

LCWS MiniSchool

Online, March 15^h, 2021

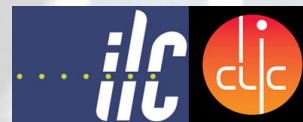
Electron-Positron Colliders

energy and luminosity, damping rings, polarization,...

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DER FORSCHUNG | DER LEHRE | DER BILDUNG

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Contents:

- **Introduction:** Acceleration, Luminosity, Colliders, ...
- **Acceleration:** Cavities, Key Parameters, nc and sc Linacs
- **Acc. Phys. Basics:** Emittance, Optical Functions and Resonances, ...
- **Luminosity:** Crossing Angle, Hourglass, Beam-Beam, ...
- **Add. Systems:** Polarization, Damping Rings, ...
- **e⁺-e⁻ Projects:** ILC, CLIC, FCC-ee, CEPC

Accelerators for Particle Physics

Particle Physicists wish list comprises the following:

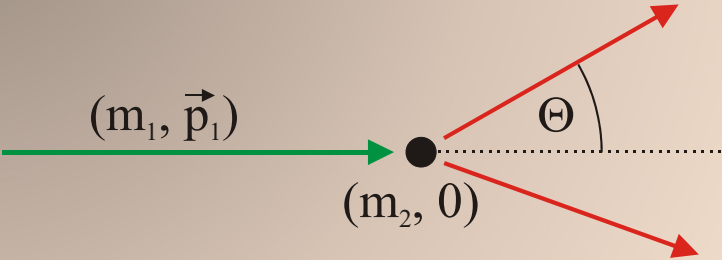
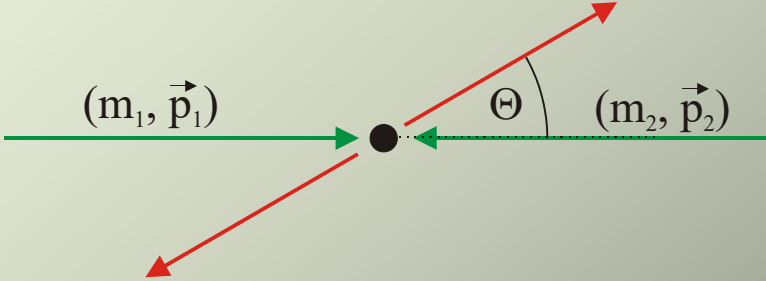
- TeV beams of all kind of particles (γ , e , μ , p , ...)
- highest luminosity, that means in particular:
 - a) premium beam quality and performance
 - b) ultimate intensity while having stable beam delivery all the time
- polarized particles of all kinds (preferably antiparticles like e^+ and \bar{p})
- enough free space to place huge detectors

2 Classes of High-Energy Accelerators:

- **Hadron Colliders:** Highest achievable energies
→ “**discovery potential**”
- **e^+ - e^- Colliders:** well-known and understood electromagnetic vertex
→ “**precision machines**”

Why Colliders?

(Units: $\hbar = c = 1$)

Fixed Target Experiment	Colliding Beams
 $S = P_1 + P_2 = (E_1 + m_2, \vec{p}_1 + \vec{p}_2)$ $\vec{\beta}_{CMS} = \frac{\vec{p}_1}{E_1 + m_2}$ $M_{inv}^2 = S^2 = 2 E_1 m_2 + m_1^2 + m_2^2$	 $S = P_1 + P_2 = (E_1 + E_2, \vec{p}_1 + \vec{p}_2)$ $\vec{\beta}_{CMS} = \frac{\vec{p}_1 + \vec{p}_2}{E_1 + E_2} = 0$ $M_{inv}^2 = S^2 = (E_1 + E_2)^2$

Example: p-p Collisions, want $S = 1$ TeV
requires:

$$E = 500 \text{ TeV}$$

$$E = 0.5 \text{ TeV}$$



Beam Acceleration

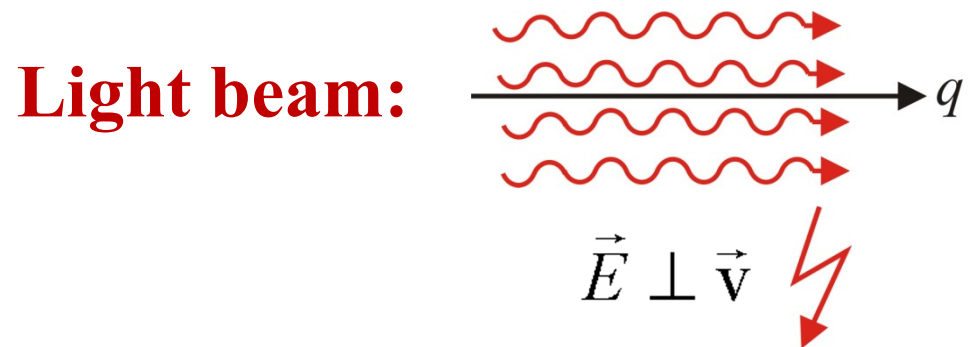
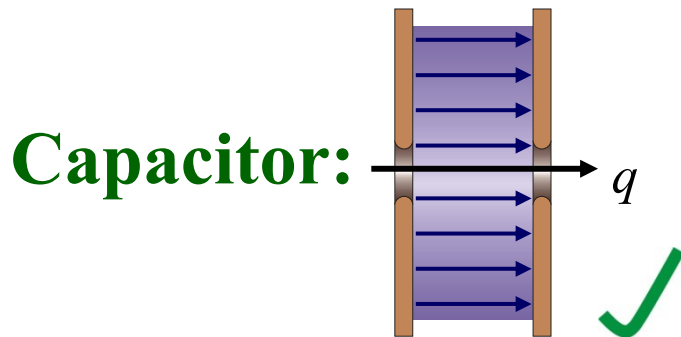


Charged particles are influenced by the

Lorentz force: $\vec{F} = e \cdot \vec{E} + e \cdot (\vec{v} \times \vec{B})$

$$\text{Energy gain: } \Delta W_{kin} = \int \vec{F} \cdot d\vec{s} = e \cdot \int E_{\parallel} \cdot ds = e \cdot U$$

→ We need a longitudinal electrical field E_{\parallel} !



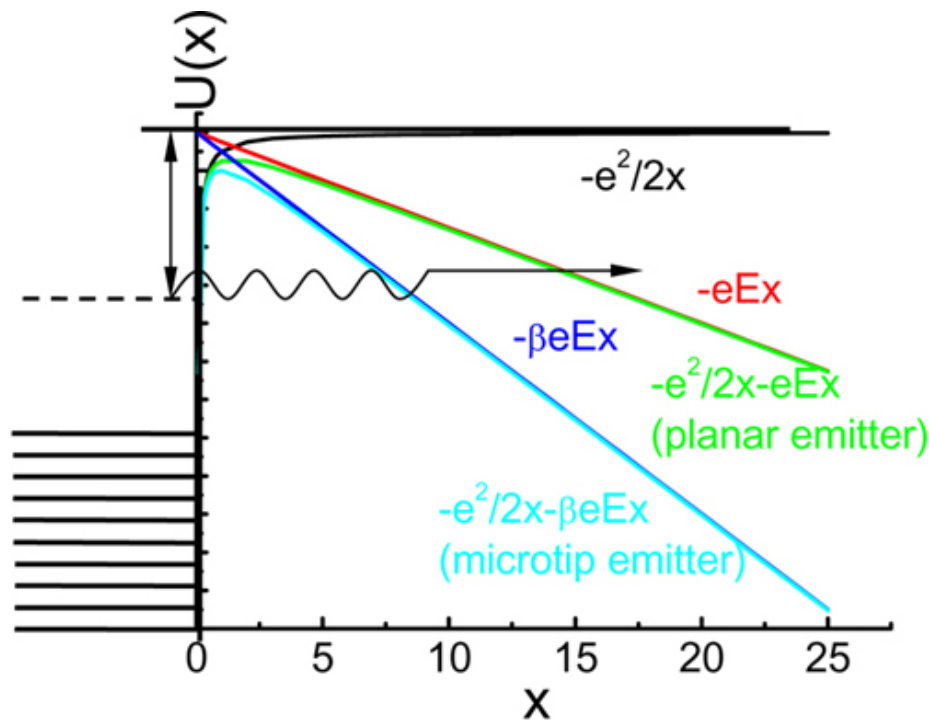
Field Emission / Breakdown

Coulomb-Potential:

$$U = \int \vec{F} \cdot d\vec{s} = \frac{q^2}{4\pi\epsilon_0} \int \frac{ds}{r^2} = \frac{1}{4\pi\epsilon_0} \cdot \frac{-q^2}{2r}$$

homogeneous E-Field:

$$U = \int \vec{F} \cdot d\vec{s} = \int q\vec{E} \cdot d\vec{s} = -qEr$$



Tunneling!
Enhancement
Factor β !!

DC

AC

$$E_{\max} \leq 10 - 100 \text{ MV/m}$$



Beam Acceleration

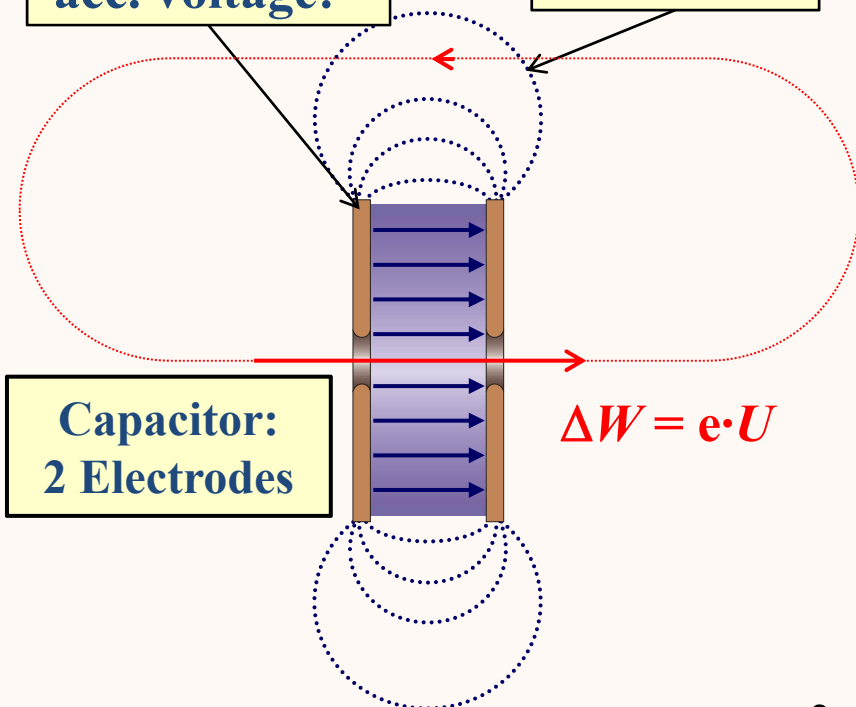


Breakdown:

$$E = U/R$$

limits max.
acc. voltage!

$$\oint \vec{E} \cdot d\vec{s} = 0$$

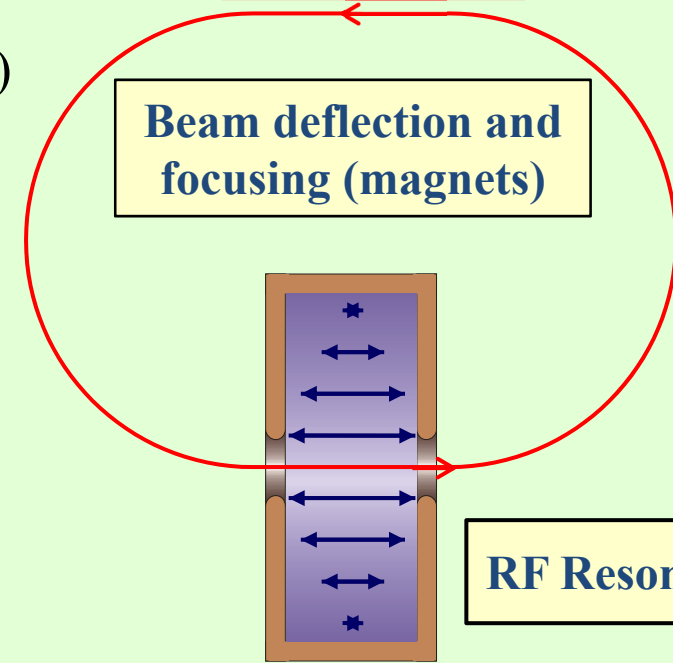


☹ Electrostatic Acceleration ☹

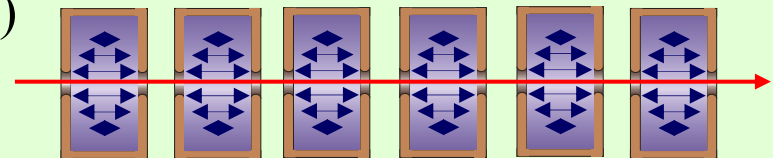
$$\Delta W = n \cdot e \cdot U$$

a)

Beam deflection and
focusing (magnets)

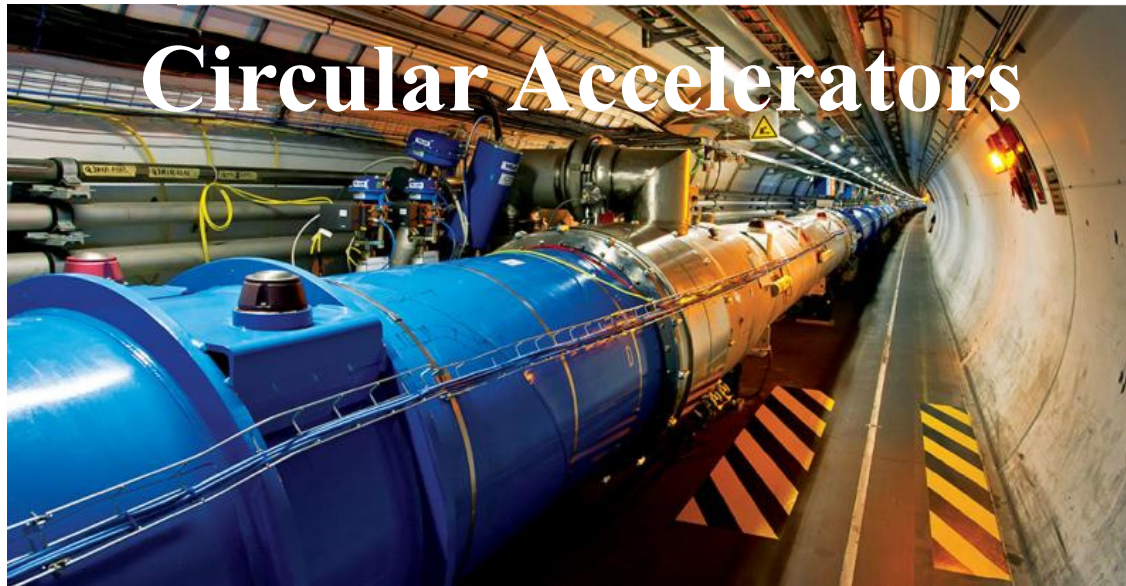


b)



☺ RF-based Acceleration ☺

Building a TeV Accelerator



Circular Accelerators

Example LHC $\rightarrow e^+e^-$:

Bending Magnets: $B = 8.33\text{T}$

Bending Radius: $R = \frac{p}{eB}$

Beam Energy $E_{\text{kin}} = 0.5\text{ TeV!}$

$$R = \frac{pc}{ecB} = \frac{5 \cdot 10^{11}}{3 \cdot 10^8 \cdot 8.33} \approx 200\text{m}$$

$$\Rightarrow L = 2\pi R + x \approx 5\text{km}$$



Linear Accelerators

Example XFEL $\rightarrow e^+e^-$:

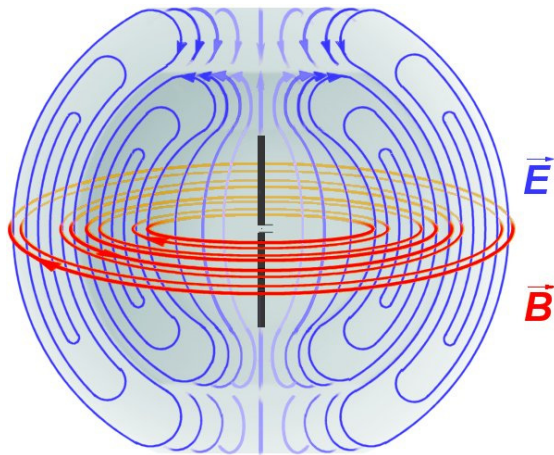
Achieved: $U_{\text{accel}} = 29.5\text{ MV/m}$

Beam Energy $2E_{\text{kin}} = 1\text{ TeV!}$

$$\Rightarrow L = \frac{2E_{\text{kin}}}{U_{\text{accel}}} + x \approx 50\text{km}$$

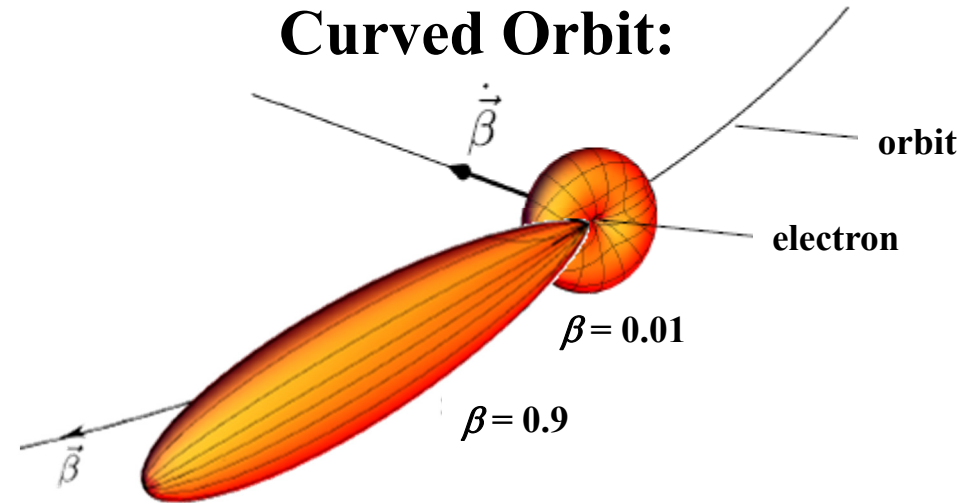
Acceleration \leftrightarrow Radiation:

Hertz Dipole:



$$P = \frac{e^2}{12\pi\epsilon_0 c^3} \cdot \omega^4 d^2$$

Curved Orbit:



$$P = \frac{e^2 c}{6\pi\epsilon_0} \cdot \frac{\gamma^4}{R^2}$$

„Circumference Voltage“ (electrons):

$$U [\text{kV}] = 88.5 \cdot \frac{E^4 [\text{GeV}^4]}{R [\text{m}]}$$

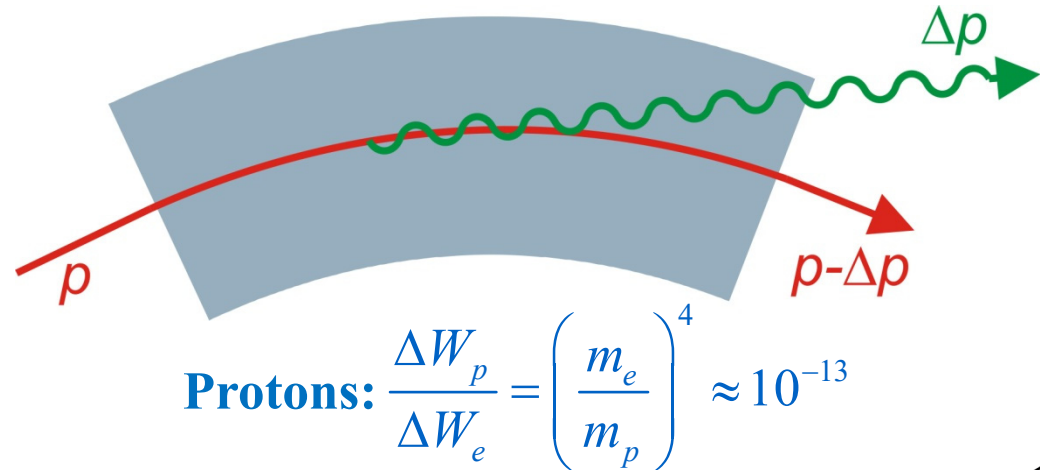


Limitations in Circular Accelerators

Electrons:

→ Synchrotron Radiation
energy loss per turn:

$$\Delta W[\text{keV}] = 88.5 \cdot \frac{E^4[\text{GeV}^4]}{R[\text{m}]}$$



Example:

LHC bending radius $R = 2.8\text{km}$ (circumference = 27km)

electron beam energy $E_{\text{kin}} = 500\text{GeV} = 0.5\text{TeV}$:

→ energy loss per turn $\Delta W = 2 \text{ TeV}!!!$

Acceptable:
 $\Delta W < 10 \text{ GeV}$
→ $R > 500\text{km}!$

Large Electron Positron Collider

LEP Parameters:

$$E \leq 104.5 \text{ GeV}$$

$$R \approx 3.1 \text{ km}$$

$$B \approx 0.12 \text{ Tesla}$$

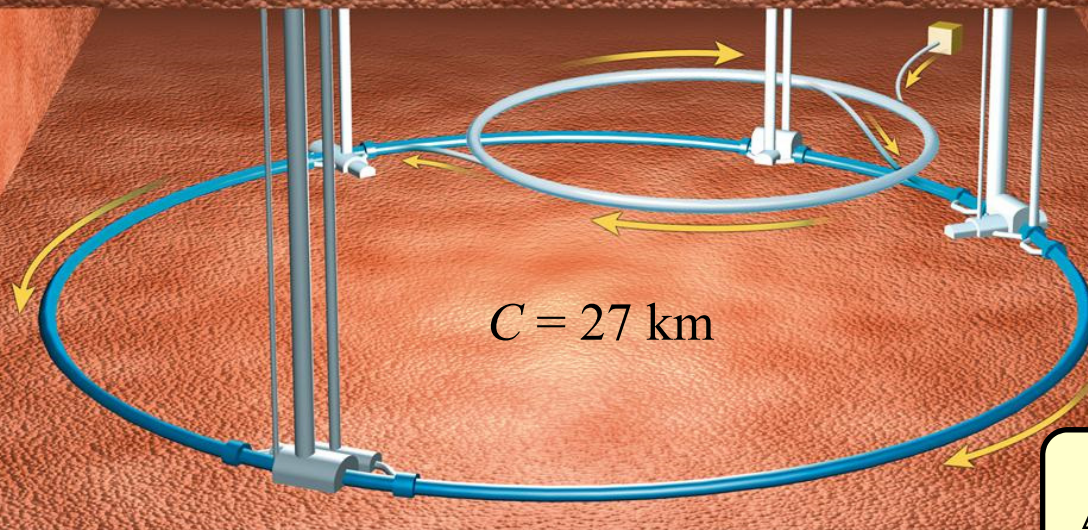
$$P_{\text{RF}} \approx 30 \text{ MW}$$

$$\mathcal{L} \approx 10^{32} \text{ cm}^{-2}\text{s}^{-1}$$

$$P_{\text{RF}} \sim E^4$$

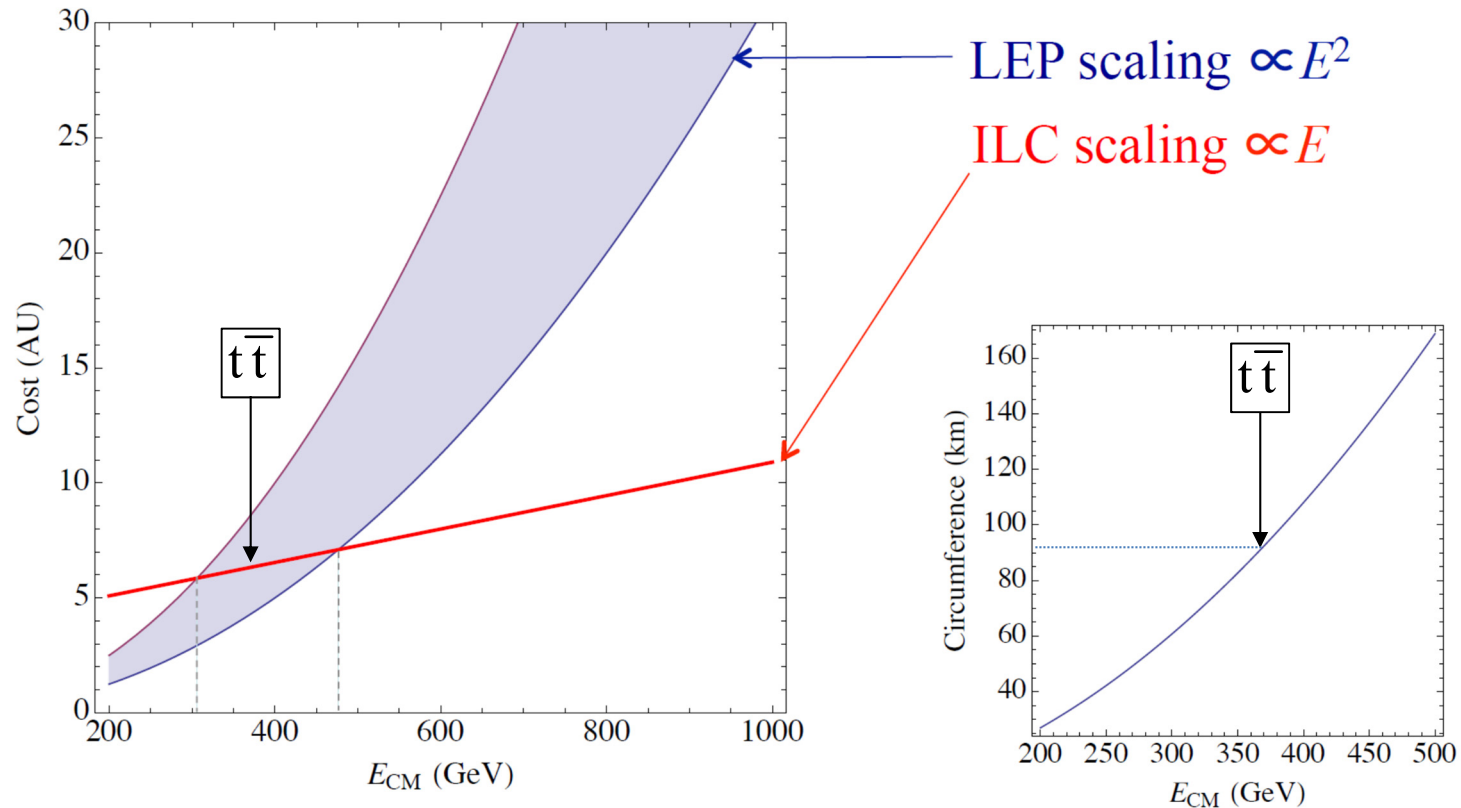
if “upgraded”:

$$P_{\text{RF}} \sim E^8$$



$$\Delta W \approx 3.5 \text{ GeV}$$

\$ Scaling of Colliders



Linear Collider clearly “wins” @ $E_{CM} > 500$ GeV!!

Circular Collider: $\$_{RF} \propto \frac{E^4}{R}$, $\$_{CC} \propto R \Rightarrow$ Optimum: $\frac{E^2}{R} = \text{konst.} \rightarrow \$_{\Sigma} \propto E^2$



Avg. Beam Current



Important for achievement of enough wanted reactions in collisions.

Obviously: the more (colliding particles) the better!

Circular Collider (FCC-ee):

- RF has to compensate SR losses, 50MW per beam acceptable
- max average beam current:

$$I_{avg} = 29 \text{ mA @ H, } I_{avg} = 5,4 \text{ mA @ } \bar{t}\bar{t}$$

Linear Collider (ILC):

- RF $\rightarrow P_{beam}$, but limited: e.g. 5 x 1312 bunches/sec with $N_b = 10^{10}$ particles (ILC)
- max average beam current:

$$I_{avg} = 11 \mu\text{A @ H and @ } \bar{t}\bar{t}$$

\rightarrow has this consequences?

Luminosity

... the unknown divinity ...

One of the most important acc. parameter for particle physicists!

- Luminosity**

$$\dot{N} = \sigma \cdot \mathcal{L}$$

- Integrated Luminosity:**

$$\dot{N} = \sigma \cdot \int_{t\text{-meas.}} \mathcal{L} \cdot dt = \sigma \cdot \mathcal{J}$$

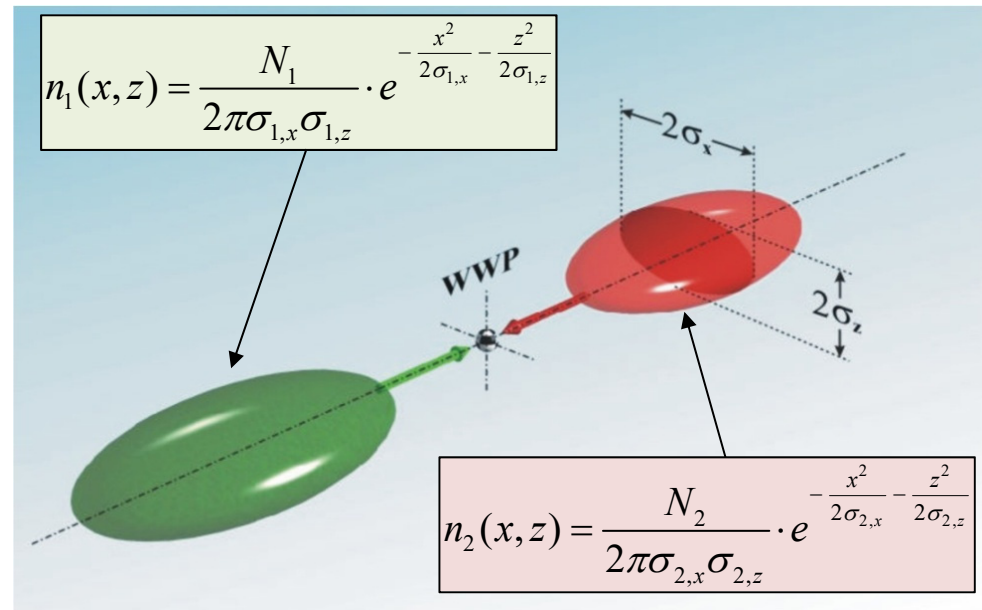
$$N_{b,b} = \sigma \cdot \iint n_1(x, z) \cdot n_2(x, z) \cdot dx dz$$



e⁺-e⁻, p-p Collider:

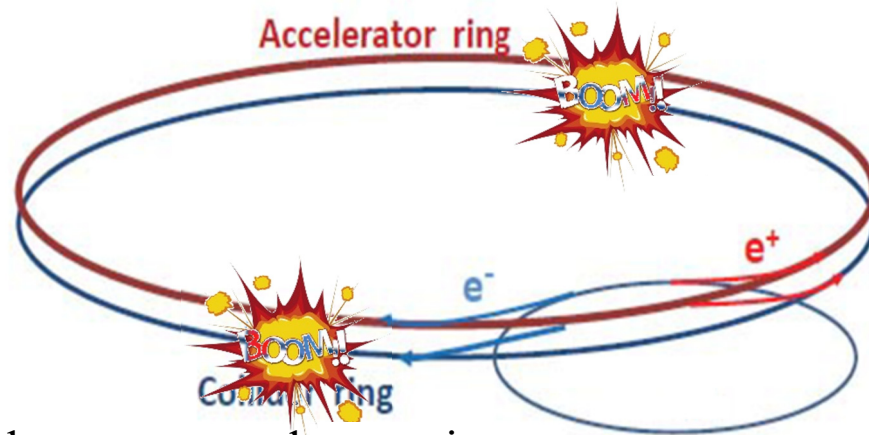
$$\sigma_1 = \sigma_2 = \sigma$$

$$\mathcal{L} = \frac{n_b \cdot f_{rev}}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_z}$$



Colliders

Circular

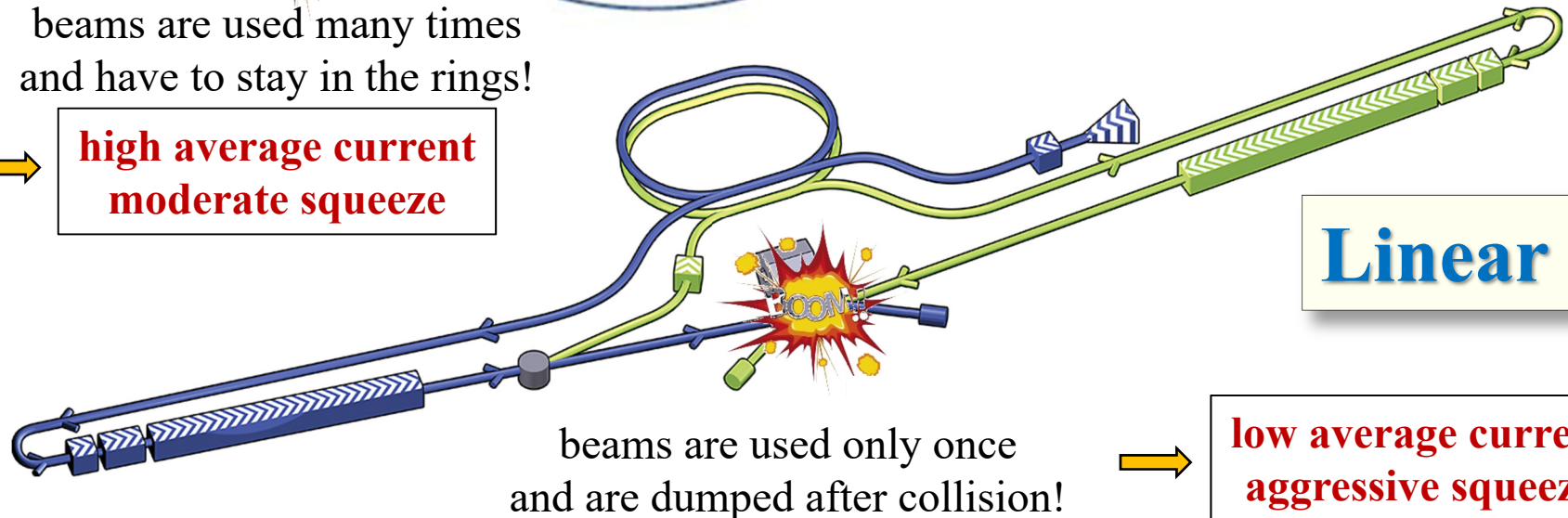


beams are used many times
and have to stay in the rings!

high average current
moderate squeeze

Luminosity:

$$\mathcal{L} = \frac{n_b \cdot f_{rev}}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_z}$$



beams are used only once
and are dumped after collision!

Linear

low average current
aggressive squeeze

Introduction Summary

Essence: What do we have to learn in the next hour?

- **How do we accelerate electrons (positrons) to \sim TeV?**
 - **Crash course in RF acceleration:**
 - Cavities and their important parameters
 - Standing wave (sc) and travelling wave (nc) Linac structures
- **How can we achieve a maximum (acceptable) luminosity?**
 - **Crash course in beam dynamics in accelerators:**
 - How much can and should we squeeze? (\rightarrow final focus, damping rings, ...)
 - What limits the intensity? (\rightarrow RF, beam-beam, instabilities, ...)
 - **What else matters?** (beam-beam, beamstrahlung, wakefields, ...)
- **What about polarized beams?**
 - **Summary: Linear vs. Circular Collider – pros and cons**

Acceleration



Linear Collider:

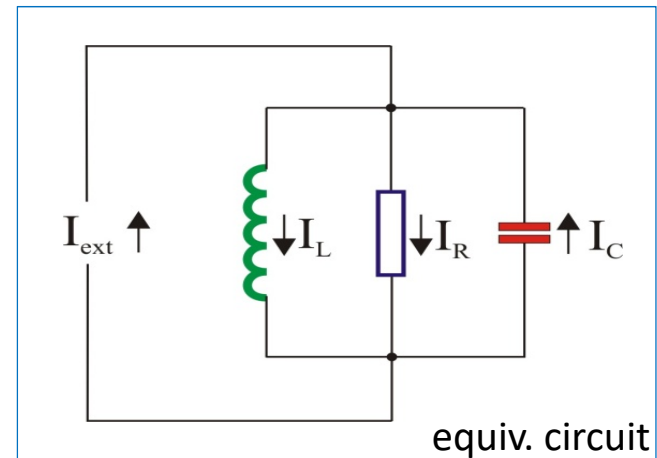
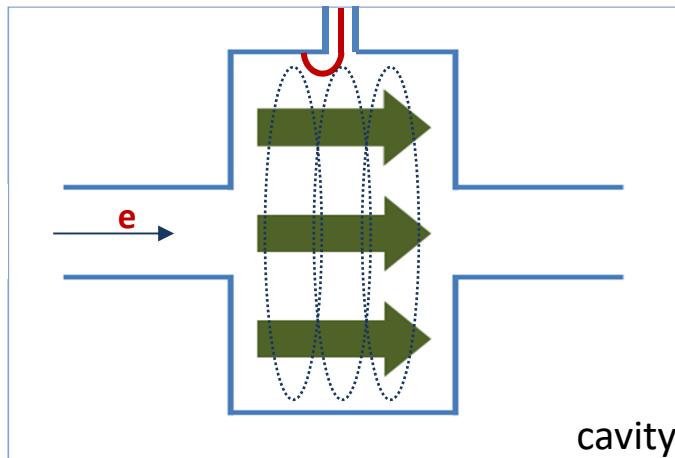


Circular Collider:



Cavities

General Idea: high accelerating field caused by resonance magnification



Parameters of interest:

- resonance frequency
- quality factor
- shunt impedance

$$\omega_0 = 1/\sqrt{LC} = \text{determined by geometry}$$

$$Q = \omega_0 RC = \frac{R}{\omega_0 L} = \frac{2\pi \cdot W_{\text{stored}}}{T_{\text{RF}} \cdot P_{\text{walls}}} = \omega_0 \tau_e$$

$$R_s = R = Z(\omega_0) = \text{resistance on resonance}$$

$R_s/Q = \text{geom.}$

Accelerating voltage: $P_{\text{walls}} = \frac{U^2}{2R_s} \rightarrow \text{requires } P_{\text{RF}} = \frac{U^2}{2R_s} + U \cdot I_{\text{beam}}$

Shunt Impedance

Determines unwanted power losses in cavity walls!

Typical values and scaling of R_S and Q ($f_{res} = 1.3$ GHz):

- normal conducting cavities (copper, ~1 meter long resonator):

$$R_S \approx 10^7 \Omega, \quad Q \approx 10^4 \quad R_S \sim \sqrt{f_{res}}, \quad Q \sim 1/\sqrt{f_{res}}$$

- superconducting cavities (niobium, ~1 meter long resonator):

$$R_S \approx 10^{13} \Omega, \quad Q \approx 10^{10} \quad R_S \sim 1/f_{res}, \quad Q \sim 1/f_{res}^2$$

$$R_S/Q \sim f_{res}$$

Losses in superconducting cavities about factor $10^5 - 10^6$ smaller!

Carnot efficiency ($T_{Cav} = 2.2\text{K}$): $\eta_{Carnot} = \frac{T_{Cav}}{T_{room} - T_{Cav}} \approx 0.7\%$

Overall cooling efficiency: $\eta \approx 0.1-0.2\%$, but R_S gain $> 10^5$!



Superconducting RF

But: Maximum accelerating field limited by H_{C2} of BCS theory to ≈ 54 MV/m!

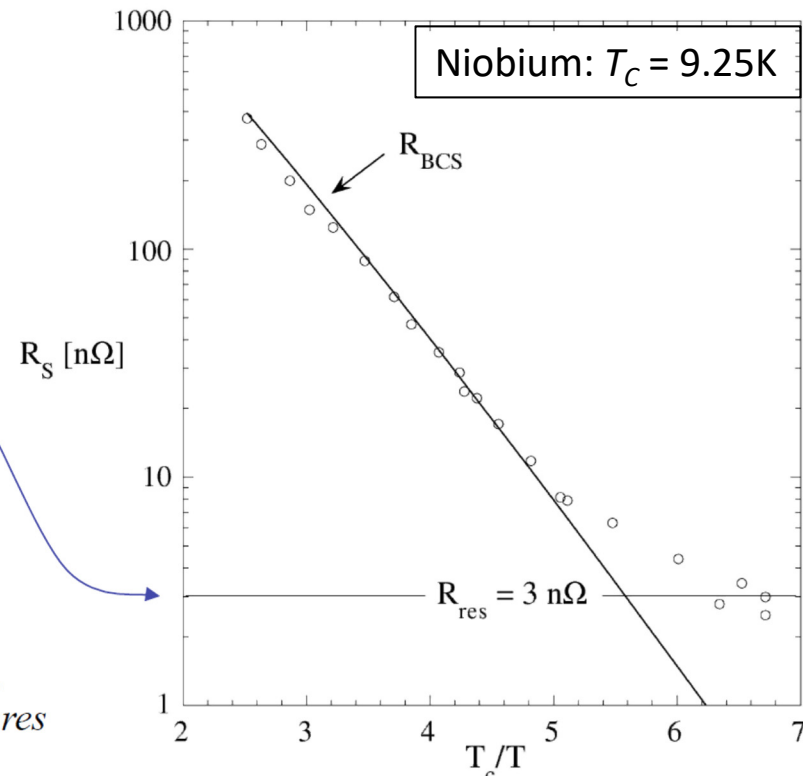
Choice of optimum frequency and temperature:

$$R_{BCS} \propto \frac{f^2}{T} \exp(-1.76T_c / T)$$

Two important parameters:

- residual resistivity R_{res}
- thermal conductivity

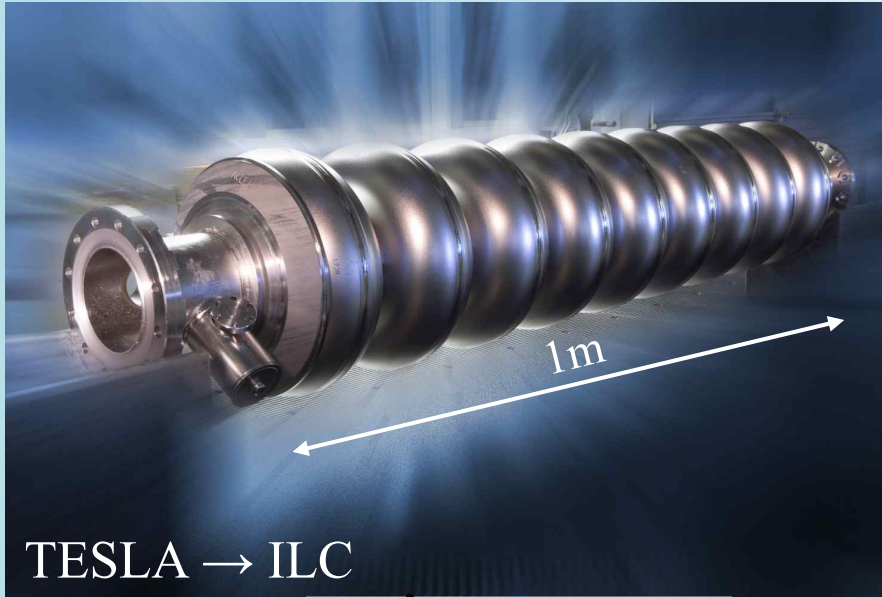
$$\text{losses} \begin{cases} \propto \text{surface area} \propto f^1 \\ R_s \propto f^2 \text{ when } R_{BCS} > R_{res} \end{cases}$$



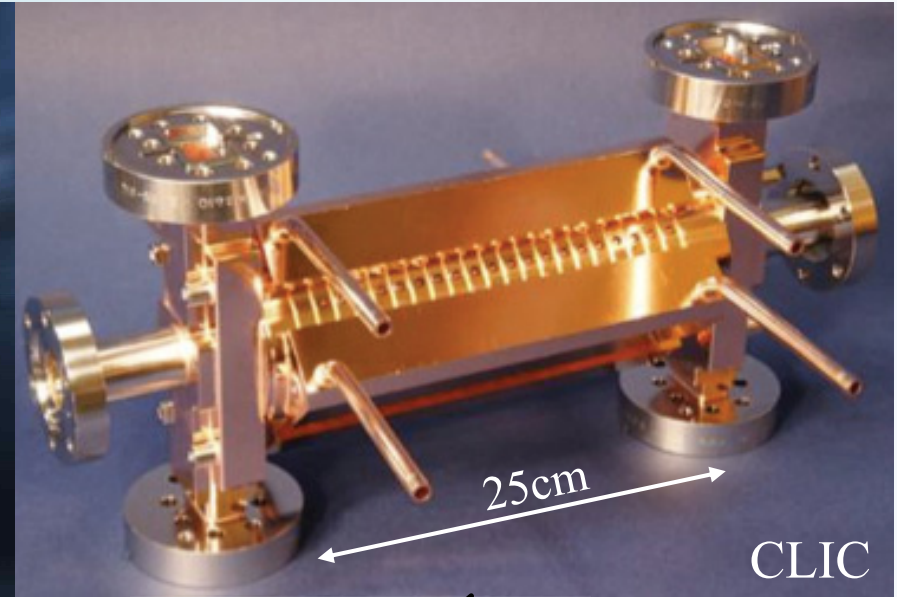
$$f_{\text{TESLA}} = 1.3 \text{ GHz}$$

$$f > 3 \text{ GHz}$$

⚡ Linear Collider: Acceleration ⚡



TESLA → ILC



CLIC

SW
 $f = 1.3 \text{ GHz}$

$$E_{\parallel} = \sqrt{2 \cdot r_s \cdot \frac{P}{L}}$$

$$E_{\parallel} = \sqrt{\frac{r_s}{Q} \cdot \frac{\omega}{v_g} \cdot P(s)}$$

TW
 $f = 12 \text{ GHz}$

Envisaged gradients:

$$E_{acc} = 31.5 \frac{\text{MV}}{\text{m}}$$

$$E_{acc} = 72(100) \frac{\text{MV}}{\text{m}}$$

Shunt Impedance and its Importance

RF power needed for generating the acc. field:

$$P_{RF} = \frac{U^2}{2R_S}$$

Let's assume 25cm and 1m long structures and $E_{kin} = 250$ GeV

a) n.c. ($E_{acc} = 72$ MV/m): $L_{RF} = 3.5$ km \rightarrow 13889 structures

RF power
$$P_{RF} = 13889 \cdot \frac{(7 \cdot 10^7 \text{ V/m})^2}{2 \cdot 10^7 \Omega} \approx 10^{11} \text{ W}$$

b) s.c. ($E_{acc} = 30$ MV/m): $L_{RF} = 8.3$ km \rightarrow 8333 structures

RF power
$$P_{RF} = 8333 \cdot \frac{(3 \cdot 10^7 \text{ V/m})^2}{2 \cdot 10^{13} \Omega} \approx 4 \cdot 10^5 \text{ W}, \eta_{cryo} = 10^{-3}$$

**P
U
L
S
E
D**

nc versus sc Linacs

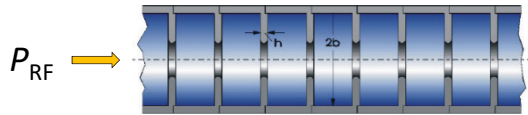
Normal Conducting Linac

Breakdown limits E_{\max} !

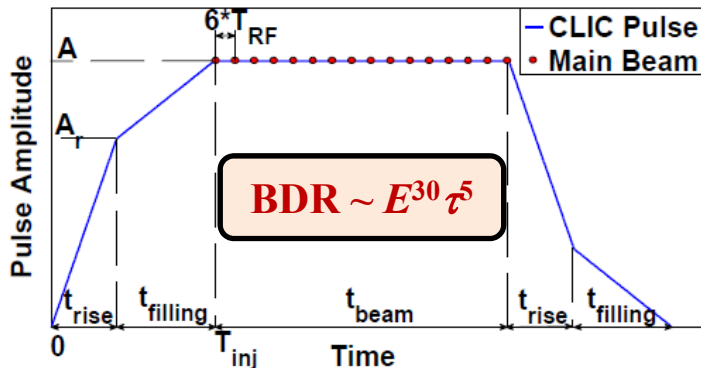
- short beam & RF pulses
- short filling times
- TW structures ($\tau_{\text{fill}} = v_g \cdot L$)
- “high” RF frequency (tolerances!)

CLIC @ CERN:

$$f_{RF} = 12 \text{ GHz}, I_b = 1.2 \text{ A}, t_b = 244 \text{ ns}$$



CLIC PULSE SHAPE OPTIMIZATION



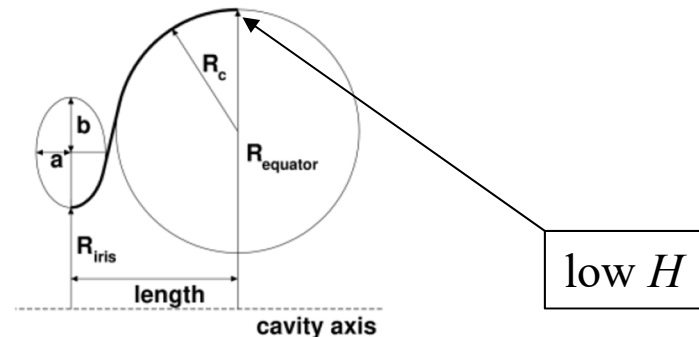
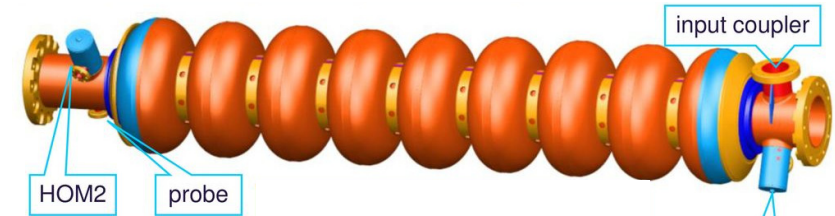
Superconducting Linac

Supercritical field H_{C2} limits E_{\max} !

- optimization for low H @ walls
- long RF pulses possible
- SW structures (\leftrightarrow low losses)
- “low” RF frequency (size)

TELSA, FLASH, XFEL \rightarrow ILC:

$$f_{RF} = 1.3 \text{ GHz}, N_b = 10^{10}, t_b = 0.65 \text{ ms}$$



Collision

→ Luminosity

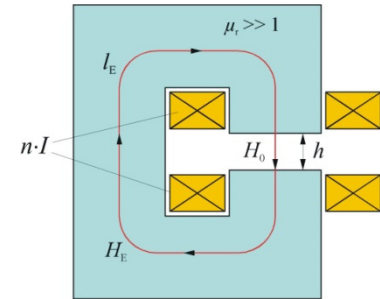


Magnets

Beam guidance:

dipole magnets

$$\frac{1}{R} = \kappa = \frac{e}{p} \cdot B_z, \quad B_z = \text{const.}$$

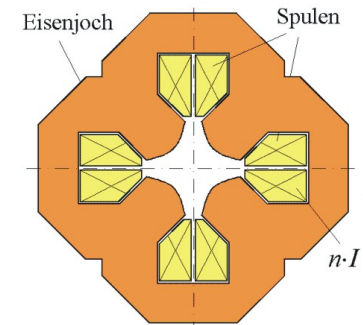


Beam focusing:

quadrupole magnets

$$\frac{1}{f} = kL, \quad B_x = \frac{p}{e} k z, \quad B_z = \frac{p}{e} k x$$

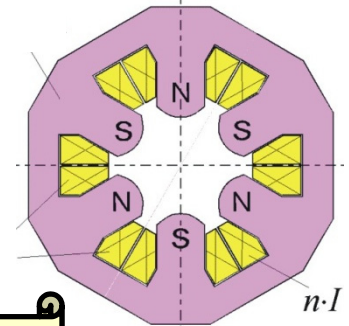
=g



Chromatic Correction:

sextupole magnets

$$B_x = \frac{p}{e} m x z, \quad B_z = \frac{p}{2e} m (x^2 - z^2)$$

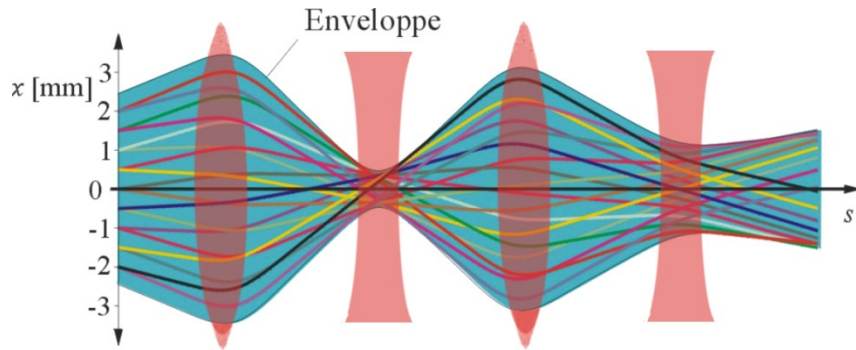


Properties defined by pole profiles

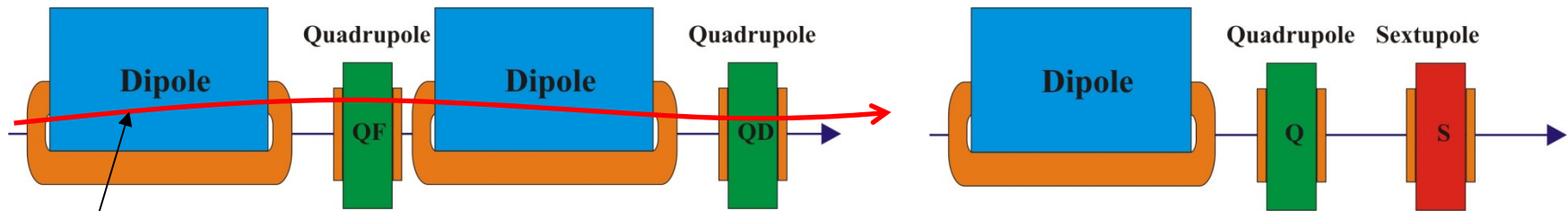
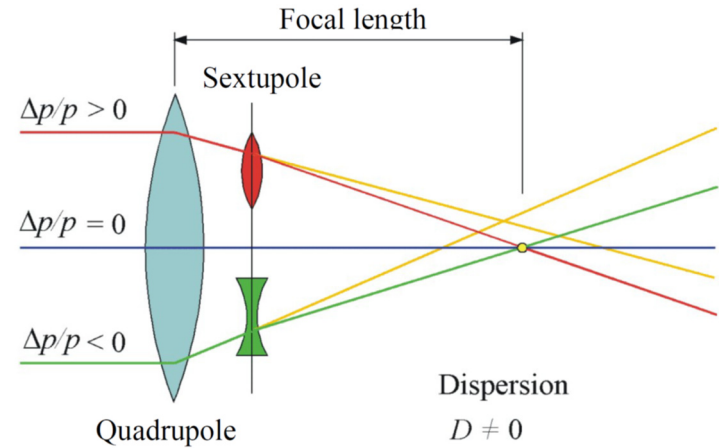
$$B \leq 2 \text{ T}$$

Strong (AG) Focusing:

Strong Focusing:



Chromatic Correction:



betatron
oscillation

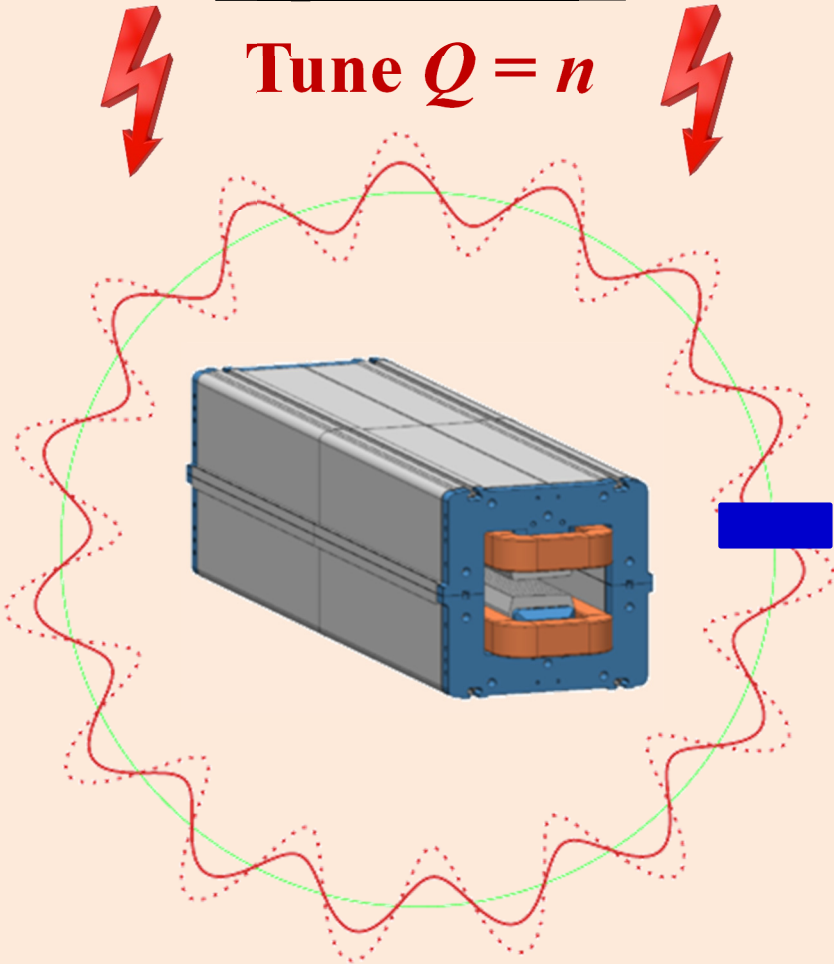
Simplest arrangement: FODO

Optical Resonances

Tune $Q = \#$ betatron oscillations per turn

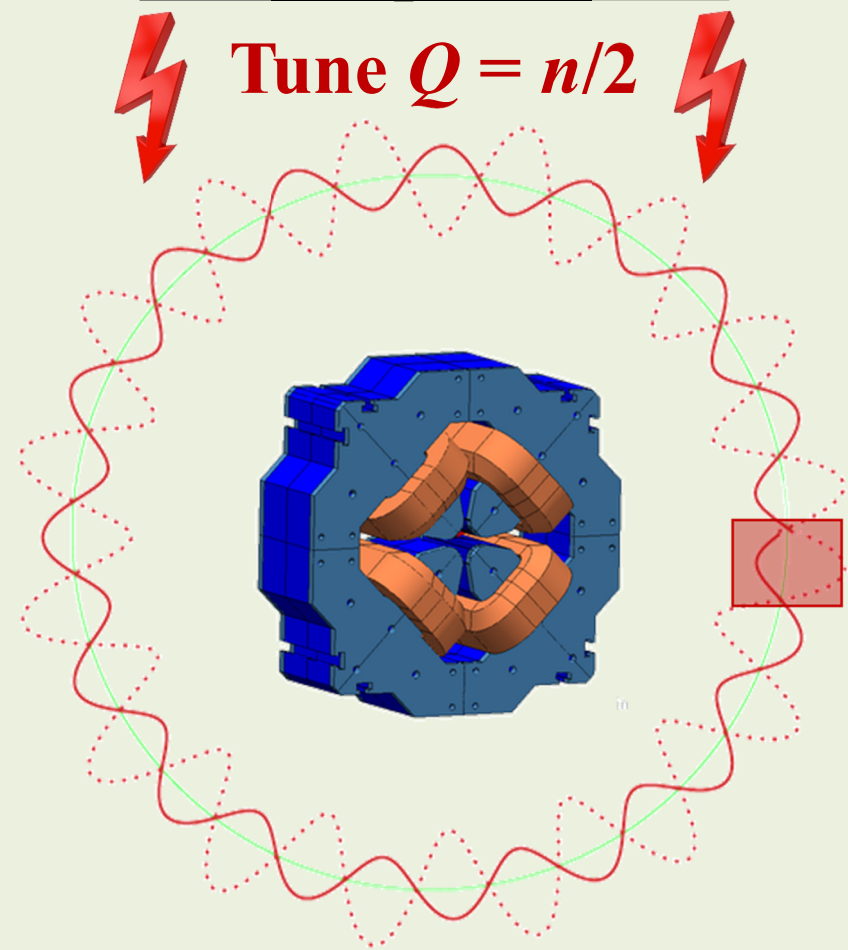
Dipole Error

Tune $Q = n$



Quadrupole Error

Tune $Q = n/2$

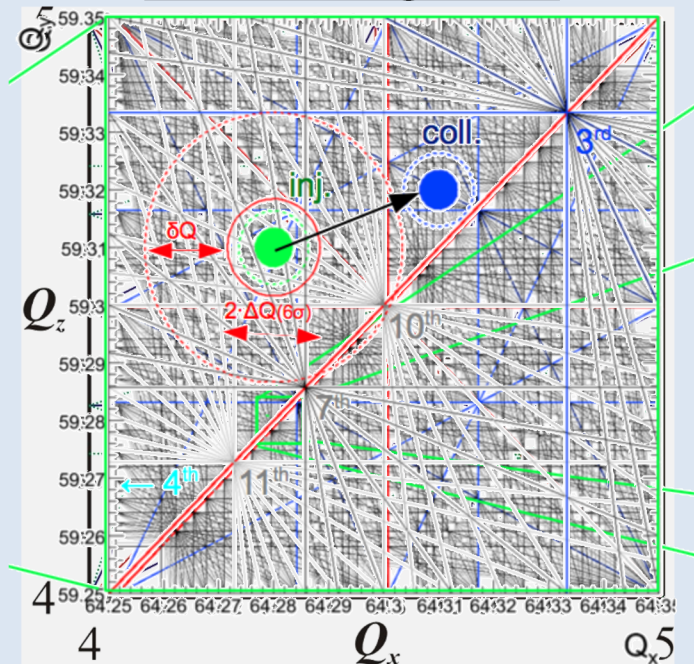


Tune and Optical Resonances:

Optical Resonances:

$$m \cdot Q_x + l \cdot Q_y = n$$

Tune Diagram:



Circular Accelerators:

- Beam-Beam Interaction
- Space Charge Forces
- Beam-Wall Interaction
- Capture of Ions / Electrons

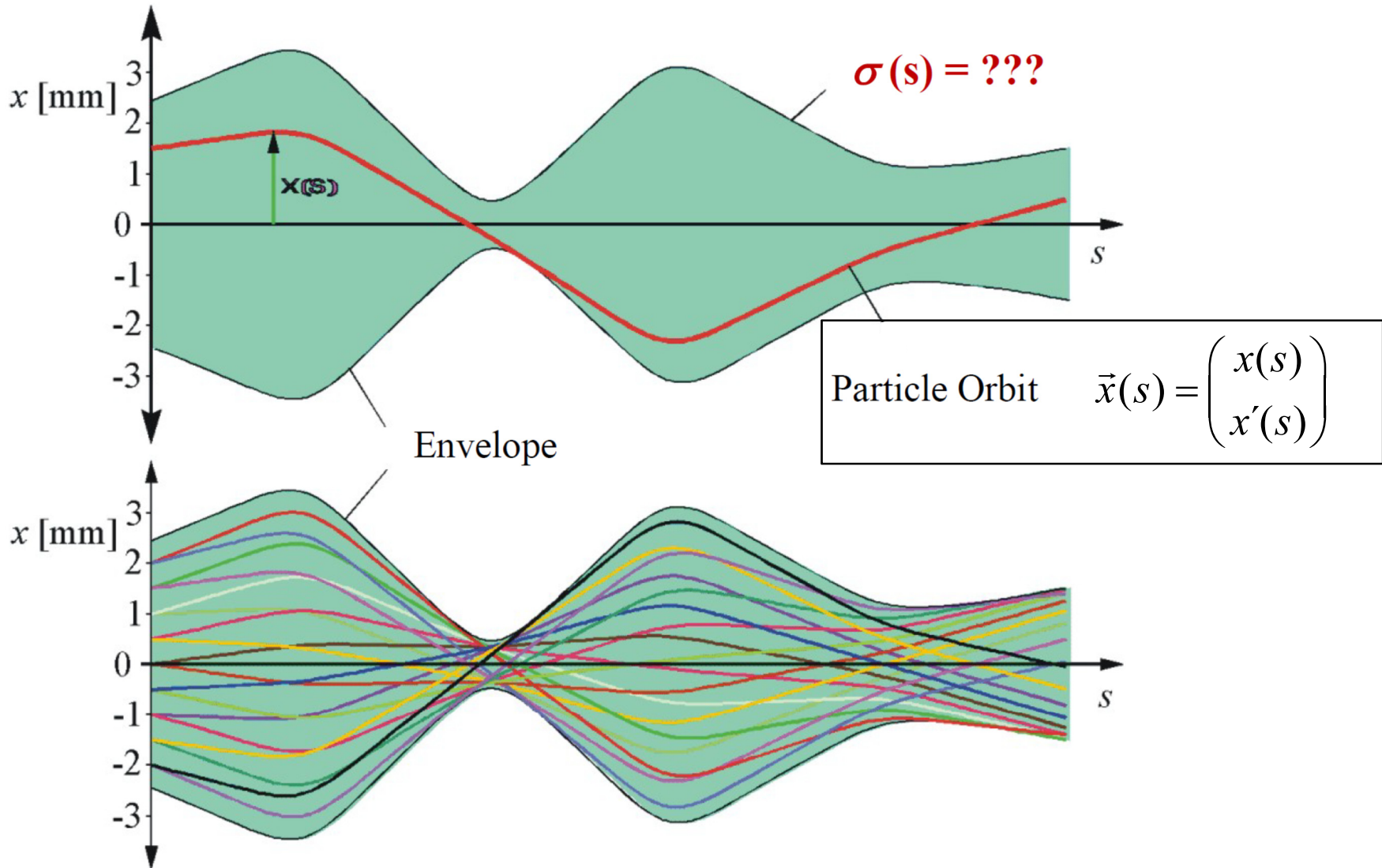


Tune Spread!

Intensity Limitation!

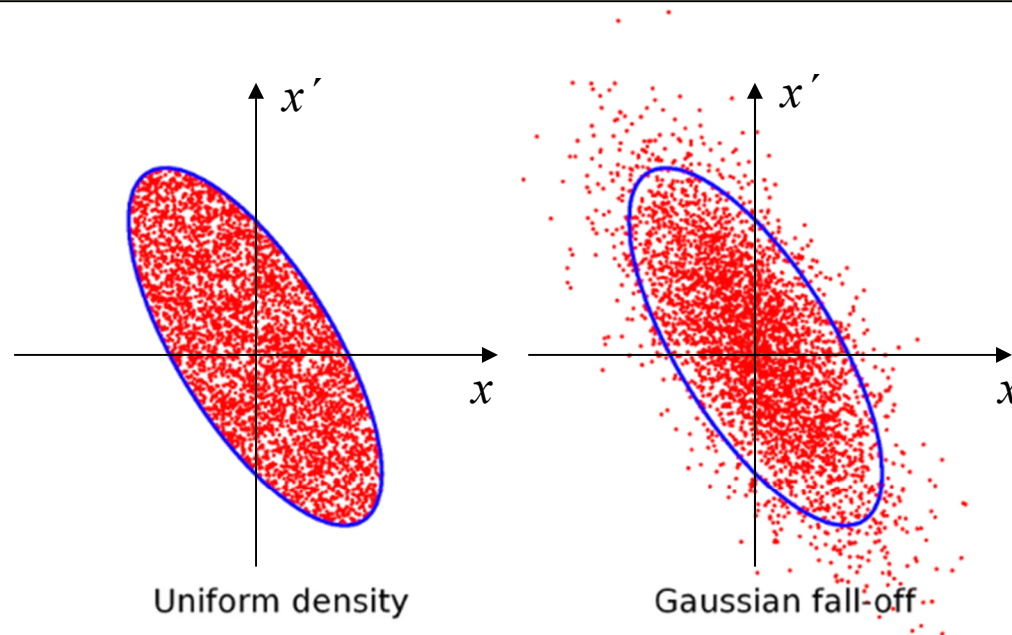
**Doesn't affect a
Linear Accelerator**

Particle Trajectories \leftrightarrow Beam



Beam Emittance

Each particle is represented by a point (x, x') in phase space!

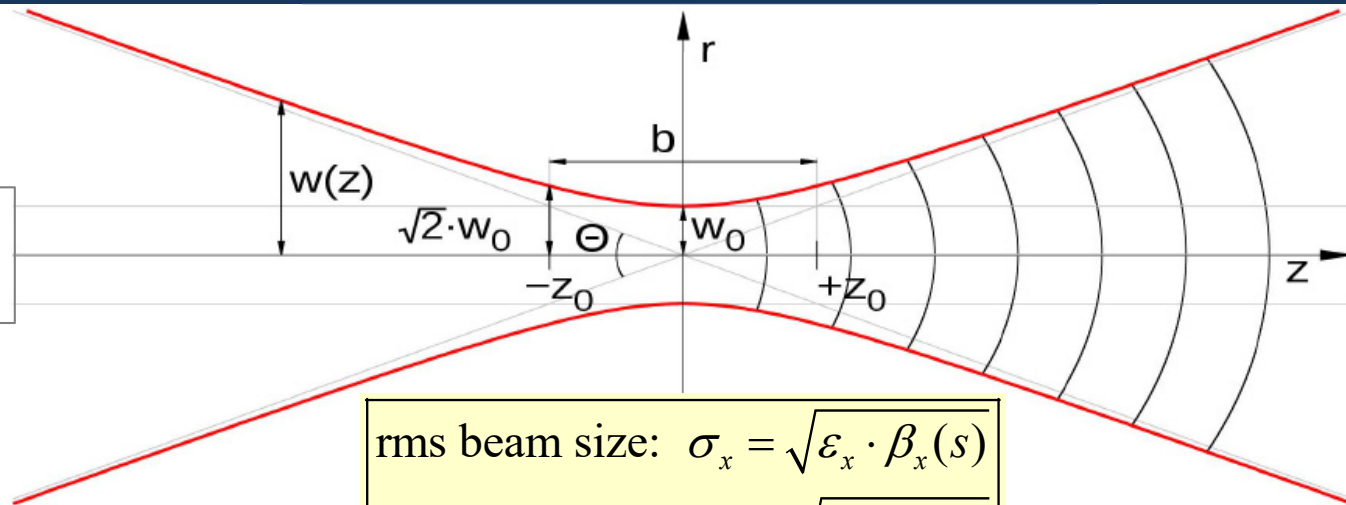


Emittance $\varepsilon_x = \text{rms area in phase space} / \pi$

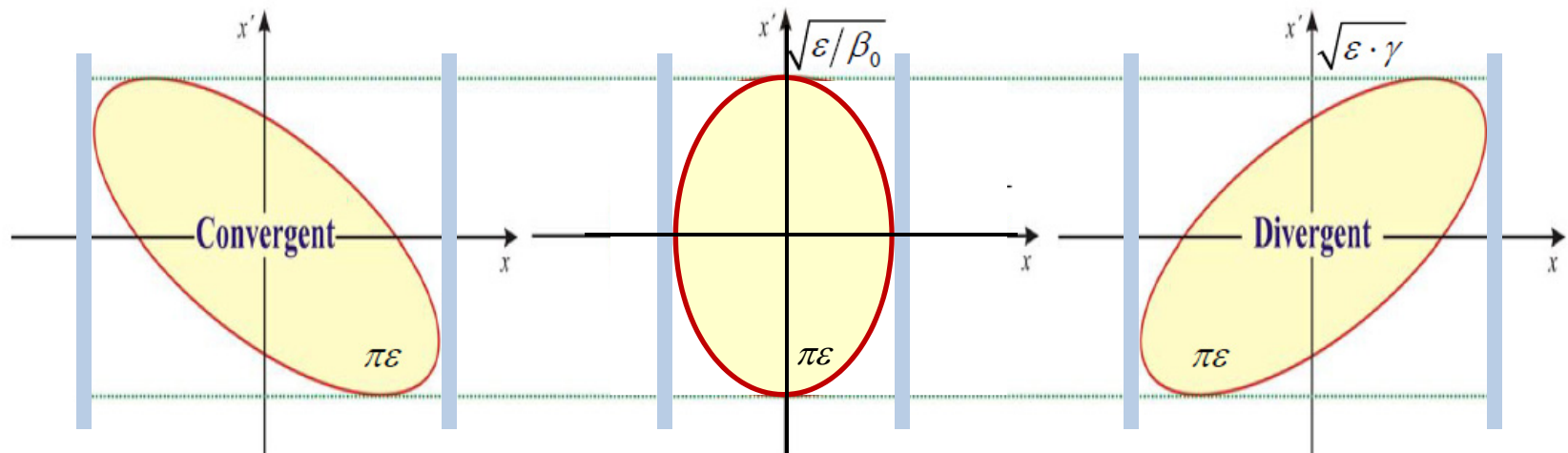
Liouville: area in phase space remains constant \rightarrow emittance $\varepsilon = \text{konst.}$

Take care: $x' = \frac{dx}{ds} = \frac{dx}{dt} \frac{dt}{ds} = \frac{v_x}{\beta c} = \frac{1}{\beta\gamma} \frac{p_x}{m_0} \rightarrow$ norm. emittance $\varepsilon_n = \beta\gamma\varepsilon = \text{konst.}$

Beam Optics

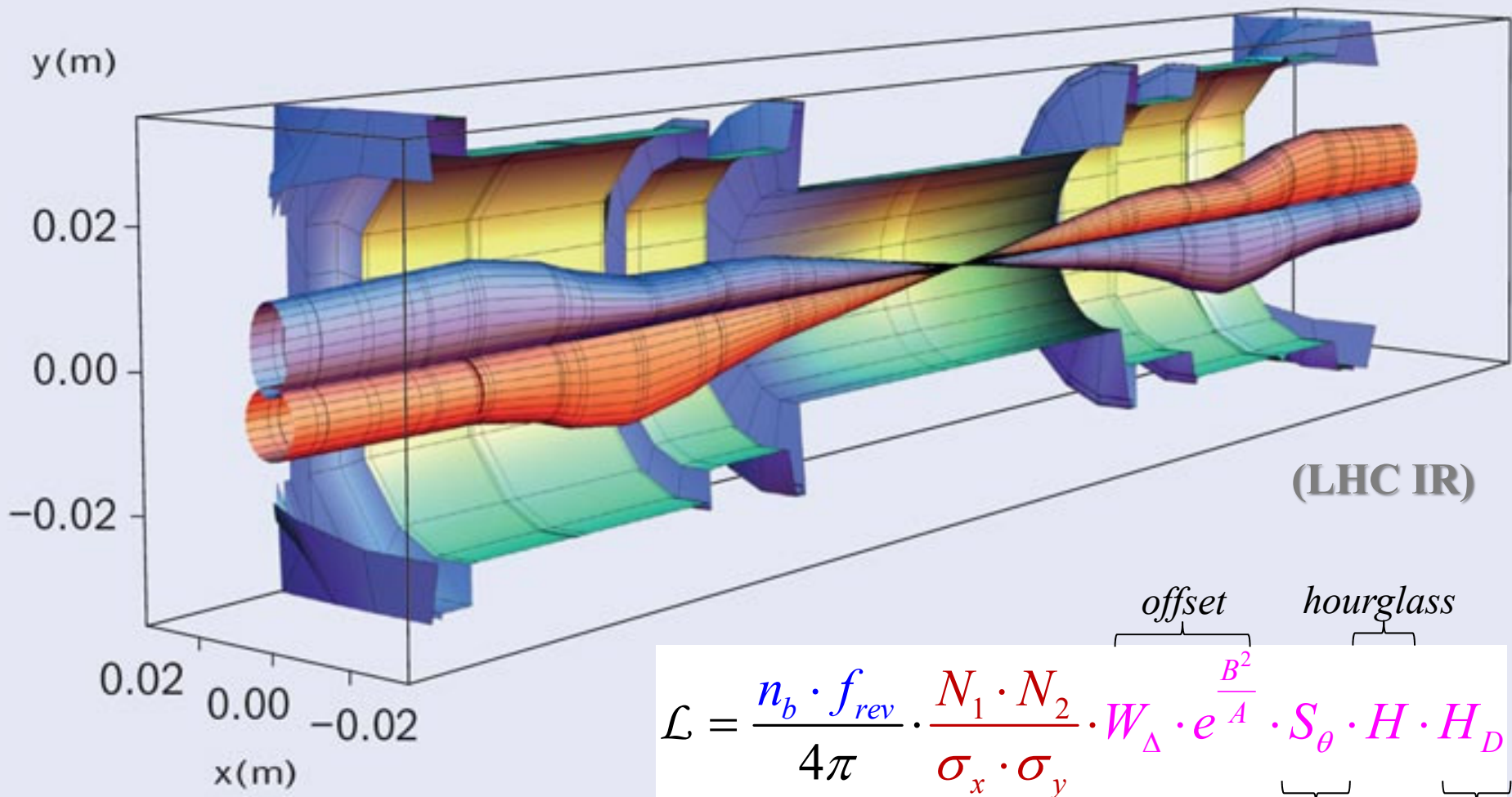


rms beam size: $\sigma_x = \sqrt{\varepsilon_x \cdot \beta_x(s)}$
 rms beam div.: $\sigma_{x'} = \sqrt{\varepsilon_x \cdot \gamma_x(s)}$

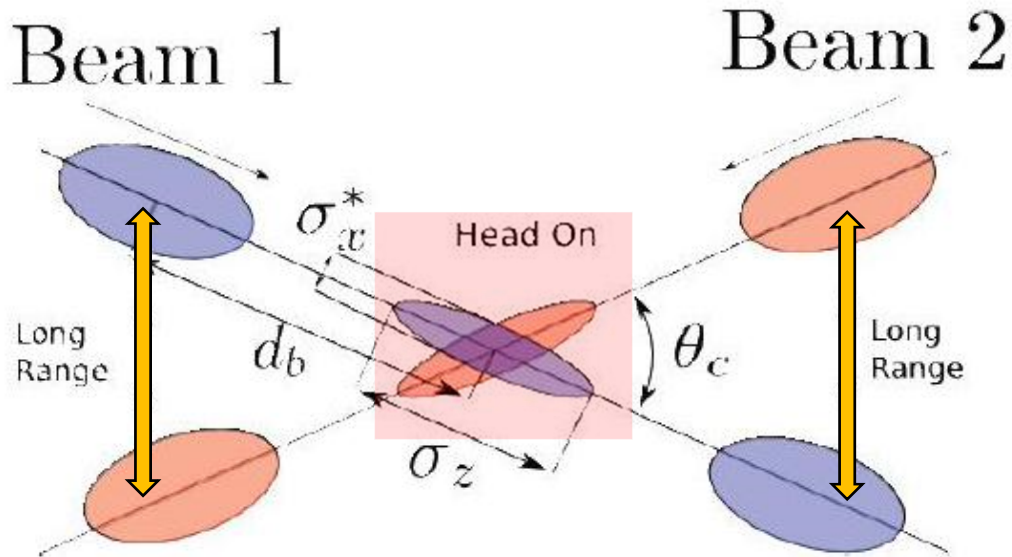


Beam size is determined by emittance ε and (lokal) beta function $\beta(s)$!

Luminosity Optimization



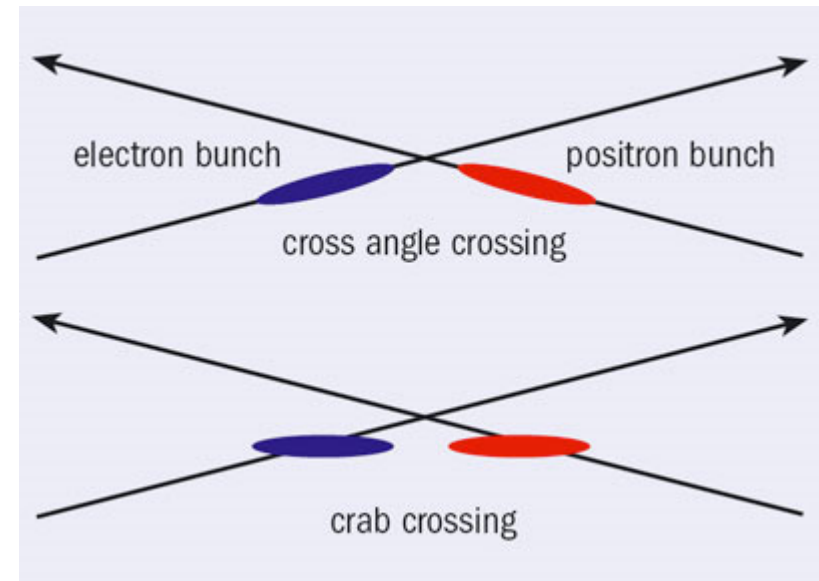
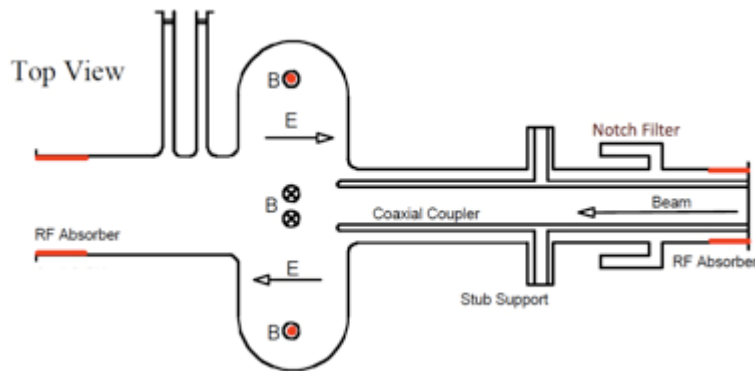
Beam Crossing



- Sufficient beam separation
- Small crossing angle
- Long bunch separation
- ...

$$\mathcal{L} = \frac{n_b \cdot f_{rev}}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_y} \cdot S_\theta$$

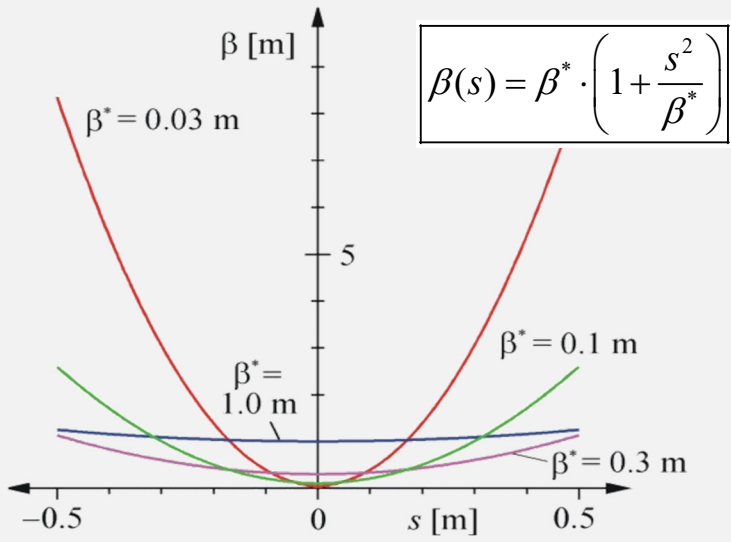
One option: **Crab-Cavities:**



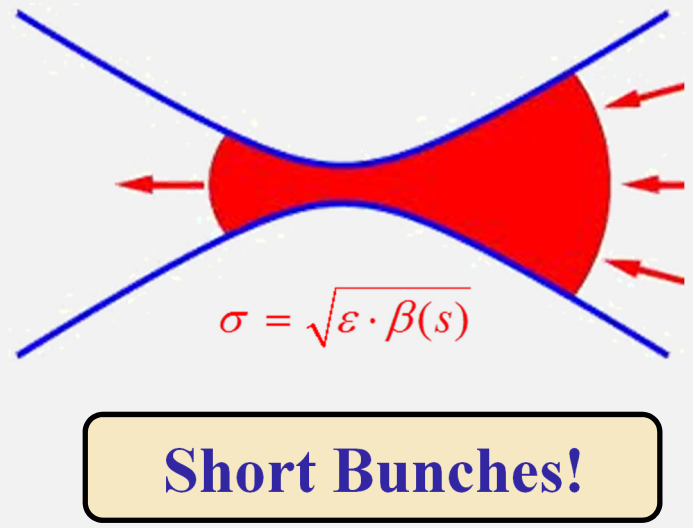
“Beta Squeeze”

$$\sigma_{x,y} = \sqrt{\varepsilon_{x,y} \cdot \beta_{x,y}}$$

Beam Broadening:

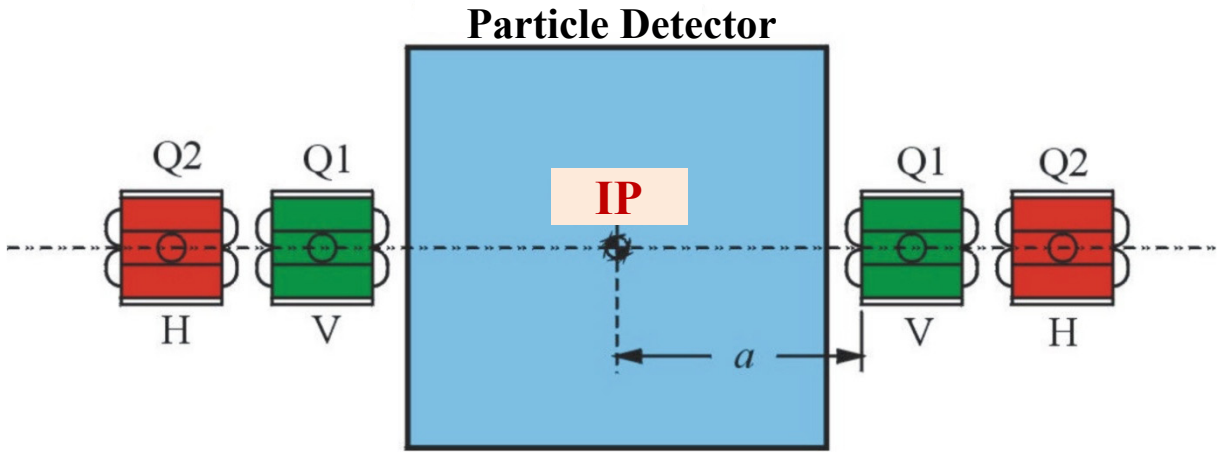


Hourglass Effect:

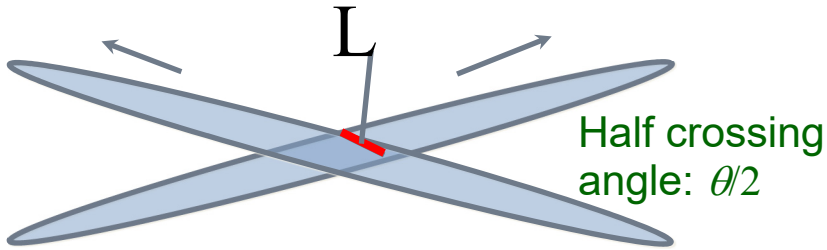


$$\sigma_s \approx \beta^*$$

$$\mathcal{L} = \frac{f_{rev} n_b}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_y} \cdot H$$

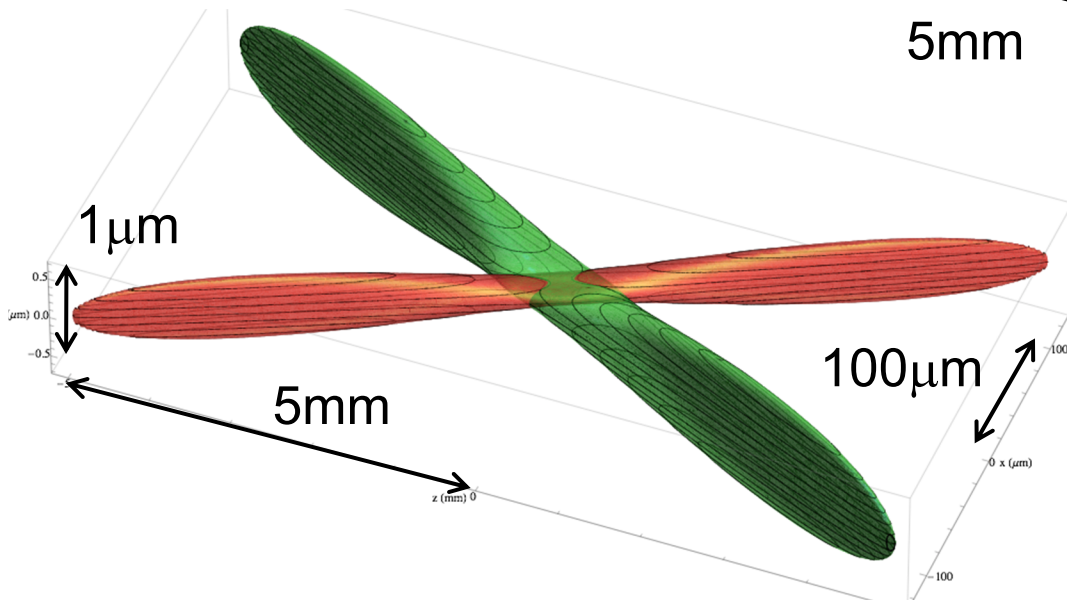


Approach: strong vertical squeeze

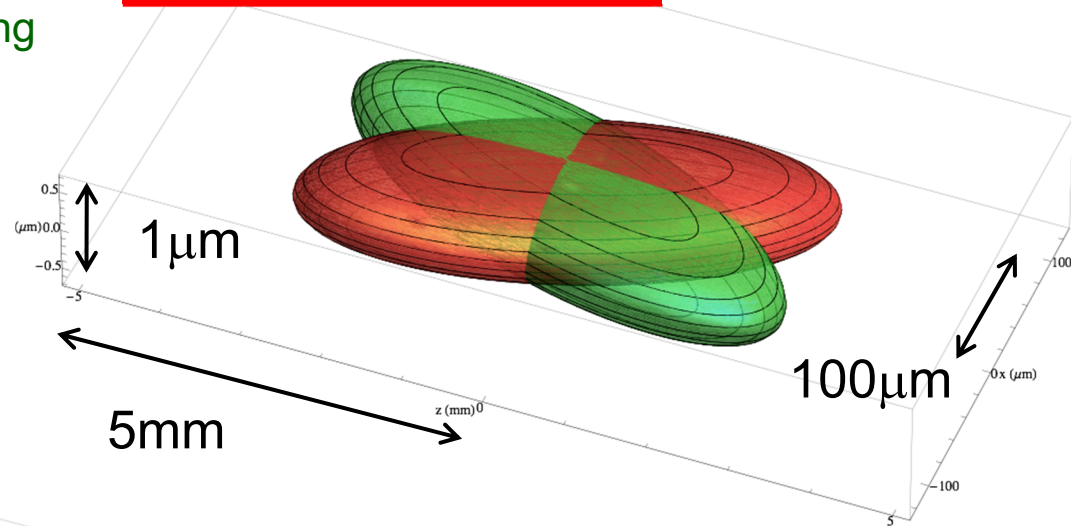


Hourglass condition: $\beta_y^* \geq L = \sigma_x / \theta$

SuperKEKB



present KEKB (w/o crab)

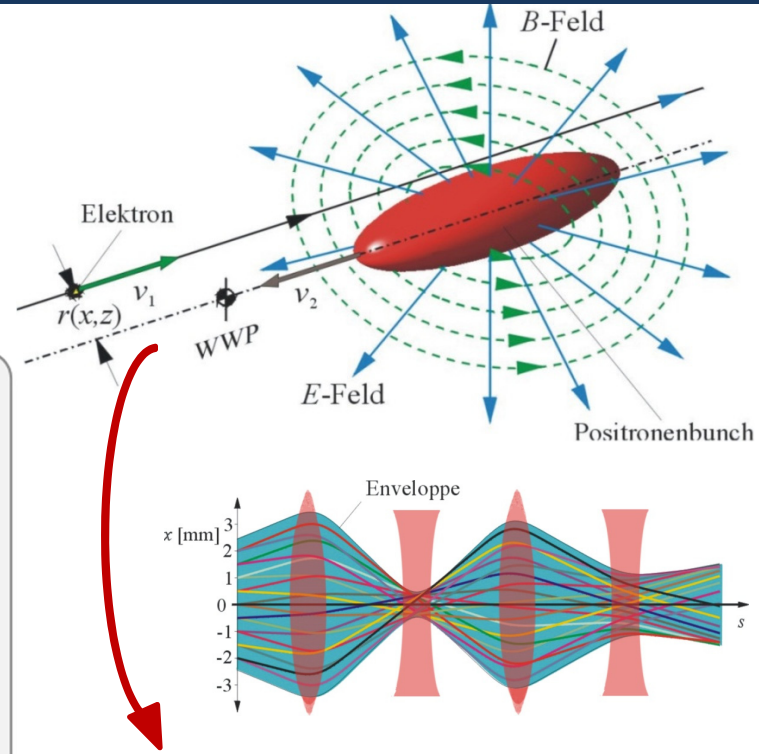


→ *Nano Beams*

Beam-Beam Effects ↔

$$\mathcal{L} = \frac{f_{rev} n_b}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_z} \dots$$

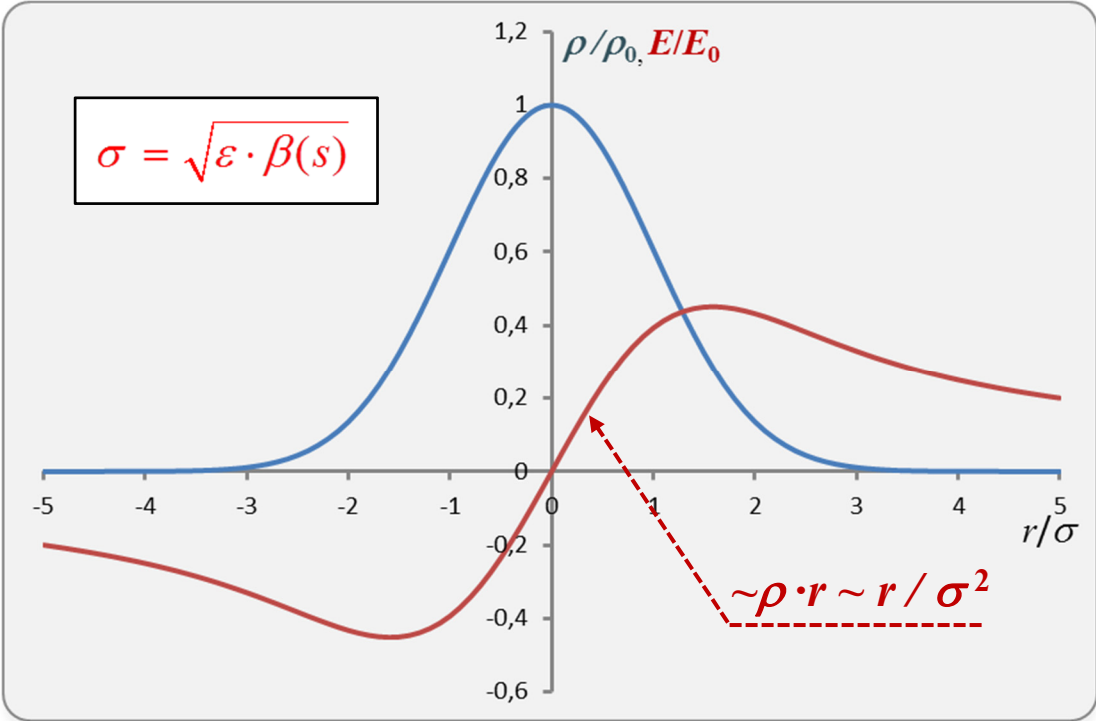
Additional Focusing or Defocusing in the Interaction Region



Beam-Beam Parameters:

$$\xi_{x,y} = \frac{r_e N}{2\pi \gamma_r} \frac{\beta_{x,y}^*}{\sigma_{x,y} (\sigma_x + \sigma_y)}$$

$$\sigma_{x,y} = \sqrt{\epsilon_{x,y} \beta_{x,y}}$$



$$\sigma = \sqrt{\epsilon \cdot \beta(s)}$$

Sets limit on emittance in head-on collisions!

Storage Rings

Important Relations:

a) Luminosity

$$\mathcal{L} = \frac{n_b \cdot f_{rev}}{4\pi} \cdot \frac{N_1 \cdot N_2}{\sigma_x \cdot \sigma_y} \cdot S_\theta \cdot H$$

b) Beam-Beam Parameters

$$\xi_{x,y} = \frac{r_e N}{2\pi\gamma_r} \frac{\beta_{x,y}^*}{\sigma_{x,y} (\sigma_x + \sigma_y)}$$

→ Rewrite Luminosity Formula ($\xi_y > \xi_x$)

Beam-beam parameter

Lorentz factor

Beam current

$$\mathcal{L} = \frac{\gamma_r}{2er_e} \cdot \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \cdot \frac{I_{beam} \cdot \xi_y}{\beta_y^*} \cdot S_\theta \cdot H$$

Hourglass effect:
 $\beta_y^* \geq \sigma_x / \theta$
(small ε_x)

Aspect ratio at IP

Vertical beta function at IP

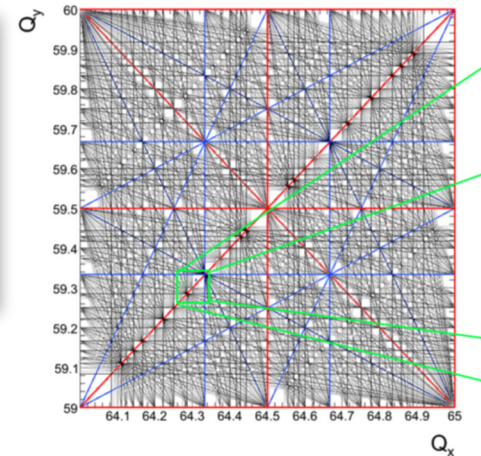
Beam-Beam Parameters

$$\xi_{x,y} = \frac{r_e N}{2\pi\gamma_r} \frac{\beta_{x,y}^*}{\sigma_{x,y}(\sigma_x + \sigma_y)}, \quad \sigma_{x,y} = \sqrt{\varepsilon_{x,y}\beta_{x,y}}$$

Circular Colliders: $\xi_{x,y} < 0.05$ typ.

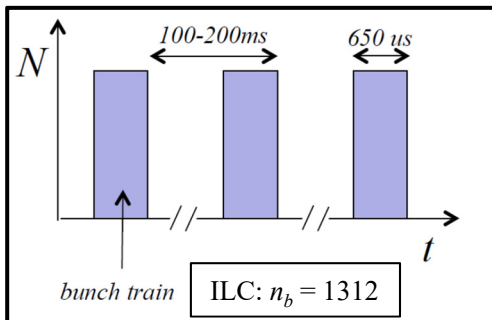
Linear Colliders: $\xi_x = 0.54, \xi_y = 1.44$ (ILC)

$$\mathcal{L} = \frac{\gamma_r}{2er_e} \cdot \left(1 + \frac{\sigma_y^*}{\sigma_x^*}\right) \cdot \frac{I_{beam} \cdot \xi_y}{\beta_y^*} \cdot S_\theta \cdot H$$



But:

Time structure of linear / circular colliders are different:



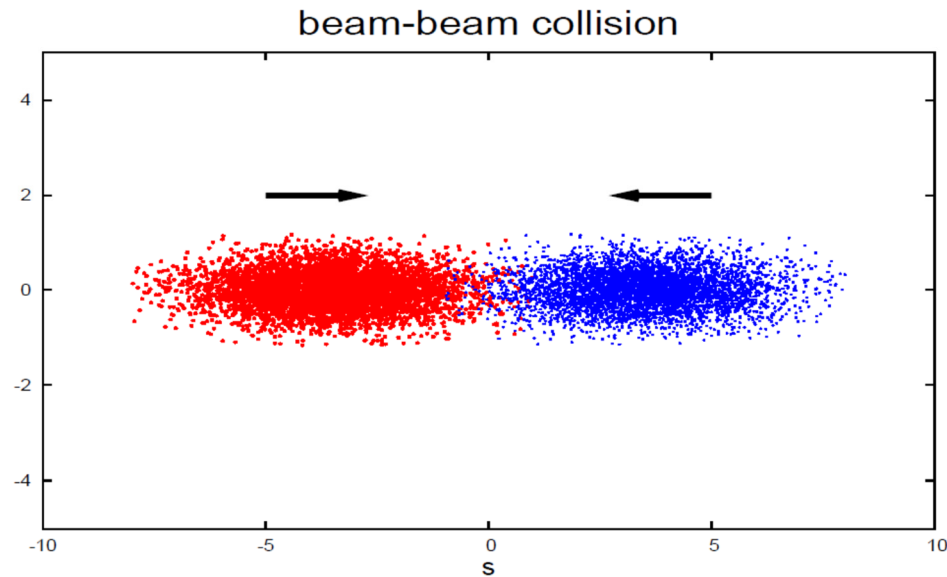
Comparison FCC-ee (@Higgs) ↔ ILC:

- SR: $I_{beam} = f_{rev} n_b q N = 3000 \cdot 393 \cdot q \cdot 1.5 \cdot 10^{11} = 29 \text{ mA}$
- LC: $I_{beam} = f_{rep} n_b q N = 5 \cdot 1312 \cdot q \cdot 1 \cdot 10^{10} = 11 \mu\text{A}$

Linear Colliders

$$\xi_y > 1:$$

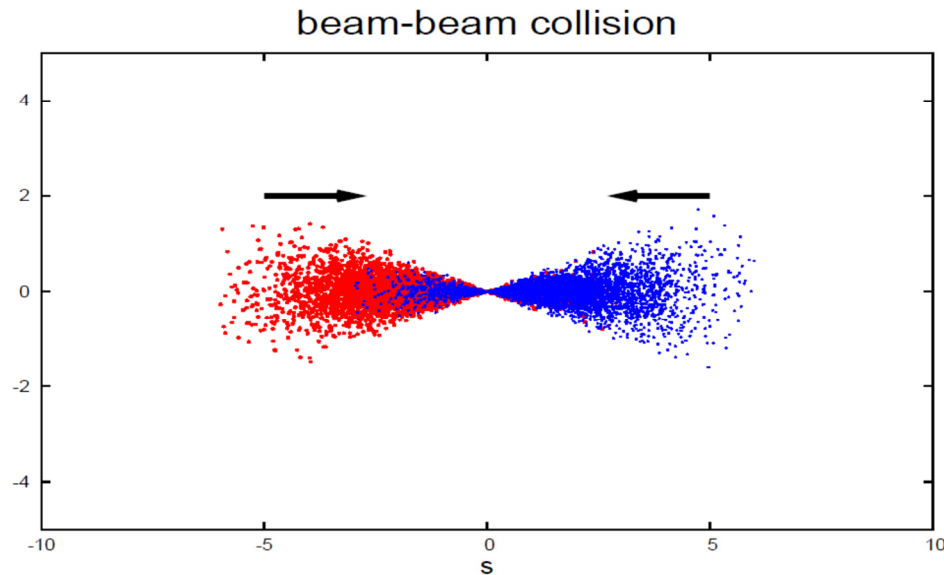
Pinch effect - disruption



Linear Colliders

$$\xi_y > 1:$$

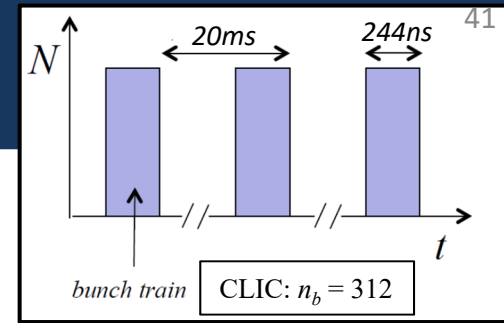
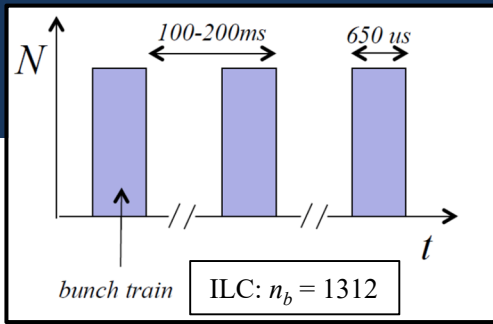
Pinch effect - disruption



➤ Additional focusing by opposing beams

Enhancement
Factor H_D

Linear Collider



Important Relations:

a) Luminosity

$$\mathcal{L} = \frac{n_b \cdot f_{rep}}{4\pi} \cdot \frac{N \cdot N}{\sigma_x \cdot \sigma_y} \cdot H_D$$

b) RF to beam power efficiency

$$P_{beams} = f_{rep} n_b N \cdot E_{cm} = \eta_{RF} \cdot P_{RF}$$

→ Rewrite Luminosity Formula

$$\mathcal{L} = \frac{1}{4\pi E_{cm}} \cdot (\eta_{RF} P_{RF}) \cdot \left(\frac{N}{\sigma_x \sigma_y} \cdot H_D \right)$$

Beam-beam effects:

- beamstrahlung
- disruption

Choice of linac technology:

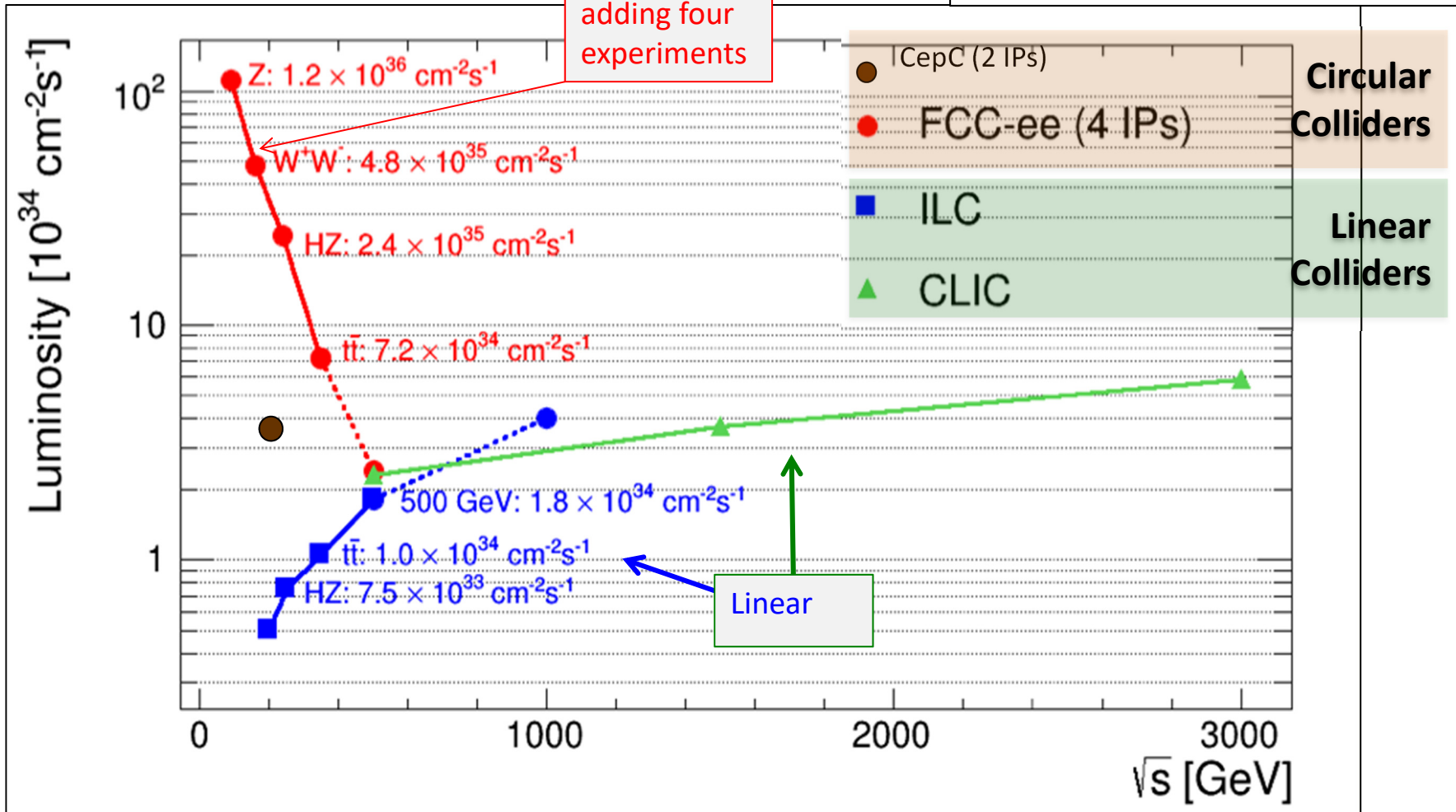
- efficiency
- available power

Strong final focus:

- Optical aberrations
- Stability issues and tolerances

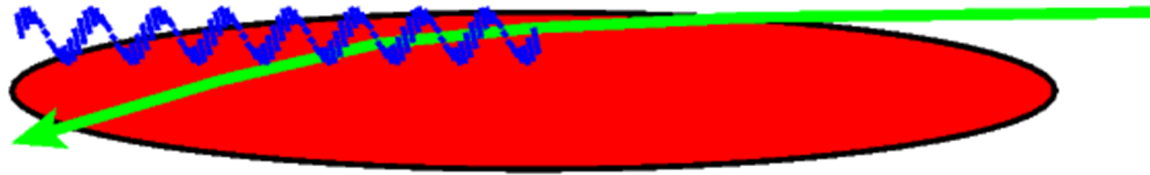
Circular vs. Linear Collider

Modified from original version:
<http://arxiv.org/pdf/1308.6176v3.pdf>



Beamstrahlung

Particles are deflected in magnetic field of colliding bunch:



Peak field:
$$B_{\max} = \frac{2E_{\perp, \max}}{c} = \frac{eN}{2\pi\epsilon_0 c \sigma_x \sigma_s} = \text{up to 1000 Tesla!}$$

Classical treatment of synchrotron radiation:
$$\Delta E \sim \frac{\gamma^4}{R^2} \sim \gamma^2 B^2$$

- **particles with high energy loss will be lost**
 - **short beam life time**
 - **impact on luminosity and actual collision energy**
- } Storage rings

Beamstrahlung $\rightarrow \mathcal{L}$

RMS energy loss for weak beamstrahlung:

$$\delta_{BS} \approx 0.86 \frac{er_e^3}{2m_0c^2} \cdot \frac{E_{cm}}{\sigma_s} \cdot \frac{N^2}{(\sigma_x + \sigma_y)^2} \propto \frac{E_{cm}}{\sigma_s} \cdot \frac{N^2}{\sigma_x^2}$$

➤ use flat beams ($\sigma_x \gg \sigma_y$) but keep $\sigma_x + \sigma_y$ large to reduce δ_{BS}

a) **Luminosity**

$$\mathcal{L} = \frac{1}{4\pi E_{cm}} \cdot (\eta_{RF} P_{RF}) \cdot \left(\frac{N}{\sigma_x \sigma_y} \cdot H_D \right)$$

b) **Vertical rms beam size**

$$\sigma_y = \sqrt{\frac{\varepsilon_{n,y} \beta_y}{\gamma_r}}$$

→ **Again Rewrite Luminosity Formula ($\delta_{BS} \approx \text{few } \%$)**

$$\mathcal{L} \propto \frac{\eta_{RF} P_{RF}}{4\pi E_{cm}} \cdot \sqrt{\frac{\delta_{BS}}{\varepsilon_{n,y}}} \cdot \underbrace{\sqrt{\frac{\sigma_s}{\beta_y}} \cdot H}_{\text{hourglass: } \beta_y \approx \sigma_s} \cdot H_D \propto \frac{\eta_{RF} P_{RF}}{4\pi E_{cm}} \cdot \sqrt{\frac{\delta_{BS}}{\varepsilon_{n,y}}} \cdot H_D$$

damping
rings!

Luminosity: Beamstrahlung Limit

$$\mathcal{L} \propto \frac{\rho P_{SR}}{E^{13/3}} \left(\frac{\xi_y \eta^2}{\varepsilon_{g,y}} \right)^{1/3}$$

Circular ↔ Linear

$$\mathcal{L} \propto \frac{\eta_{RF} P_{RF}}{4\pi E_{cm}} \sqrt{\frac{\delta_{BS}}{\varepsilon_{n,y}}} H_D$$

P_{SR} : syn.rad.power

ρ : bending radius

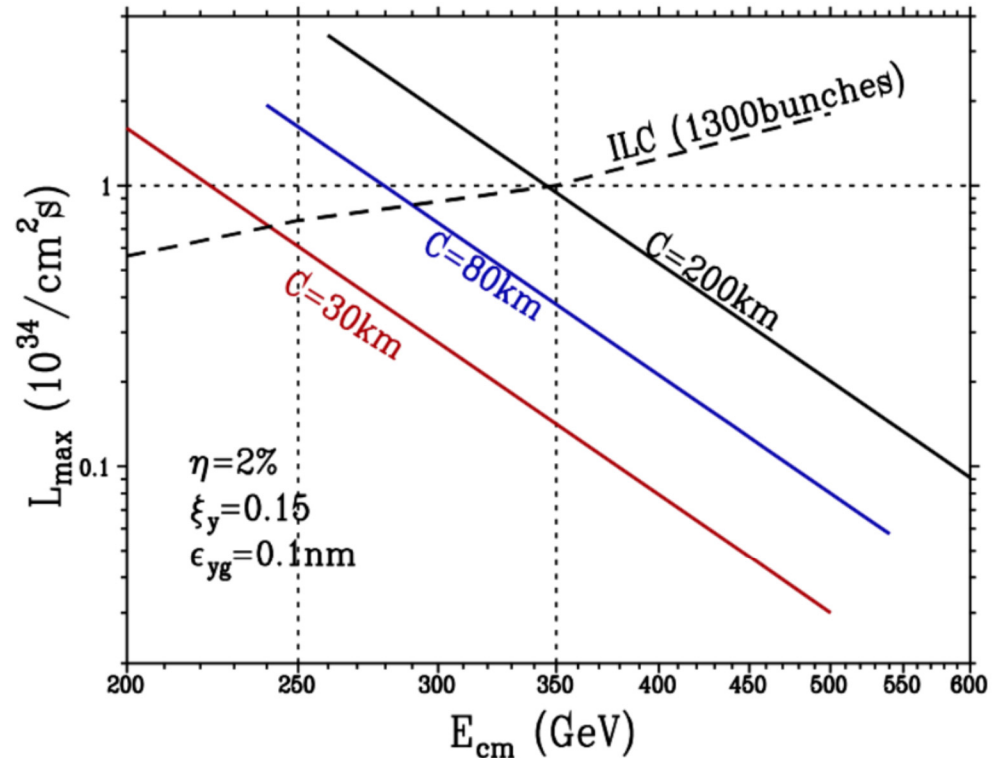
ξ_y : tune-shift

$\varepsilon_{g,y}$: geometric emit.

?????

example with

- $\eta=2\%$
- $\xi_y=0.15$
- $\varepsilon_{gy}=0.1\text{nm}$



Beam Emittance

a) Adiabatic Damping

$$\varepsilon = \frac{1}{\beta\gamma} \varepsilon_n \quad \begin{matrix} E_{kin}=250\text{GeV} \\ = 2 \cdot 10^{-6} \varepsilon_n \end{matrix}$$

in particular not sufficient for positrons!

b) Radiative Damping

equilibrium emittance in storage rings

only dependent on the magnetic lattice

→ low emittance lattice (suppress dispersion)

Damping rings required for Linear Collider!

$e^+ - e^-$ in Storage Rings

Equilibrium Emittance \leftrightarrow “Radiation” Damping

2 Effects!

Cooling:

- photon emission \rightarrow recoil (long. and transverse)
- acceleration restores long. momentum
- \rightarrow **Net reduction of transv. momentum: damping!**

Heating:

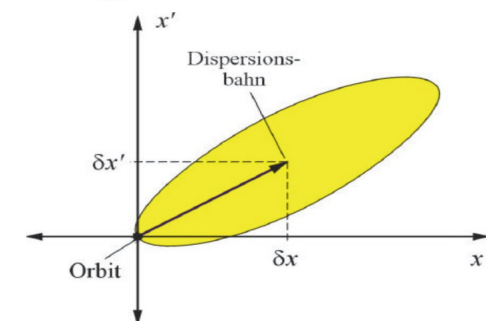
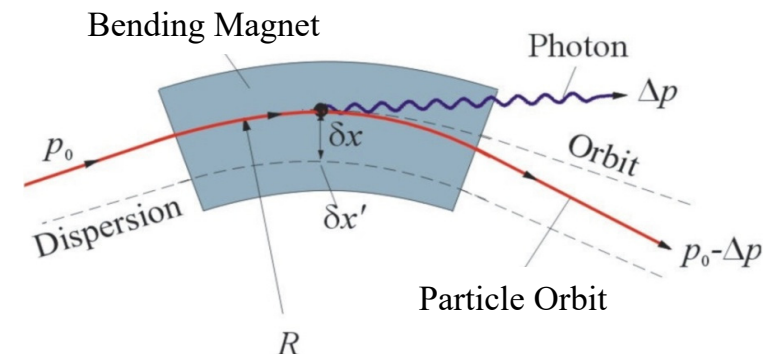
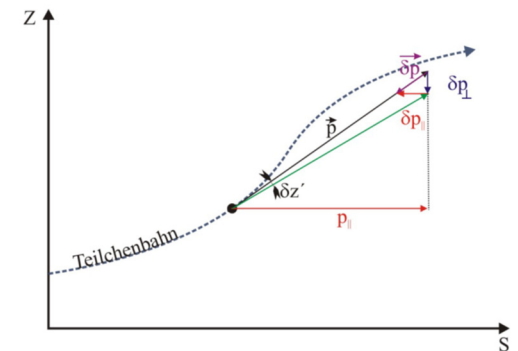
- photon emission in dispersive sections
- shift of ideal dispersion orbit by δx , $\delta x'$
- \rightarrow **Excitation of betatron oscillations: heating!**

Equilibrium Emittance:

- **Cooling = Heating**

$$\varepsilon_x = \frac{55}{32\sqrt{3}} \cdot \frac{\hbar c \gamma^2}{J_X m_0 c^2} \cdot \frac{\left\langle \frac{1}{R^3} \cdot \mathcal{H}(s) \right\rangle}{\left\langle \frac{1}{R^2} \right\rangle}$$

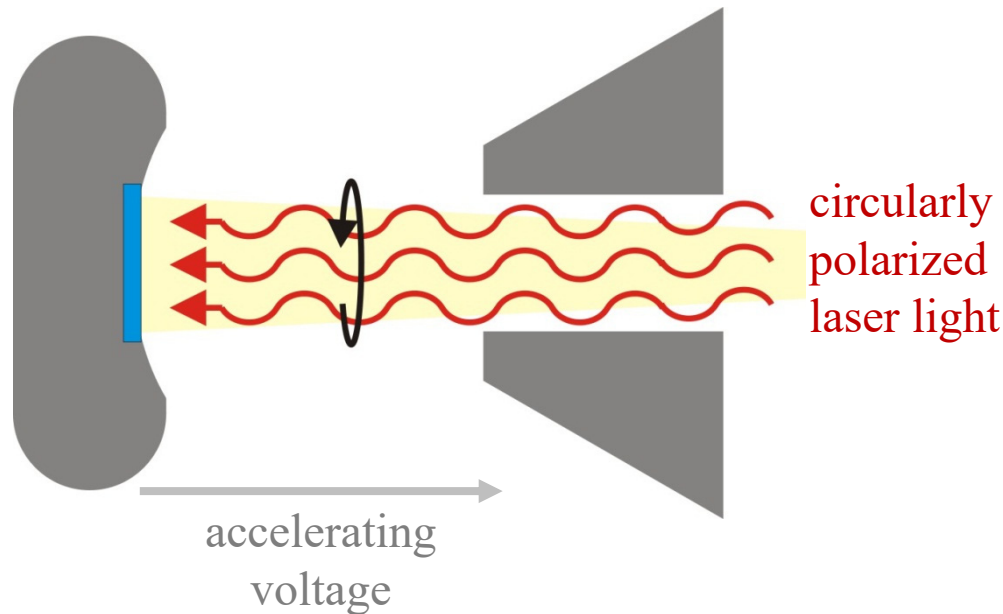
Dispersion!



Polarized Electrons

Functional Principle:

semiconductor
photocathode
based on GaAs



Pierce & Meier, 1976

Achieved at:

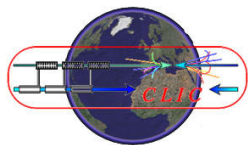
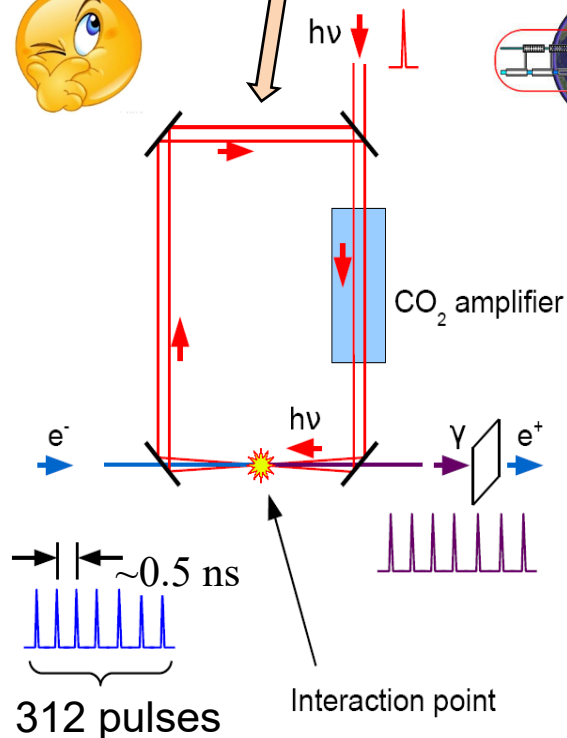
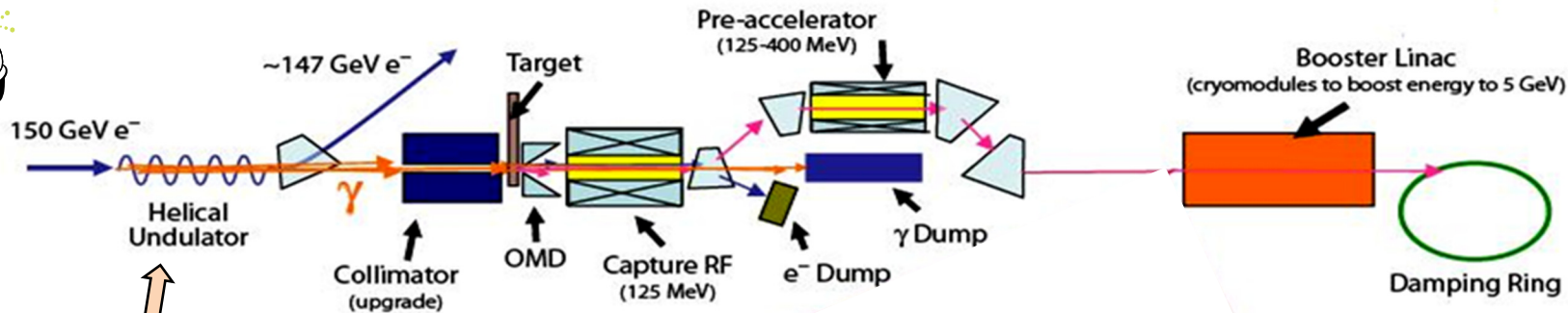
- SLAC
- MIT Bates
- AmPs
- **CEBAF**
- **Bonn**
- **Mainz**
- **Darmstadt**

Photoelectron emission from GaAs

polarization transfer from laser photons to emitted electrons

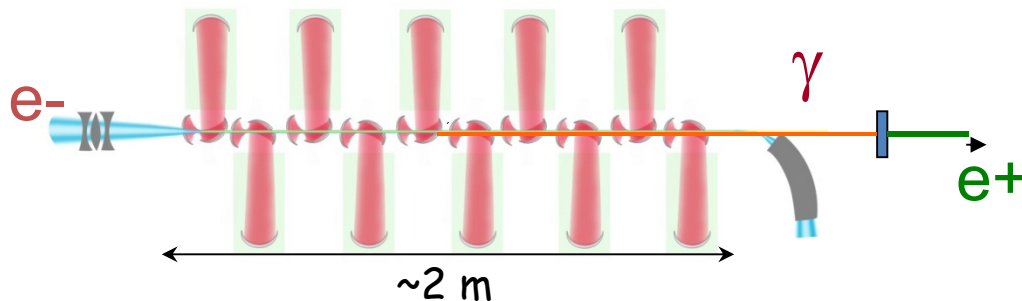


ILC Positron Source Layout



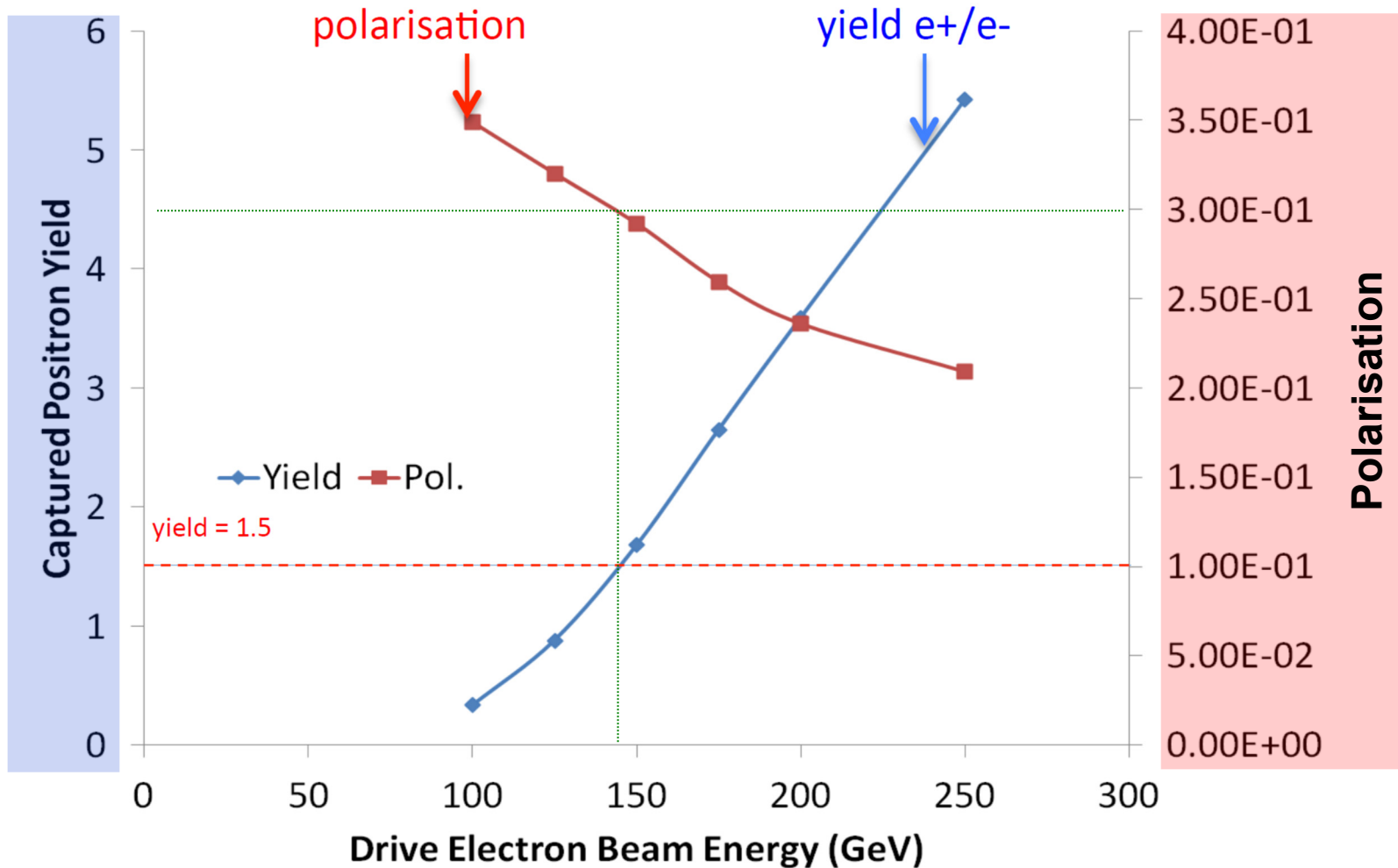
CLIC Compton Linac

- Compton backscattering inside a CO₂ laser amplifier cavity
- Production of 1 photon per electron (demonstrated at BNL)



- 10 consecutive Compton IPs to accumulate γ flux

Polarized Positrons @ ILC



Self Polarization in Storage Rings

Transition Rates :

- no spin flip: $w_{\uparrow\uparrow}, w_{\downarrow\downarrow}$
- with spin flip: $w_{\uparrow\downarrow}, w_{\downarrow\uparrow}$

Probability of a spin-flip transition:

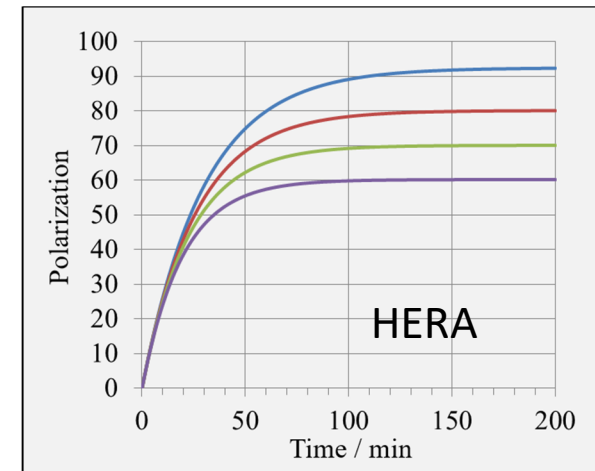
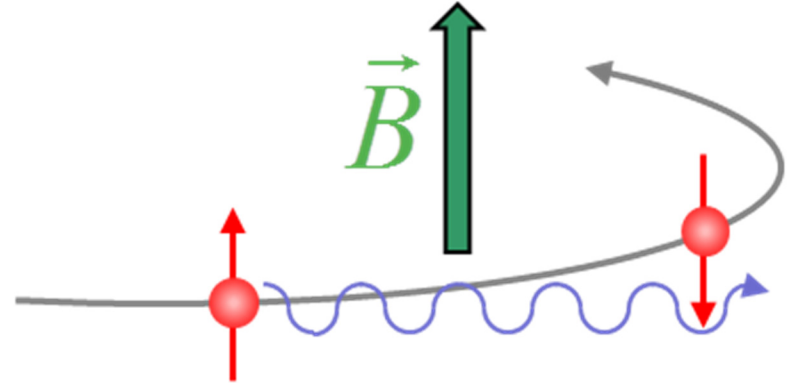
$$\frac{w_{\uparrow\downarrow} + w_{\downarrow\uparrow}}{(w_{\uparrow\uparrow} + w_{\downarrow\downarrow}) + (w_{\uparrow\downarrow} + w_{\downarrow\uparrow})} = \frac{1}{3} \cdot \left(\frac{\hbar\omega_c}{E} \right)^2 < 10^{-10} = \text{very small, but:}$$

The beam will get polarized in a while due to $w_{\uparrow\downarrow} > w_{\downarrow\uparrow}$!

Sokolov-Ternov-Effect: $P(t) = P_{ST} \left(1 - e^{-t/\tau_P} \right)$

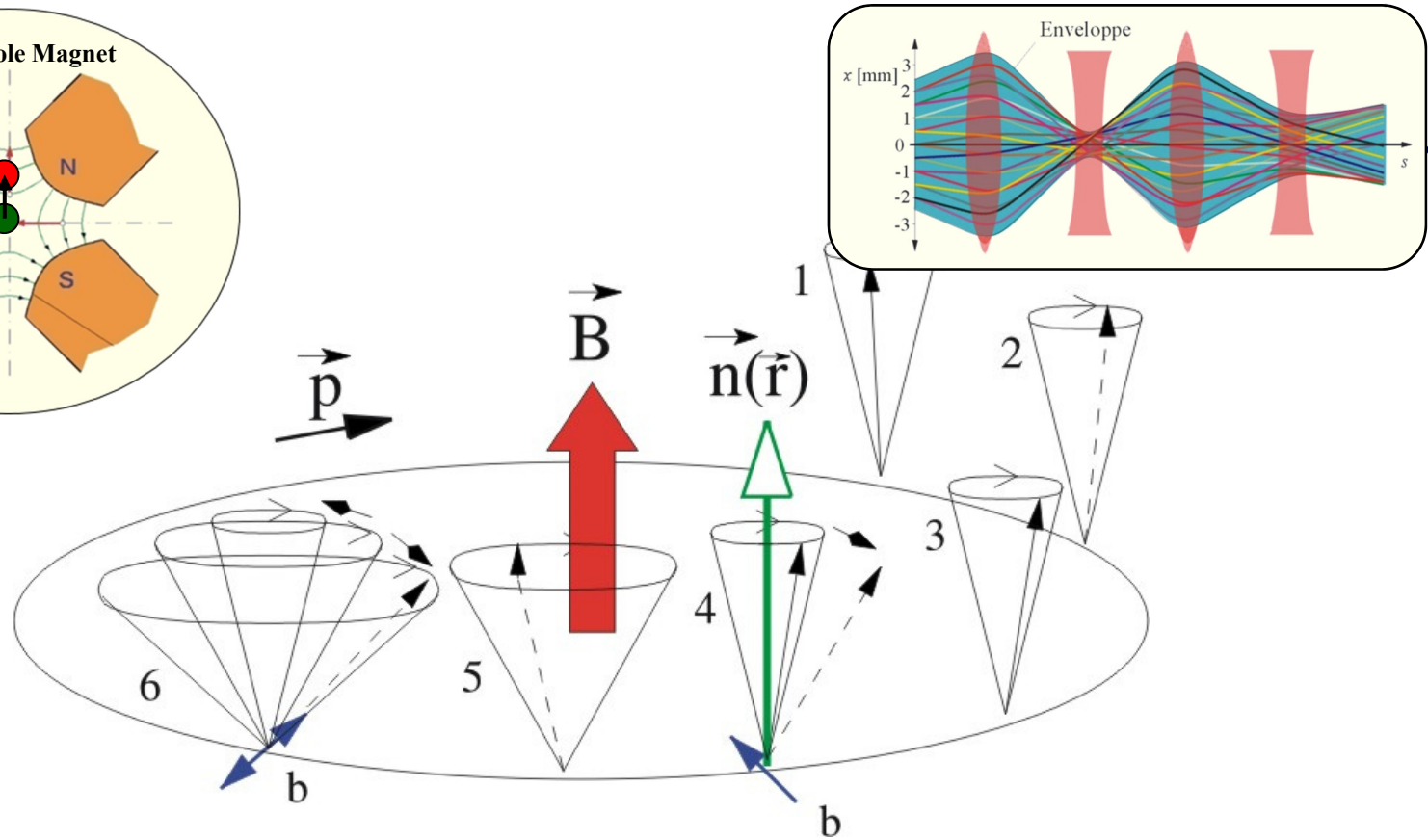
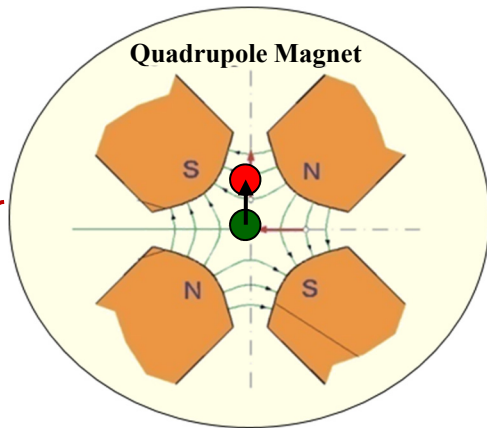
Rise time: $\tau_P = \left(\frac{8}{5\sqrt{3}} \frac{c\lambda_c r_e}{2\pi} \left(\frac{\gamma^5}{R^3} \right)^{-1} \right)^{-1}$ 92.4%

Depolarizing effects: $P_\infty = P_{ST} \frac{\tau_{depol}}{\tau_P + \tau_{depol}}$ and $\frac{1}{\tau} = \frac{1}{\tau_P} + \frac{1}{\tau_{depol}}$



**But not @
> 100GeV!**

Depolarizing Resonances



Imperfection Resonance: $\gamma \cdot a = n, \quad n \in \mathbb{Z}$

Intrinsic Resonance: $\gamma \cdot a = n \cdot P \pm Q_z, \quad n \in \mathbb{Z}$

Circular ↔ Linear Collider

Can both achieve $\mathcal{L} > 10^{34} \text{ cm}^{-2}$

Circular Collider

Linear Collider

Beam Emittance:

Radiative Equilibrium!
→ low emittance lattice
("well-known" from SR sources)

Adiabatic Damping!
not sufficient to reduce initial values
→ **additional damping rings required**

Beam Polarization:

Self polarization ("moderate" E_{beam})
reduced by depol. resonances
not enough for HEP requirements
but
can help to precisely determine E_{beam}

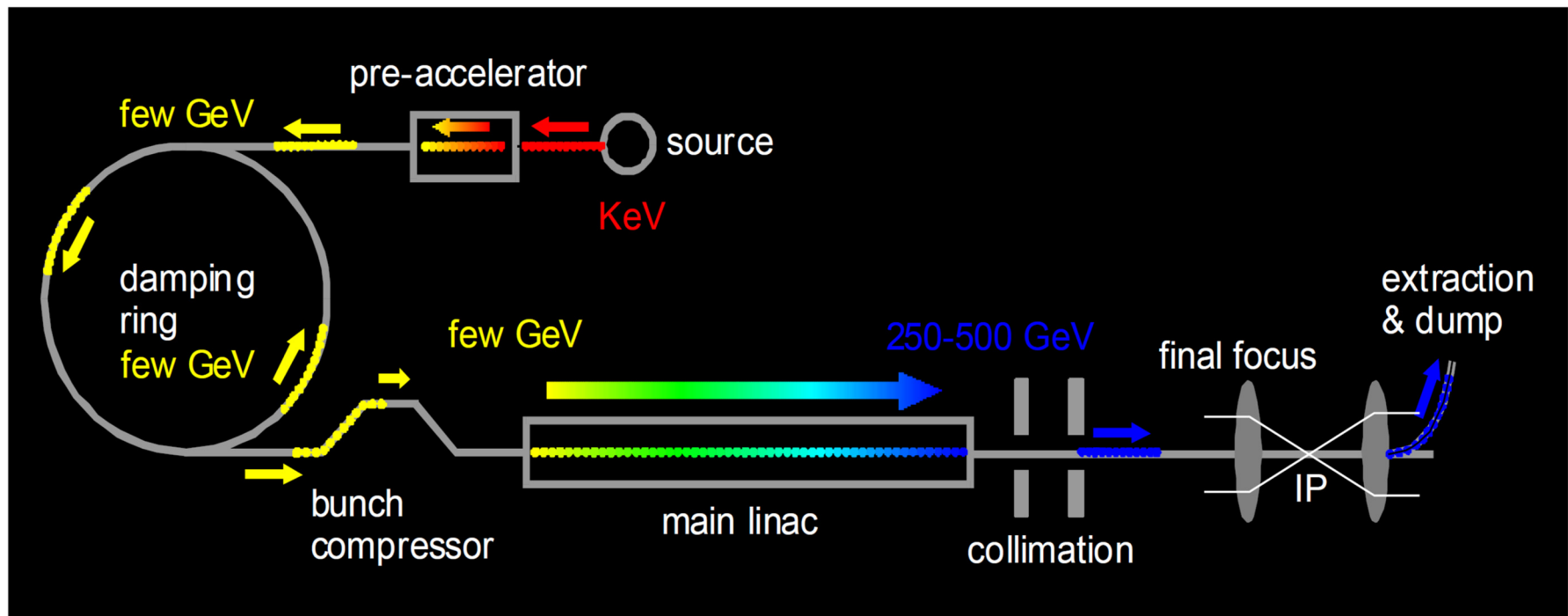
Acceleration of polarized beams
electrons: photoemission from GaAs
positrons: from pol. MeV-photons
aiming at:
 $P(e^-) = 80\%$, $P(e^+) = 30\%$

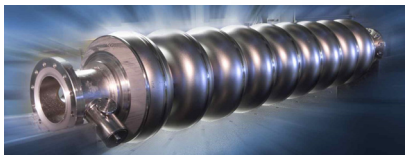
works up to $\sim 350 \text{ GeV}$

works up to $\sim 1 \text{ (3) TeV}$

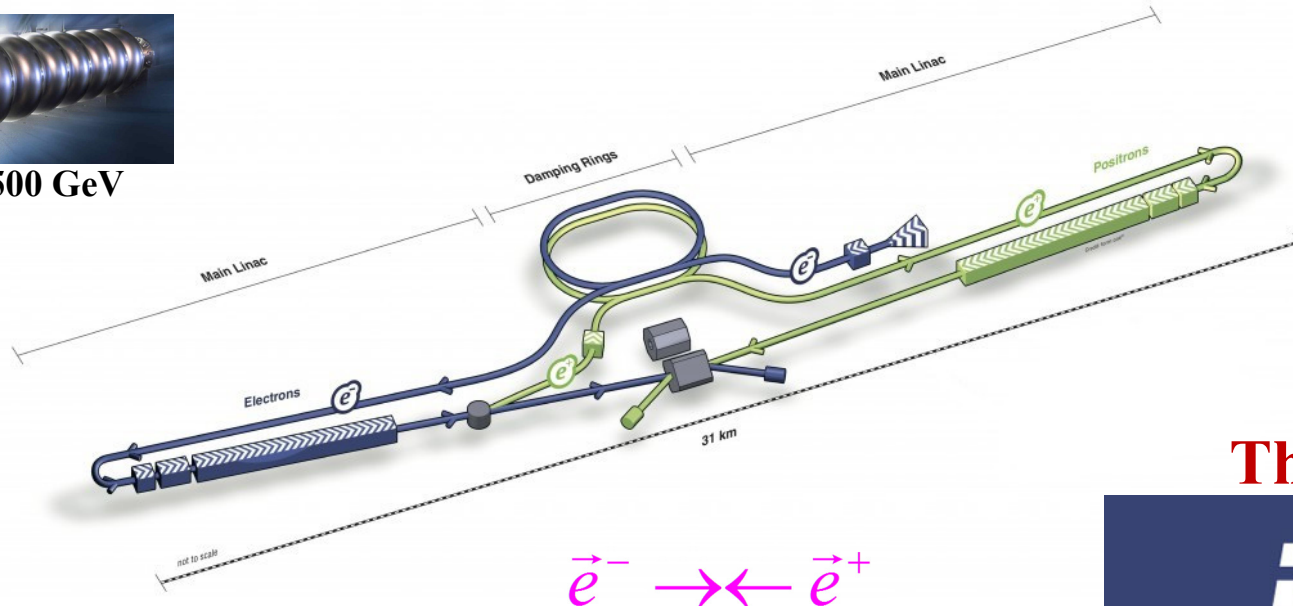
Linear Colliders

The 'Generic' Linear Collider (1/2)





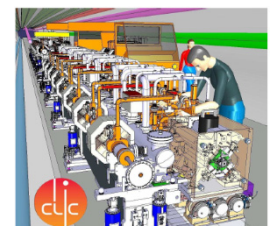
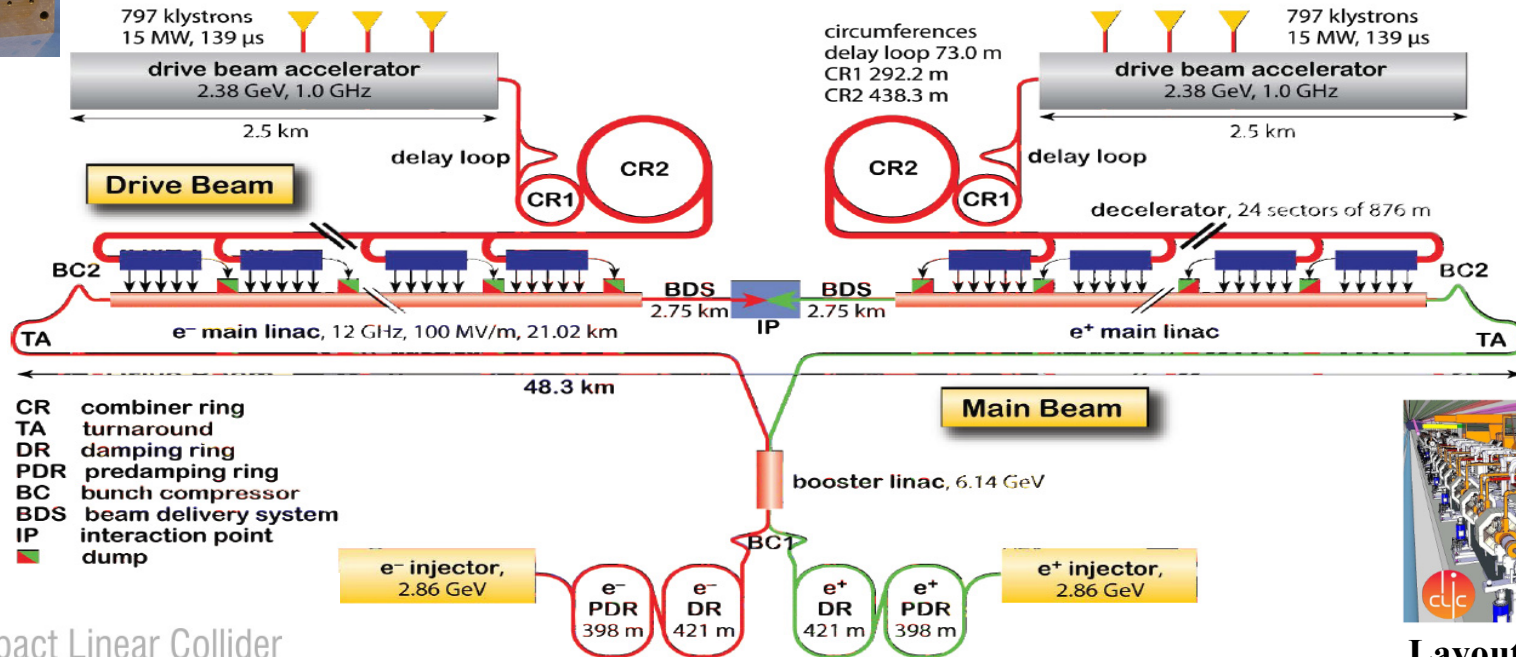
Layout at 500 GeV



The "Rivals":

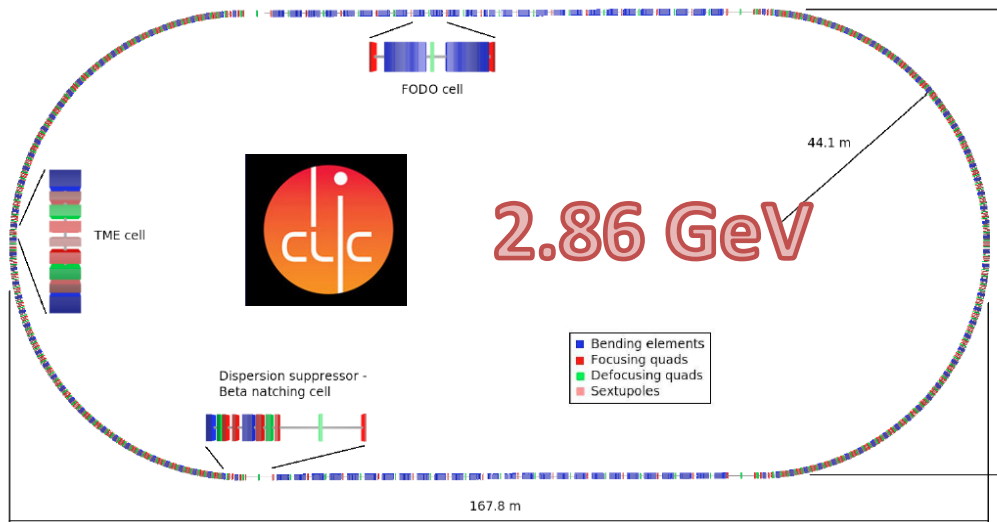
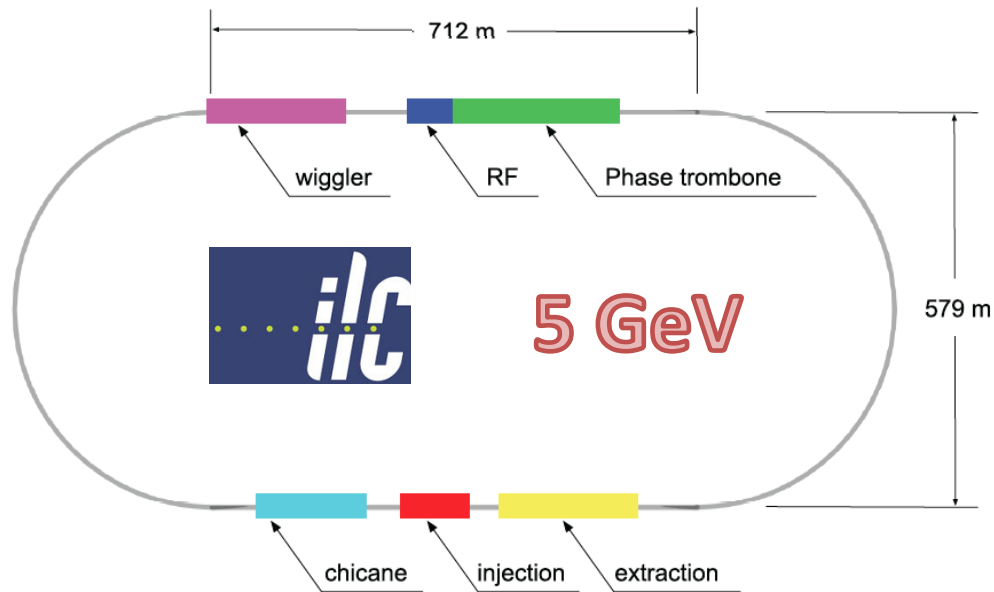


was "almost" dead – but not completely ...



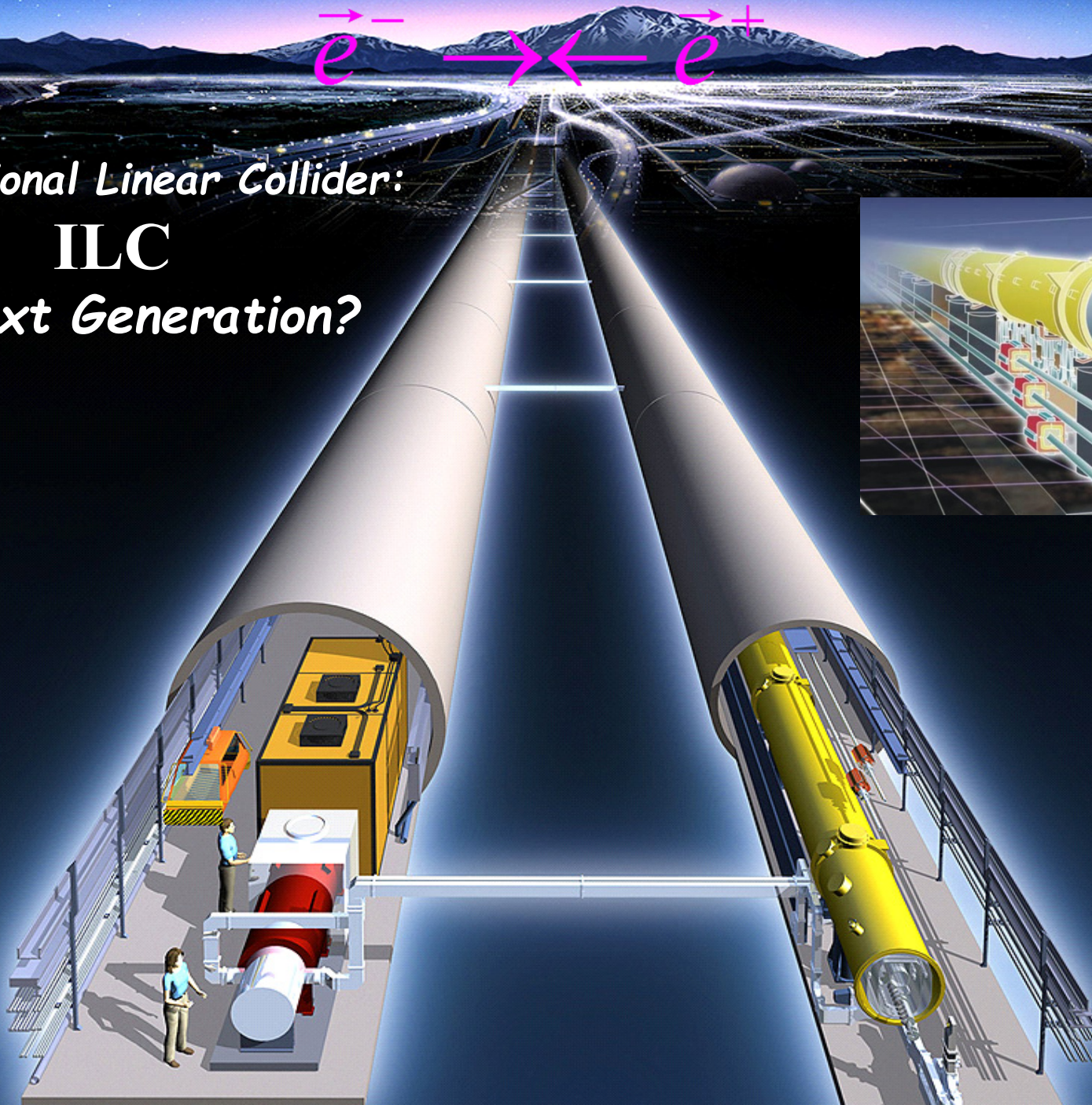
Layout at 3 TeV

Damping Rings

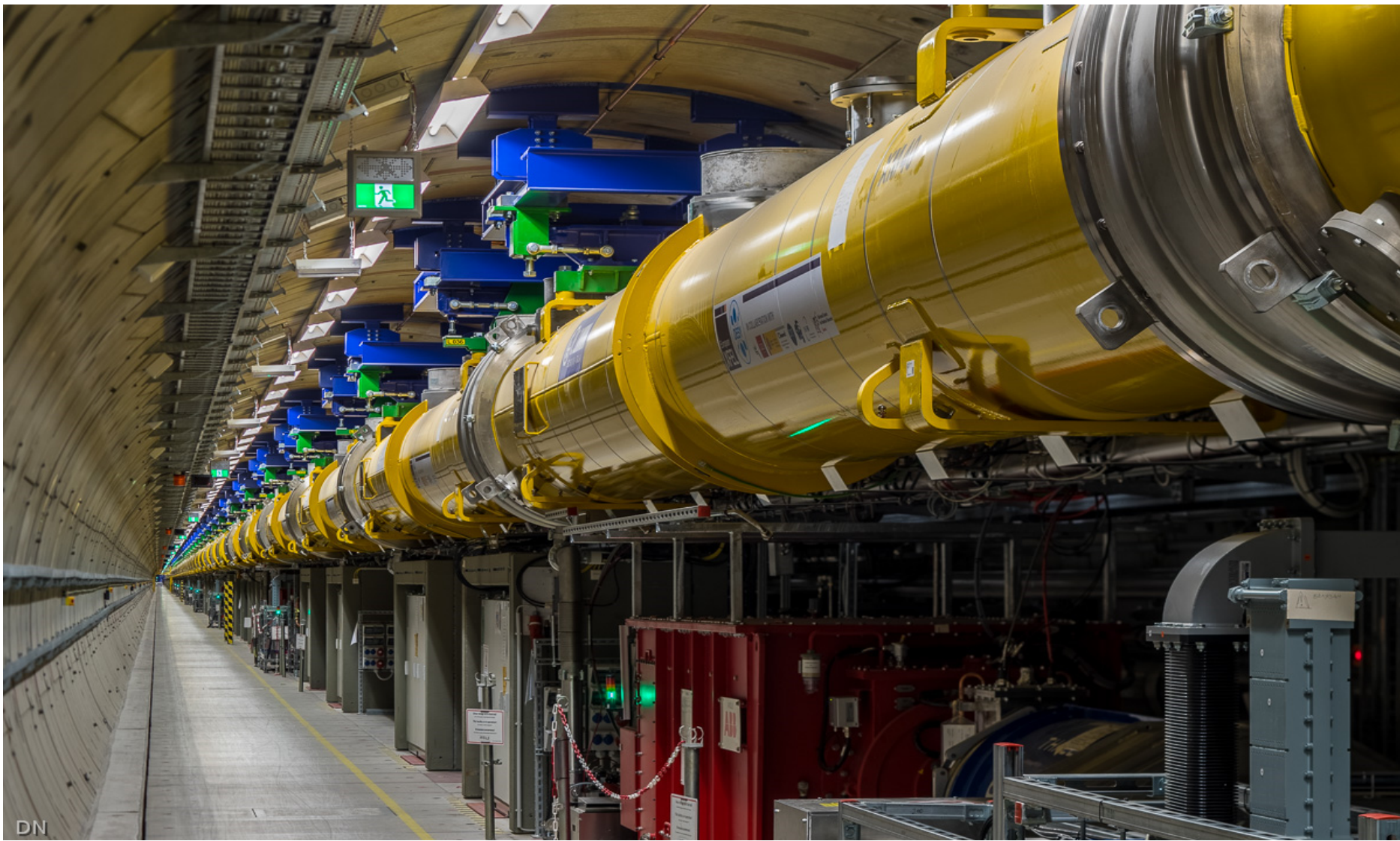


Parameters	CLIC	ILC
Particles per bunch	4×10^9	2×10^{10}
Machine repetition rate [Hz]	50	5
Linac RF pulse length [μ s]	0.156	1600
Bunch spacing in linac/DR [ns]	0.5/1	554/6
Particles per machine pulse	1.3×10^{12}	5.3×10^{13}
Injected normalized emittance (e^+) [μ m.rad]	7000	8
Injected rms energy spread [%]	± 4.5	± 0.75
H/V Extracted normalized emittances [nm]	500/5	5000/20
Extracted rms bunch length [mm]	1.8	6
Extracted rms energy spread [%]	0.1	0.15

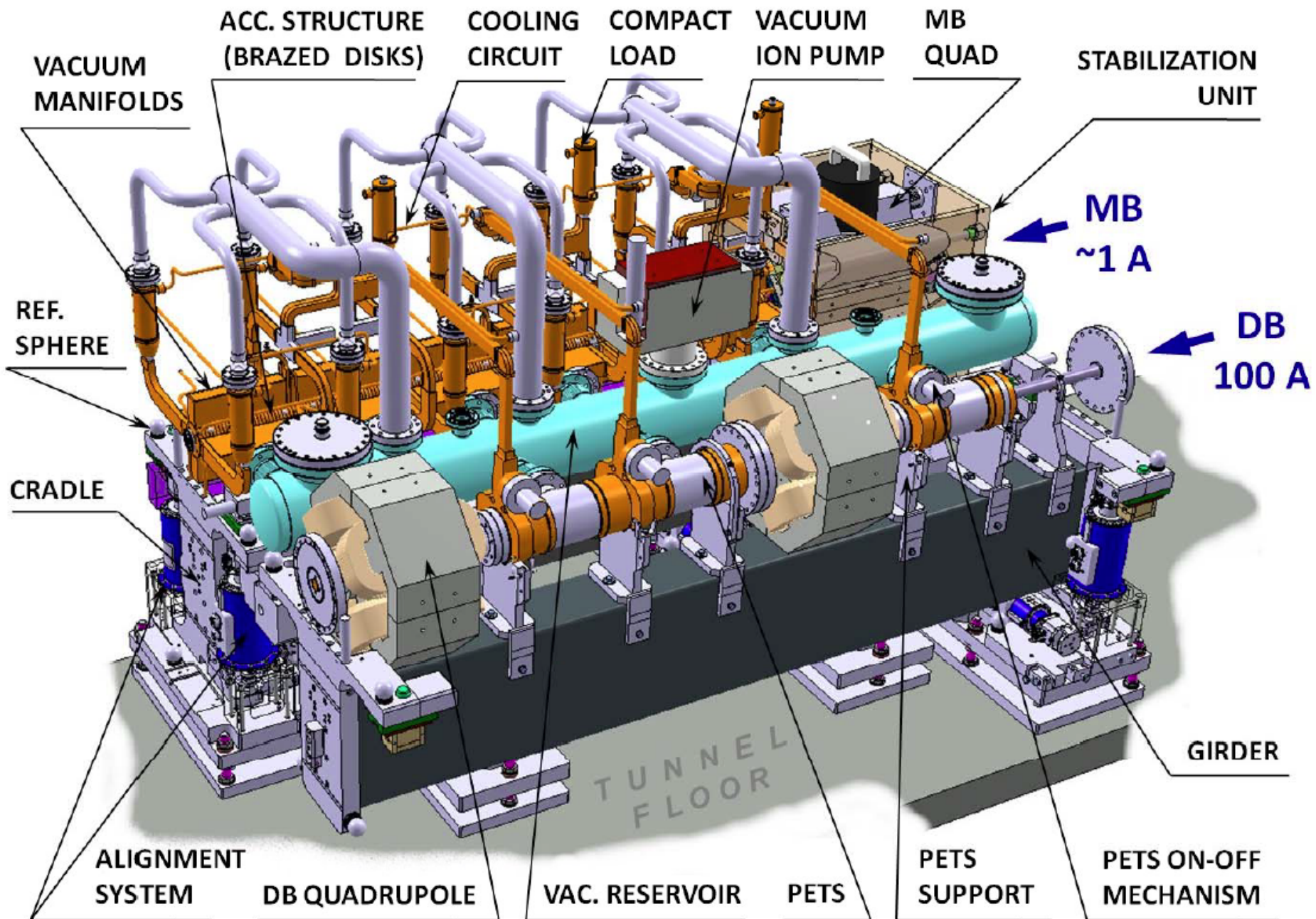
International Linear Collider:
ILC
The Next Generation?



ca. 1 kilometer “cold” LINAC



DN



0.5 / 3 TeV Parameters



Physics

Max. E_{cm}	500 GeV	3 TeV
Luminosity	$1.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$	$2.0 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
Polarisation (e-/e+)	80% / 30%	none
δ_{BS}	4.5%	29%

tiny emittances
nano-beams at IP
strong beam-beam

Beam (interaction point)

σ_x / σ_y	574 nm / 6 nm	45 nm / 1 nm
σ_z	300 μm	44 μm
$\gamma\epsilon_x / \gamma\epsilon_y$	10 μm / 35 nm	660 μm / 20 μm
β_x / β_y	11 mm / 0.48 mm	6.9 mm / 0.068 mm
bunch charge	2×10^{10}	0.6 nC

High-power high-current
beams. Short / long bunch
trains. SRF / NC RF

Structure)

Number of bunches / pulse	1312	312
Bunch spacing	554 ns	0.5 ns
Pulse current	5.8 mA	1.2 A
Beam pulse length	727 μs	156 ns
Pulse repetition rate	5 Hz	50 Hz

Accelerator (general)

Average beam power	10.5 MW (total)	14 MW
Total AC power	163 MW	415 MW
(linacs AC power)	107 MW)	2 x 63.9 MW (drive beam)

Beyond the LHC: the FCC's

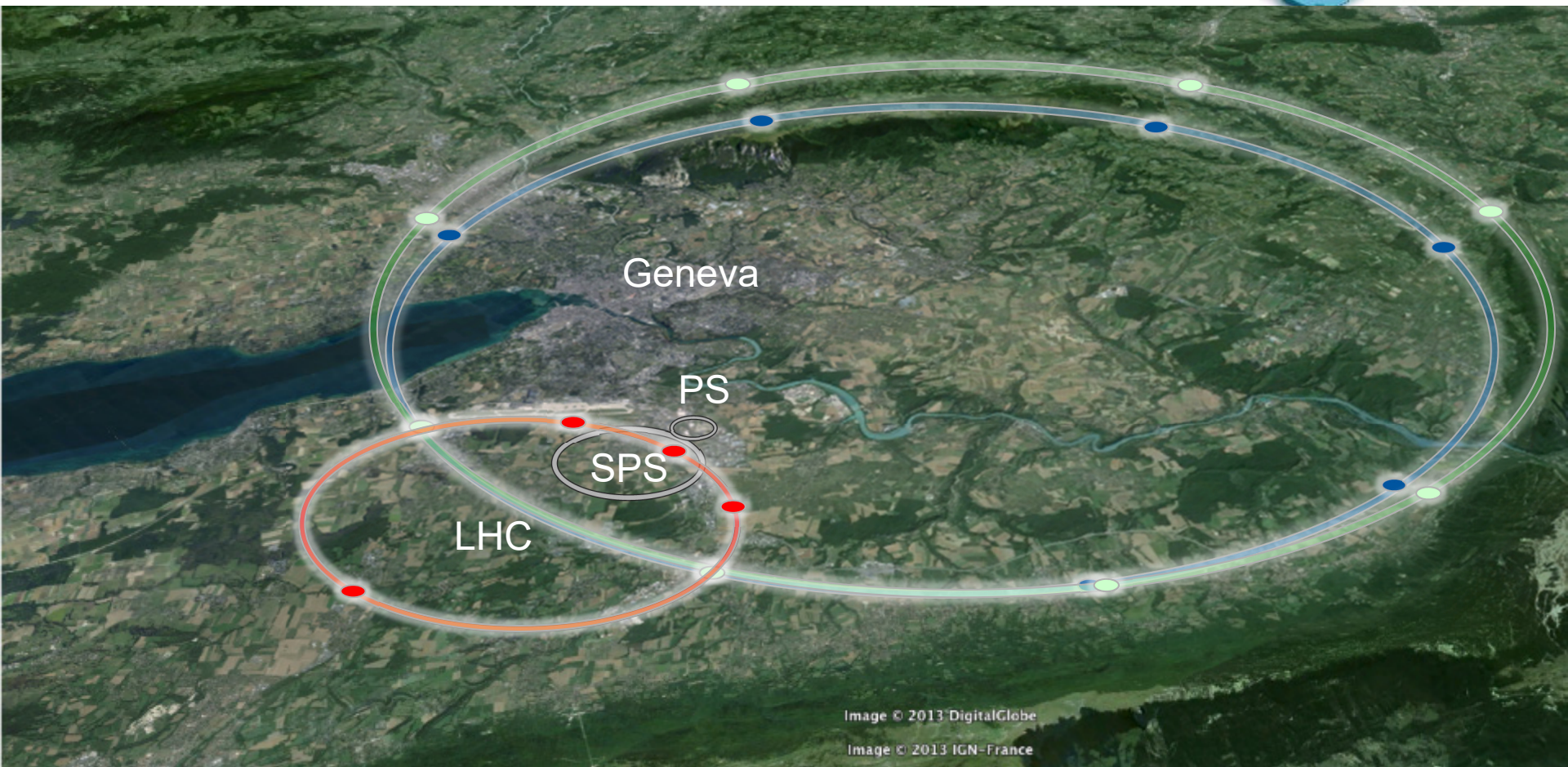


Image © 2013 DigitalGlobe
Image © 2013 IGN-France

LHC	HE-LHC	FCC-hh	FCC-hh
27 km, 8.33 T	27 km, 20 T	80 km, 20 T	100 km, 16 T
14 TeV (c.o.m.)	33 TeV (c.o.m.)	100 TeV (c.o.m.)	100 TeV (c.o.m.)
1300 tons NbTi	3000 tons LTS	9000 tons LTS	6000 tons Nb ₃ Sn
0.2 tons HTS	700 tons HTS	2000 tons HTS	3000 tons Nb-Ti



FCC Study (Future Circular Colliders)

CDR and cost review for the next ESU (2018)

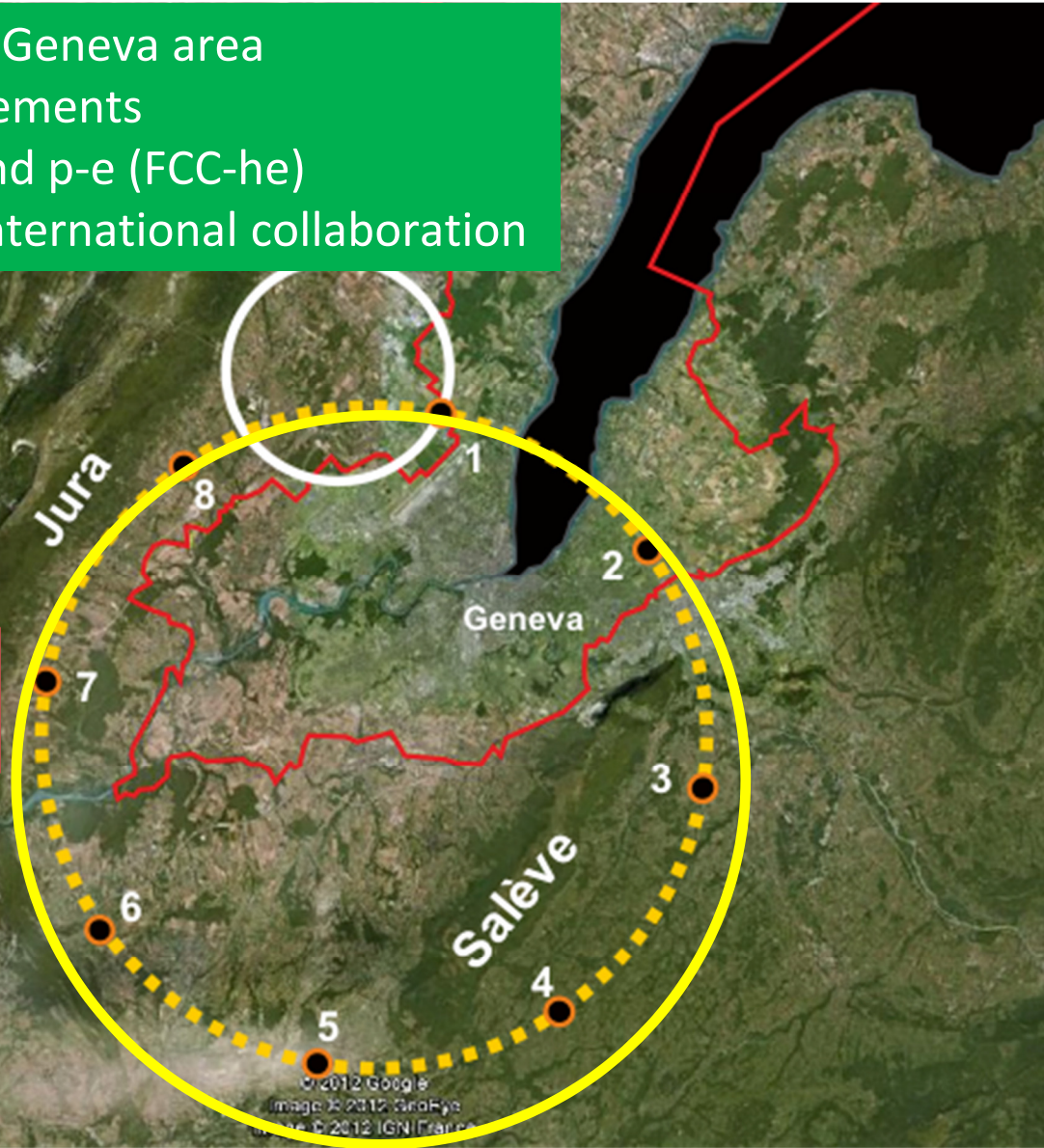
- 80-100 km tunnel infrastructure in Geneva area
- design driven by pp-collider requirements
- with possibility of e^+e^- (FCC-ee) and p-e (FCC-he)
- CERN-hosted study performed in international collaboration



electron-positron:

H: $2 \times 120 \text{ GeV}$, $L = 8 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

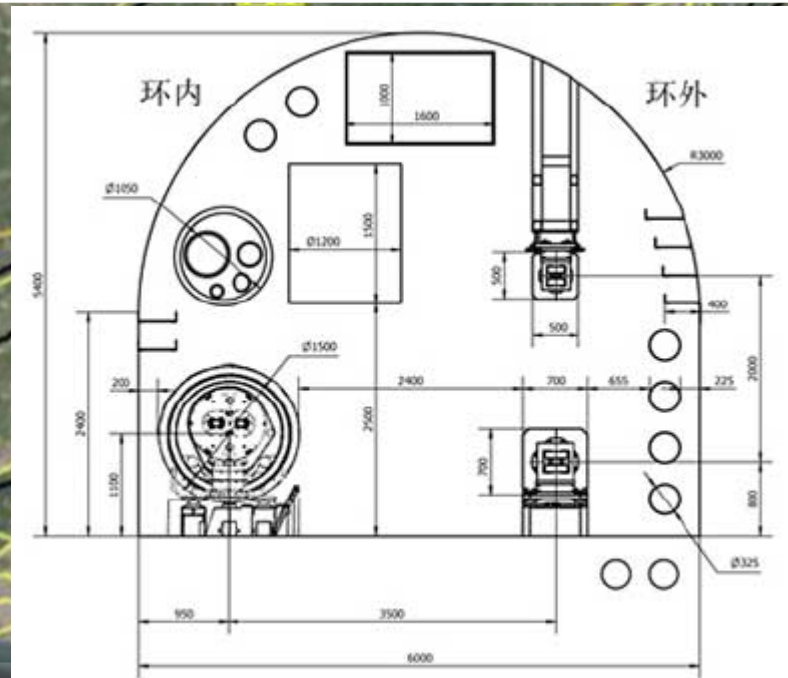
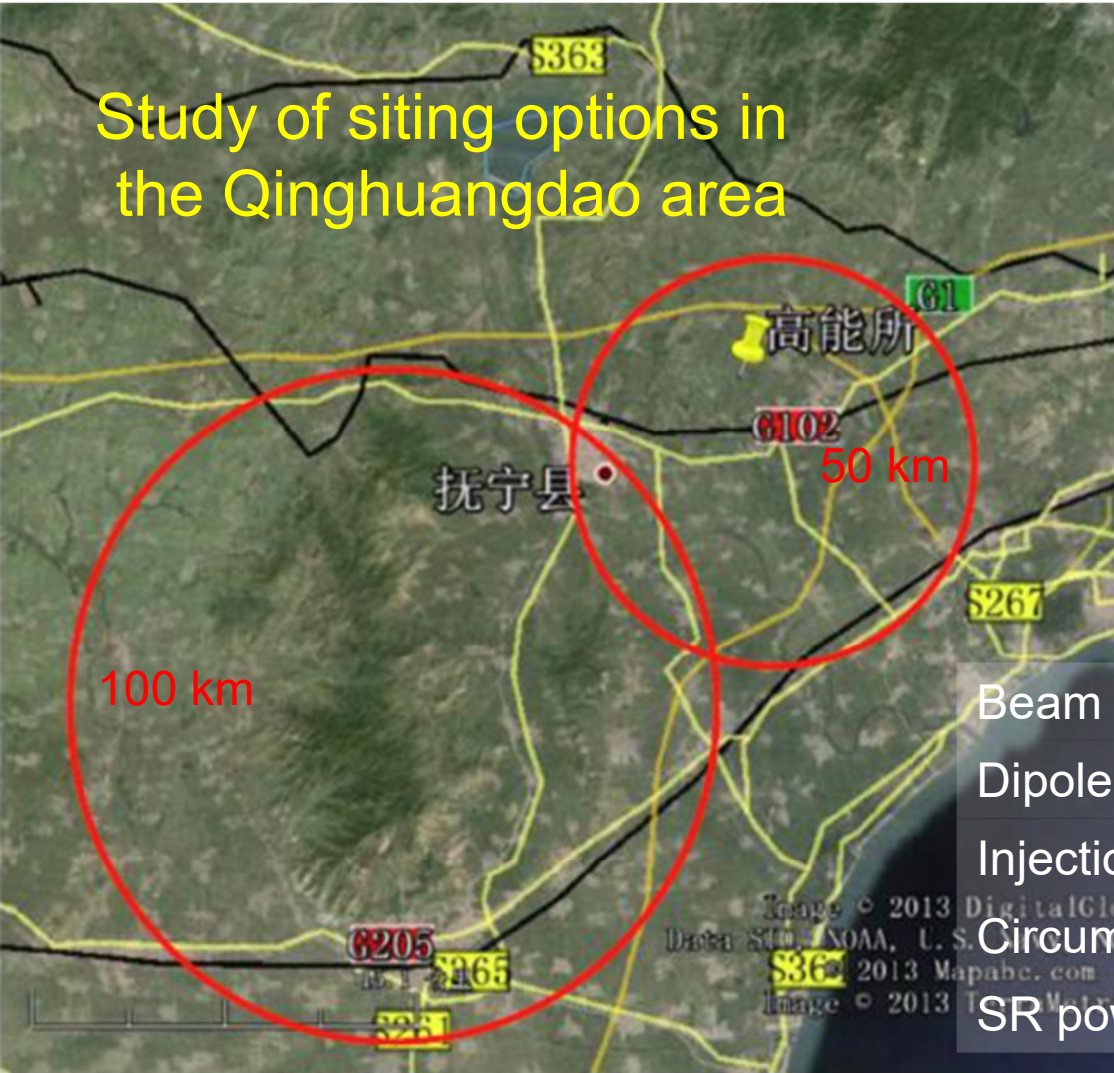
$t\bar{t}$: $2 \times 182.5 \text{ GeV}$, $L = 1.5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



parameter	Z	W	H (ZH)	ttbar
beam energy [GeV]	45.6	80	120	182.5
arc cell optics	60/60	90/90	90/90	90/90
momentum compaction [10^{-5}]	1.48	0.73	0.73	0.73
horizontal emittance [nm]	0.27	0.28	0.63	1.45
vertical emittance [pm]	1.0	1.0	1.3	2.7
horizontal beta* [m]	0.15	0.2	0.3	1
vertical beta* [mm]	0.8	1	1	2
length of interaction area [mm]	0.42	0.5	0.9	1.99
tunes, half-ring (x, y, s)	(0.569, 0.61, 0.0125)	(0.577, 0.61, 0.0115)	(0.565, 0.60, 0.0180)	(0.553, 0.59, 0.0350)
longitudinal damping time [ms]	414	77	23	6.6
SR energy loss / turn [GeV]	0.036	0.34	1.72	9.21
total RF voltage [GV]	0.10	0.44	2.0	10.93
RF acceptance [%]	1.9	1.9	2.3	4.9
energy acceptance [%]	1.3	1.3	1.5	2.5
energy spread (SR / BS) [%]	0.038 / 0.132	0.066 / 0.153	0.099 / 0.151	0.15 / 0.20
bunch length (SR / BS) [mm]	3.5 / 12.1	3.3 / 7.65	3.15 / 4.9	2.5 / 3.3
Piwinski angle (SR / BS)	8.2 / 28.5	6.6 / 15.3	3.4 / 5.3	1.39 / 1.60
bunch intensity [10^{11}]	1.7	1.5	1.5	2.8
no. of bunches / beam	16640	2000	393	39
beam current [mA]	1390	147	29	5.4
luminosity [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	230	32	8	1.5
beam-beam parameter (x / y)	0.004 / 0.133	0.0065 / 0.118	0.016 / 0.108	0.094 / 0.150
luminosity lifetime [min]	70	50	42	44
time between injections [sec]	122	44	31	32
allowable asymmetry [%]	± 5	± 3	± 3	± 3
required lifetime by BS [min]	29	16	11	10
actual lifetime by BS ("weak") [min]	> 200	20	20	25



Study of siting options in the Qinghuangdao area



Beam energy	1.2 TeV	2.1 TeV
Dipole field	12 T	20 T
Injection energy	450 MeV	2.1 TeV (1.2 T)
Circumference	54.374 km	54.374 km
SR power/beam	51.7 MW	2.1 MW



LCWS MiniSchool

$e^+ - e^-$ Colliders

Summary:

Different Electron-Positron Collider Approaches

Linear Colliders:

- **sc: high η_{RF} , long pulses and bunch spacing, reduced sensitivity to tolerances (wakefields), upgradable, lower acc. gradients**
- **nc: ultimate acc. gradients, upgradable, low η_{RF} , short pulses and bunch spacing, highly sensitive to tolerances**

Circular Colliders:

- **reach about the same luminosity values, good time structure, limited by synchrotron radiation, not upgradable, no beam polarization**