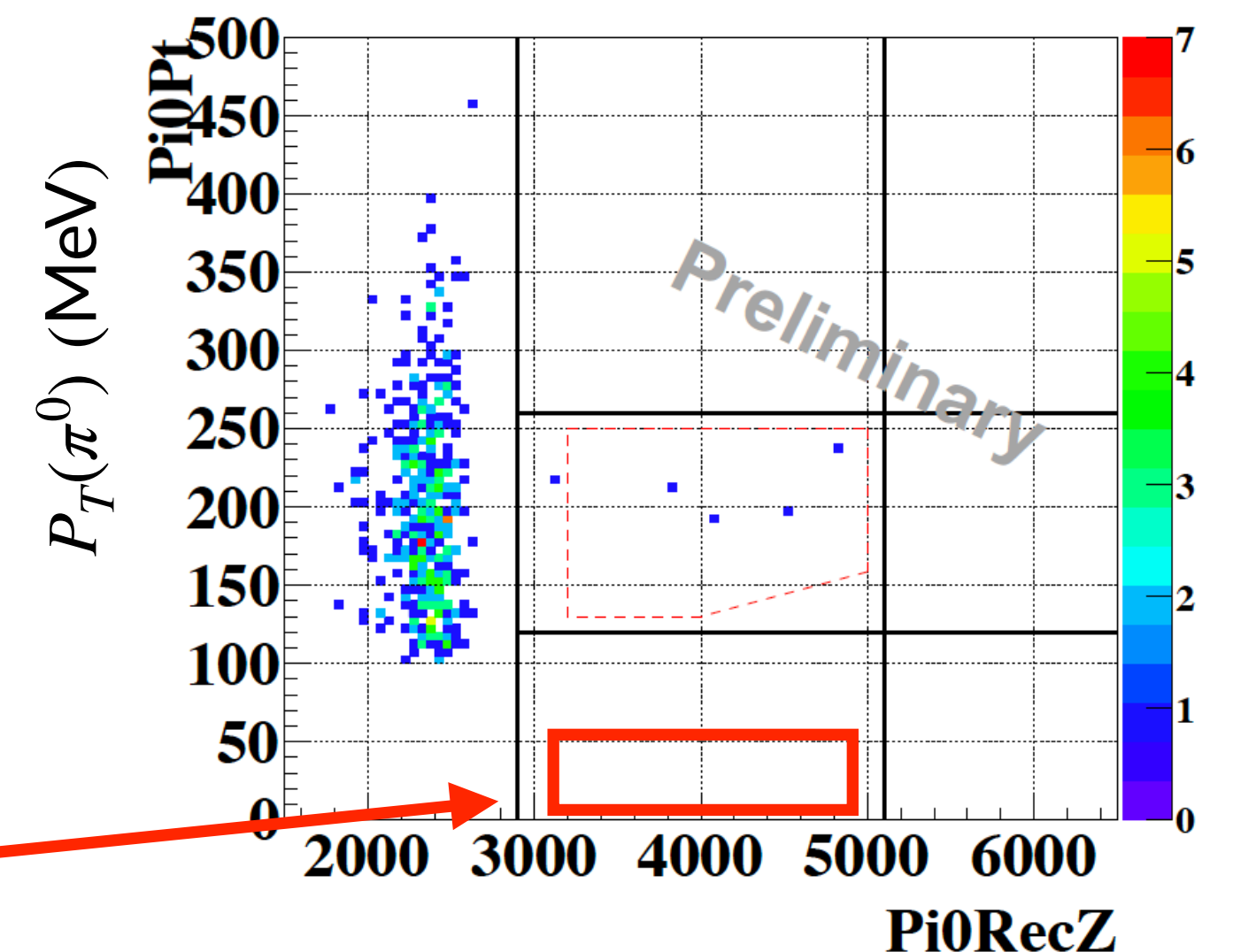
$$m_{\pi^\pm} = 139.5 \text{ MeV}$$

$$\Delta m = 354.1 \text{ MeV}$$

(Mass difference comes from the radiative corrections within the SM)

- ◆ $K_L \rightarrow \pi^0$ has a larger phase space than $K^+ \rightarrow \pi^+$
- ◆ Can new 360 MeV particle explain signals? → **Impossible**
- ◆ **Emitted π^0 is too soft, the missing pT can not become large**

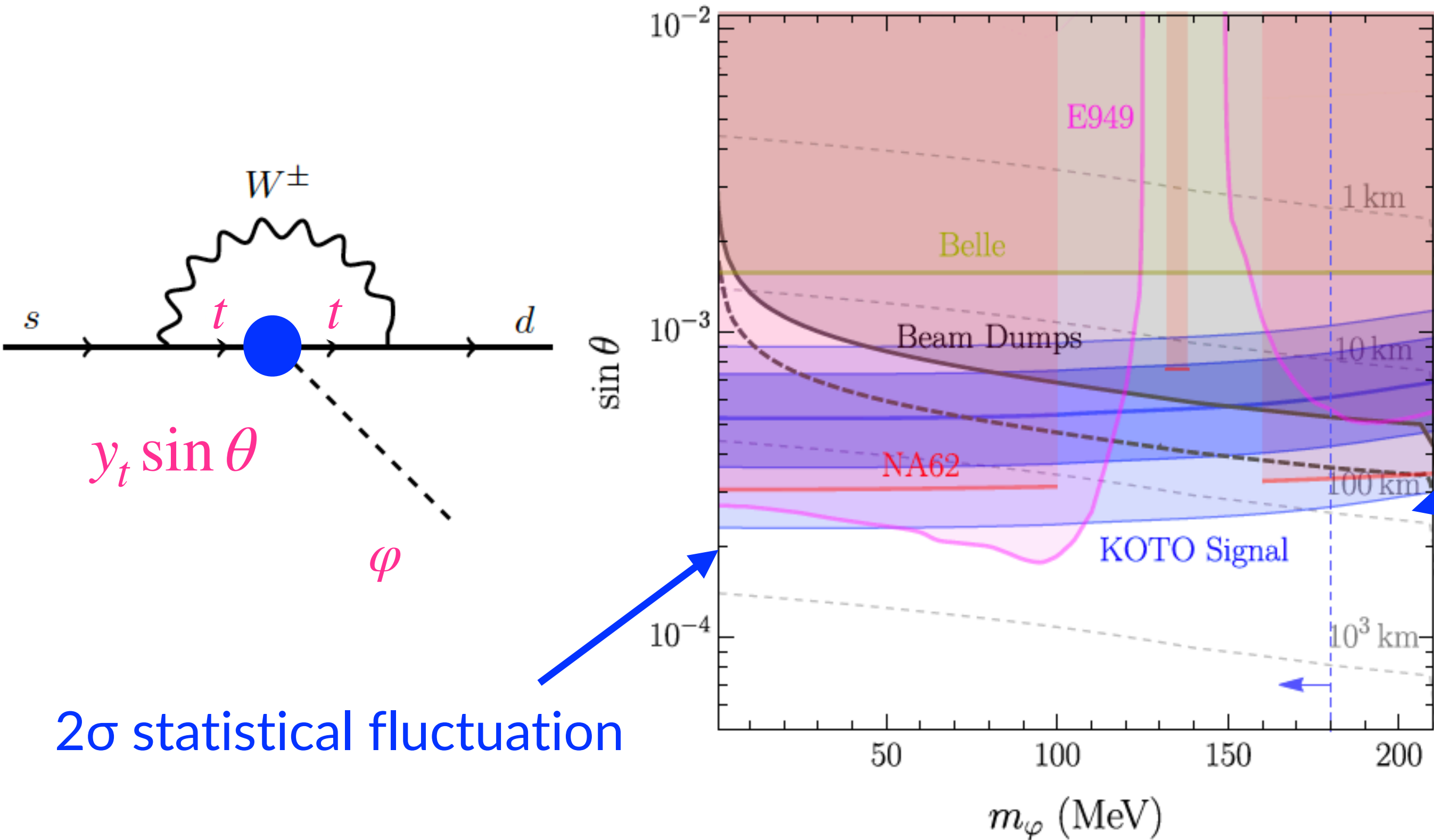
Predicted signal region [Fabbrichesi, Gabrielli '20]



Pion-mass new physics: minimal Higgs portal

[Egana-Ugrinovic, Homiller, Meade '20, Bhupal Dev, Mohapatra, Zhang '20]

- ◆ SM + light CP-even scalar φ , which mixes with the SM Higgs by $\sin \theta$



Dashed-gray contour: $c\tau_\varphi$,
 φ is stable within detectors
 $BR(\varphi \rightarrow ee) \sim 100\%$

“ π^0 blind spot”
 The constraint from $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
 is significantly loosened by the
 background of $K^+ \rightarrow \pi^+ \pi^0$
 [Fuyuto, Hou, Kohda '15]