

# Polarimetry and Spin Tracking at the ILC — a reminder on GDE work

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and Jenny List

DESY

LCWS, March 15-19, 2021

Introduction

Collision Data

Compton Polarimeters

Detector R&D

Spin Tracking

Conclusions

# Introduction

Collision Data

Compton Polarimeters

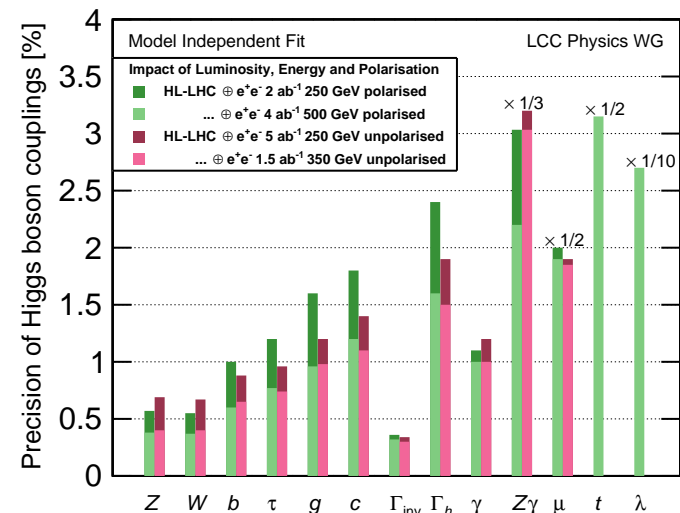
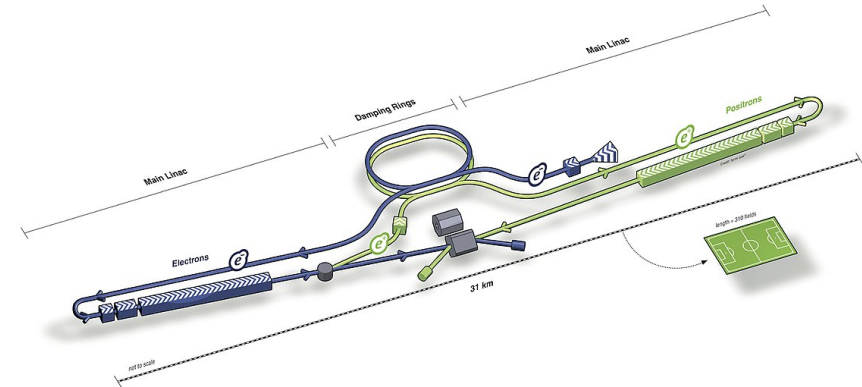
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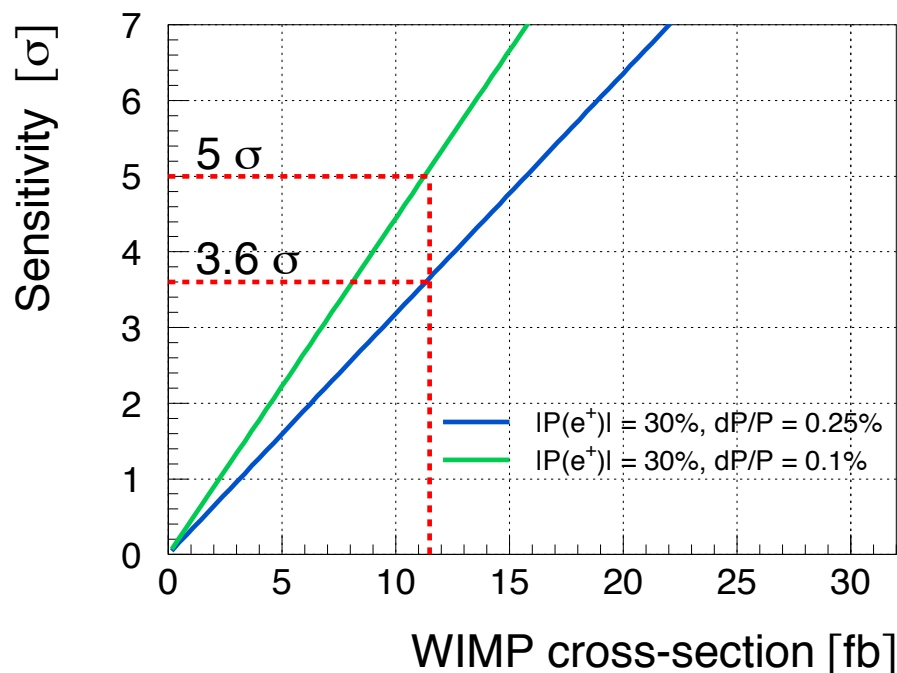
# The International Linear Collider.

- $e^+ e^-$  “Higgs factory” with  $\sqrt{s} = 250$  GeV, upgradable to up to 1 TeV
- *both* beams polarised:  
 $|P(e^-)| = 80\%$ ,  
 $|P(e^+)| = 30\% \dots 60\%$
- integral part of physics programme, for Higgs and beyond, c.f.  
<https://arxiv.org/abs/1801.02840>.
- construction under political consideration in Japan



# Impact of Polarisation Uncertainty.

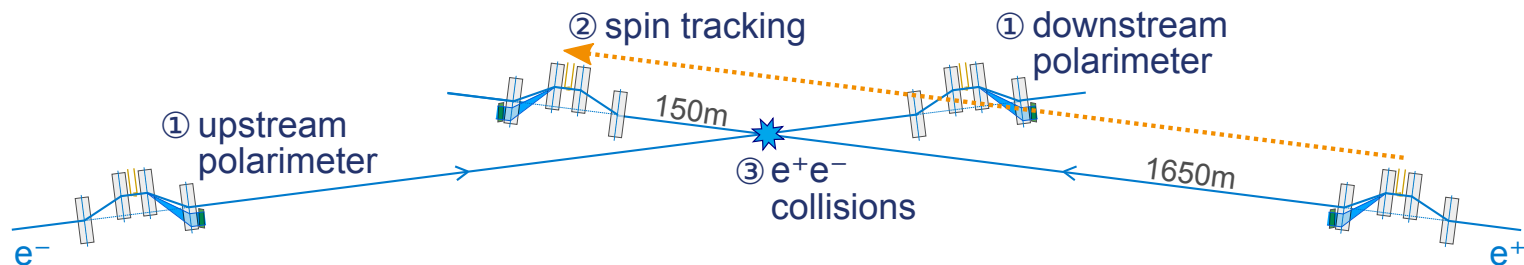
- SM precision measurements, eg.  $A_{LR}$  at  $Z$  pole will be limited by polarisation knowledge  
→ simultaneous extraction of  $A_{LR}$  and  $\langle P_{\text{eff}} \rangle_{IP}$
- BSM example: WIMP Dark Matter Search



- $500 \text{ fb}^{-1}$  at 500 GeV,  $|P(e^-, e^+)| = (0.8, 0.3)$
- ILD full simulation incl. systematics
- $dP/P = 0.25\%$   
→ “evidence for”
- $dP/P = 0.1\%$   
→ “discovery of”

# Polarimetry concept for the ILC.

Goal for ILC polarimetry: per-mille level precision on luminosity weighted average polarisation at the IP,  $\langle P_z \rangle_{IP} = \frac{\int P_z(t) \mathcal{L}(t) dt}{\int \mathcal{L}(t) dt}$



- ① Compton polarimeter measurements upstream and downstream of the  $e^+e^-$  interaction point
- ② Spin tracking to relate these measurements to the polarization at the  $e^+e^-$  interaction point
- ③ Long-term average determined from  $e^+e^-$  collision data as absolute scale calibration

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# Polarisation Average from Collision Data.

## Direct extraction from collision data

- any abundant, well-known, polarisation dependent process
- total cross-sections only (aka “(modified) Blondel scheme”):  
 $P_+(e^-) = -P_-(e^-)$  and  $P_+(e^+) = -P_-(e^+)$
- to lift condition: differential cross-sections *and* polarimeter constraints.

## Methods studied so far

- total cross-sections:  $WW$  at 500 GeV and 1 TeV (ILD)  
 single  $W$  etc at 3 TeV (CLIC)
- single-differential cross-sections:  $WW$  at 500 GeV & 1 TeV (ILD)
- double-differential cross-sections:  $WW$  at 1 TeV (SiD)
- **NEW:** global fit incl. differential cross-sections for all  
 $e^+e^- \rightarrow f\bar{f}$  and  $e^+e^- \rightarrow f\bar{f}'f''\bar{f}'''$  processes → talk by J.Beyer

<https://indico.cern.ch/event/995633/contributions/4261076/>





# Fast helicity reversal.

... for both beams:

- collect data for all helicity configurations **simultaneously**
- ensures similar polarisation (absolute) values for all data sets
- enables cancellation of time dependent effects / systematic uncertainties for collider detector!

Counter example HERA:

- **slow** helicity reversal:  
weeks between flips
- differences in  $\langle P_e \rangle_{IP}$ :  
rely on polarimeters
- uncertainty  $\sim 2\%$

Collisions	$P_e[\%]$	$\mathcal{L}[\text{pb}^{-1}]$
$e^+ p$	+32	98
$e^+ p$	-38	82
$e^- p$	+37	46
$e^- p$	-26	103

Phys. Lett. B704 (2011) 388 [arxiv:1107.3716] (H1 Leptoquarks)

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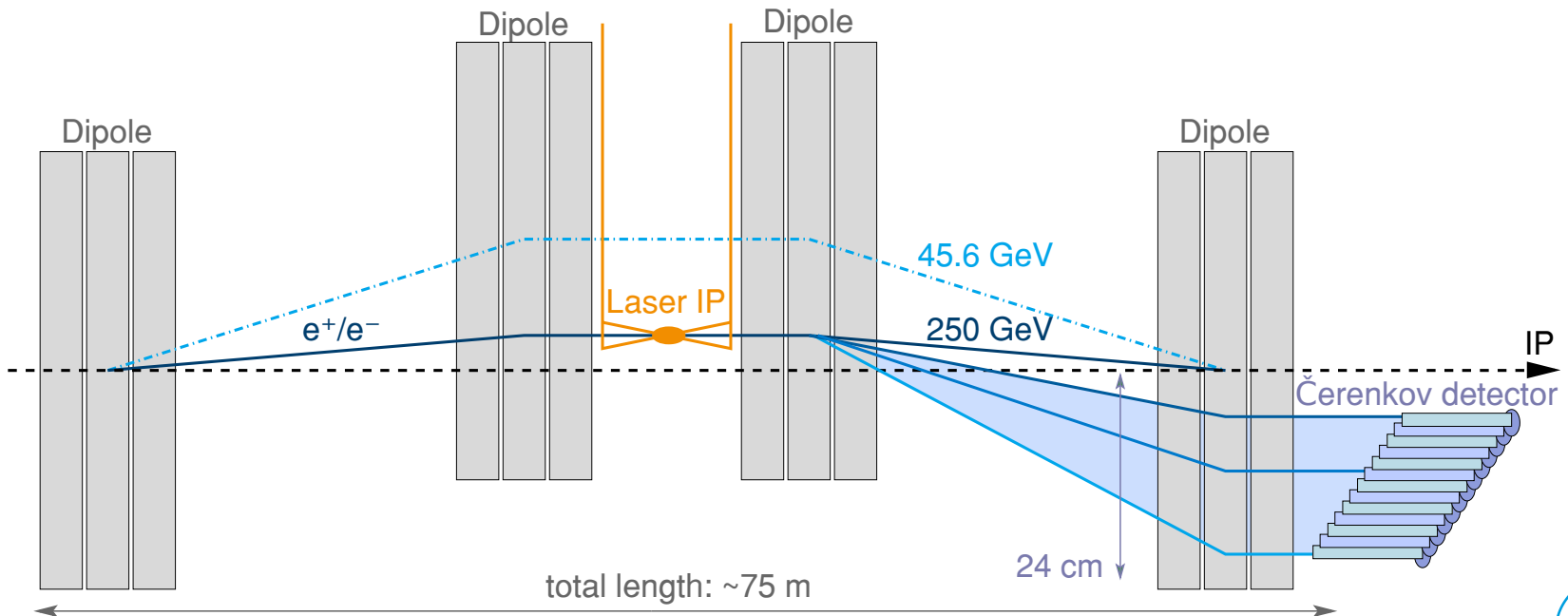
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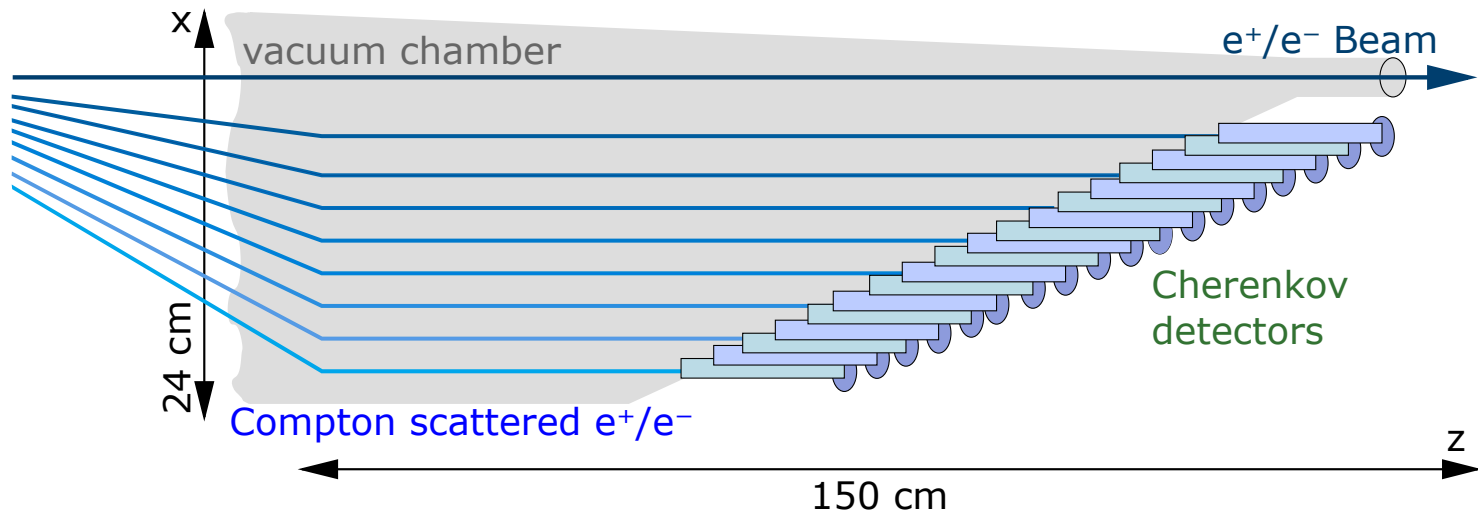
# Compton polarimetry.

- fast measurement:  $\mathcal{O}(10^3)$  Compton scatterings/bunch
- Energy spectrum of scattered  $e^+/e^-$  depends on product of lepton ( $\mathcal{P}$ ) and laser ( $\lambda$ ) polarisations
- Magnetic chicane: energy distribution  $\rightarrow$  position distribution
- Measure number of  $e^+/e^-$  per detector channel



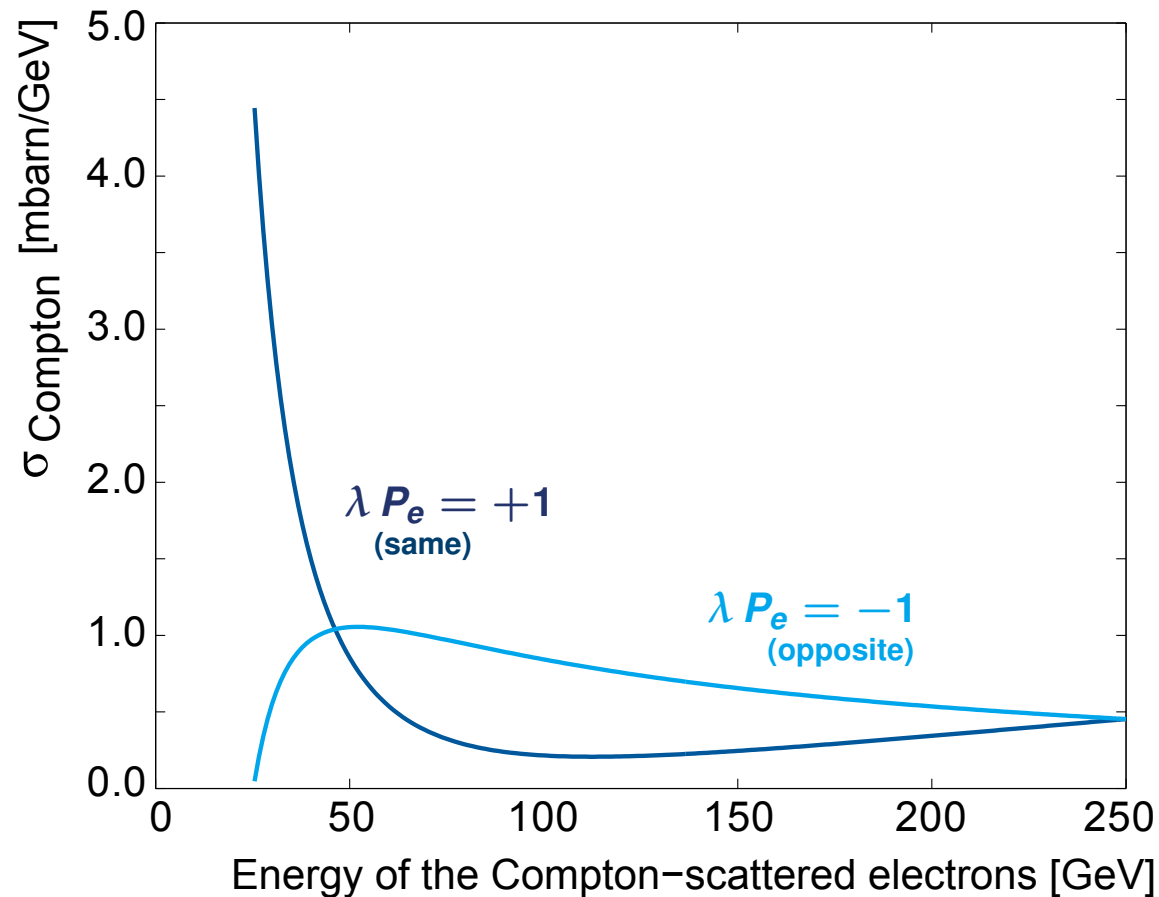
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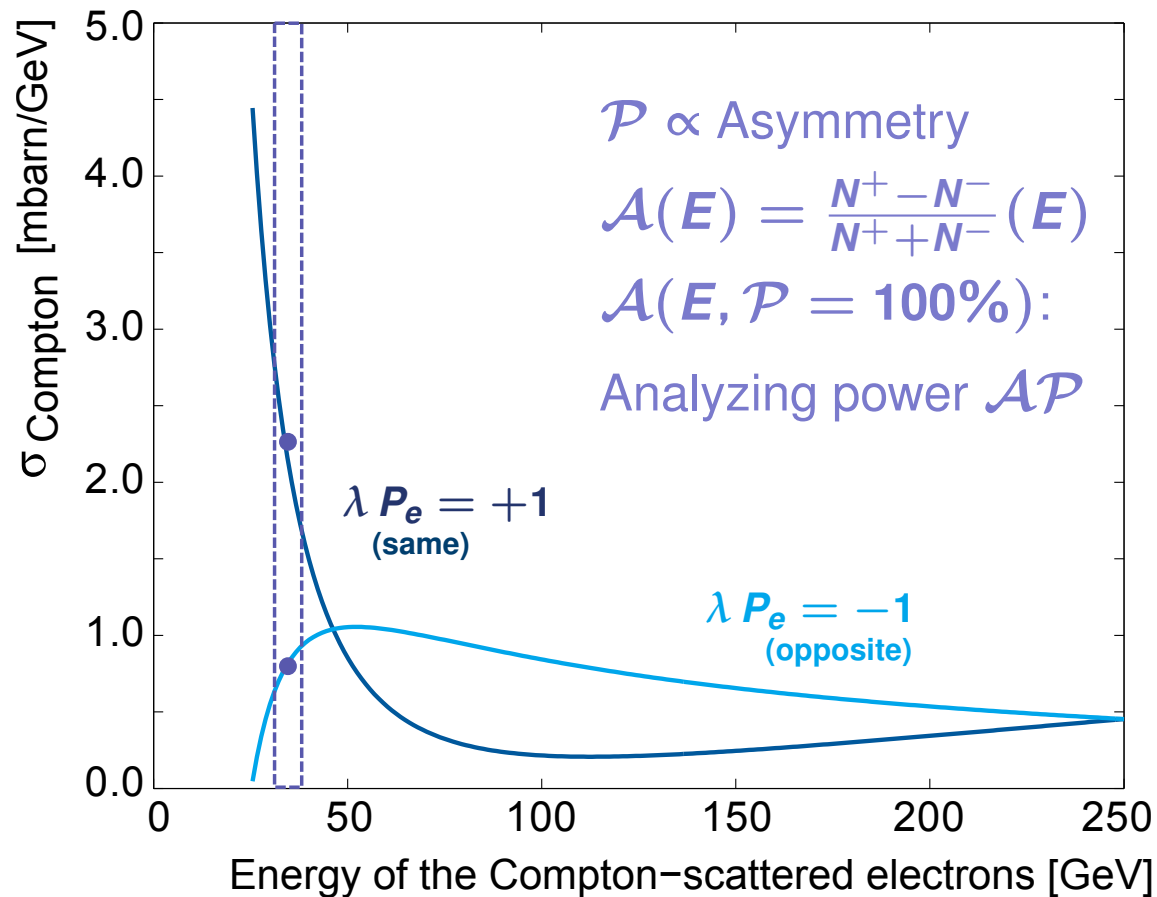
# Measurement Principle.

Compton rate asymmetry is proportional to the beam polarisation:



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# Measurement Precision.

ILC Goal: total uncertainty  $\delta P / P \approx 0.25\%$  for  $|P| \simeq 80\%$

source of uncertainty	$\delta P / P$	
	SLC achieved	ILC goals
laser polarisation	0.1%	0.1%
analyzing power	0.4%	0.15% – 0.2%
detector linearity	0.2%	0.1%
electronic noise and beam jitter	0.2%	0.05%
Total	0.5%	0.25%

- **analysing power:** prediction of count rate asymmetry per detector channel  
 ⇒ knowledge of beam parameters, design of chicane, beam-detector alignment, backgrounds
- **detector linearity, electronic noise:**  
 ⇒ detector design & calibration
- **beam jitter:** much smaller at ILC due to luminosity requirements

# Complementarity of Up- and Downstream.

## Upstream Polarimeter

- 1.8 km upstream of IP
- rather clean environment
- begin beam cond.
- samples every bunch
- stat. error 1% after few  $\mu\text{s}$
- reference for control of collision effects

## Downstream Polarimeter

- 140 m downstream of IP
- high backgrounds
- disrupted beam
- samples one bunch / train
- stat. error 1% after  $\simeq 1$  min
- access to depolarisation in collision

## Combination

- without collisions: spin transport in Beam Delivery System and Extraction Line
- with collisions: depolarisation at IP
- **cross check each other!**

[c.f. "Spin Dance" Exp., Phys. Rev. ST Accel. Beams **7** 042802 (2004)]



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# Detector Requirements.

## Magnetic Chicane...

- transforms energy spectrum into spatial distribution
- behind chicane:  $\sim 20$  cm wide
- detect Compton electrons over this area

## Detector requirements:

- Total ionising dose up to 100 Mrad / year
- read out signals of 1000-2000 Compton electrons (25-250 GeV) **every** bunch crossing
- either very linear response or “counting” electrons
- alignment to  $\sim 100$   $\mu\text{m}$  and  $\sim 1$  mrad
- suppression of background from low energetic particles

# Detector Options.

## Simple, robust, fast: Cherenkov detectors

- Cherenkov light emission proportional to number of electrons
- independent of electron energy (once relativistic)
- successfully used in best polarimeter sofar at SLC
- gas or quartz option for Cherenkov medium

# Detector Options.

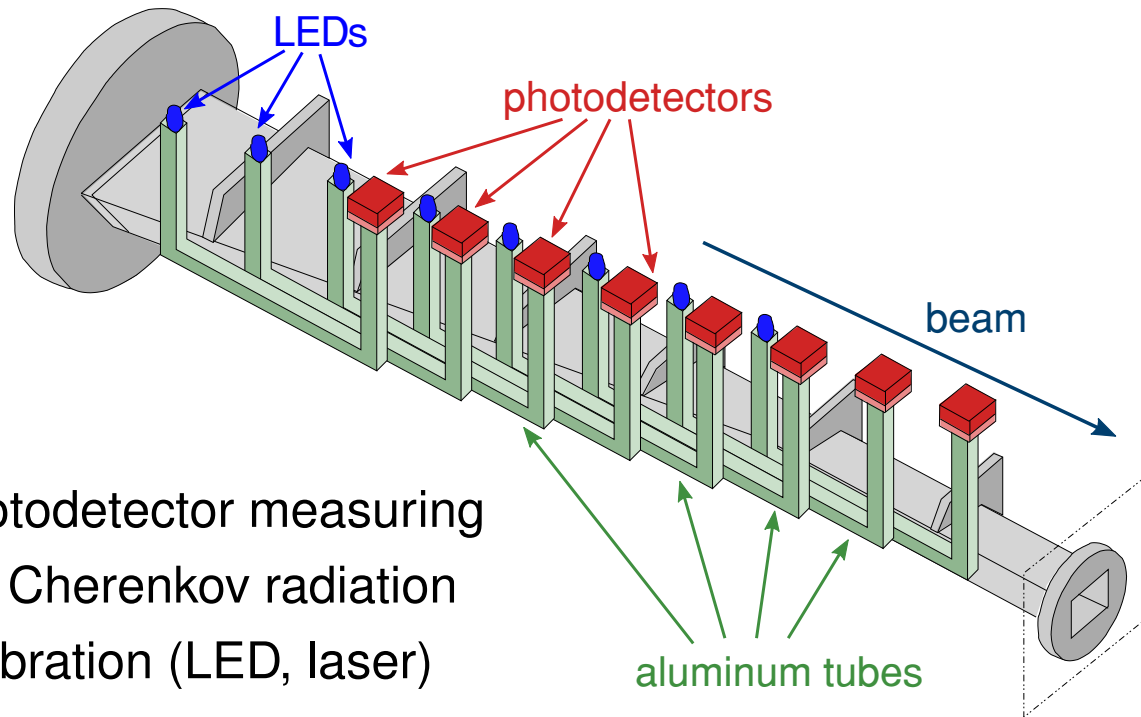
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## Goal: total uncertainty $\Delta P / P \approx 0.25 \%$ , of which

- laser: 0.1 %
- analysing power (i.e. asymmetry at  $\mathcal{P} = 1$ ): 0.2 %  
⇒ e.g. alignment
- detector linearity: 0.1 % ⇒ photodetector calibration

# Gas Cherenkov detector.



- **hind U-leg:** photodetector measuring the Cherenkov radiation
- **front U-leg:** calibration (LED, laser)

Alignment: locate Compton edge in the spectrometer

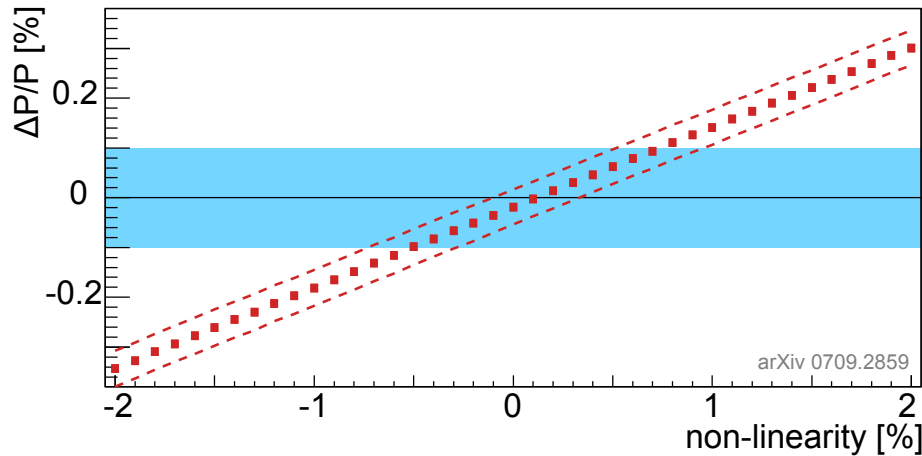
Segmented photodetectors: Tilt alignments via asymmetries

2-channel prototype tested at ELSA [JINST 7, P01019 (2012)]

⇒ tilt alignment of  $0.1^\circ$ , nearly fulfils alignment requirements

# Calibration of detector non-linearity.

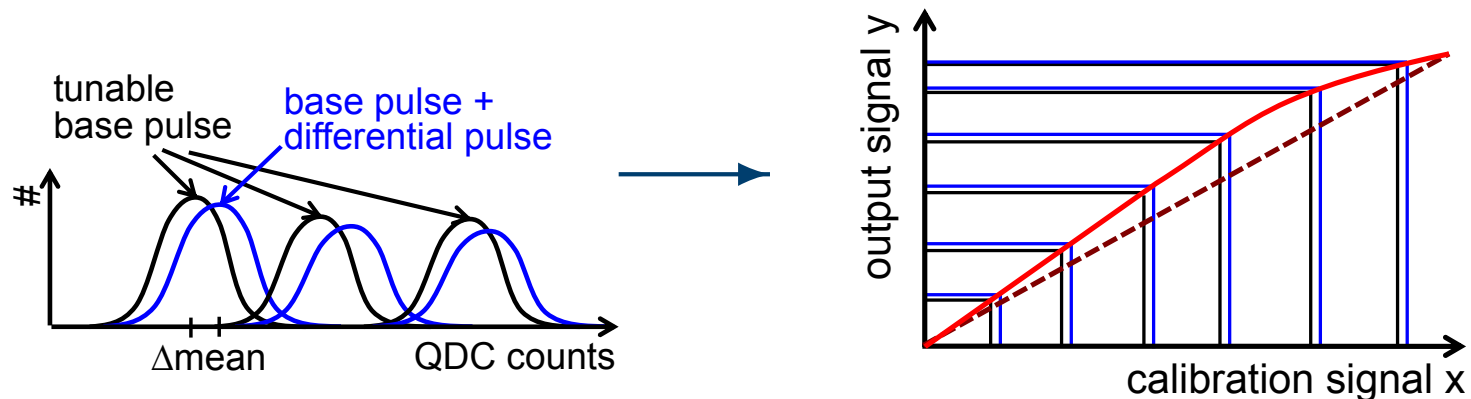
Goal: contribution to overall uncertainty  $< 0.1\%$



PMTs have to be calibrated to non-linearity  $< 0.5\%$ .

$\mathcal{P} \propto \frac{N^+ - N^-}{N^+ + N^-}$ : no absolute calibration needed.

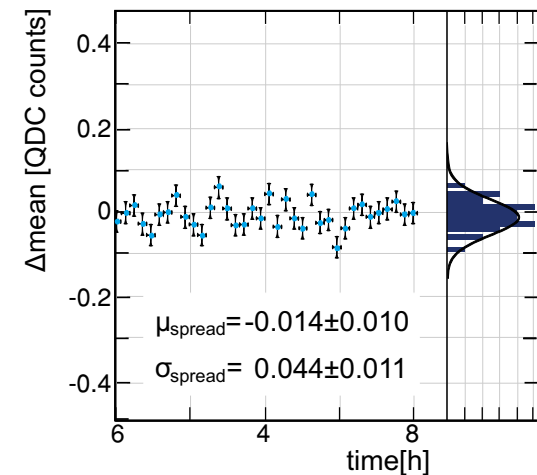
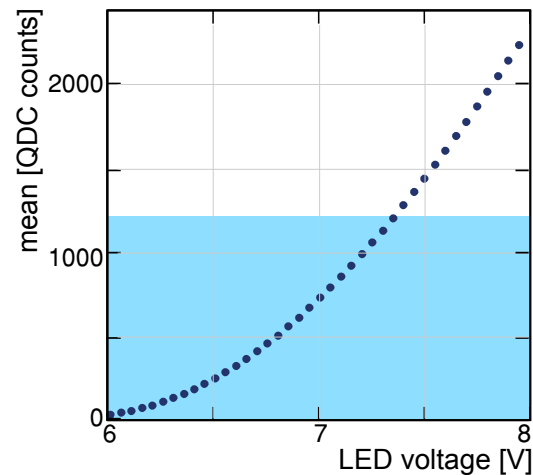
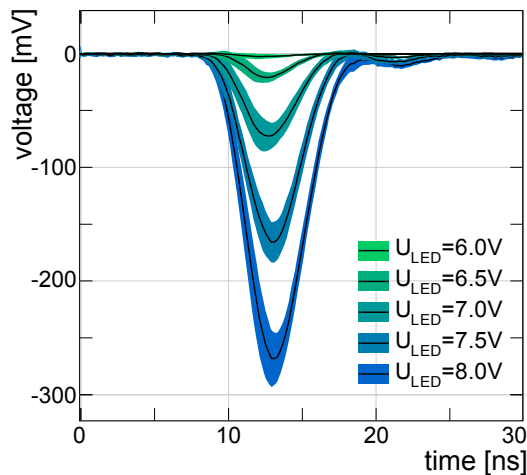
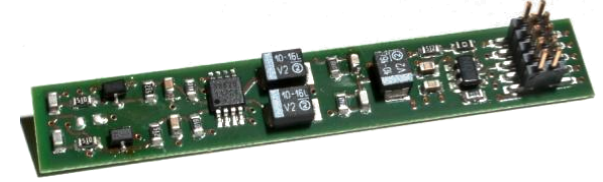
→ Differential calibration method using two LEDs:



# Calibration source requirements.

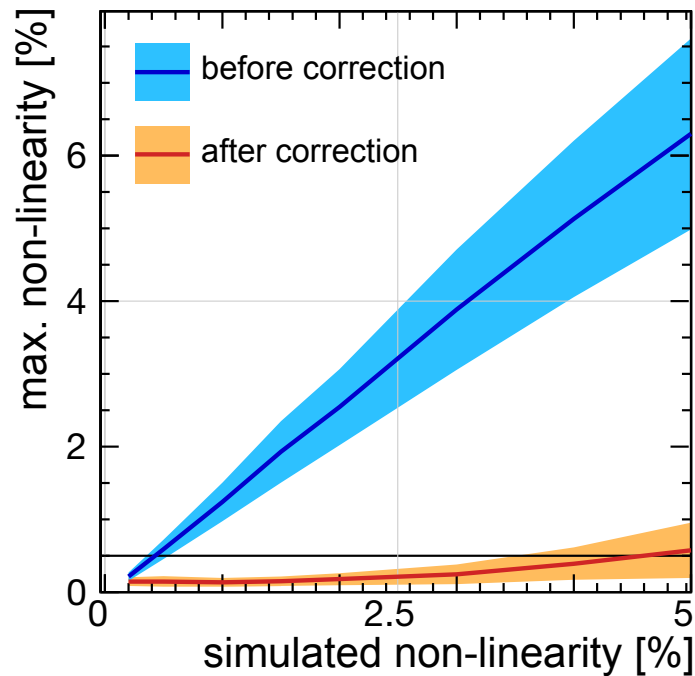
Requirements on the LED driver:

- wave length in UV range ( $\lambda = 405 \text{ nm}$ )
- applicable in detector design  $\rightarrow$  small
- short light pulses ( $< 10 \text{ ns}$ )
- coverage of the whole dynamic range of the expected signal
- reproducible and stable light pulses



# Test of non-linearity correction.

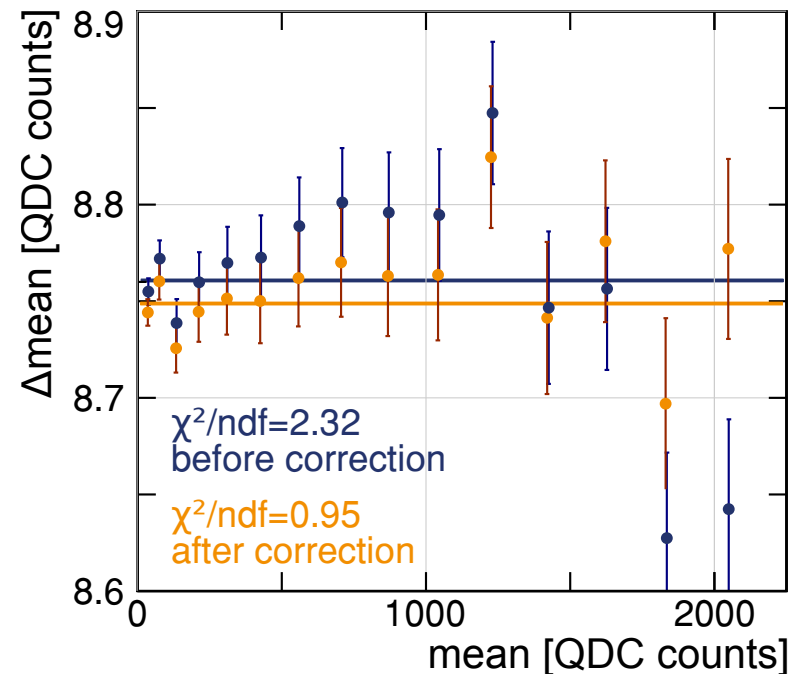
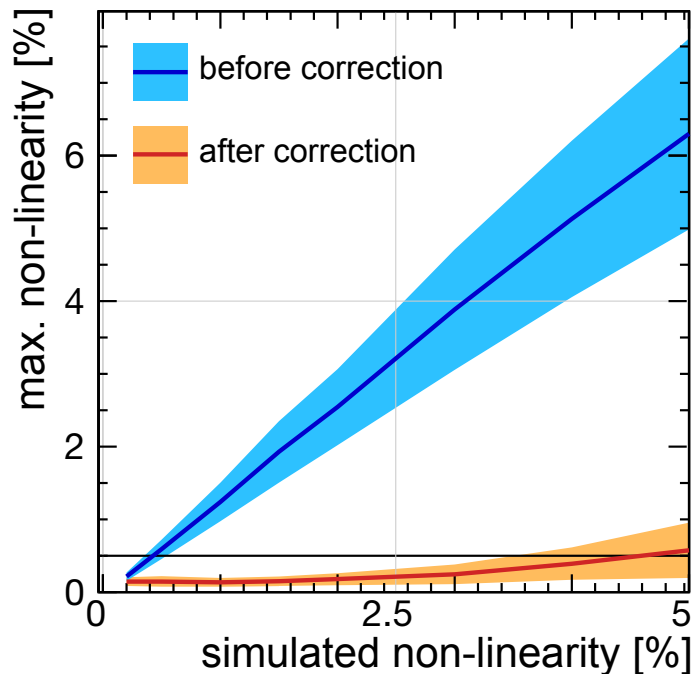
Simulations: Corrections of non-linearities up to 4 % possible.





# Test of non-linearity correction.

Simulations: Corrections of non-linearities up to 4 % possible.  
Applied method to one of the photodetectors used in testbeam:



⇒ Reached non-linearity  $< 0.2\%$  in the expected dynamic range, in single polarimeter channels even smaller.

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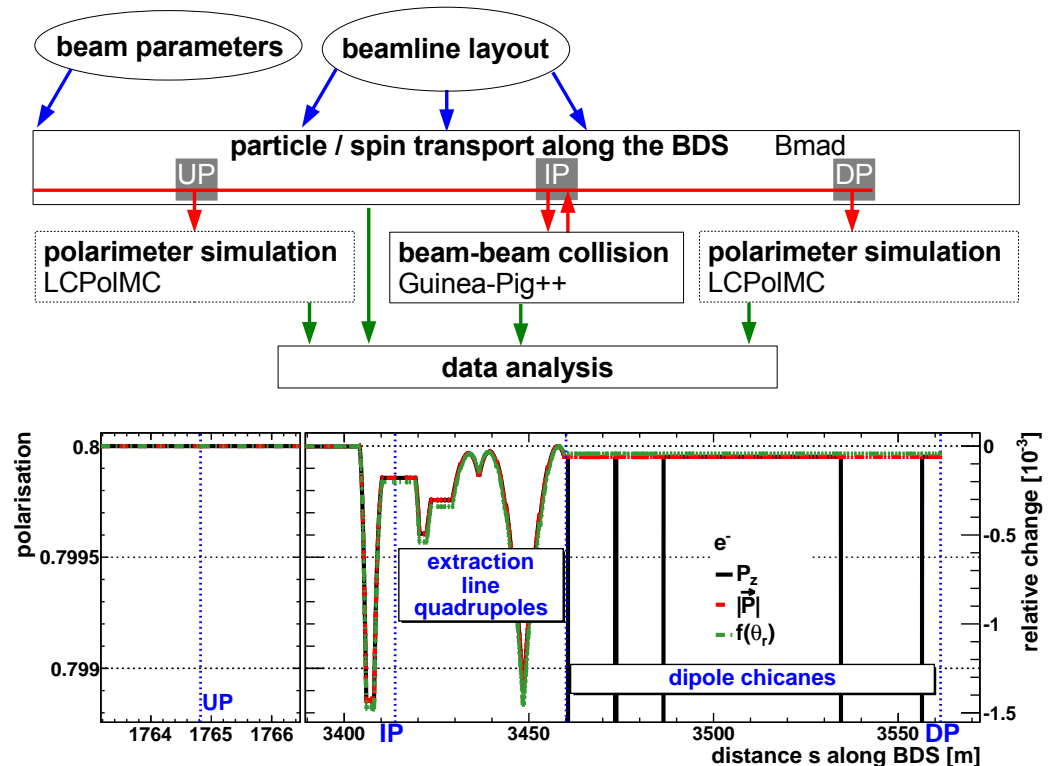
Conclusions

# Spin Tracking in BDS and Extraction Line.

Based on SB2009-Nov10  
lattice (PhD Thesis  
M.Beckmann)

- developed simulation framework STaLC
- without collisions  
⇒ cross-calibration of polarimeters
- with collisions  
⇒ what does the downstream polarimeter measure?

## Spin Transport At Linear Colliders



# Cross-calibration of Polarimeters.

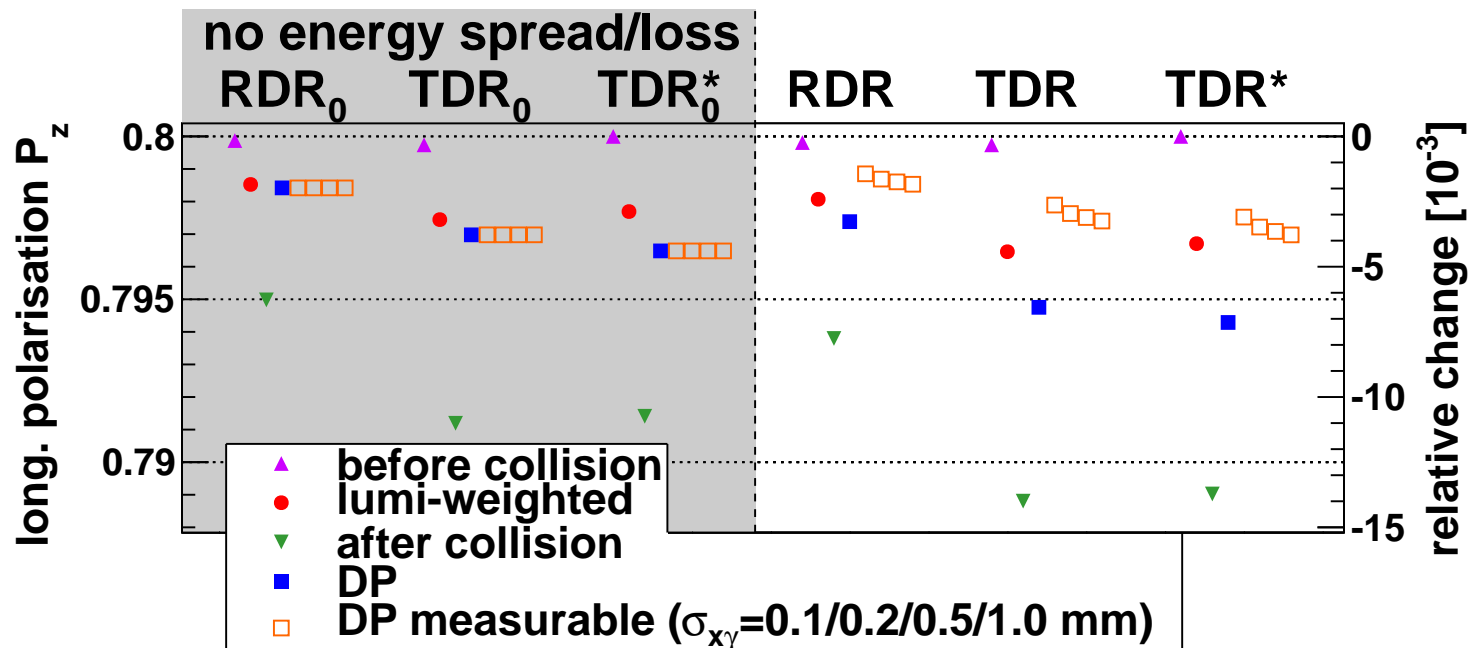
Without Collisions:

predict value at downstream location from upstream measurement

	effect on $P[10^{-3}]$
Beam and detector alignment at polarimeters ( $\Delta\theta_{bunch} = 50 \mu\text{rad}$ , $\Delta\theta_{pol} = 25 \mu\text{rad}$ )	0.72
Variation in emittances	0.03
Crabbing	< 0.01
Detector magnets	0.01
Emission of synchrotron rad.	0.005
random misalignments (10 $\mu\text{m}$ )	0.35
<b>Total</b>	<b>0.80</b>

# Collision Effects & Downstream Polarimeter.

- Extraction line optics designed to retrieve  $\langle P \rangle_{IP}$  at downstream polarimeter
- Confirmed by STaLC w/o beamstrahlung (energy loss, grey background)
- **With beamstrahlung**: few permille difference to  $\langle P \rangle_{IP}$
- **Measured polarisation depends on laser spot size** (here: perfect centering!)
- **Effect doubles from RDR  $\rightarrow$  TDR parameters**



# Conclusions Spin Tracking.

In the presence of significant Beamstrahlung:

- Downstream polarimeter does *not* measure directly any more  $\langle P \rangle_{IP}$
- difference DP measurement vs  $\langle P \rangle_{IP}$  depends on
  - laser spot size & position
  - luminosity ( $\simeq$  energy loss in collision)
- $\Rightarrow$  correcting for this requires
  - absolute reference from upstream polarimeter
  - luminosity & beam parameter monitoring
  - long-term scale of  $\langle P \rangle_{IP}$  from collision data

**TODO: spin tracking for up to date 250 GeV parameters**

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# Conclusions.

Per mille-level precision on lumi-weighted average polarisation at IP required by physics, needs combination of

- long-term scale calibration from  $e^+ e^-$  collision data (fast helicity reversal!)
- upstream (UP) and downstream (DP) polarimeters
  - **UP**: time resolution, absolute reference
  - **DP**: collision effects
  - **combined**: cross-calibration, lumi-weighted polarisation @ IP
- spin tracking and understanding of collision effects

## Compton Polarimeters:

- beam-detector alignment & detector linearity crucial
- R&D well underway, requirements  $\simeq$  reached in prototypes
- cross-calibration without collisions:  $\sim 0.1\%$  from alignment
  - esp. orbit and spin at UP and DP locations (2 km apart)



# More Details.

## ➤ E&P workshop Zeuthen 2008

<http://indico.desy.de/conferenceDisplay.py?confId=585>

## ➤ its Executive Summary

arXiv:0903.2959 [physics.acc-ph]

## ➤ downstream polarimeter 6-magnet chicane

<http://www.slac.stanford.edu/cgi-wrap/getdoc/slac-pub-12425.pdf>

## ➤ publication on beam energy and polarisation measurements

JINST **4** (2009) P10015, arXiv:0904.0122 [physics.ins-det]

## ➤ publications on polarimeter detector R&D:

JINST **7** (2012) P01019, arXiv:1011.6314 [physics.ins-det]

JINST **10** (2015) 05, P05014, arXiv:1502.06955 [physics.ins-det]

JINST **11** (2016) 01, P01014, arXiv:1509.03178 [physics.ins-det]

## ➤ publication on BDS spin tracking

JINST **9** (2014) P07003, arXiv:1405.2156 [physics.acc-ph]

**Backup Slides .**

# For historic information: Recommendations to GDE and Research Director (2008).

- Separate the functions of the upstream polarimeter chicane. Do not include an MPS energy collimator or laser-wire emittance diagnostics; use instead a separate setup for these two.
- Modify the extraction line polarimeter chicane from a 4-magnet chicane to a 6-magnet chicane to allow the Compton electrons to be deflected further from the disrupted beam line.
- Include precise polarisation and beam energy measurements for **Z**-pole calibration runs into the baseline configuration.
- Keep an initial positron polarisation of 30-45% for physics, don't reduce to 22% .
- Implement parallel spin rotator beamlines with a kicker system before the damping ring to provide rapid helicity flipping of the positron spin.
- Move the pre-DR positron spin rotator system from 5 GeV to 400 MeV. This eliminates expensive superconducting magnets and reduces costs.
- Move the pre-DR electron spin rotator system to the source area. This eliminates expensive superconducting magnets and reduces costs.

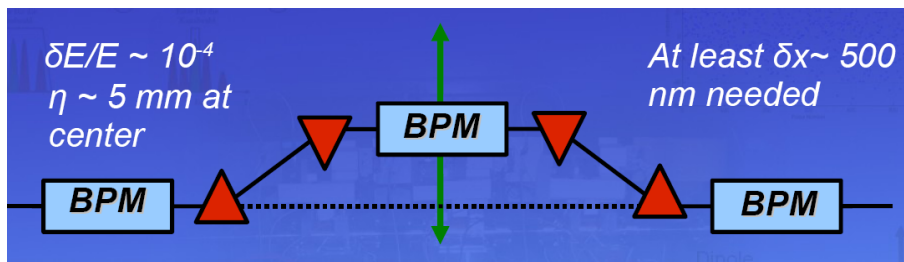


# The Baseline Energy Spectrometers.

Upstream:

Chicane + BPMs

- ▶ 700 m upstream of IP
- ▶ measure beam position in chicane
- ▶ prototype at Endstation A at SLAC
- ▶ resolutions of  $\simeq 1 \mu\text{m}$  achieved

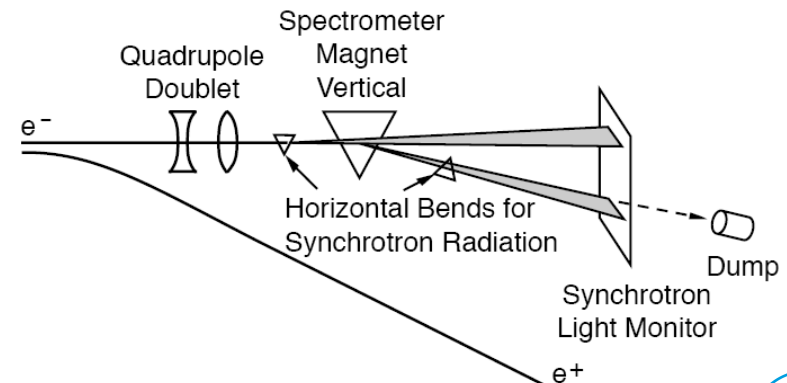


...+ collision data!

Downstream:

Synchrotron Radiation Imaging

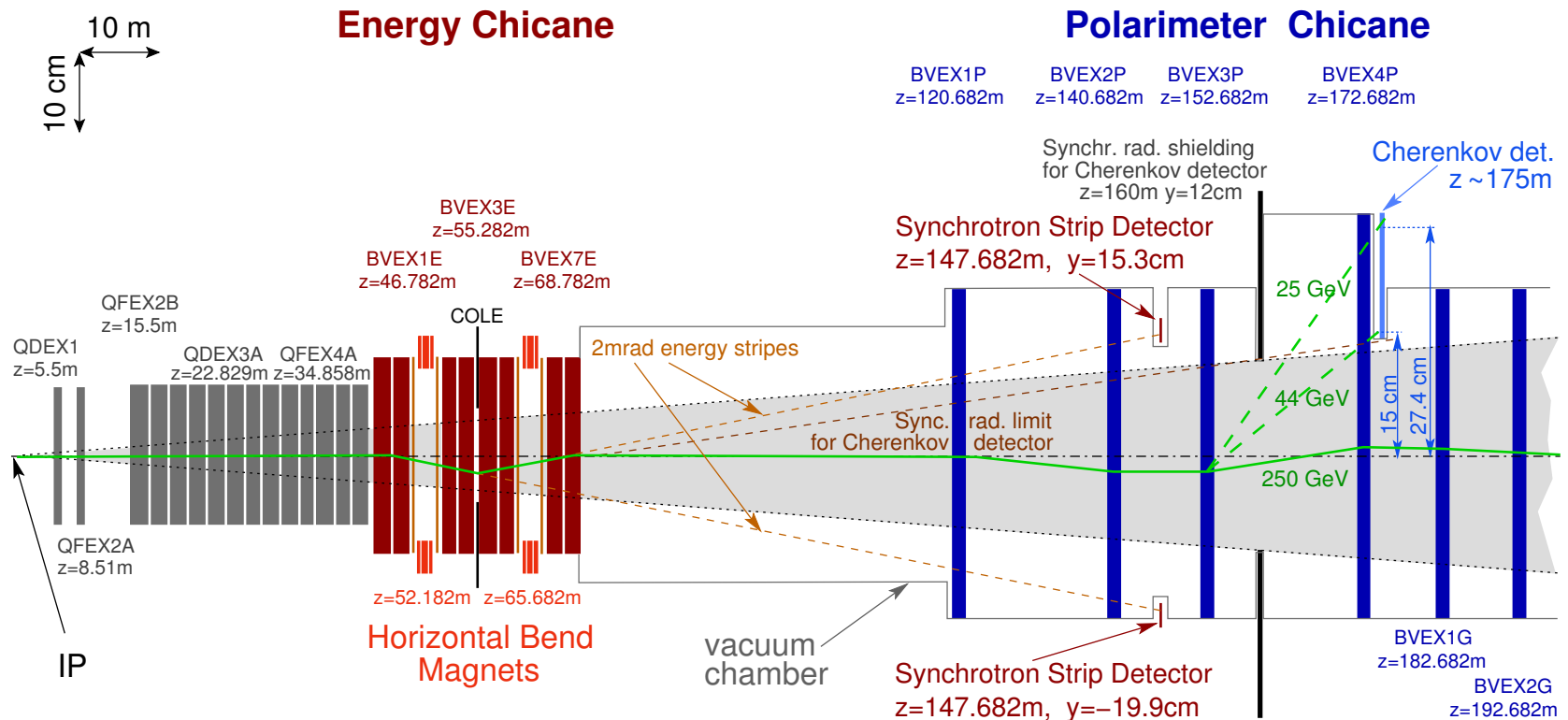
- ▶ detector test at Endstation A
- ▶ chicane provides 2mrad vertical bend + wigglers
- ▶ secondary focus 150 m downstream of IP (polarimeter!)
- ▶ array 100  $\mu\text{m}$  quartz fibers detects Cherenkov light



# Downstream Polarimeter & Energy Measurement.

6-magnet chicane suggested in 2007 by Ken Moffeit et al:

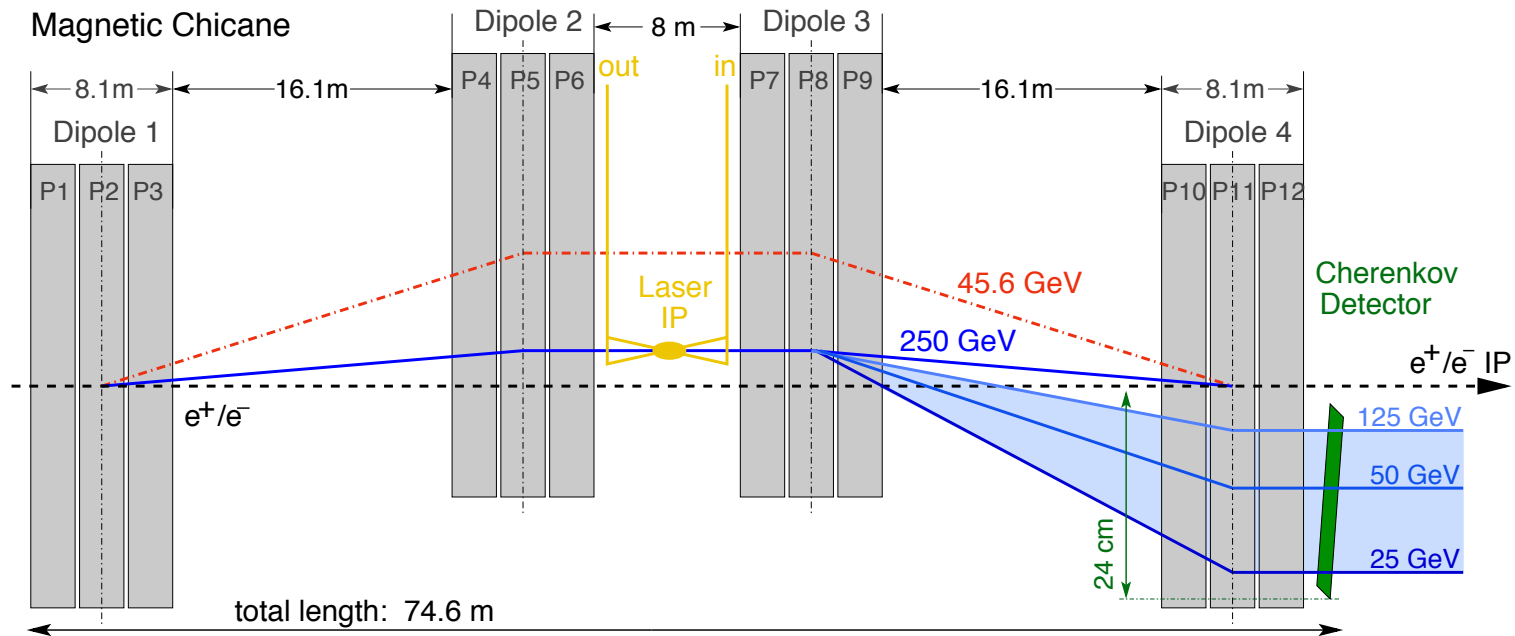
- kick Compton  $e^-$  further out of the synchrotron radiation fan



# Design of the Upstream Polarimeter Chicane.

## Why a 4-Dipole-Chicane?

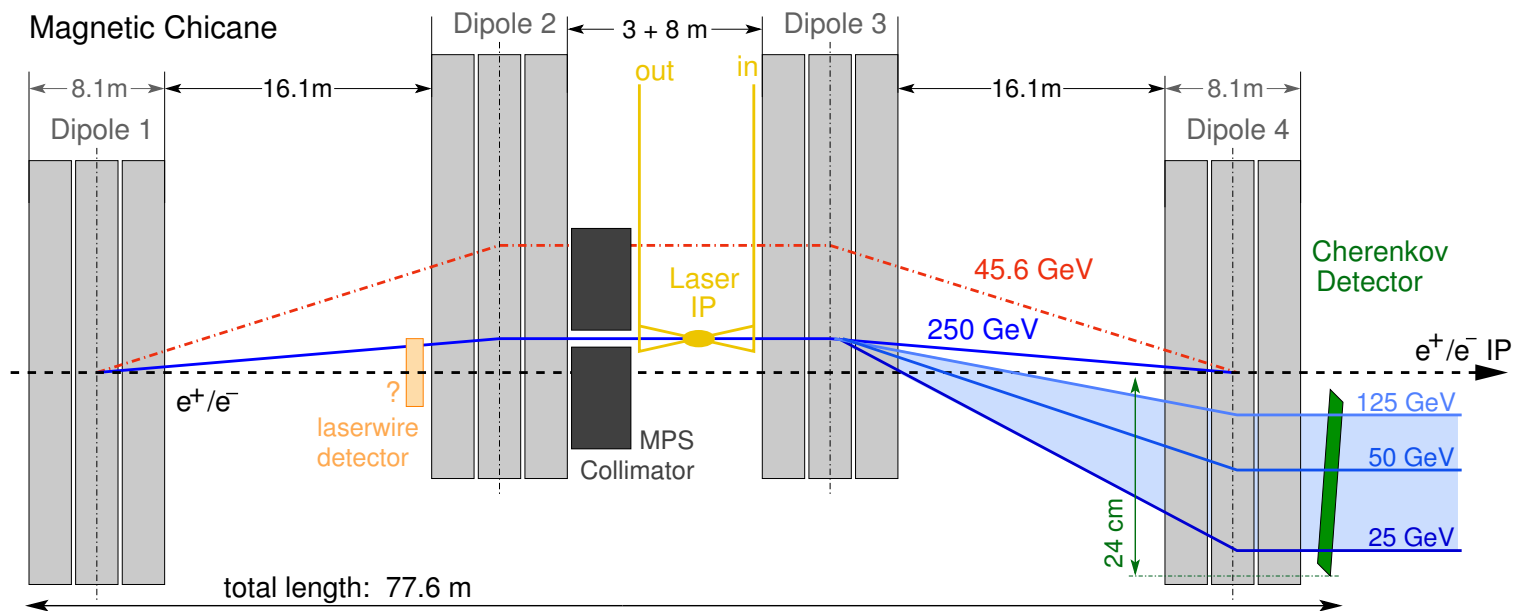
- Compton spectrum position at detector independent of  $E_{beam}$  if  $B$ -field constant
- price to pay: Compton IP moves laterally with  $E_{beam}$



# Design of the Upstream Polarimeter Chicane.

## RDR Design:

- energy collimation and emittance diagnostics in same chicane
- $\Rightarrow$  laterally fixed Compton IP  $\Rightarrow$  scaled field operation!
- collimator & laser-wire will create severe backgrounds

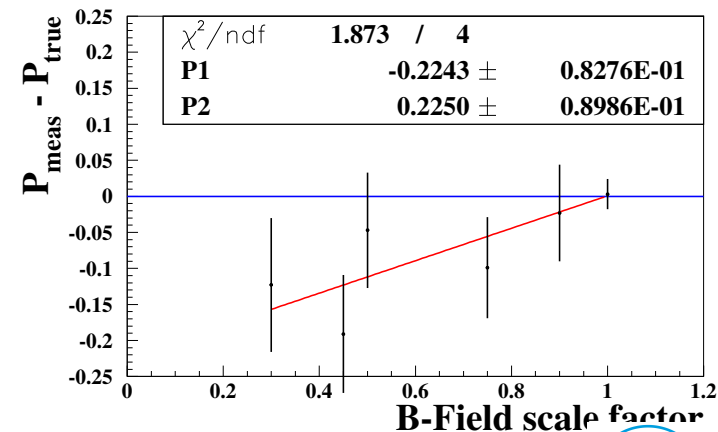
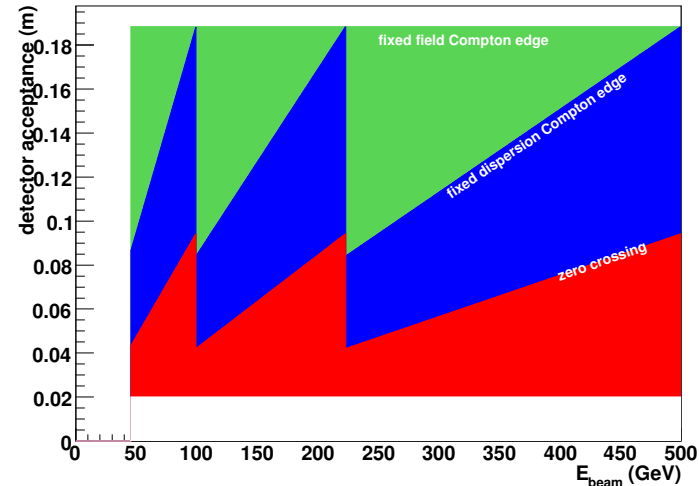


# Scaled vs Fixed Field Operation.

## Effects of scaled field on measurement:

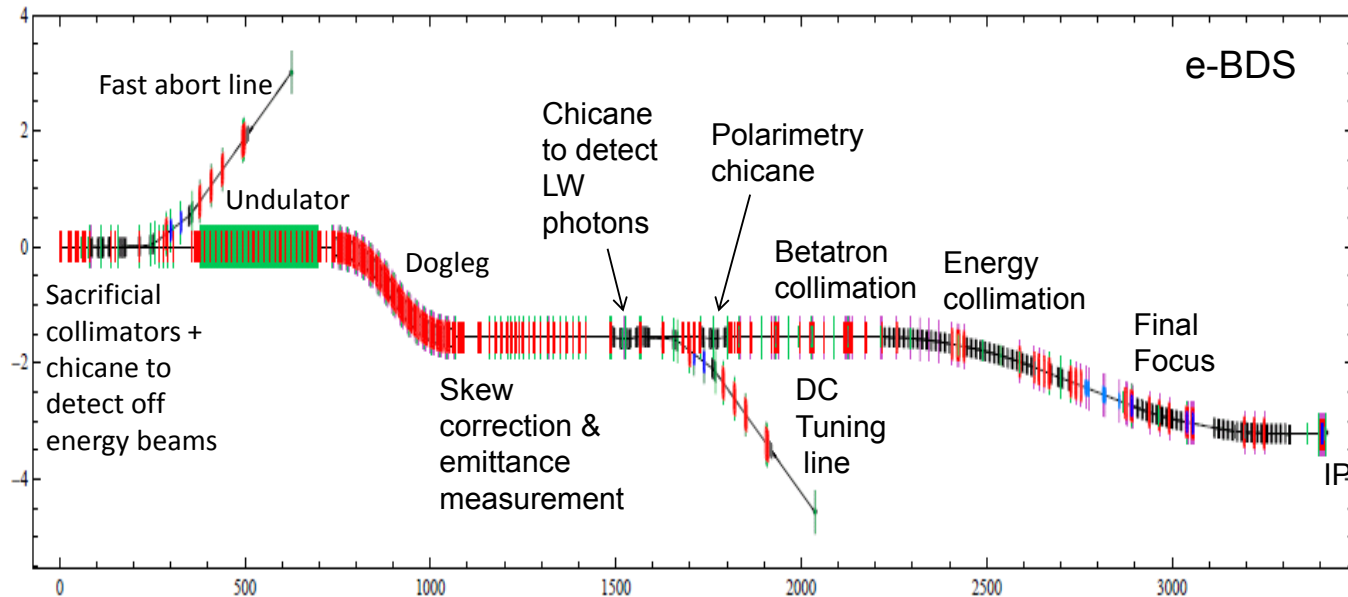
- acceptance: varies with  $E_{beam}$   
⇒ inhomogeneous quality of polarisation measurement
- alignment: via Compton edge position w.r.t. main beam  
⇒ effect on  $\delta\mathcal{P}/\mathcal{P}$  doubles
- systematic deviations for large scale factors

not compatible with extreme precision requirements c.f. ILC-NOTE-2008-047

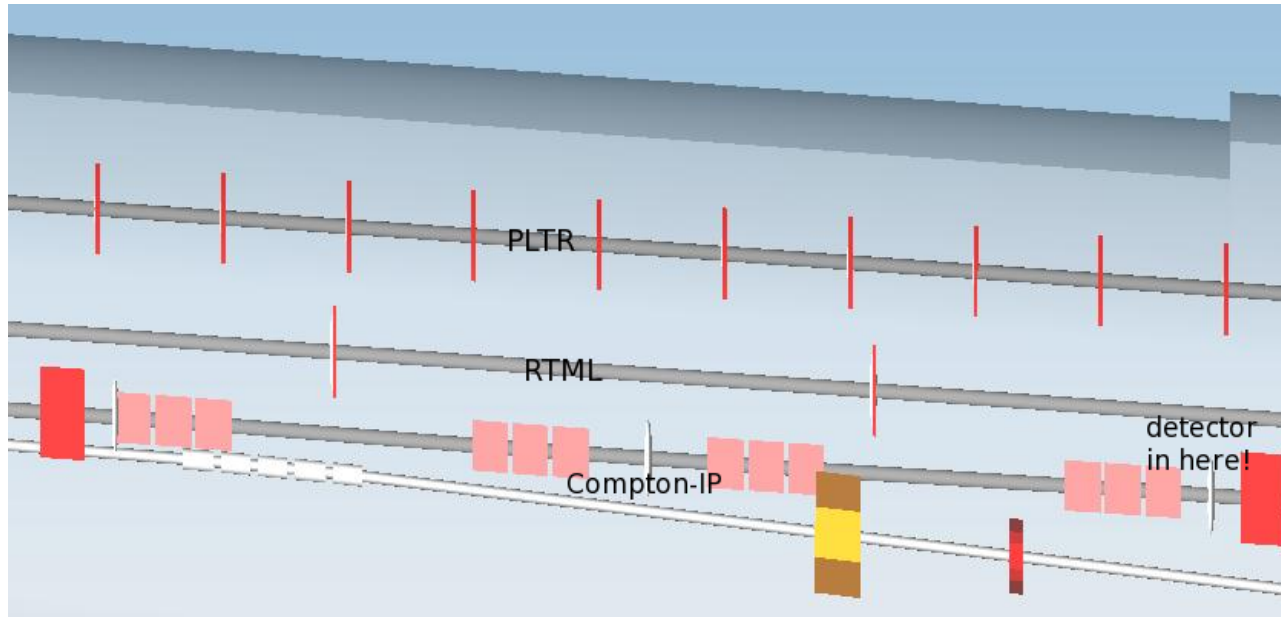




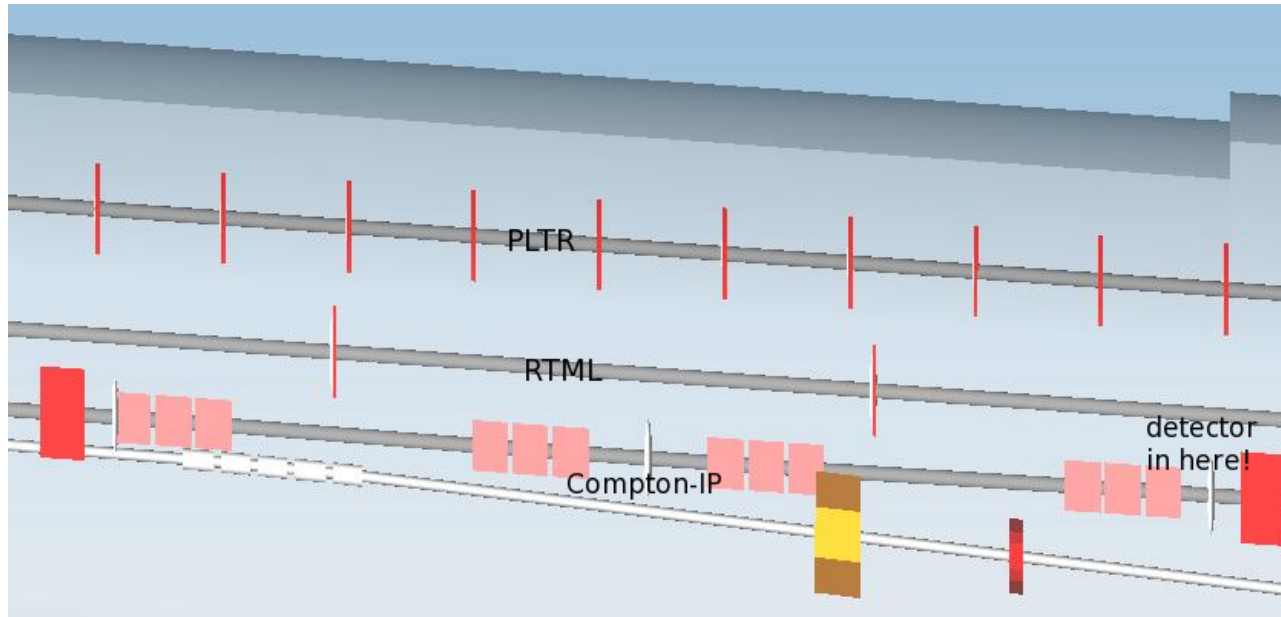
# The Upstream Polarimeter in SB2009-Nov10 lattice.



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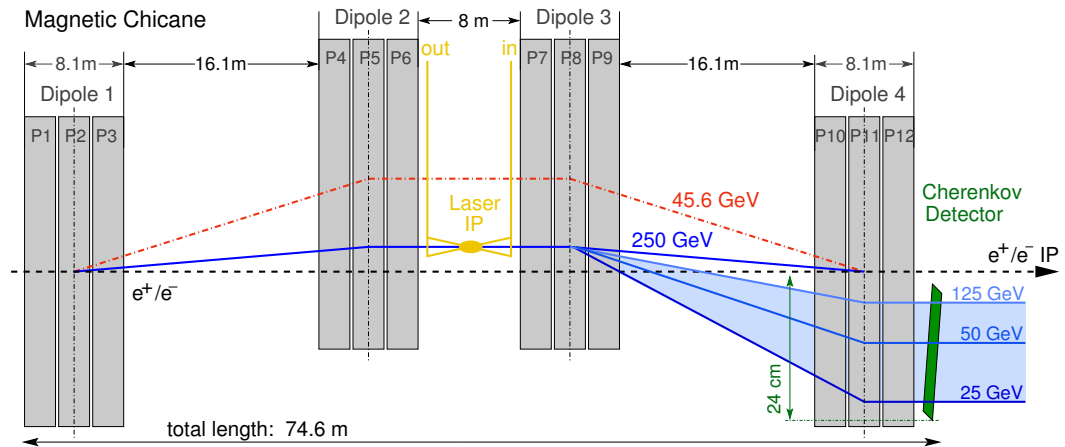
- distance Compton-IP to dump line ca 30 cm at 250 GeV
- down to ca 20 cm at lowest energies - enough?

[c.f. Baseline Technical Review Workshop 2011]

# Vacuum Chamber in Chicane Region.

need special beam pipe through out whole chicane

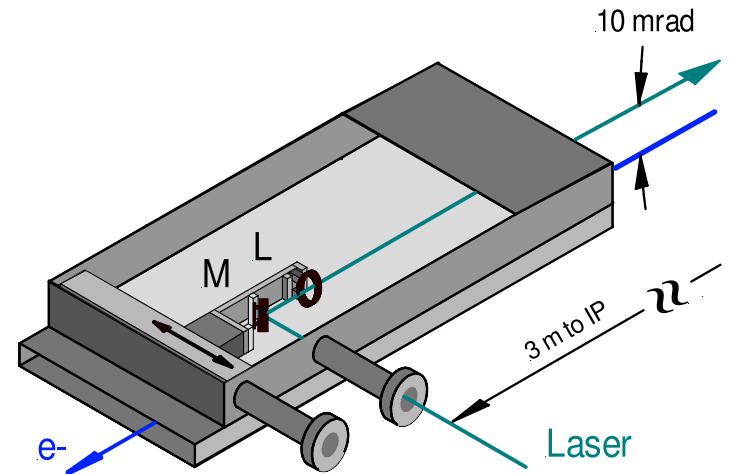
- to allow for varying bending angle
- to guide laser in and out
- to let fan of Compton scattered electrons pass
- to extract Compton fan to detector



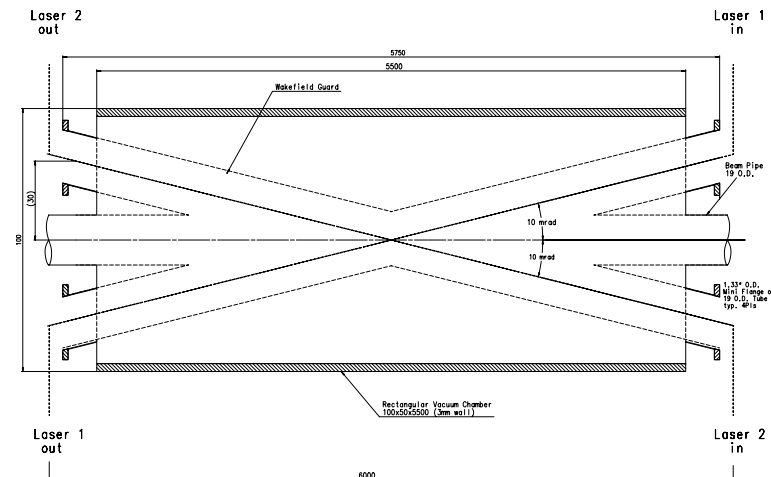
Attention: deflection of chicane the otherway round as on previous page!

# Vacuum Chamber: Laser in / out.

- Laser enters chicane *horizontally* (far side from tune-up dump line!)
- final mirror / lens movable to adjust to  $e^-$  beam
- had been designed to some extent for TESLA (!) by N. Meyners, P. Schüler

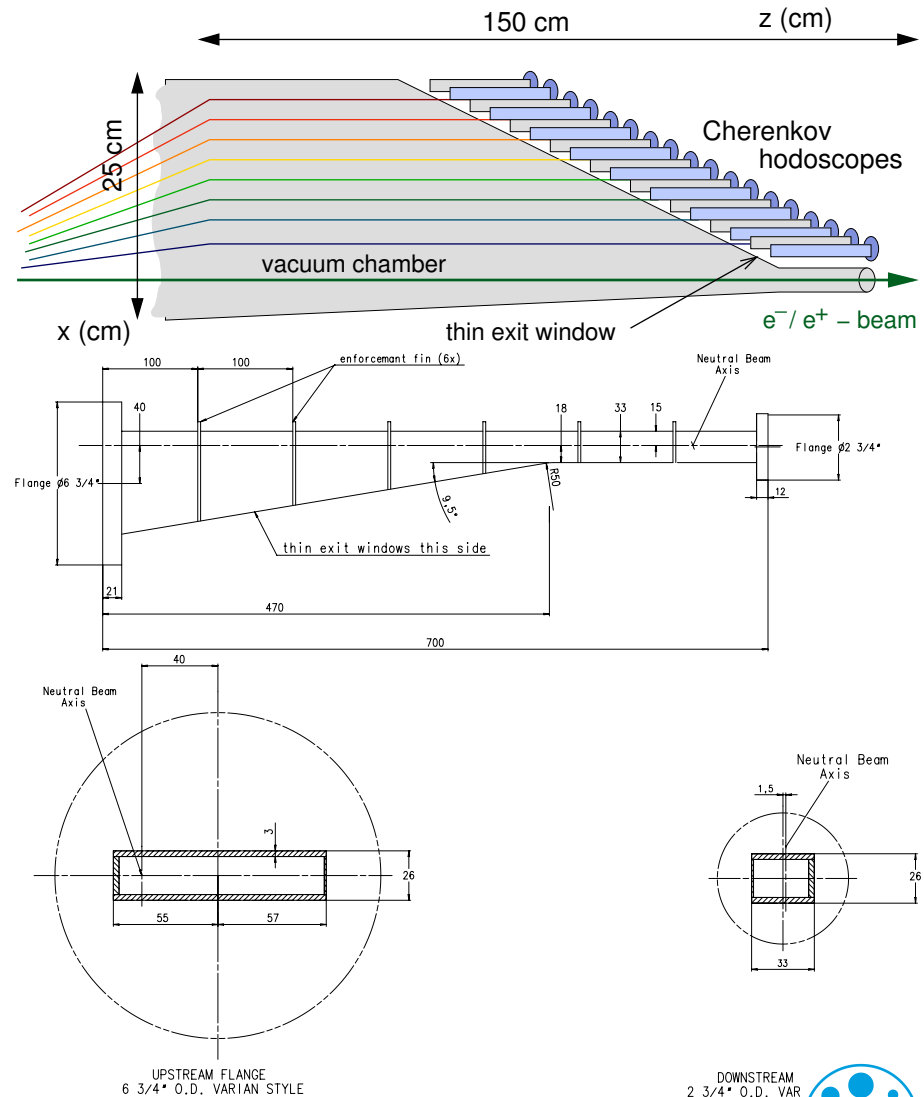


Movable Laser Beam

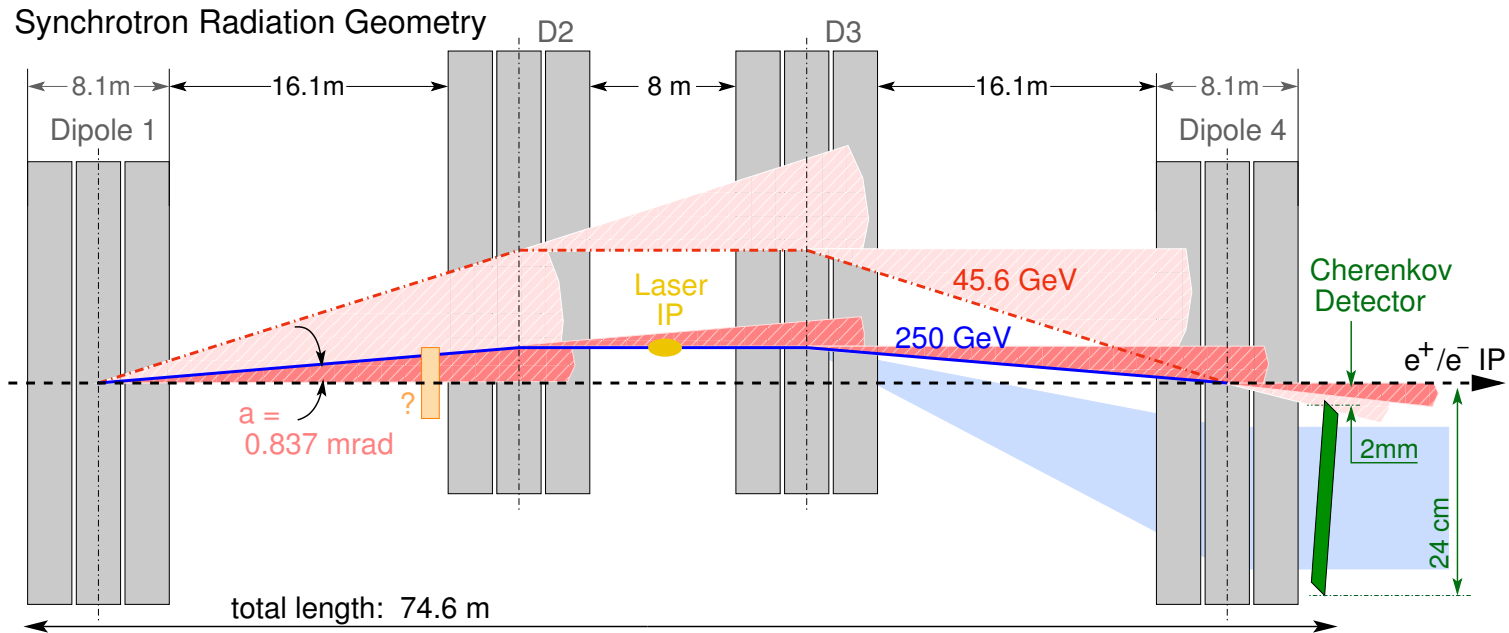


# Vacuum Chamber: Compton fan exit.

- need tapered exit window to avoid wake fields
- again estimate from TESLA:  $\simeq 10^\circ$  is fine (opinions?)
- need  $\simeq 1.5$  m for detector array, make it 2 m for shielding, accessibility,...
- fine with SB2009-Nov10 lattice

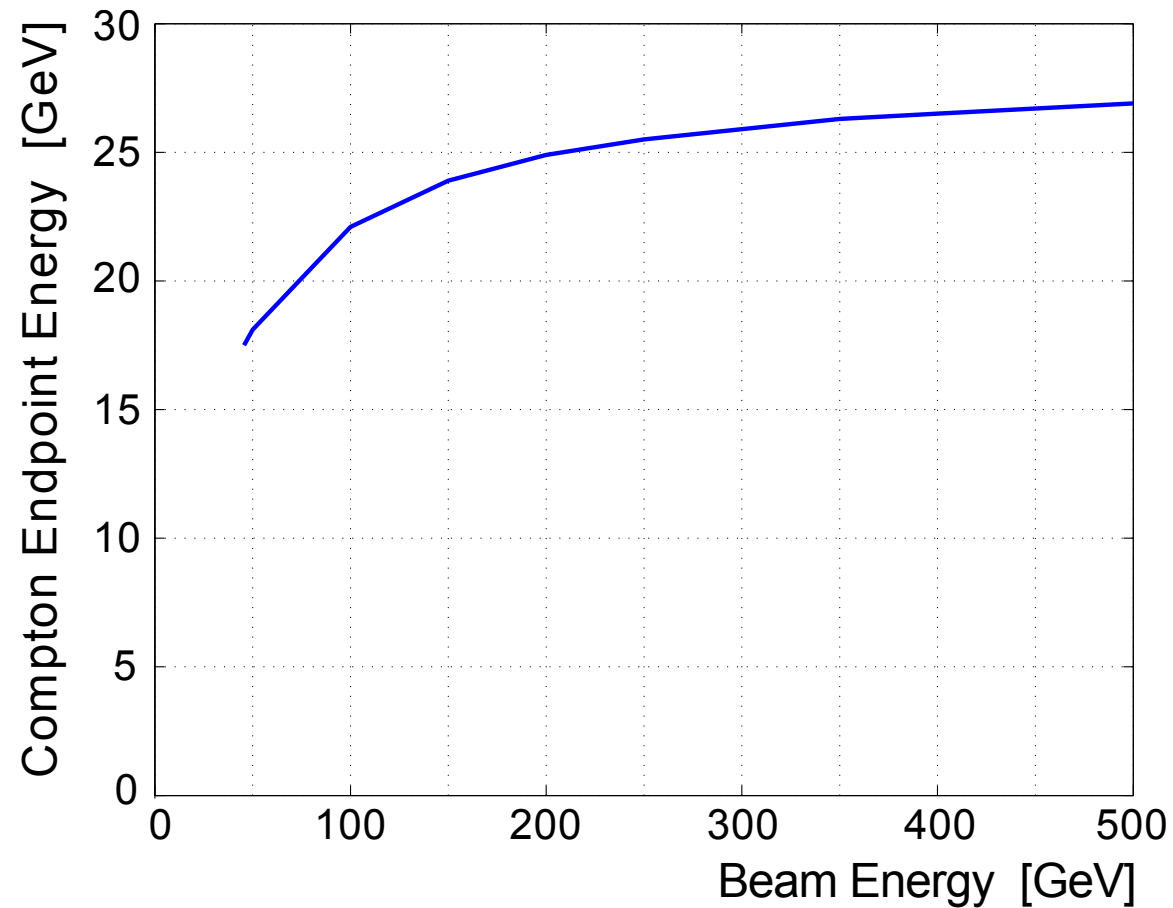


# Synchrotron Radiation.



# Compton edge.

Compton edge position nearly independent of beam energy

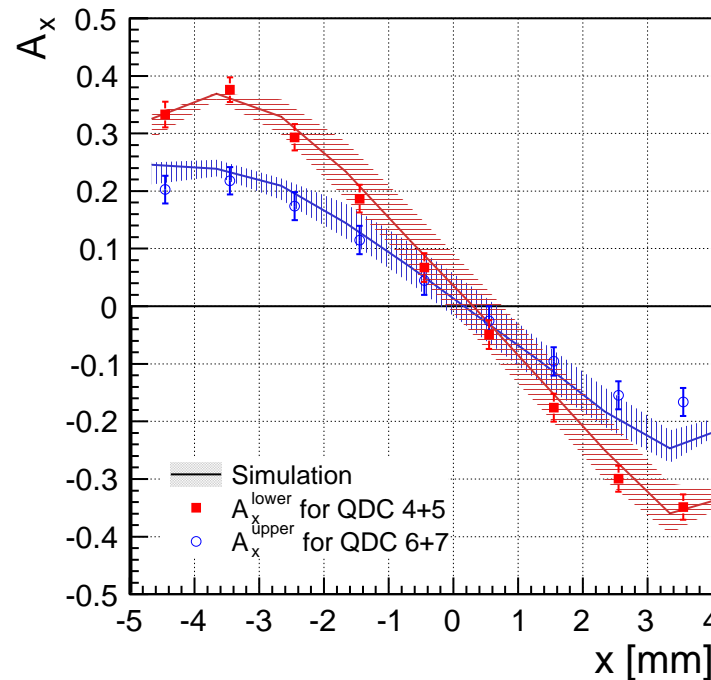




# Gas Cherenkov detector: Alignment.

If the detector is tilted

- beam path through the detector varies  $\Rightarrow$  different light path
- different light pattern on the photocathode  
 $\Rightarrow$  alignment via spatial assymetries possible:

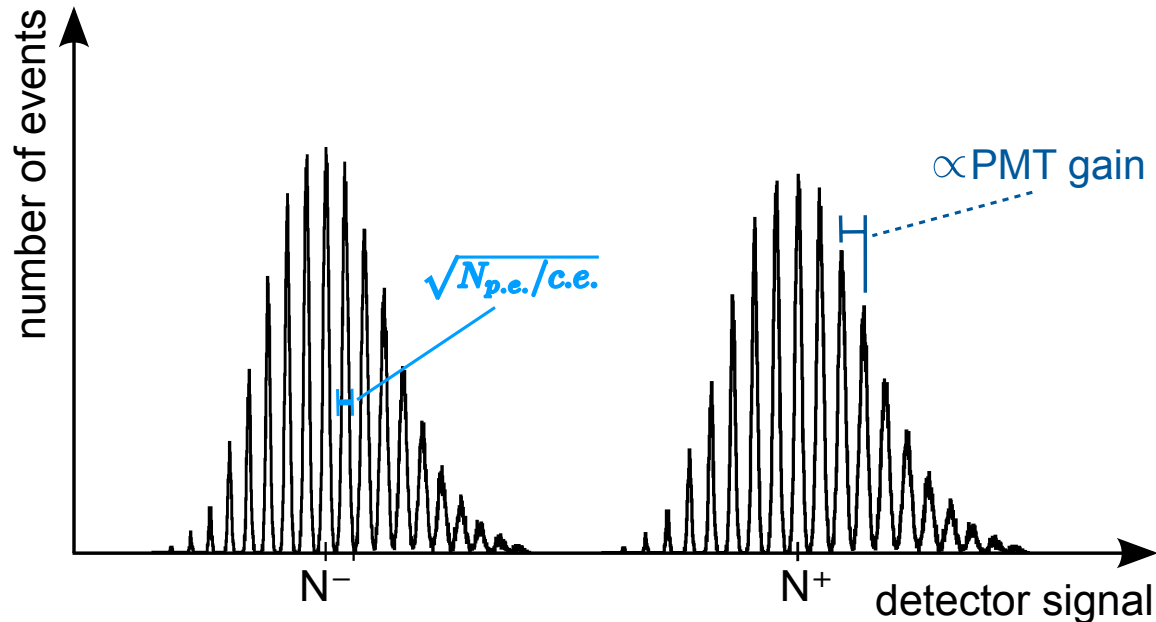


$\Rightarrow$  Reached a tilt alignment of  $0.1^\circ$ . [JINST 7, P01019 (2012)]

# Quartz Cherenkov detector.

Alternative detector concept: quartz detector

- Higher refractive index  $\rightarrow$  higher photon yield
- For enough photons per Compton  $e^-$ :  
 $\rightarrow$  calibrate gain directly from the data

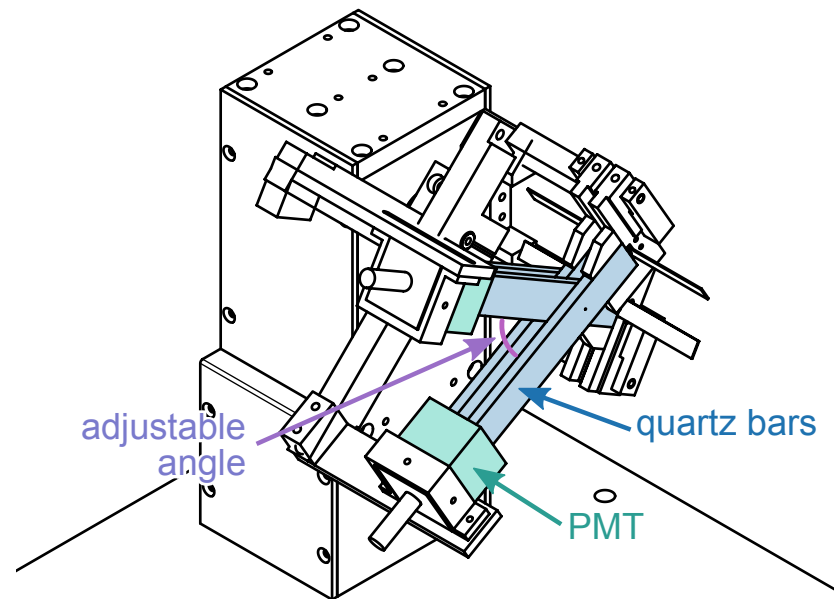


4-channel prototype operated at DESY II testbeam in 2014.

# Quartz Cherenkov detector (2).

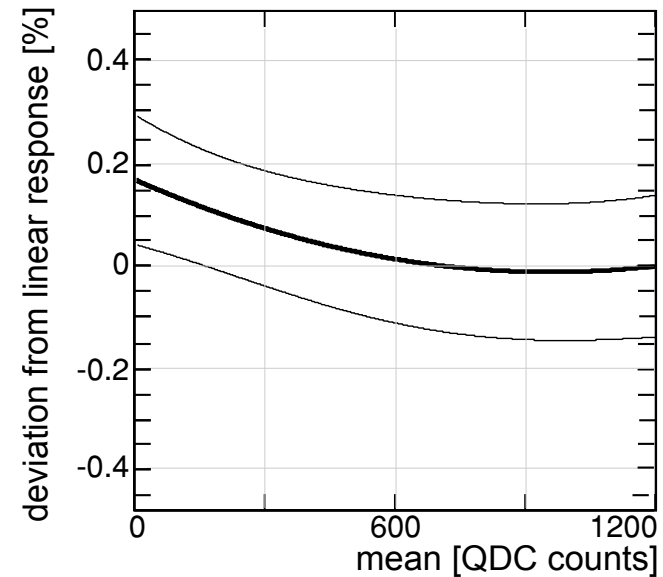
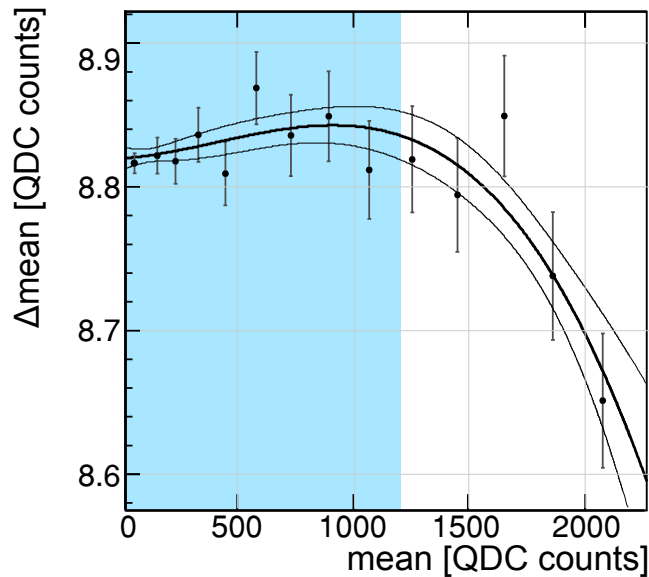
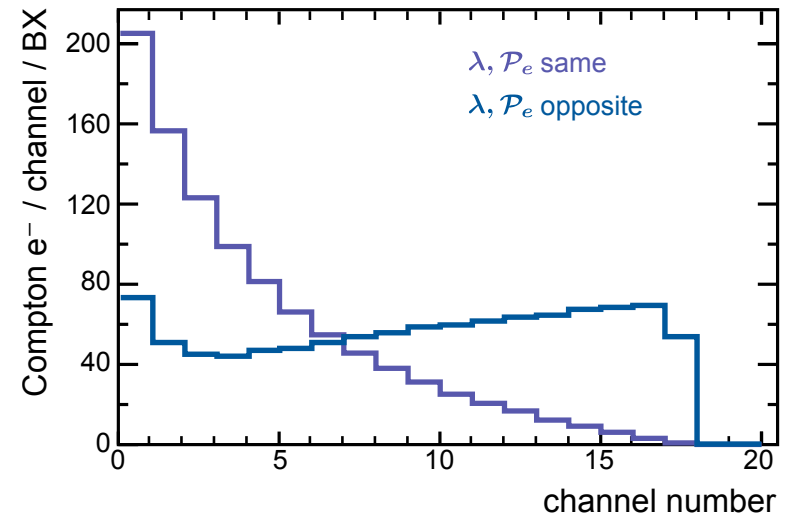
4-channel prototype operated at DESY II testbeam in 2014

- channels: quartz bars (5 mm x 18 mm x 100 mm)
- qualitative agreement with simulations (angular dependence, etc. )
- light yield smaller than predicted, studies ongoing



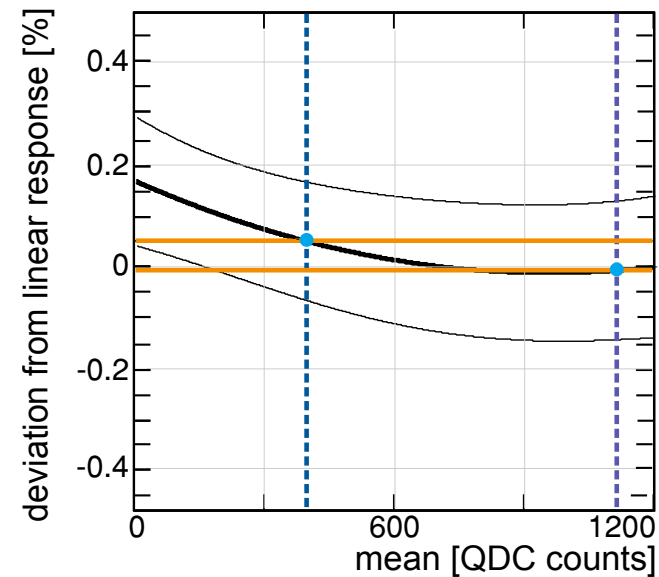
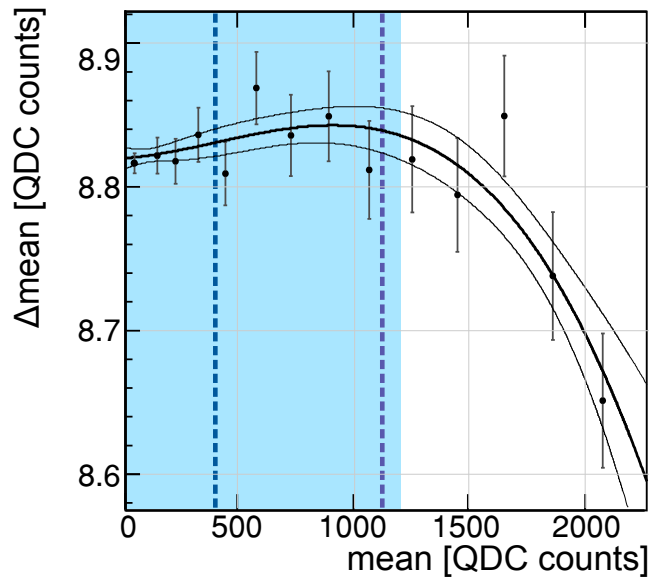
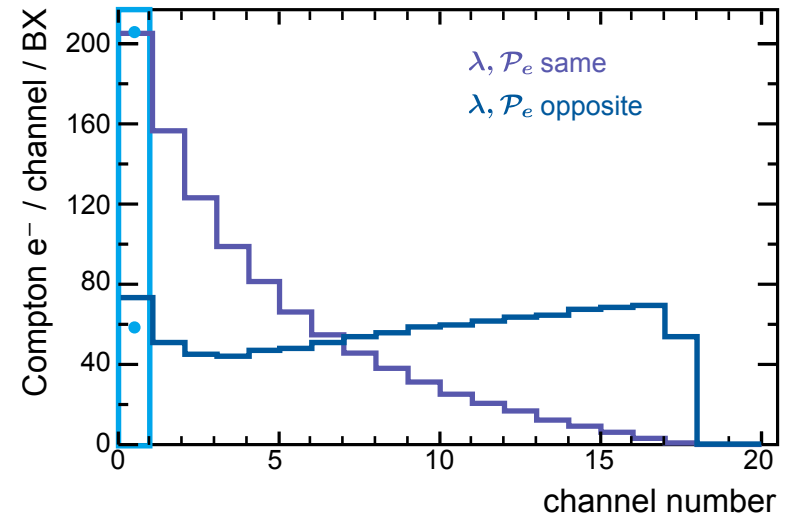
# Non-linearity in extreme polarimeter channels.

- up to 210 Compton  $e^-$  ( $\sim 1200$  QDC counts)
- overall non-linearity already small in this range (max 0.2%)
- in single channels even smaller



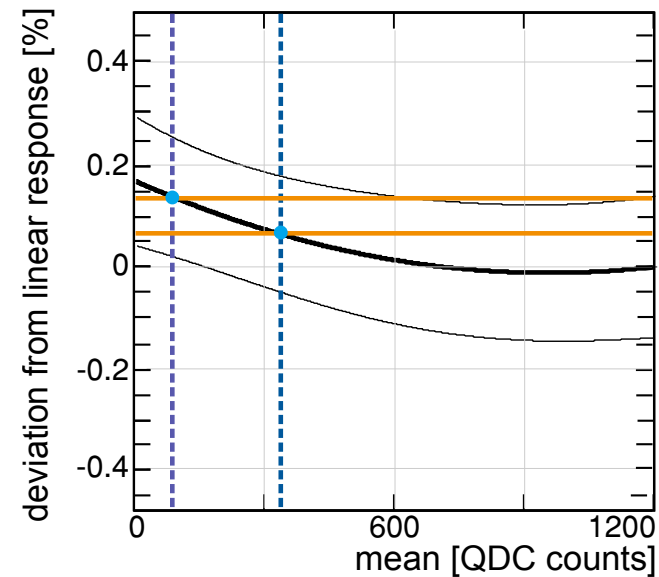
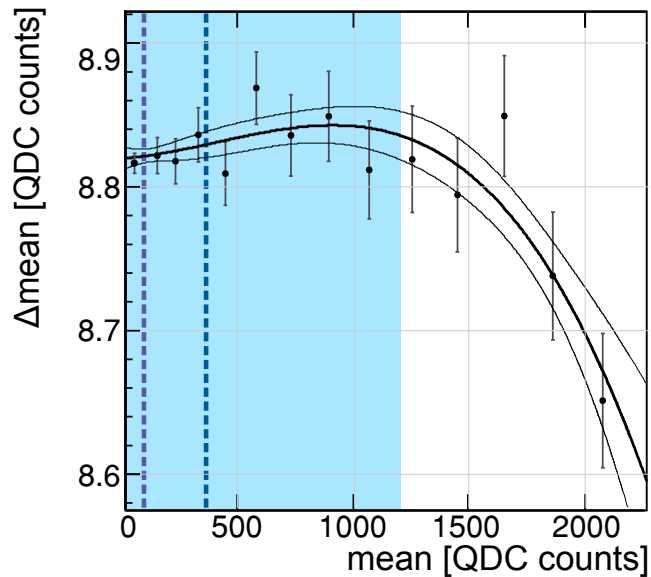
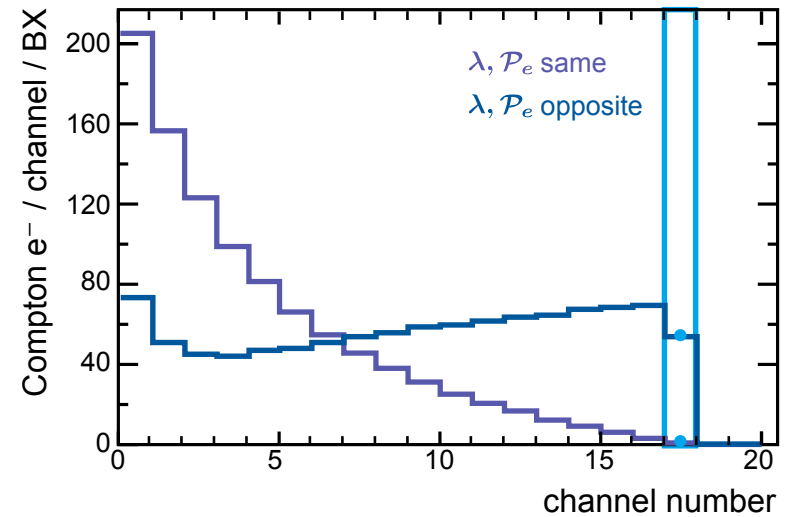
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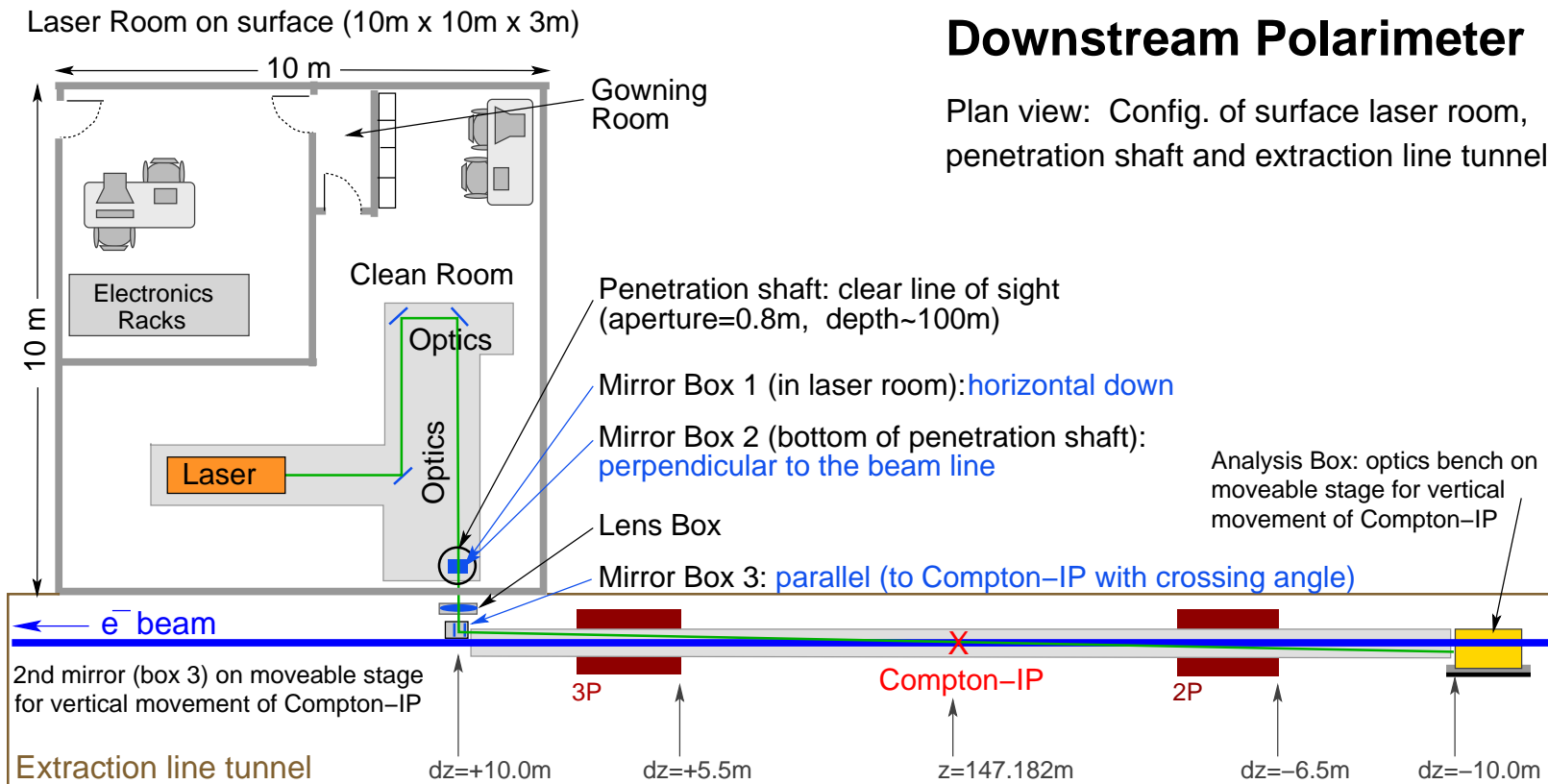


# Non-linearity in extreme polarimeter channels.

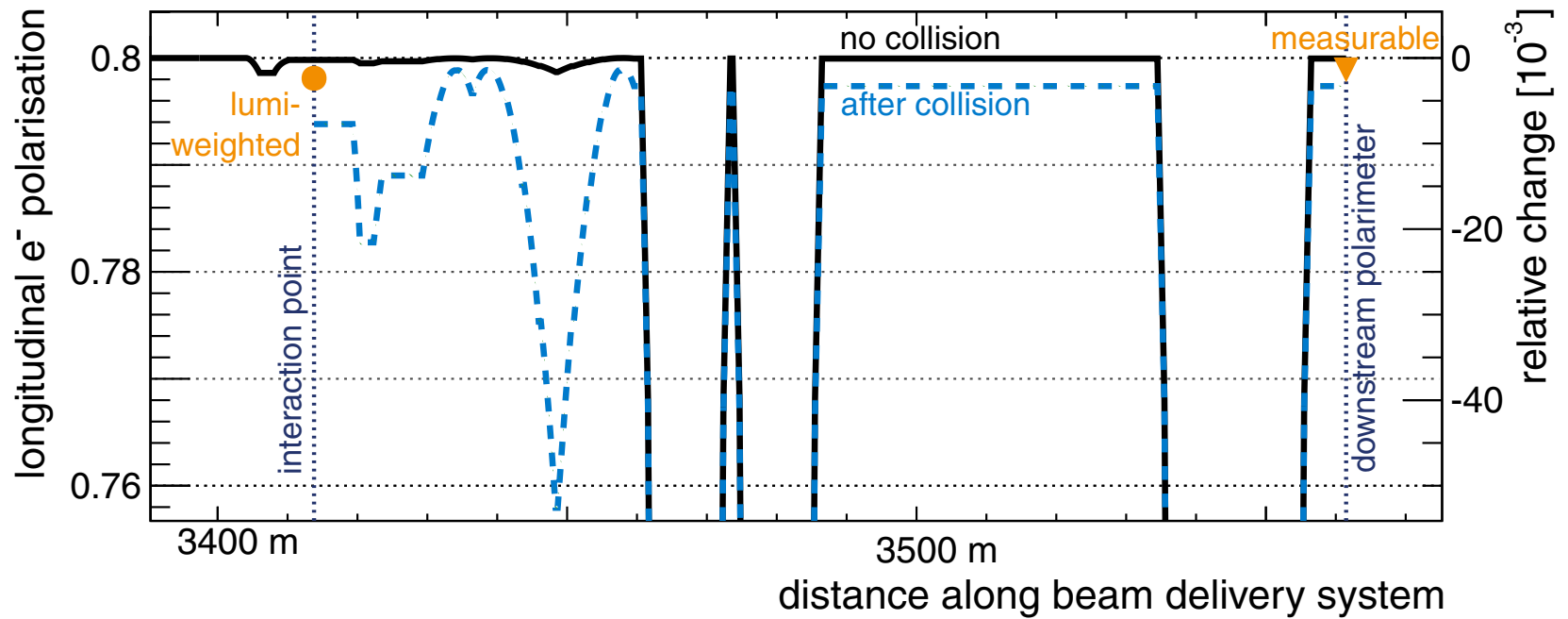
- up to 210 Compton  $e^-$  ( $\sim 1200$  QDC counts)
- overall non-linearity already small in this range (max 0.2%)
- in single channels even smaller



# Laser Room.

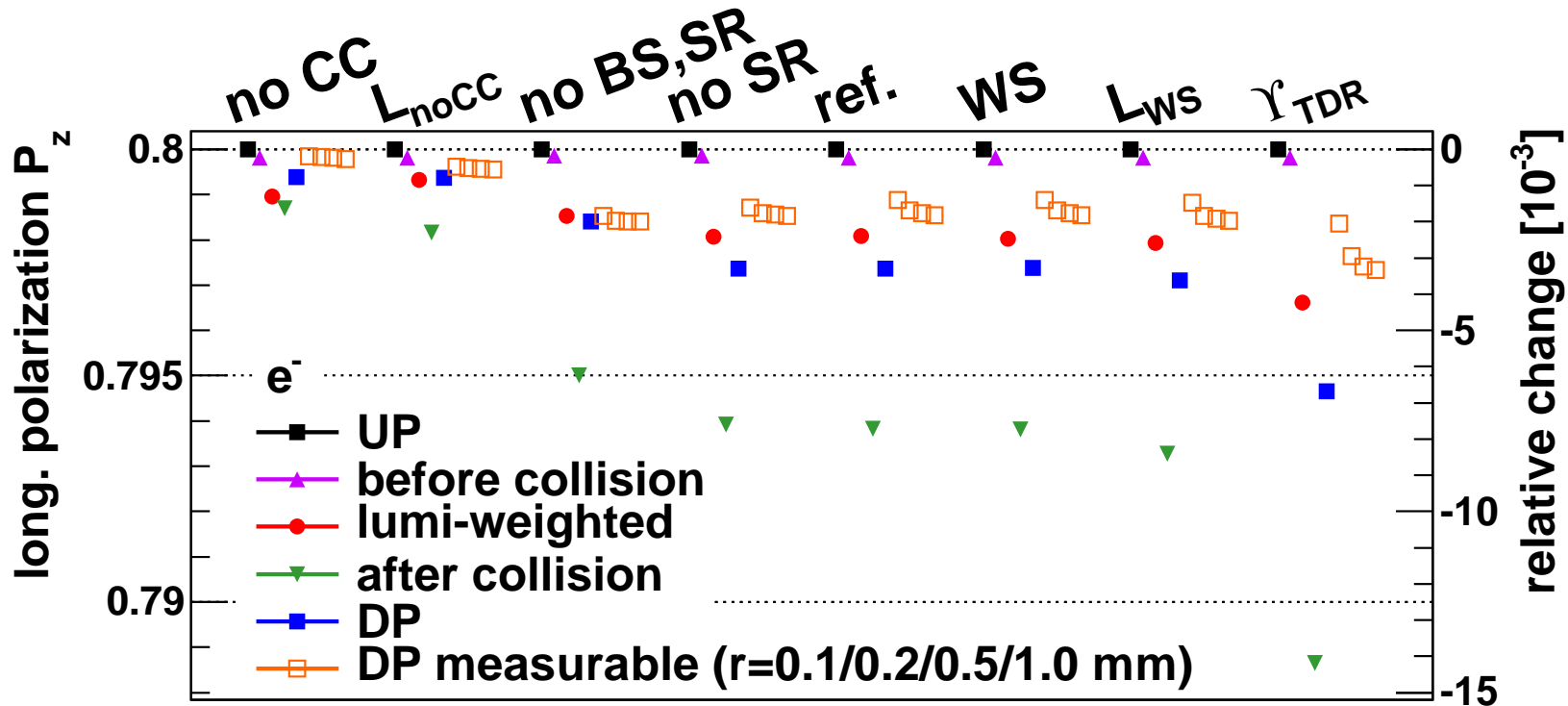


# Spin transport.



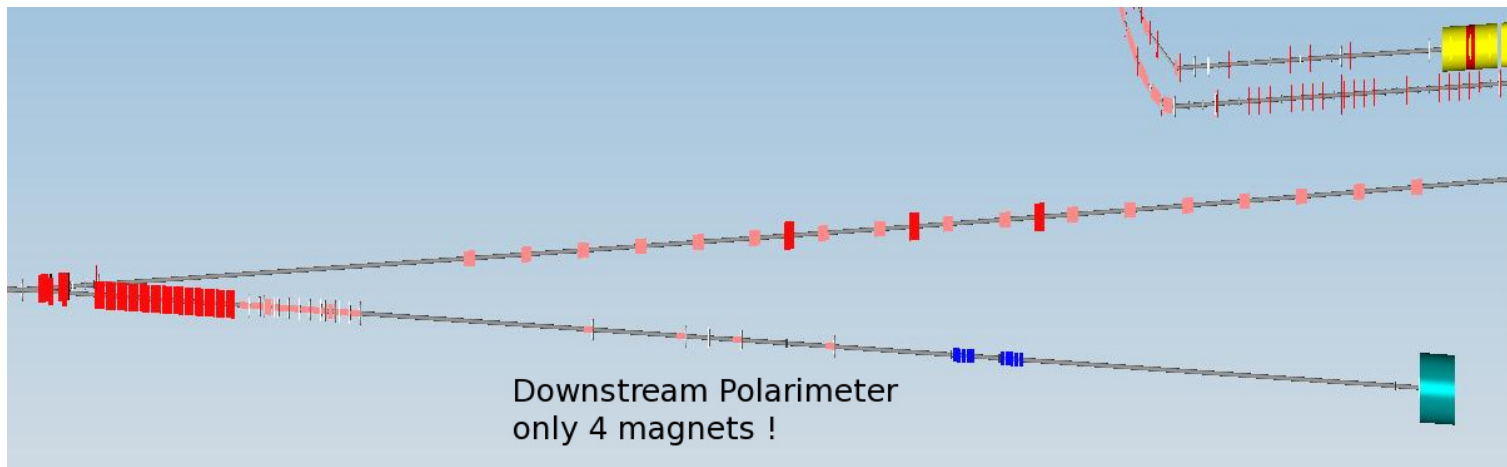


# Spin tracking (more).



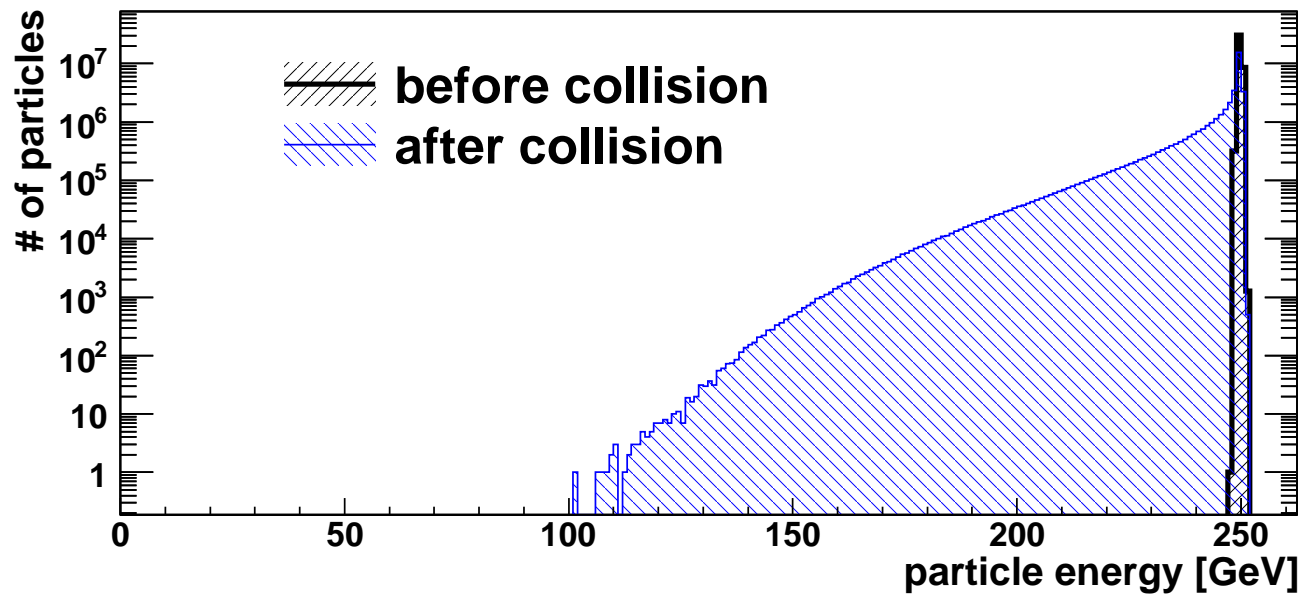
# Downstream Polarimeter in SB2009-Nov10 lattice.

- still 4-magnet chicane - should be upgraded to 6-magnet design as proposed in SLAC-PUB-12425
- necessary due to push-pull related changes to the extraction SC quadrupoles
- at the same time gives better shielding of magnets due to additional collimators
- even more impact due to worse spent beam in low power configuration....



# Beam Energy Spectrum with Collisions.

GuineaPig++, RDR nominal,  $\sqrt{s} = 500$  GeV

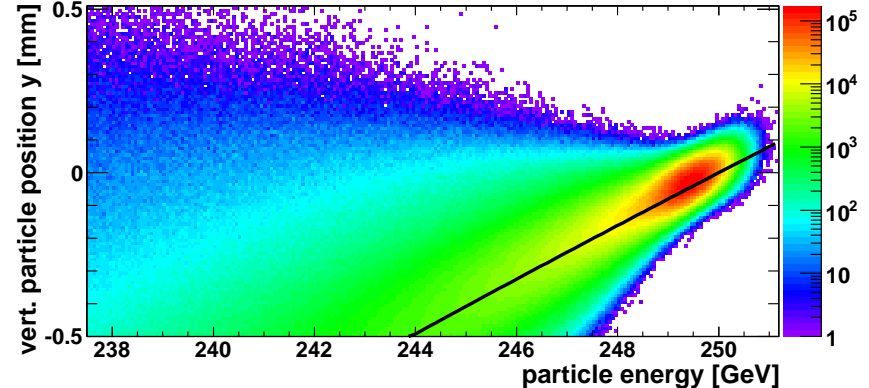
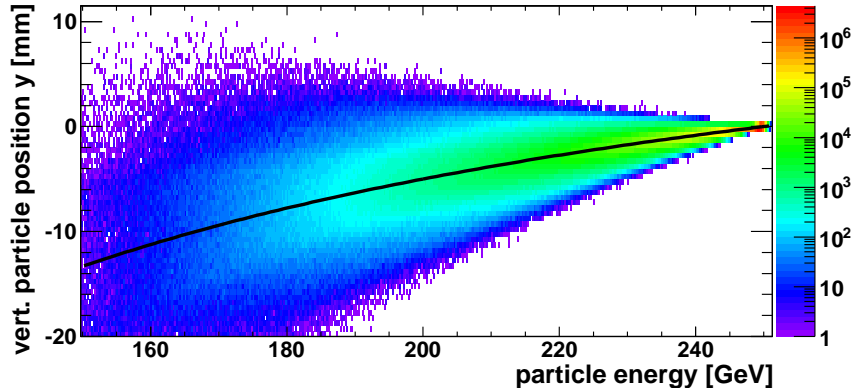


How will this influence the measurement at the downstream polarimeter?

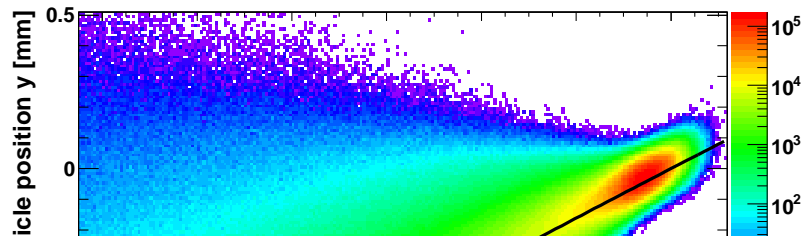
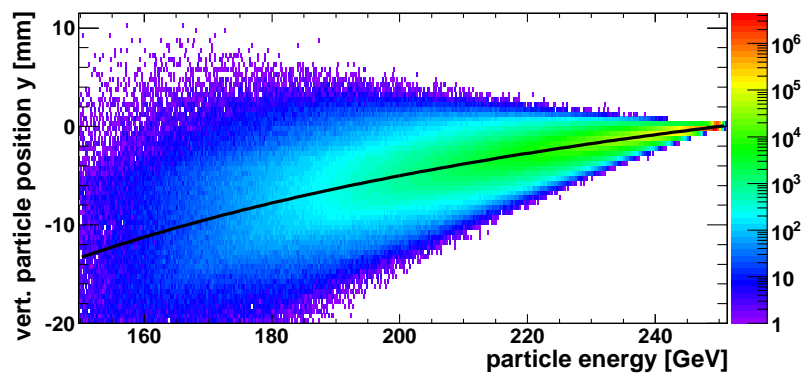
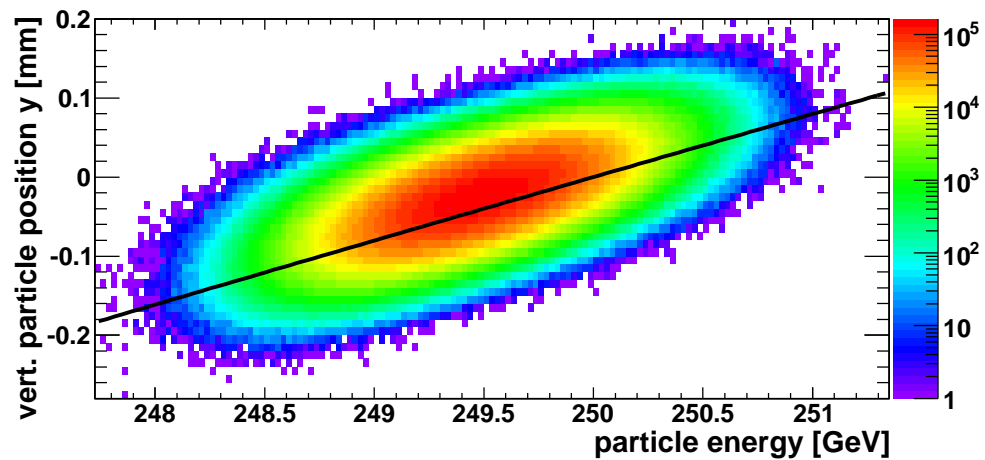
# $y$ vs $E$ at DP IP.

## Particle Tracking through SB2009-Nov10 lattice (M.Beckmann)

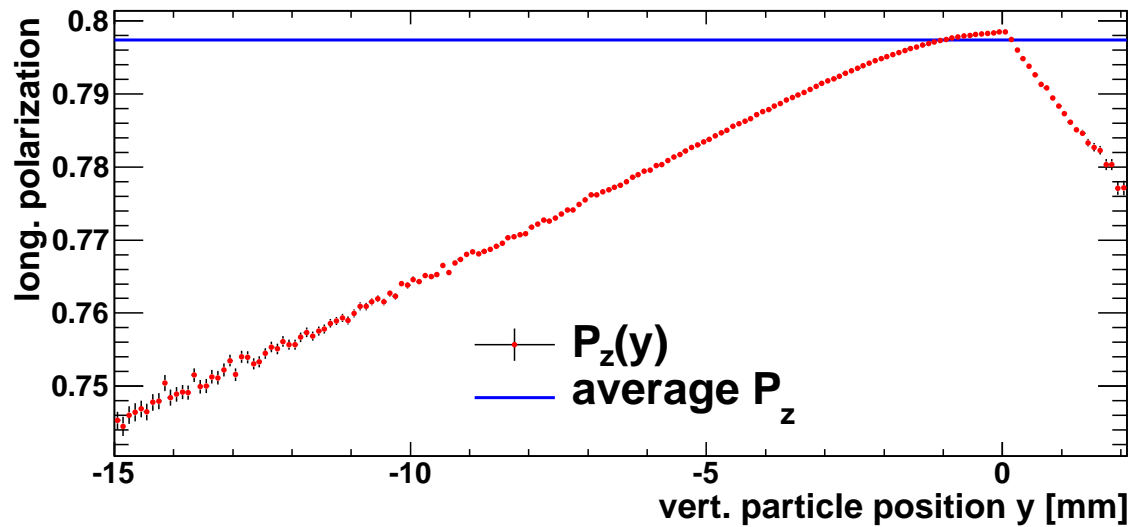
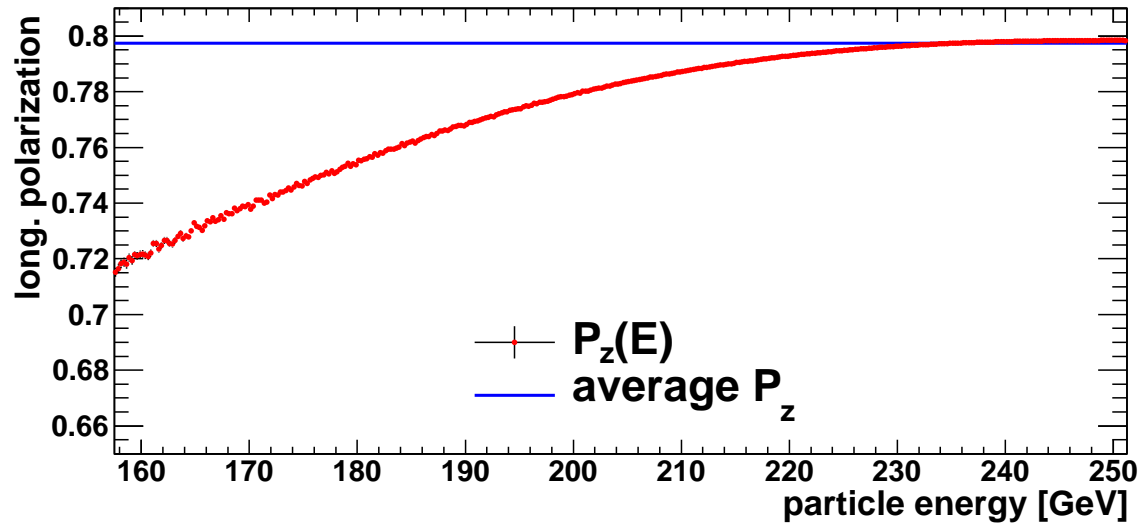
- vertical extension of spent beam at DP IP  $\mathcal{O}(\text{cm})$
- “core” size still  $\simeq 0.5 \text{ mm}$
- sizable correlation of energy and position
- which part will the laser sample?
- expect dependence of measured polarisation on laser spot size and laser-beam alignment



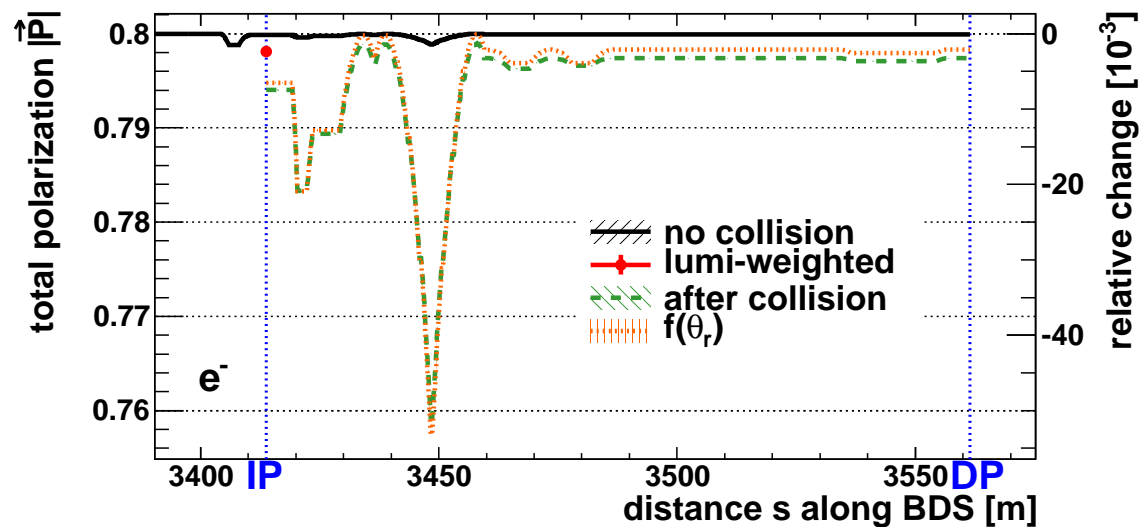
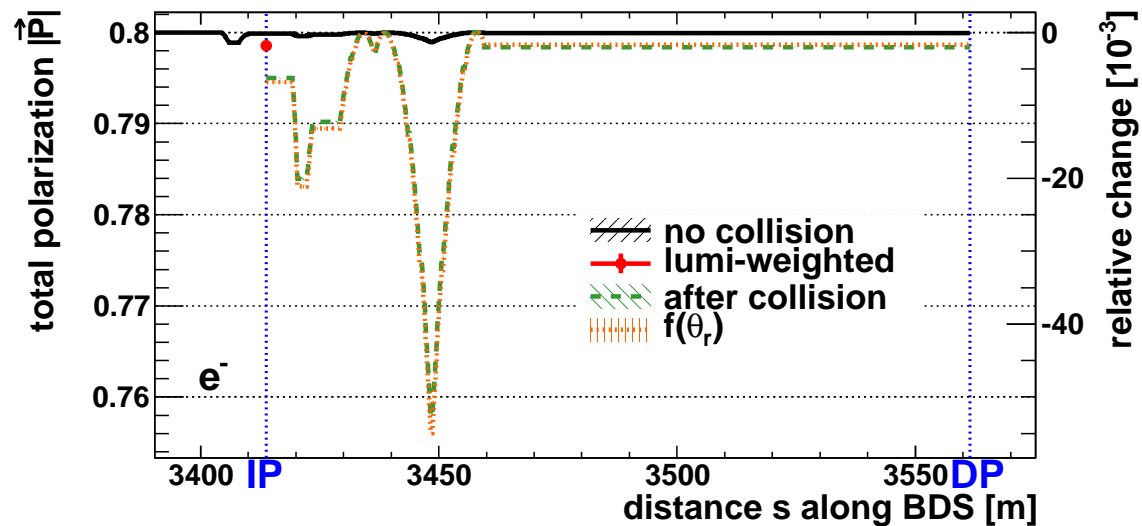
# Downstream Polarimeter: $y$ vs $E$ .



# Downstream Polarimeter: $P_z$ vs $E$ , $P_z$ vs $y$ .



# Total Polarisation IP $\rightarrow$ DP



# Polarisation for Physics.

Longitudinal polarisation  $P_z = \frac{N_R - N_L}{N_R + N_L}$

with  $N_{R,L}$ : number of right-/left-handed particles in bunch

- SM & BSM: left- and righthanded particles couple differently
  - polarised cross-sections are important observables carrying **qualitatively** new information!
  - beam polarisation can suppress background / enhance signal

- wanted for physics: **luminosity weighted average polarisation**

at the IP,  $\langle P_z \rangle_{IP} = \frac{\int P_z(t) \mathcal{L}(t) dt}{\int \mathcal{L}(t) dt}$

- Note: most physics studies sofar assume this average is known exactly and independently for  $e^-$  and  $e^+$  beam.

$P \equiv P_z$  in the following.



# Polarised Cross-sections.

$$\sigma_{P_{e^-} P_{e^+}} = \frac{1}{4} \left\{ \begin{aligned} &(1 + P_{e^-})(1 + P_{e^+})\sigma_{RR} + (1 - P_{e^-})(1 - P_{e^+})\sigma_{LL} \\ &+ (1 + P_{e^-})(1 - P_{e^+})\sigma_{RL} + (1 - P_{e^-})(1 + P_{e^+})\sigma_{LR} \end{aligned} \right\}$$

processes with s-channel  $Z/\gamma$  exchange only:

- $\sigma_{RR} = \sigma_{LL} = 0$
- $4\sigma_{P_{e^-} P_{e^+}} = (1 - P_{e^-} P_{e^+})(\sigma_{LR} + \sigma_{RL})[1 - P_{\text{eff}}^- A_{LR}]$
- with  $P_{\text{eff}}^- = 1 - \frac{P_{e^-} - P_{e^+}}{1 - P_{e^-} P_{e^+}}$  and  $A_{LR} = \frac{\sigma_{LR} - \sigma_{RL}}{\sigma_{LR} + \sigma_{RL}}$

general case:

- $\sigma_{RR} \neq \sigma_{LL} \neq 0$
- $4\sigma_{P_{e^-} P_{e^+}} = (1 + P_{e^-} P_{e^+})(\sigma_{LL} + \sigma_{RR})[1 + P_{\text{eff}}^+ A_{LLRR}] + \text{above}$
- with  $P_{\text{eff}}^+ = 1 + \frac{P_{e^-} + P_{e^+}}{1 + P_{e^-} P_{e^+}}$  and  $A_{LLRR} = \frac{\sigma_{LL} - \sigma_{RR}}{\sigma_{LL} + \sigma_{RR}}$

# Polarisation Averages.

Absolute cross-section measurements require:

- $\langle P_{e^\pm} \rangle_{IP} = \frac{\int P_{e^\pm}(t) \mathcal{L}(t) dt}{\int \mathcal{L}(t) dt}$
- $\langle P_{e^-} P_{e^+} \rangle_{IP} = \frac{\int P_{e^-}(t) P_{e^+}(t) \mathcal{L}(t) dt}{\int \mathcal{L}(t) dt}$
- correlations between lumi and polarisation?!

Direct extraction from collision data

- any abundant, well-known, polarisation dependent process:
- $\langle | P_{e^\pm} | \rangle_{IP} = \sqrt{\frac{(\sigma_{-+} + \sigma_{+-} - \sigma_{--} - \sigma_{++})(\pm\sigma_{-+} \mp \sigma_{+-} + \sigma_{--} - \sigma_{++})}{(\sigma_{-+} + \sigma_{+-} + \sigma_{--} + \sigma_{++})(\pm\sigma_{-+} \mp \sigma_{+-} - \sigma_{--} + \sigma_{++})}}$
- $\sigma_{+-}$  is total cross-section for  $P(e^-, e^+) = (+x\%, -y\%)$ , etc.
- assumes  $P_+(e^-) = -P_-(e^-)$  and  $P_+(e^+) = -P_-(e^+)$

# Correction to modified Blondel scheme.

$$P_+(e^\pm) = P^\pm + \epsilon^\pm \text{ and } P_-(e^\pm) = P^\pm - \epsilon^\pm$$

