

# Dark matter production via light mediator exchange at future $e^+e^-$ colliders

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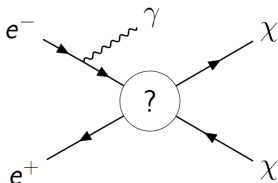
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POLAND

**The 2021 International Workshop on Future Linear Colliders**  
Theoretical Developments & Physics Analyses session  
March 17, 2021

- 1 Motivation
- 2 Analysis framework
- 3 Results
- 4 Conclusions

## Dark Matter production

The mono-photon signature is considered to be the most general way to look for **DM particle production** in future  $e^+e^-$  colliders.



DM can be pair produced in the  $e^+e^-$  collisions via exchange of a new **mediator particle**, which couples to both electrons (SM) and DM states

This process can be detected, if **additional hard photon radiation** from the initial state is observed in the detector...

## New analysis approach

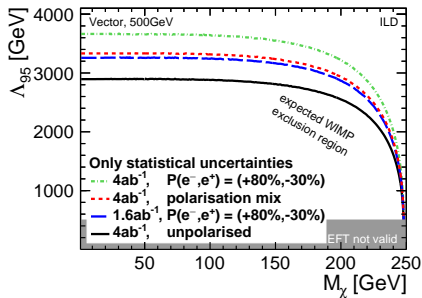
Most of the studies performed so far focused on **heavy mediator** exchange (EFT limit) and **coupling values  $\mathcal{O}(1)$**

⇒ extracted were limits on DM or mediator masses

In our study:

- focus on **light mediator** exchange (DM even lighter)
- consider **very small mediator couplings** to SM,  $\Gamma_{SM} \ll \Gamma_{tot}$

“Experimental-like” approach ⇒ focus on cross section limits as a function of mediator mass and width



ILD study: [arXiv:2001.03011](https://arxiv.org/abs/2001.03011)

Phys. Rev. D 101, 075053 (2020)

CLIC study: [arXiv:2103.06006](https://arxiv.org/abs/2103.06006)

## Running scenarios

### ILC

Total of  $4000 \text{ fb}^{-1}$  assumed at **500 GeV** (H-20 scenario)

- $2 \times 1600 \text{ fb}^{-1}$  for LR and RL beam polarisation combinations
- $2 \times 400 \text{ fb}^{-1}$  for RR and LL beam polarisation combinations

assuming polarisation of  $\pm 80\%$  for electrons and  $\pm 30\%$  for positrons

[arXiv:1903.01629](https://arxiv.org/abs/1903.01629)

### CLIC

Total of  $5000 \text{ fb}^{-1}$  assumed at **3 TeV**

- $4000 \text{ fb}^{-1}$  for negative electron beam polarisation
- $1000 \text{ fb}^{-1}$  for positive electron beam polarisation

assuming polarisation of  $\pm 80\%$  for electrons

[arXiv:1812.06018](https://arxiv.org/abs/1812.06018)

## Simulating mono-photon events

Dedicated simulation procedure for WHIZARD, with all “detectable” photons generated on Matrix Element level, matched with soft ISR.

For more details:

- ⇒ W.Kotlarski, *Simulating hard photon production with Whizard* (22:20 CET)
- ⇒ J. Kalinowski et al., *Eur. Phys. J. C* 80 (2020) 634, arXiv:2004.14486

## Detector modeling

Detector response simulated in the [Delphes framework](#).

Both ILCgen and (modified) CLICdet models include proper description of forward detectors: BeamCal and LumiCal

⇒ see backup slides for more details

## Event selection

On generator level:

- 1, 2 or 3 ME photons  
nonradiative events for signal only (for normalisation)
- all ME photons with  $q_{\pm} > 1 \text{ GeV}$  &  $E^{\gamma} > 1 \text{ GeV}$   
rejected are events with  $q_{\pm} > 1 \text{ GeV}$  &  $E^{\gamma} > 1 \text{ GeV}$  for any of the ISR photons
- at least one ME photon with  $p_T^{\gamma} > 2 \text{ GeV}$  &  $5^{\circ} < \theta^{\gamma} < 175^{\circ}$  (ILC 500 GeV)  
 $p_T^{\gamma} > 5 \text{ GeV}$  &  $7^{\circ} < \theta^{\gamma} < 173^{\circ}$  (CLIC 3 TeV)

On detector simulation level:

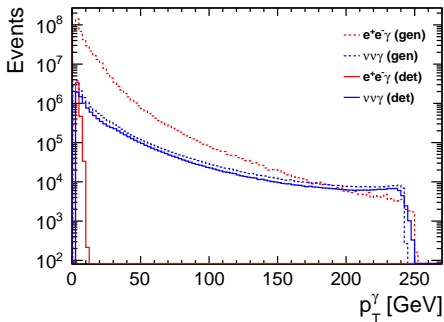
- single photon with  $p_T^{\gamma} > 3 \text{ GeV}$  &  $|\eta^{\gamma}| < 2.8$  (ILC)  
 $p_T^{\gamma} > 10 \text{ GeV}$  &  $|\eta^{\gamma}| < 2.6$  (CLIC)
- no other activity in the detector  
other reconstructed objects
  - no electrons
  - no LumiCal photons
  - no BeamCal photons
  - no jets

see backup slides for definition of  $q_{\pm}$  variables

## Background distributions

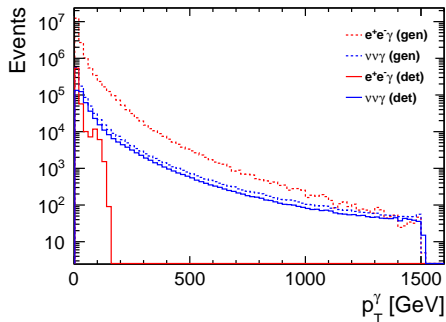
Two SM backgrounds considered:

**Bhabha scattering** and (radiative) **neutrino pair production**



ILC 500 GeV

(-80%/+30%)  $1600 \text{ fb}^{-1}$



CLIC 3 TeV

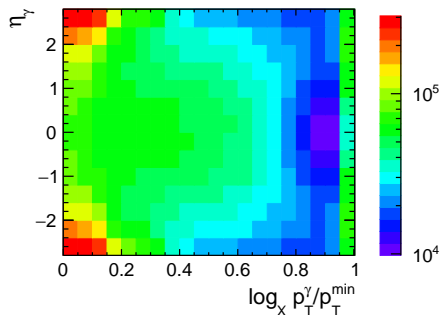
(+80%)  $1000 \text{ fb}^{-1}$



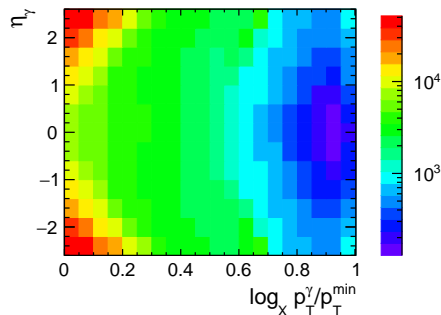
## Background distributions

For mono-photon events, two variables fully describe event kinematics

⇒ use 2D distribution of  $(p_T^\gamma, \eta)$  to constrain DM production



ILC 500 GeV  
(-80%/+30%)  $1600 \text{ fb}^{-1}$



CLIC 3 TeV  
(+80%)  $1000 \text{ fb}^{-1}$

## Simplified DM model

Simplified model covering most popular scenarios of DM pair-production

Cross section for  $e^+e^- \rightarrow \chi\chi$  for  
 $M_\chi = 50 \text{ GeV}$  and  $M_Y = 300 \text{ GeV}$

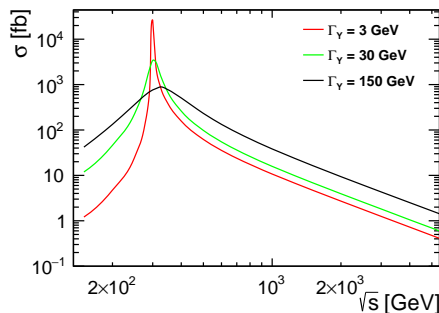
Possible DM candidates:

- real or complex scalar
- Majorana or Dirac fermion
- real vector

Possible mediators:

- scalar
- pseudo-scalar
- vector
- axial-vector

(mixed couplings, eg. V-A or V+A, also possible)

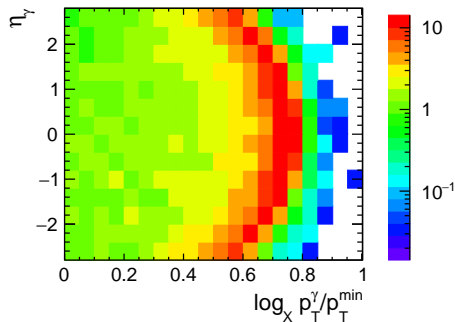


## Signal distributions

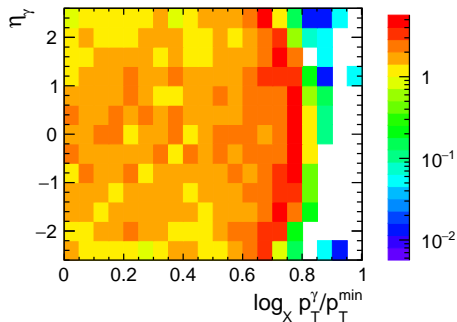
For fermion DM with  $M_\chi = 50 \text{ GeV}$  and vector mediator with  $\Gamma/M = 0.03$

Mediator mass:

400 GeV @ ILC



2.4 TeV @ CLIC

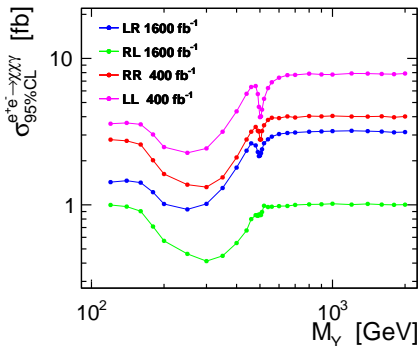


Signal normalised to unpolarised DM pair-production cross section of 1 fb

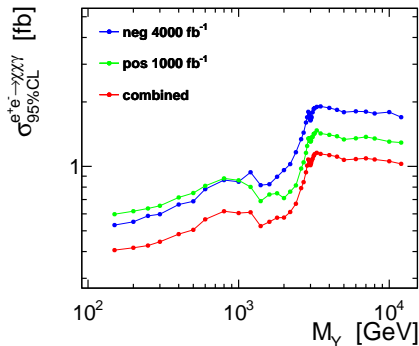
## Cross section limits for radiative events (with tagged photon)

Vector mediator with  $\Gamma/m = 3\%$

ILC @ 500 GeV



CLIC @ 3 TeV

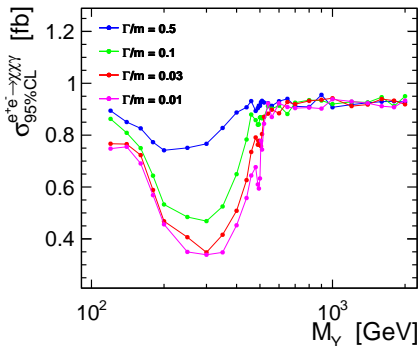


Limits calculated with CL<sub>s</sub> approach using RooFit v3.60

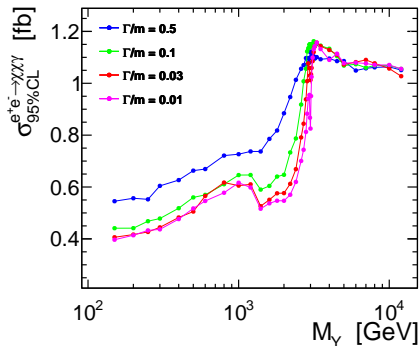
**Cross section limits** for radiative events (with tagged photon)

Vector mediator, combined limits

ILC @ 500 GeV



CLIC @ 3 TeV



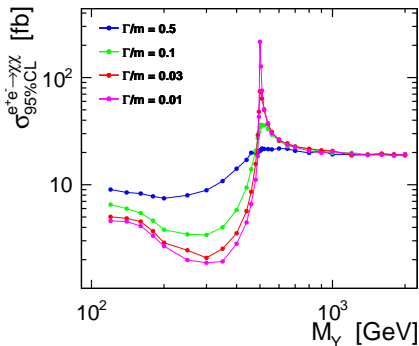
Limits calculated with  $CL_s$  approach using RooFit v3.60

## Cross section limits for total DM production cross section

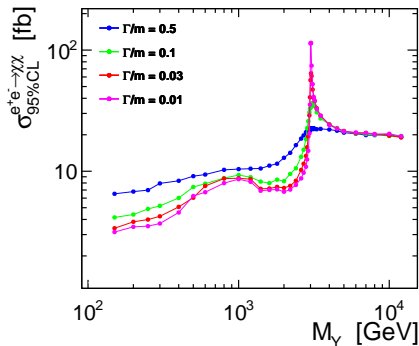
Corrected for probability of hard photon tagging! see backup slides

Combined limits for mediator with  $\Gamma/m = 3\%$

ILC @ 500 GeV



CLIC @ 3 TeV



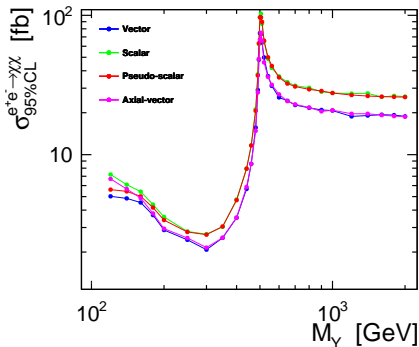
Radiation suppressed for narrow mediator with  $M_\gamma \sim \sqrt{s} \Rightarrow$  weaker limits

## Cross section limits for total DM production cross section

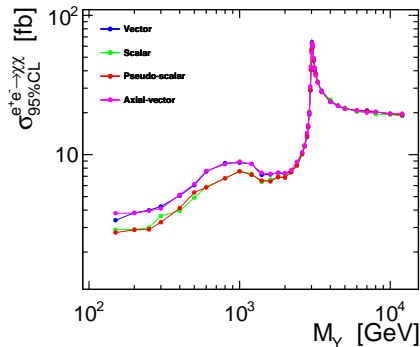
Corrected for probability of hard photon tagging! see backup slides

Combined limits for mediator with  $\Gamma/m = 3\%$

ILC @ 500 GeV



CLIC @ 3 TeV



Radiation suppressed for narrow mediator with  $M_\gamma \sim \sqrt{s} \Rightarrow$  weaker limits

## Systematic uncertainties

PRELIMINARY

following ILD study: Phys. Rev. D 101, 075053 (2020), [arXiv:2001.03011](https://arxiv.org/abs/2001.03011)

Considered sources of uncertainties:

- Integrated luminosity uncertainty of 0.26%  
uncorrelated between polarisations
- Luminosity spectra shape uncertainty  
correlated between polarisations
- Uncertainty in neutrino background normalisation of 0.2% (th+exp)  
correlated between polarisations
- Uncertainty in Bhabha background normalisation of 1% (th+exp)  
correlated between polarisations

⇒ nuisance parameters in the model fit (7 for ILC, 5 for CLIC)

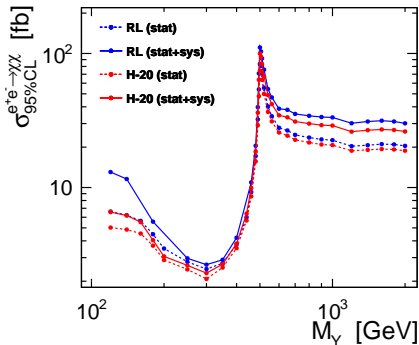


## Systematic uncertainties

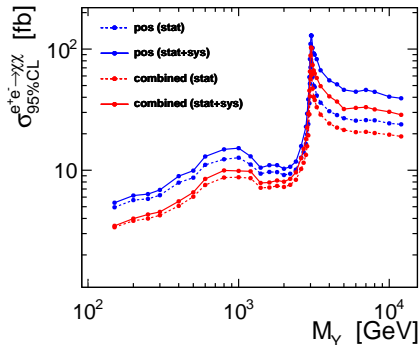
PRELIMINARY

Limits for mediator with  $\Gamma/m = 3\%$ 

ILC @ 500 GeV



CLIC @ 3 TeV

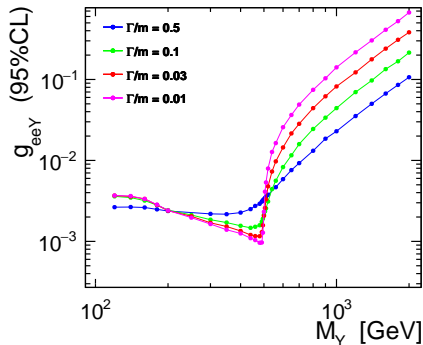


Influence of systematic effects reduced for light mediators,  $M_Y < \sqrt{s}$

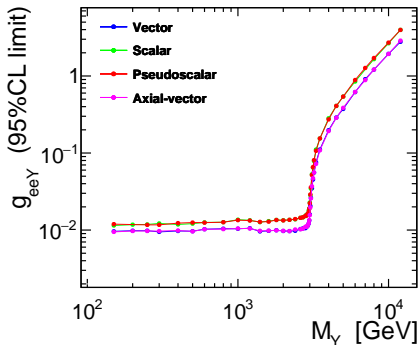
## Coupling limits with systematic uncertainties

Combined coupling limits for assumed mass and width of the mediator.

ILC @ 500 GeV



CLIC @ 3 TeV



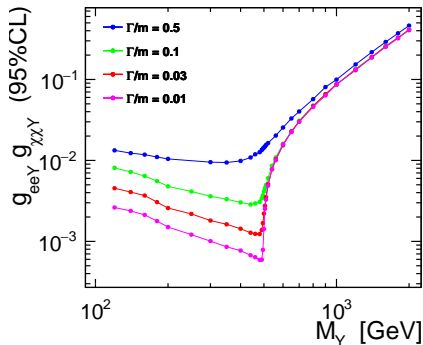
Almost uniform sensitivity to  $g_{ee\gamma}$  up to kinematic limit.

Coupling limits weakly dependent on the assumed coupling structure!

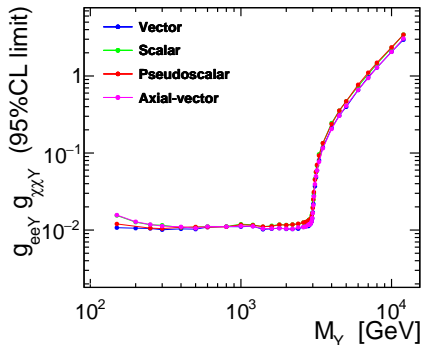
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Combined coupling limits for assumed mass and width of the mediator.

ILC @ 500 GeV



CLIC @ 3 TeV



Almost uniform sensitivity to  $g_{eeY}$  up to kinematic limit.

Coupling limits weakly dependent on the assumed coupling structure!

New framework for **mono-photon analysis** developed  
**focus on light mediator exchange and very small mediator couplings to SM**

Mono-photon production at  $e^+e^-$  colliders sensitive  
to wide range of **DM pair-production scenarios**

- $\mathcal{O}(1 \text{ fb})$  limits on the radiative production  $e^+e^- \rightarrow \chi\chi\gamma_{\text{tag}}$
- $\mathcal{O}(10 \text{ fb})$  limits on the DM pair-production  $e^+e^- \rightarrow \chi\chi(\gamma)$   
except for the resonance region  $M_\gamma \sim \sqrt{s}$
- $\mathcal{O}(10^{-3} - 10^{-2})$  limits on the mediator coupling to electrons  
up to the kinematic limit  $M_\gamma \leq \sqrt{s}$

Limits largely independent on the mediator type/coupling

For heavy mediators, limits from EFT analysis can be reproduced

For light mediators limits more stringent than those expected from direct  
resonance search in SM decay channels

**Thank you!**

## Simulating mono-photon events

W.Kotlarski, *Simulating hard photon production with WHIZARD*,  
PD1+PD4 session this evening (CET)

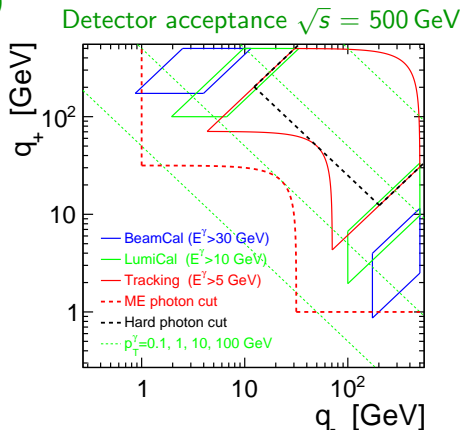
Two variables, calculated separately  
for each emitted photon:

$$q_- = \sqrt{4E_0 E_\gamma} \cdot \sin \frac{\theta_\gamma}{2},$$

$$q_+ = \sqrt{4E_0 E_\gamma} \cdot \cos \frac{\theta_\gamma}{2},$$

are used to separate “soft ISR”  
emission region from the region  
described by ME calculations.

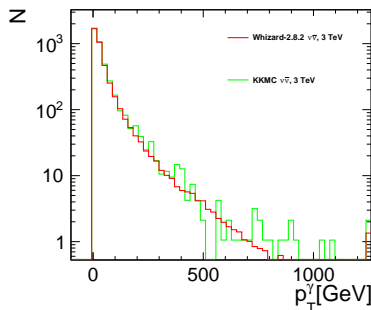
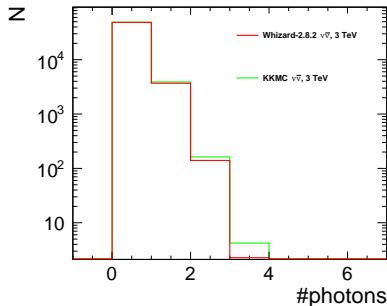
All “detectable” photons are simulated with Matrix Elements



## Simulating mono-photon events

## Validation of the procedure

WHIZARD predictions were compared to the results from the KKMC code for  $e^+e^- \rightarrow \nu\bar{\nu} + N\gamma$



$\Rightarrow$  very good agreement observed (both for shape and normalisation)

For more details:

J. Kalinowski et al., Eur. Phys. J. C 80 (2020) 634, arXiv:2004.14486

## Simplified DM model

Dark matter particles,  $X_i$ , couple to the SM particles via an mediator,  $Y_j$ .

Each simplified scenario is characterized by one dark matter candidate and one mediator from the set listed below:

	particle	mass	spin	charge	self-conjugate	type
DM	$X_R$	$m_{X_R}$	0	0	yes	real scalar
	$X_C$	$m_{X_C}$	0	0	no	complex scalar
	$X_M$	$m_{X_M}$	$\frac{1}{2}$	0	yes	Majorana fermion
	$X_D$	$m_{X_D}$	$\frac{1}{2}$	0	no	Dirac fermion
	$X_V$	$m_{X_V}$	1	0	yes	real vector
mediator	$Y_R$	$m_{Y_R}$	0	0	yes	real scalar
	$Y_V$	$m_{Y_C}$	1	0	yes	real vector
	$T_C$	$m_{T_C}$	0	1	no	charged scalar



## Simplified DM model

Lagrangian describing mediator coupling to electrons given by

$$\mathcal{L}_{eeY} \ni \bar{e}(g_{eY_R}^1 + v\gamma^5 g_{eY_R}^5)eY_R + \bar{e}\gamma_\mu(g_{eY_V}^1 + \gamma^5 g_{eY_V}^5)eY_V^\mu$$

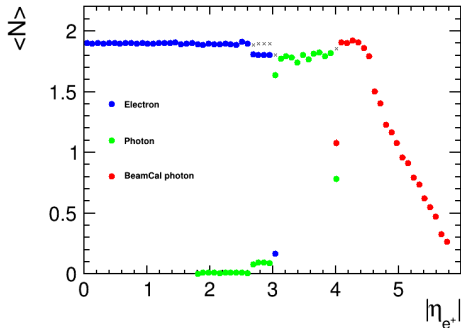
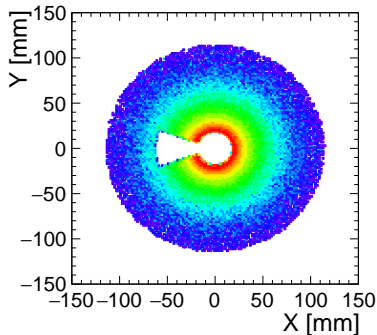
The interaction of mediators with dark matter is described by

$$\begin{aligned} \mathcal{L}_{XXY} \ni & g_{X_R Y_R} X_R^2 Y_R + i g_{X_C Y_V} (X_C^* (\partial_\mu X_C) - (\partial_\mu X_C^*) X_C) Y_V^\mu + \\ & \bar{X}_D (g_{X_D Y_R}^1 + v\gamma^5 g_{X_D Y_R}^5) X_D Y_R + \bar{X}_D \gamma_\mu (g_{X_D Y_V}^1 + \gamma^5 g_{X_D Y_V}^5) X_D Y_V^\mu \\ & \bar{X}_M (g_{X_M Y_R}^1 + v\gamma^5 g_{X_M Y_R}^5) X_M Y_R + g_{X_M Y_V}^5 \bar{\psi}_M \gamma_\mu \gamma^5 \psi_M Y_V^\mu \end{aligned}$$

## Detector simulation for ILC running at 500 GeV

ILCgen model for Delphes includes proper modelling of forward detectors

**BeamCal** Reconstruction efficiency for  $e^+e^- \rightarrow e^+e^-$



Included in the official Delphes repository as [delphes\\_card\\_ILCgen.tcl](#)

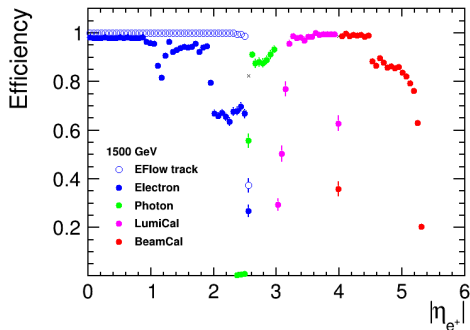
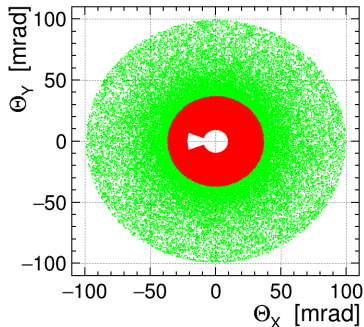
## Detector simulation

for CLIC running at 3 TeV

CLICdet model for Delphes also modified to include forward calorimeters

LumiCal + BeamCal

Reconstruction efficiency for  $e^+e^- \rightarrow e^+e^-$



Included in the repository as [delphes\\_card\\_CLICdet\\_Stage3\\_fcal.tcl](#)

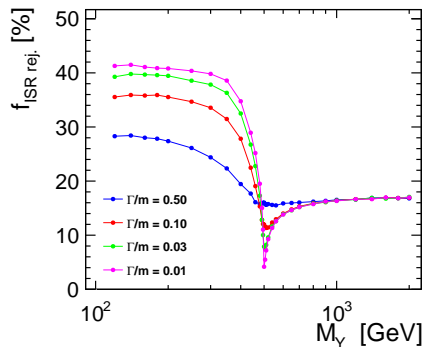
## ILC vs CLIC comparison of simulation and analysis setup

	ILCgen @ 500 GeV	CLICdet @ 3 TeV
<b>Generator level cuts</b>		
$p_T^\gamma$ min.	2 GeV	5 GeV
$\Theta^\gamma$ min.	$5^\circ$	$7^\circ$
<b>Detector acceptance (Delphes model)</b>		
tracking	$ \eta  < 3$	$ \eta  < 2.54$
ECAL	$ \eta  < 3$	$ \eta  < 3$
LumiCal	$3 <  \eta  < 4$	$3 <  \eta  < 4$
BeamCal	$4 <  \eta  < 5.8$	$4 <  \eta  < 5.3$
<b>Detector level cuts</b>		
$p_T^\gamma$ min.	3 GeV	10 GeV
$ \eta^\gamma $ max.	2.8 ( $7^\circ$ )	2.6 ( $8.5^\circ$ )

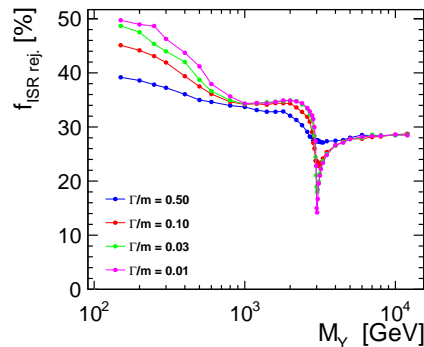
## ISR rejection efficiency

Fraction of events generated by WHIZARD removed by ISR rejection procedure (ISR photons emitted in the phase-space region covered by ME)

ILC @ 500 GeV



CLIC @ 3 TeV

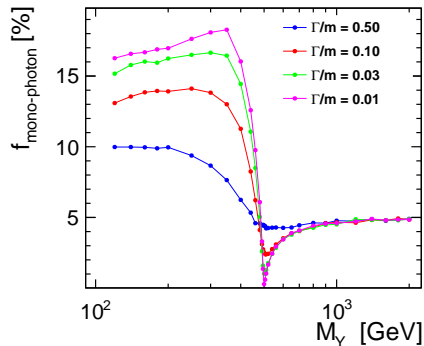


## Tagging efficiency

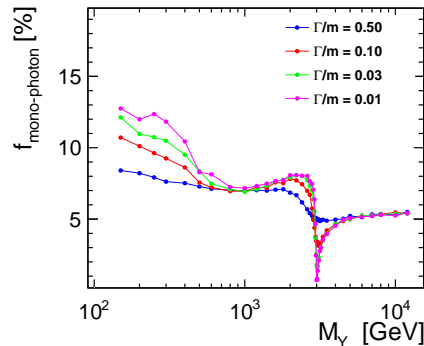
Detectable hard photon emitted only in a fraction of signal event

$$\sigma(e^+e^- \rightarrow \chi\chi\gamma_{\text{tag}}) = f_{\text{mono-photon}} \cdot \sigma(e^+e^- \rightarrow \chi\chi(\gamma))$$

ILC @ 500 GeV



CLIC @ 3 TeV



Emission strongly suppressed for narrow mediator with  $M_Y \sim \sqrt{s}$

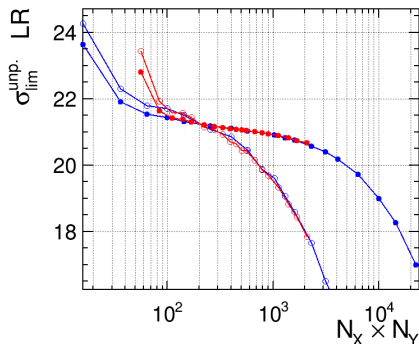
## Number of bins

The higher number of bins in 2D  $(p_T^\gamma, \eta^\gamma)$  distribution,  
the higher sensitivity to BSM scenarios...

but also to statistical fluctuations in MC samples (mainly for signal)

Expected limits vs number of bins

for 100k (open) and 1M (full circles) MC events in signal sample



$$\Rightarrow N_{bin} \leq 300$$

to avoid problems due to  
limited MC statistics

20 × 14 bins used for ILC

20 × 13 bins used for CLIC

## Effective mass scale limits

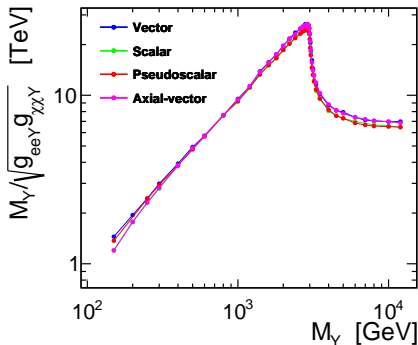
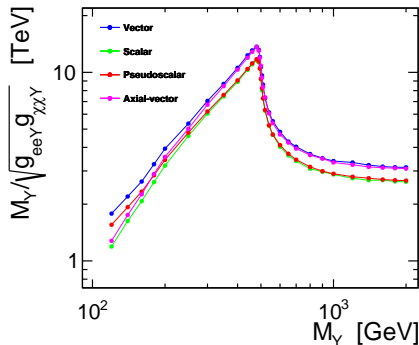
$$\Lambda^2 = \frac{M_Y^2}{|g_{eeY}g_{\chi\chi Y}|}$$

For  $M_Y \gg \sqrt{s}$ , limits on the effective mass scale of new interactions no longer depend on the assumed mediator mass or width

⇒ EFT approximation can be used

ILC @ 500 GeV  $\Lambda^{\text{lim}} \sim 3 \text{ TeV}$

CLIC @ 3 TeV  $\Lambda^{\text{lim}} \sim 7 \text{ TeV}$





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