

Measurement of $\sigma(e^+ e^- \rightarrow HZ) \times \text{Br}(H \rightarrow ZZ^*)$ at the 250 GeV ILC

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- Conclusions

Introduction

The width of the Higgs boson *is difficult to measure at LHC in a model-independent approach* (the uncertainty *~20% after luminosity upgrade*)

We propose to use the process $e^+e^- \rightarrow HZ$ with the subsequent decay $H \rightarrow ZZ^*$ to measure:

$$\sigma(e^+e^- \rightarrow HZ) \times Br(H \rightarrow ZZ^*) = C \cdot g_Z^4 / \Gamma_H$$

Only one of Z bosons is reconstructed in lepton mode.

$$Z \rightarrow jj \text{ or } ll, \quad Z^* \rightarrow ll \text{ or } jj$$

Constant,
Error < 1%
expected in
calculations

Coupling HZZ
Error < 0.5% expected
from other ILC studies

Higgs boson width

Studied MC processes

Signal subprocesses with large significance:

Significant backgrounds:

- | | | |
|---|--------------------------------------|---|
| 1) $e^+e^- \rightarrow Z_1(j_1j_2)H,$ | $H \rightarrow Z(j_1j_2)Z^*(l_1l_2)$ | ← 6-fermion $jjjj l^+l^-$ - background for channel 1
Examples: $WW\gamma$ and $ZZ\gamma$ |
| 2) $e^+e^- \rightarrow Z_1(j_1j_2)H,$ | $H \rightarrow Z(l_1l_2)Z^*(j_1j_2)$ | |
| 3) $e^+e^- \rightarrow Z_1(\nu\bar{\nu})H,$ | $H \rightarrow Z(j_1j_2)Z^*(l_1l_2)$ | ← $b\bar{b} \rightarrow jj l^+l^- \nu\bar{\nu}$ - background for channel 3 |
| 4) $e^+e^- \rightarrow Z_1(\nu\bar{\nu})H,$ | $H \rightarrow Z(l_1l_2)Z^*(j_1j_2)$ | |

No significant backgrounds are found for channels with on-shell $Z \rightarrow l_1l_2$, random lepton pairs have low mass

We tried to study events with 4 leptons, however number of such signal events is very small.

Event selection

Initial samples: $e^+e^- \rightarrow q\bar{q}H$
 $e^+e^- \rightarrow \nu_e\bar{\nu}_eH$
 $e^+e^- \rightarrow \nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}H$

Number of initial events for each sub-process = 500000

Sub-process	MC generator level extraction, N events	Isolated leptons tagging, N events	Weight factors	Number of weighted events
$Z_1 \rightarrow j_1j_2, Z \rightarrow j_1j_2, Z^* \rightarrow l_1l_2$	605	416	0.803	334
$Z_1 \rightarrow j_1j_2, Z \rightarrow l_1l_2, Z^* \rightarrow j_1j_2$	578	508	0.803	407
$Z_1 \rightarrow \nu_e\bar{\nu}_e, Z \rightarrow j_1j_2, Z^* \rightarrow l_1l_2$	636	544	0.071	38
$Z_1 \rightarrow \nu_e\bar{\nu}_e, Z \rightarrow l_1l_2, Z^* \rightarrow j_1j_2$	594	468	0.071	33
$Z_1 \rightarrow \nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}, Z \rightarrow j_1j_2, Z^* \rightarrow l_1l_2$	626	534	0.157	83
$Z_1 \rightarrow \nu_{\mu,\tau}\bar{\nu}_{\mu,\tau}, Z \rightarrow l_1l_2, Z^* \rightarrow j_1j_2$	588	455	0.157	71

- Extraction of all sub-processes from initial samples
- ILT: *finding events with 2 leptons*
- Polarization weight factors to correct for $P = (\pm 0.8, \mp 0.3)$:

$$w = \frac{\sigma_{LR\,eff} \cdot \mathcal{L}}{N_{events}}$$

$$\mathcal{L} = 2000 \text{ fb}^{-1}$$

$$LR: \sigma_{LR\,eff} = \sigma_{LR} \cdot \frac{(1 + 0,8)}{2} \cdot \frac{(1 + 0,3)}{2}$$

We tried to study RL polarization signal events. However number of such signal events is too small.

- Jet reconstruction: *Jet Finder* processor with *Valencia algorithm* is used to force reconstruction of **2 or 4 jets**.

Minimum χ_{min}^2 calculation

$$Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll$$

$$\chi_{min}^2 = \frac{(M_{Z_1} - M_{Z_{nom}})^2}{\sigma_{M_{Z_1}}^2} + \frac{(M_Z - M_{Z_{nom}})^2}{\sigma_{M_Z}^2} + \frac{(P_{Z_1} - P_{Z_{nom}})^2}{\sigma_{P_{Z_1}}^2} + \frac{(P_{Z+Z^*} - P_{Z_{nom}})^2}{\sigma_{P_{Z+Z^*}}^2};$$

$$Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow jj$$

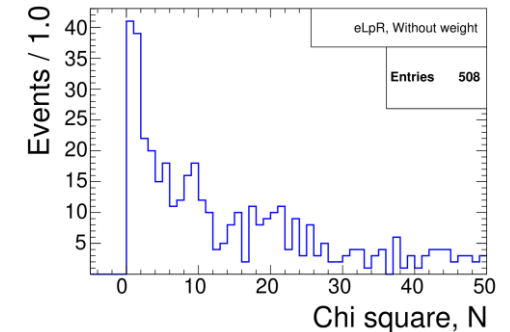
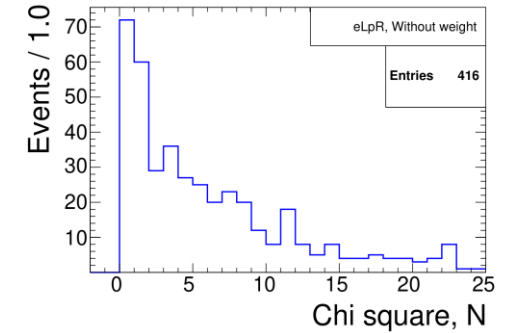
$$\chi_{min}^2 = \frac{(M_{Z_1} - M_{Z_{nom}})^2}{\sigma_{M_{Z_1}}^2} + \frac{(P_{Z_1} - P_{Z_{nom}})^2}{\sigma_{P_{Z_1}}^2} + \frac{(P_{Z+Z^*} - P_{Z_{nom}})^2}{\sigma_{P_{Z+Z^*}}^2} + \frac{(E_{Z_1} - E_{Z_{nom}})^2}{\sigma_{E_{Z_1}}^2};$$

In case of 4 jets in event we match jets to Z bosons selecting combination with minimal χ_{min}^2 from 6 possible

6 combinations of jets:

- 1) J1+J2 , J3+J4
- 2) J1+J3 , J2+J4
- 3) J1+J4 , J2+J3
- 4) J2+J3 , J1+J4
- 5) J2+J4 , J1+J3
- 6) J3+J4 , J1+J2

All σ are estimated from data



$$M_{Z_{nom}} = 91.2 \text{ GeV}$$

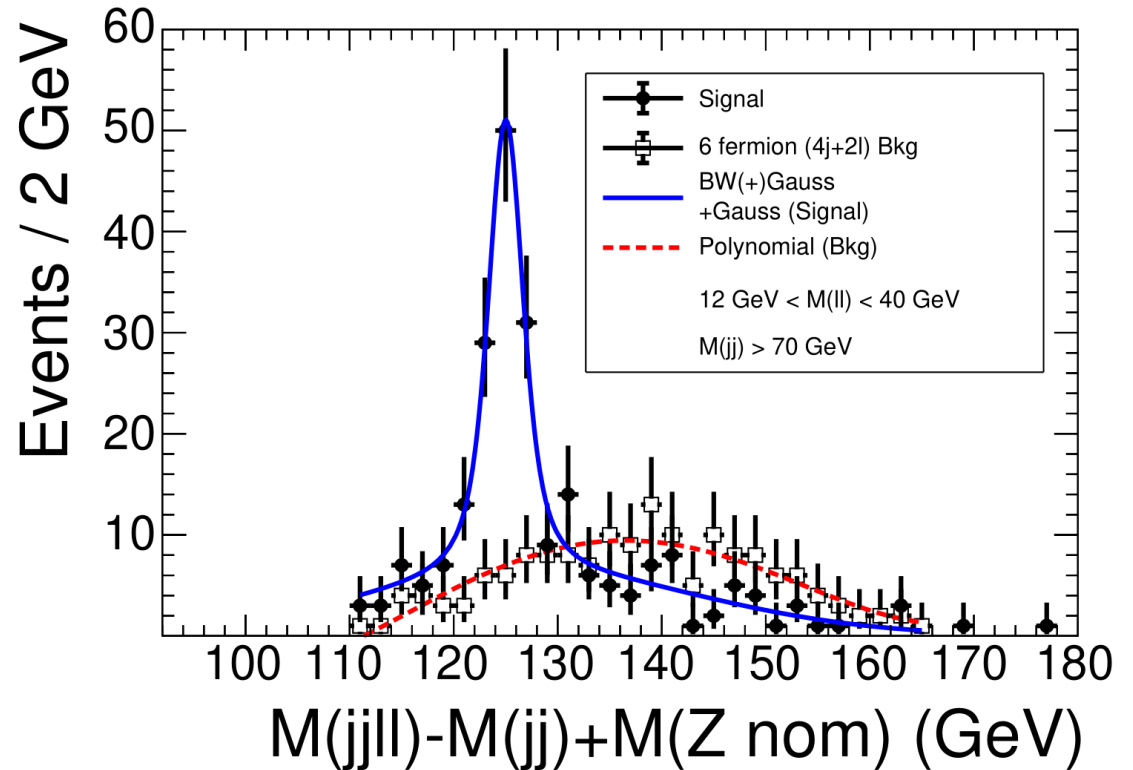
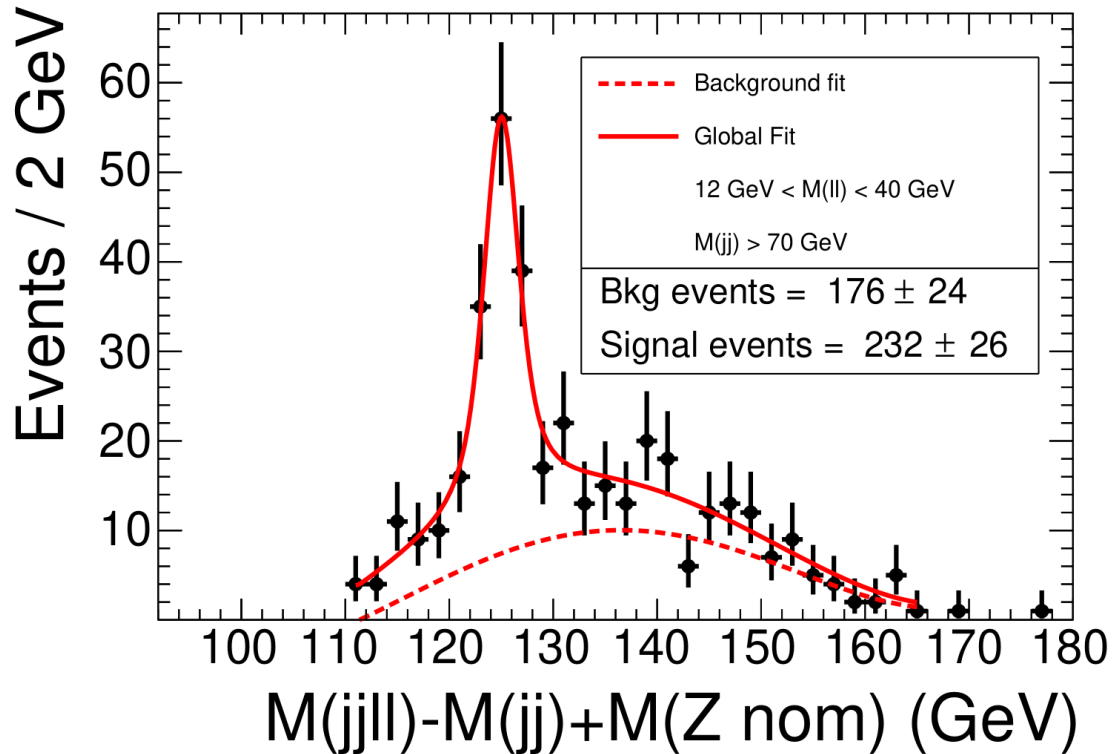
$$P_{Z_{nom}} = 60.0 \text{ GeV}$$

$$E_{Z_{nom}} = 110.0 \text{ GeV}$$

$$e^+ e^- \rightarrow Z_1 H(Z Z^*)$$

$$Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll$$

Background $jjjj l^+ l^-$ events come from $WW\gamma$ and $ZZ\gamma$ with off-shell γ (estimated for 2000 fb^{-1})



Fixed shapes, free normalizations in this fit

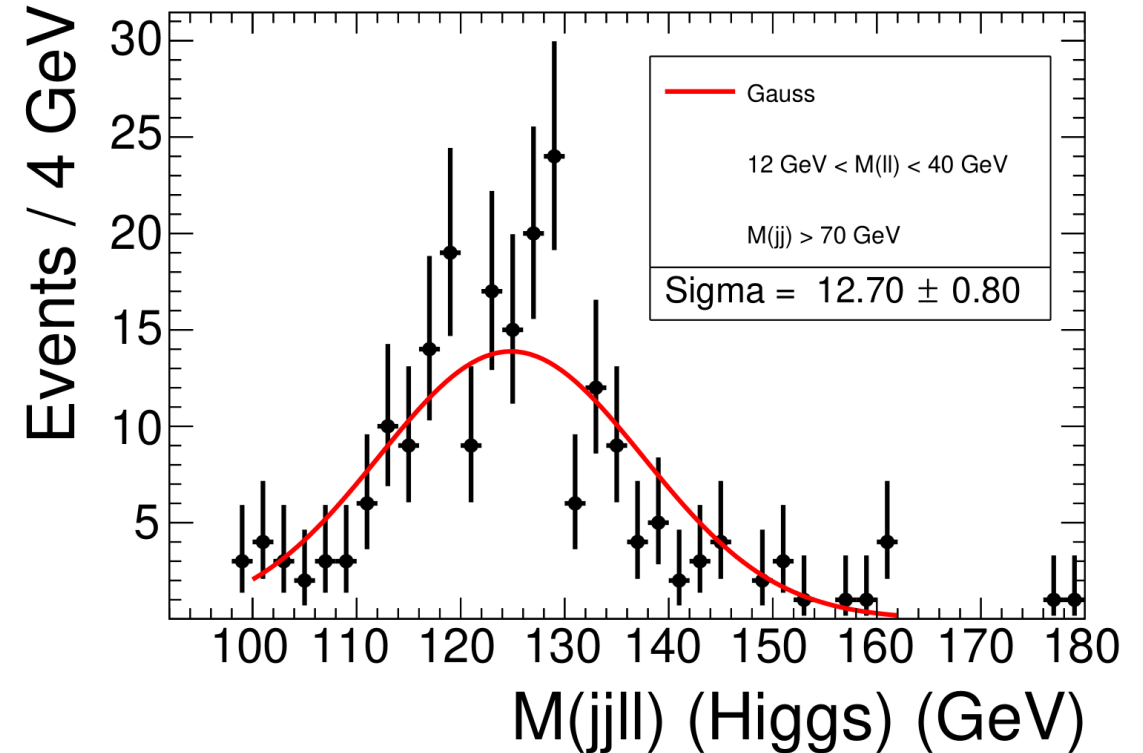
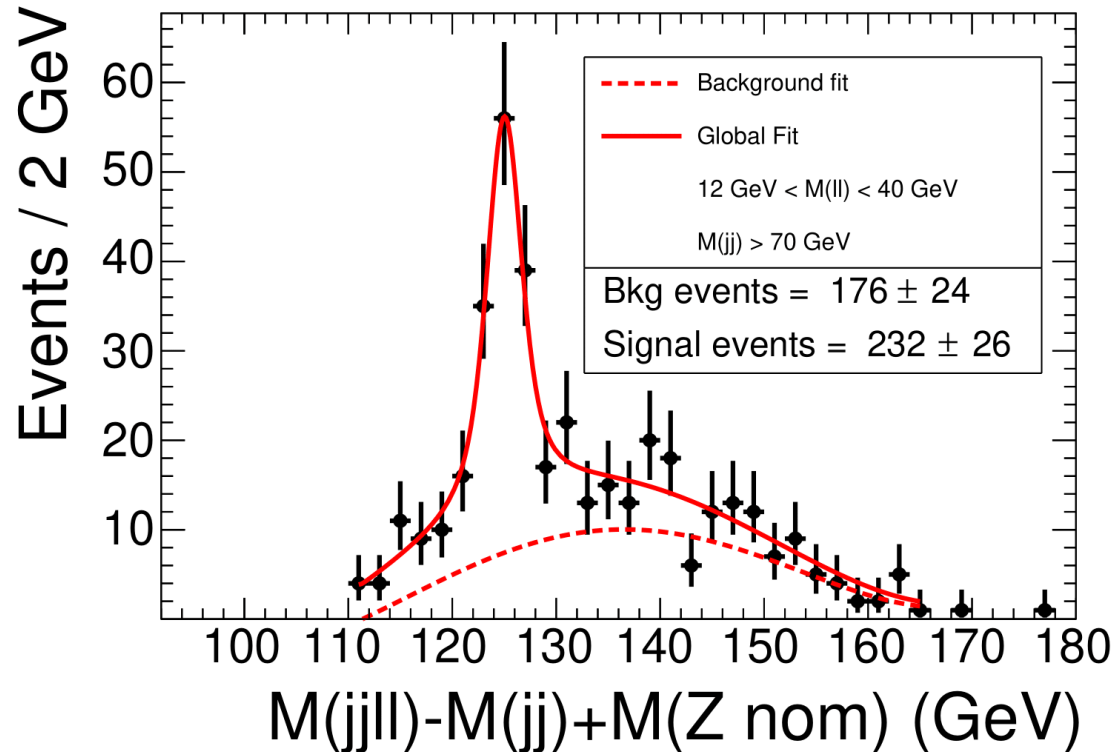
$$\sqrt{s} = 250 \text{ GeV} \quad \mathcal{L} = 2000 \text{ fb}^{-1}$$

Statistical uncertainty = **11.2 %**

Signal is modelled by **Gaussian** \oplus **BW** + **Gaussian** function (wide gaussian comes from $Z^* Z^*$ tail).
Background is described by **Chebychev3** function

$$e^+ e^- \rightarrow Z_1 H(Z Z^*)$$

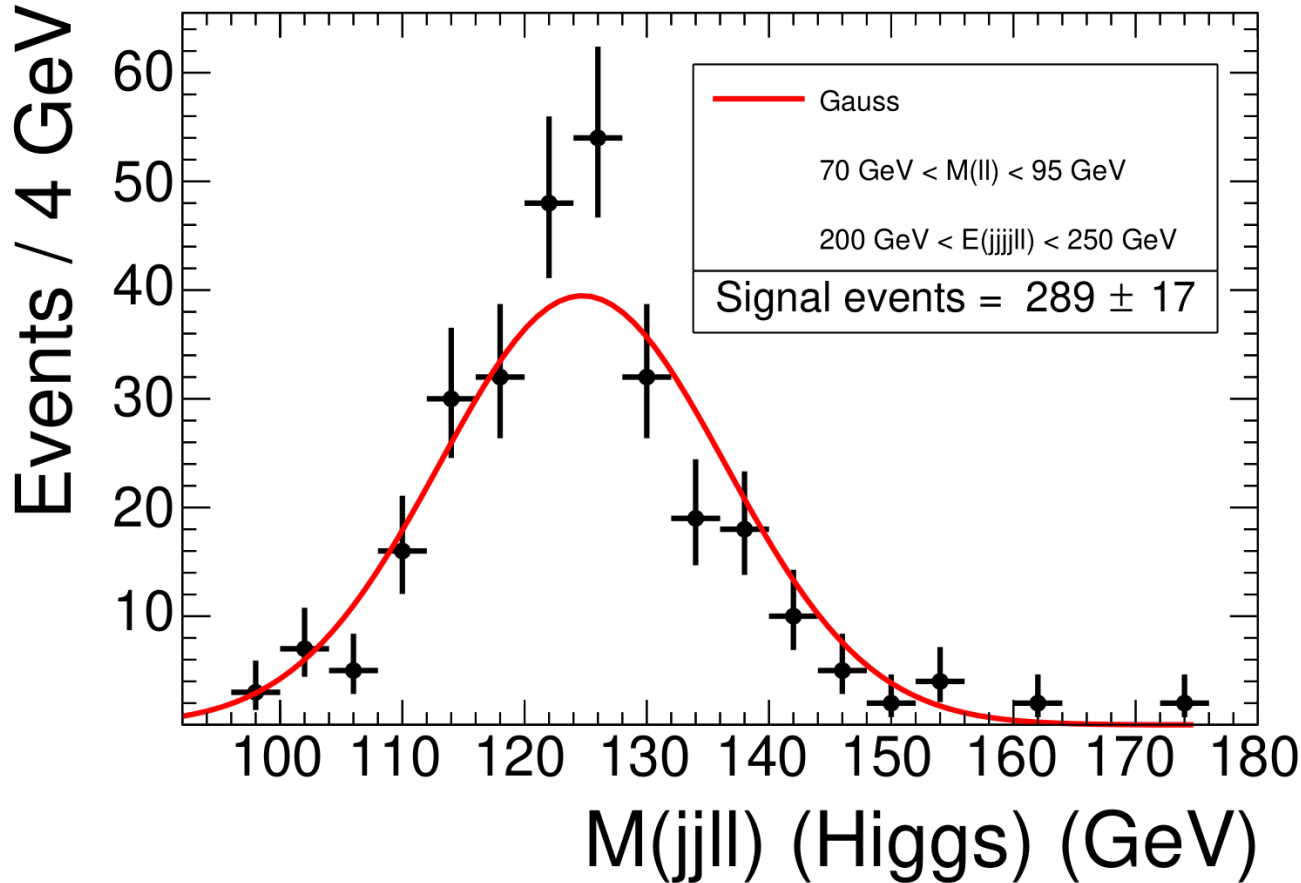
$$Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll$$



Mass difference method allows to obtain more narrow peak comparing to **direct mass reconstruction**

$$e^+ e^- \rightarrow Z_1 H(Z Z^*)$$

$$Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow jj$$



Signal is modelled by **Gaussian function**

Suppression of random **ll** backgrounds
and **Z*Z*** events using **M(ll)** and **E(jjjll)**
cuts

Gaussian $\sigma = 11.2$ GeV

$\sqrt{s} = 250$ GeV $\mathcal{L} = 2000$ fb⁻¹

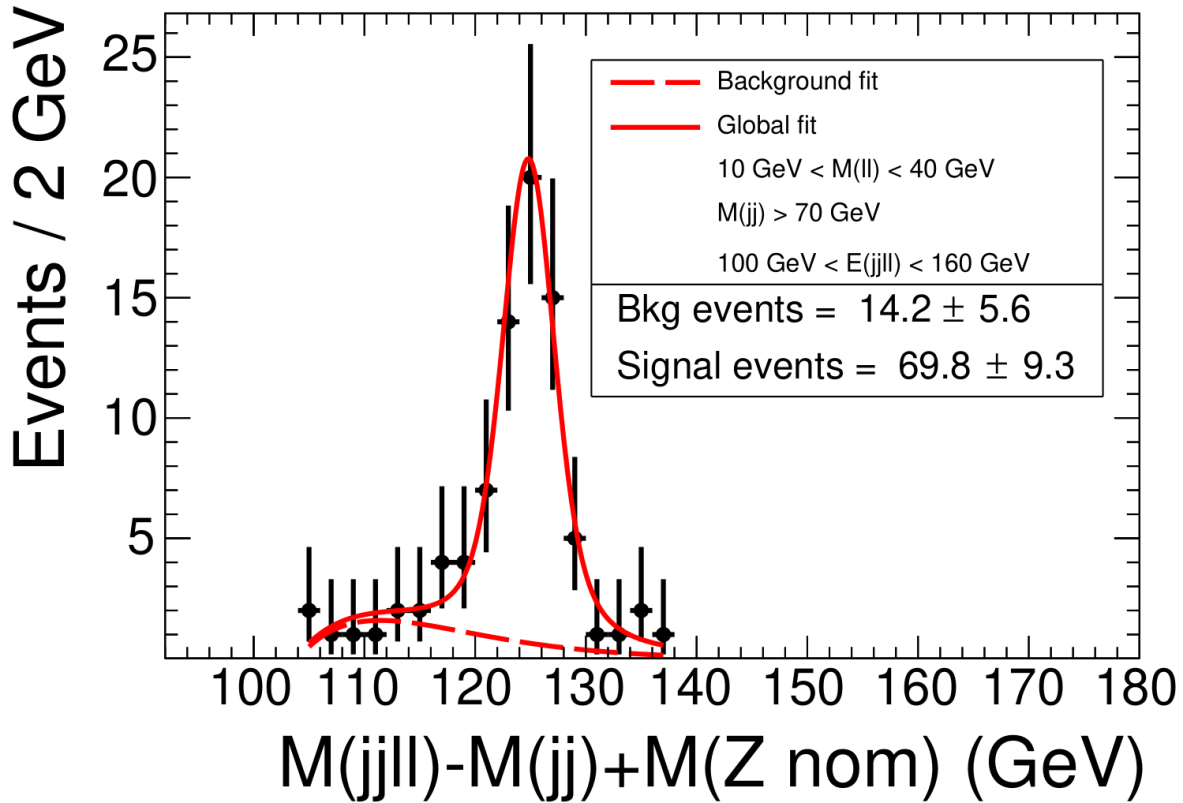
Statistical uncertainty = 5.9 %

$$e^+ e^- \rightarrow Z_1 H(Z Z^*)$$

$$Z_1 \rightarrow \nu\nu, Z \rightarrow jj, Z^* \rightarrow ll$$

$$\sqrt{s} = 250 \text{ GeV}$$

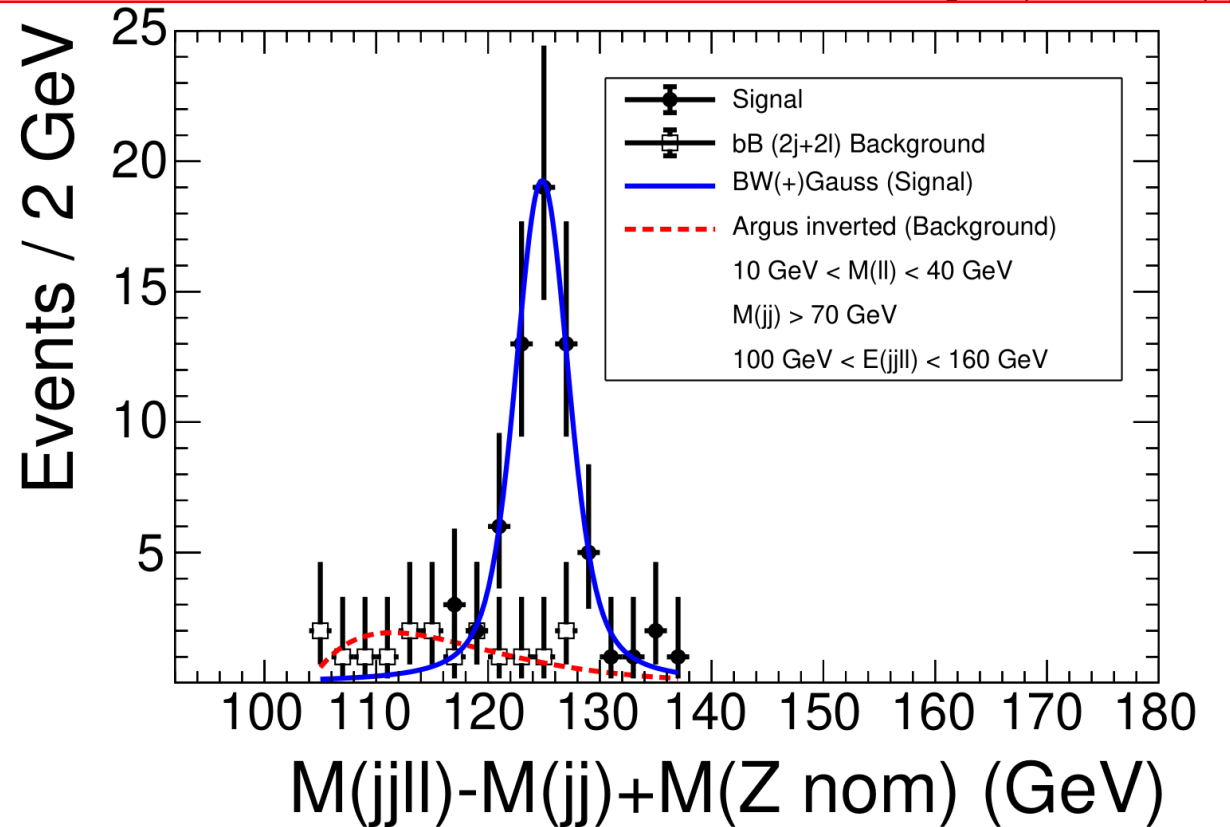
$$\mathcal{L} = 2000 \text{ fb}^{-1}$$



Fixed shapes, free normalizations in this fit

Statistical uncertainty = **13.5 %**

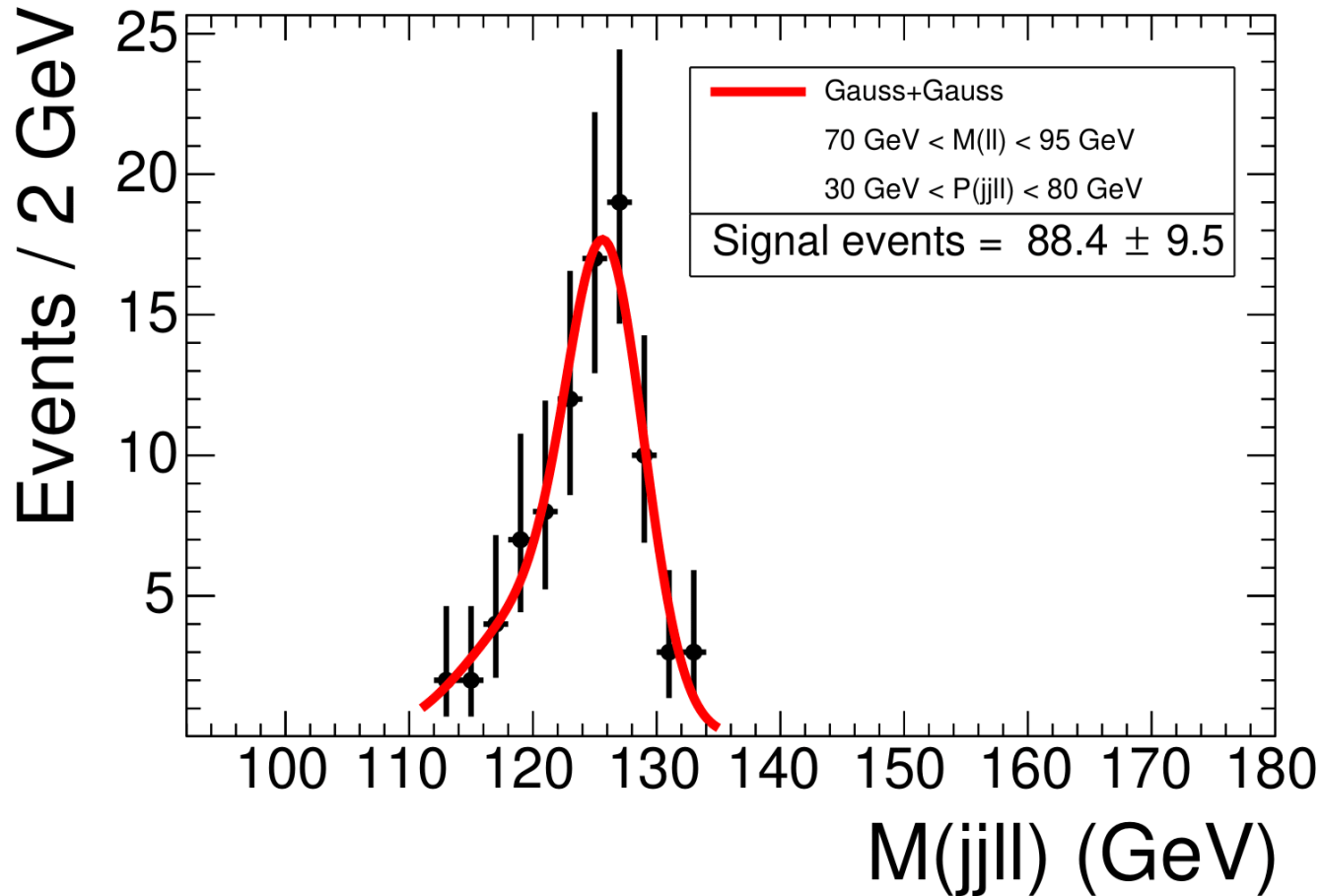
$$Argus_inverted(m, m_0, c, p) = N \cdot m \cdot \left[\left(\frac{m}{m_0} \right)^2 - 1 \right]^p \cdot \exp \left[c \cdot \left(\left(\frac{m}{m_0} \right)^2 - 1 \right) \right]$$



Signal is modelled by **Gaussian ⊕ BW** function
 Background is described by **Argus** function

$$e^+ e^- \rightarrow Z_1 H(Z Z^*)$$

$$Z_1 \rightarrow \nu\nu, Z \rightarrow ll, Z^* \rightarrow jj$$



Signal is modelled by **Gaussian+Gaussian** function

Small tail from Z^*Z^* events

Suppression of random ll backgrounds and Z^*Z^* events using $M(ll)$ and $P(jjll)$ cuts

Signal is narrow because there are only 2 jets in event: no wrong Z-jet matching, wrong particle-jet matching does not change results

$$\sqrt{s} = 250 \text{ GeV} \quad \mathcal{L} = 2000 \text{ fb}^{-1}$$

Statistical uncertainty = 10.7 %

Integrated significance of this method

We use this formula calculate **integrated statistical significance**:

$$Sign = \sqrt{\left(\frac{N_{ch\ 1}}{Err_{ch\ 1}}\right)^2 + \left(\frac{N_{ch\ 2}}{Err_{ch\ 2}}\right)^2 + \left(\frac{N_{ch\ 3}}{Err_{ch\ 3}}\right)^2 + \left(\frac{N_{ch\ 4}}{Err_{ch\ 4}}\right)^2}$$

$$Sign = \sqrt{\left(\frac{232}{26}\right)^2 + \left(\frac{289}{17}\right)^2 + \left(\frac{69.8}{9.3}\right)^2 + \left(\frac{88.4}{9.5}\right)^2}$$

Integrated statistical significance and uncertainty obtained:

$$Sign = 22.6 \sigma$$

$$Stat. Uncertainty = 4.4\%$$

Dominant systematic uncertainty is expected to come from description of background shapes. It is difficult to estimate this uncertainty precisely without real data. This uncertainty is expected to be smaller than statistical uncertainty. Systematics due to event selection efficiency and reconstruction efficiency should be small.

Conclusions

We studied $e^+e^- \rightarrow HZ$ process with subsequent $H \rightarrow ZZ^*$ decay. The analysis was performed assuming integrated luminosity 2000 fb^{-1} collected at e^+e^- collisions with center-of-mass energy 250 GeV.

4 channels were studied; corresponding signals and backgrounds are estimated using MC simulation.

Summing up results obtained in 4 studied channels we obtain statistical significance of this method = 22.6σ and statistical uncertainty = 4.4%.

Thank you for attention

ISR and overlay removing

$\gamma\gamma$ overlay removed using *kT jet clustering*

From arXiv:2009.04340:

ISR photon candidate is selected if its energy E_{photon} is *greater than 10 GeV*

All charged particles in a cone with $\cos \theta_{\text{cone}} = 0.95$ around the photon *are summed up.*

$E_{\text{sum}} < 5\% E_{\text{photon}}$ -> ISR photon

Jet reconstruction

Valencia algorithm is used to force the remaining particles *into 2 or 4 jets*.

It contains 3 parameters: R - generalized jet radius, γ and β - special capture parameters in beam distance

We use $\beta = 1$ and tune R and γ with this method *from arXiv:1607.05039*:

$$\Delta M(Z) = M_{reco}(Z) - M_{gen}(Z)$$

$$Median = Q(0.5)$$

Choosing combination of minimum of IQR34, RMS90 and close to 0 median

$$IQR_{34} = \frac{Q(0.84) - Q(0.16)}{2}$$

$$M_{mean} = \frac{\sum \Delta M(Z)}{N_{entries}}$$

$$RMS_{90} = \sqrt{(|M_{mean}^2 - M_{mean}|)}$$

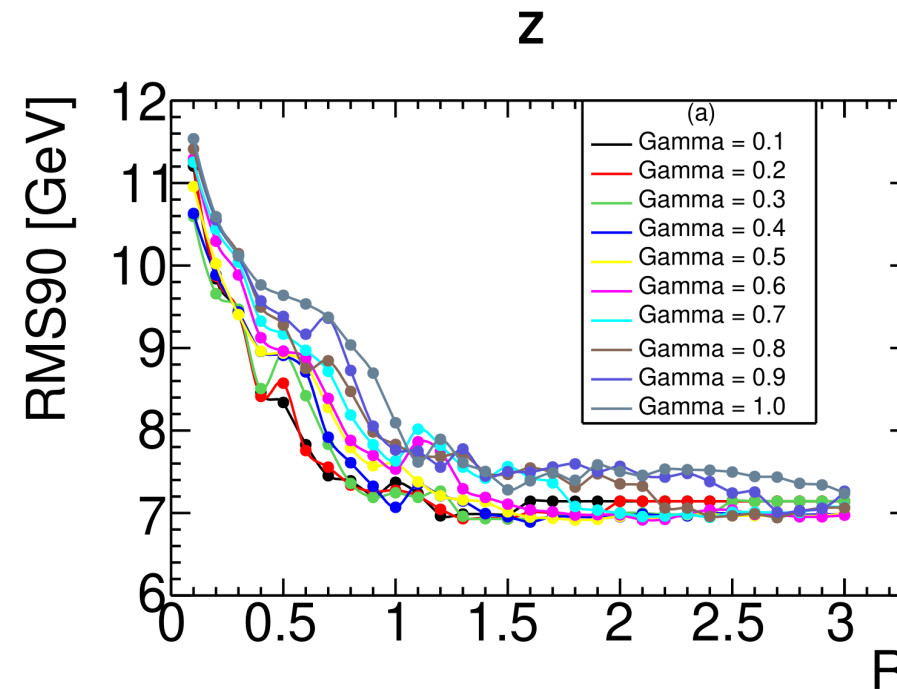
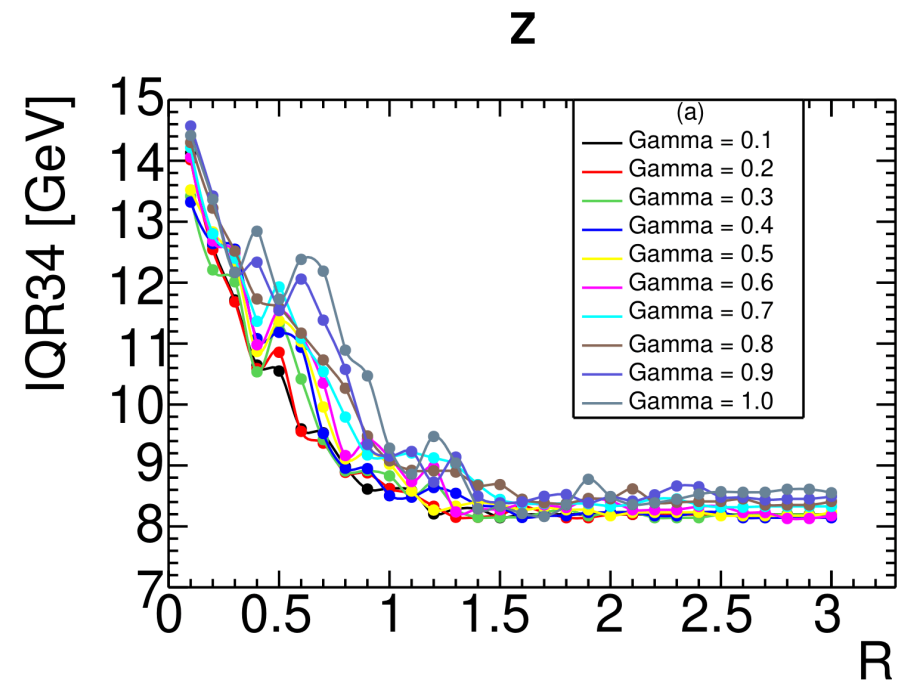
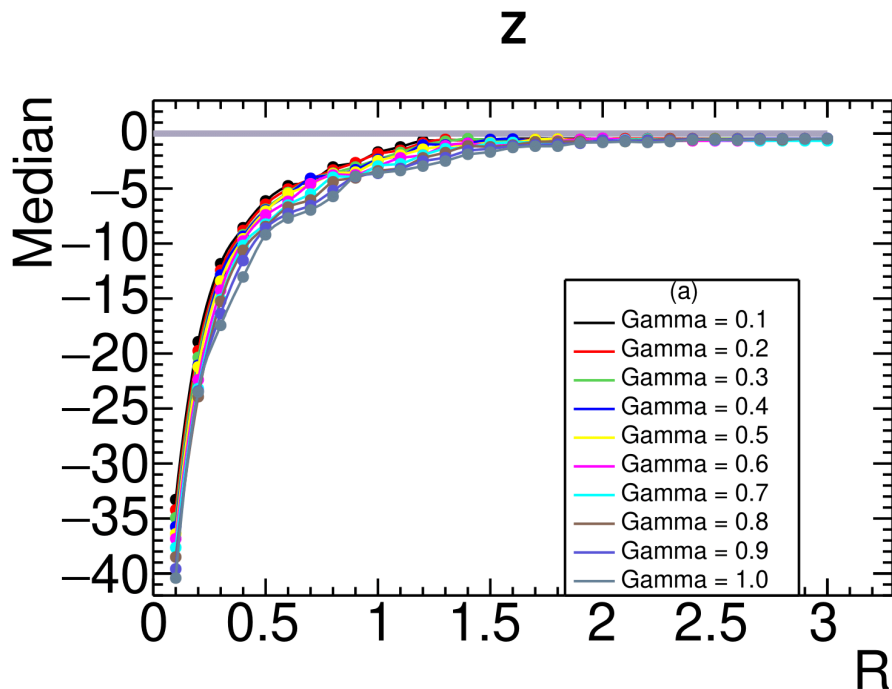
$$M_{mean}^2 = \frac{\sum (\Delta M(Z))^2}{N_{entries}}$$

Jet reconstruction

Example of tune for $Z(jj)$

$$Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll$$

$R[0.1, 3.0]$ and $\gamma[0.1, 1.0]$ ranges

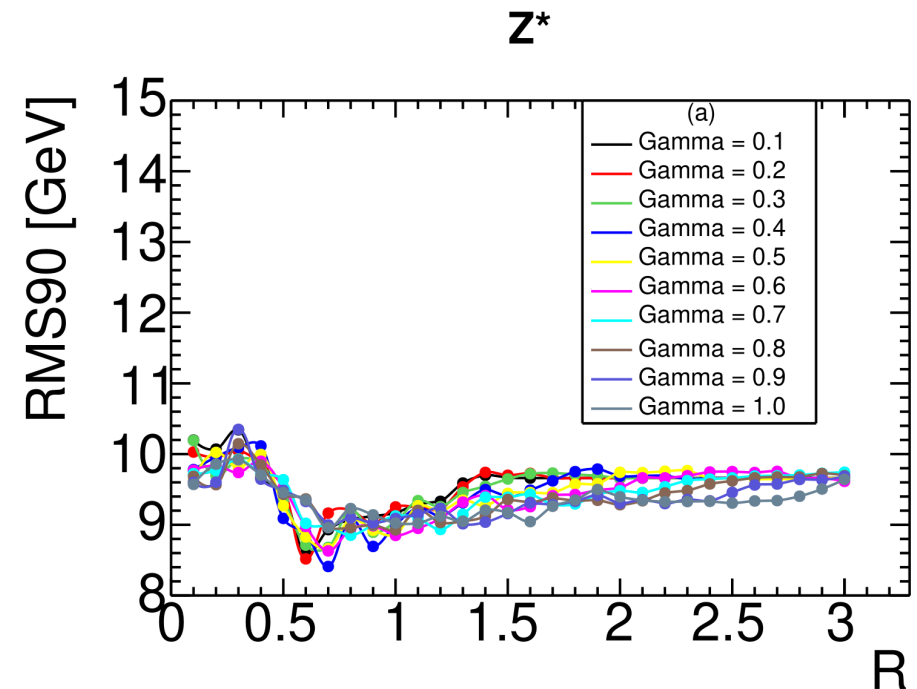
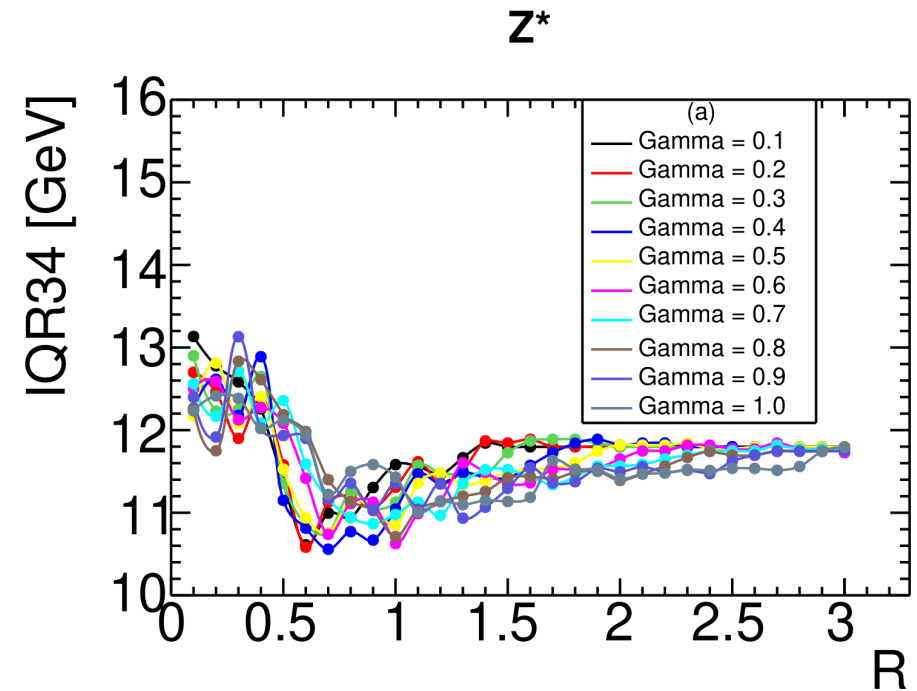
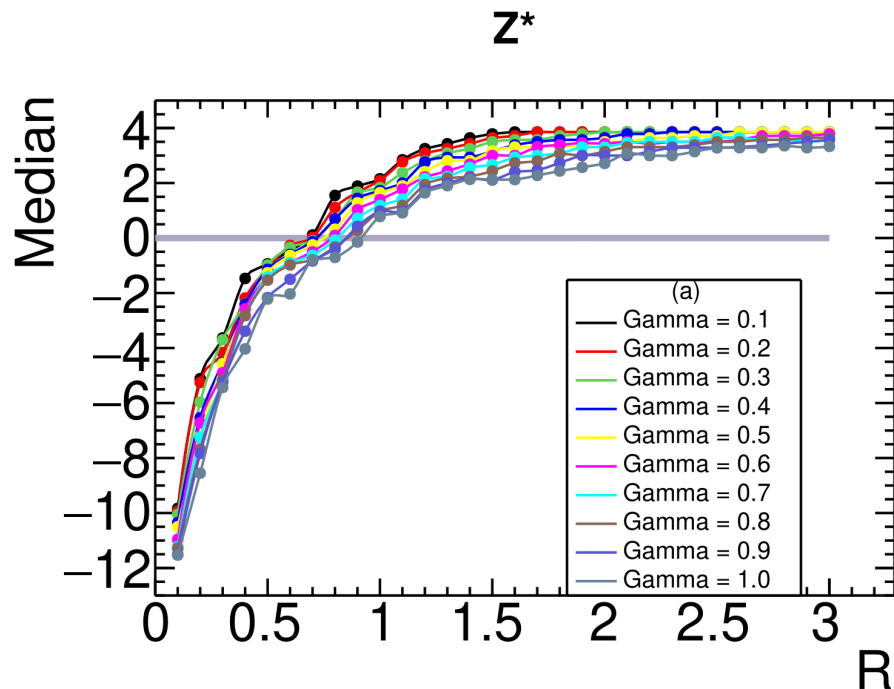


Jet reconstruction

Example of tune for $Z^*(jj)$

$Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow jj$

$R[0.1, 3.0]$ and $\gamma[0.1, 1.0]$ ranges



Jet reconstruction

Valencia algorithm parameters tuned for each sub-process:

$$Z_1 \rightarrow jj, Z \rightarrow jj, Z^* \rightarrow ll : \quad \beta = 1, \underline{\gamma = 0.4}, R = 1.6$$

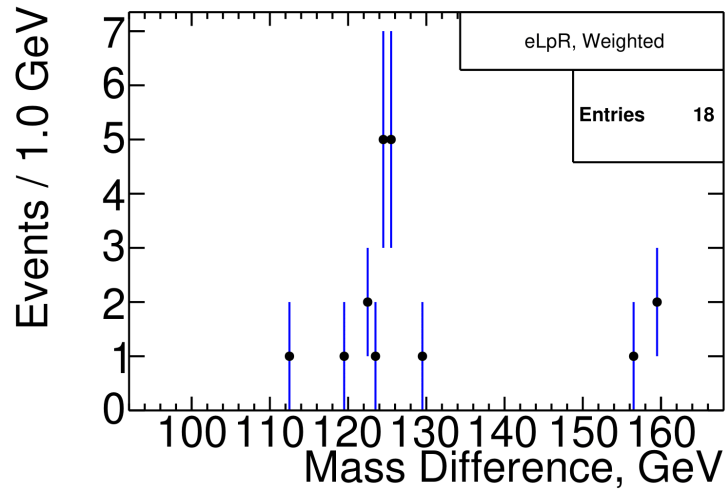
$$Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow jj : \quad \beta = 1, \underline{\gamma = 0.4}, R = 0.7$$

$$Z_1 \rightarrow \nu\nu, Z \rightarrow jj, Z^* \rightarrow ll : \quad \beta = 1, \underline{\gamma = 0.6}, R = 1.4$$

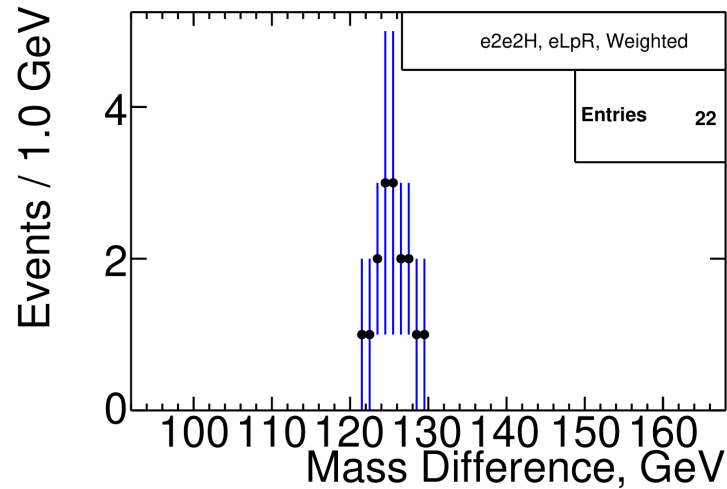
$$Z_1 \rightarrow \nu\nu, Z \rightarrow ll, Z^* \rightarrow jj : \quad \beta = 1, \underline{\gamma = 0.3}, R = 1.4$$

4 leptons channels

$$Z_1 \rightarrow jj, Z \rightarrow ll, Z^* \rightarrow ll$$



$$Z_1 \rightarrow ll, Z \rightarrow jj, Z^* \rightarrow ll$$



$$Z_1 \rightarrow ll, Z \rightarrow ll, Z^* \rightarrow jj$$

