

Measuring Higgs Boson Self-couplings with $2 \rightarrow 3$ VBS Processes

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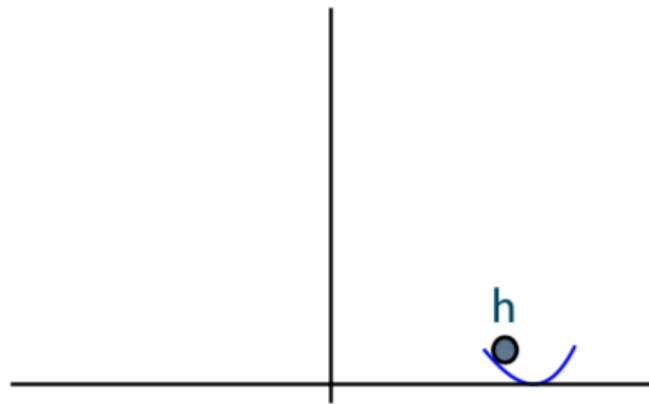
In collaboration with Chih-Ting Lu, Yongcheng Wu

Table of Contents

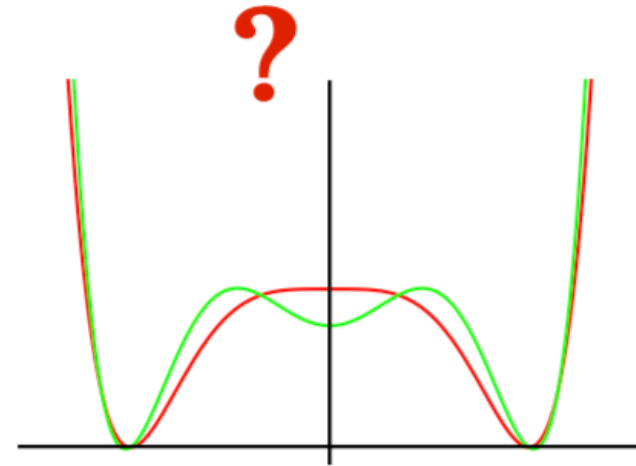
- 1. Introduction
- 2. Feynman diagrams and amplitudes
- 3. Cross section and Simulation in Madgraph

Higgs Self-couplings

- Higgs Potential: Direct related to origin of EW symmetry breaking
- Goal: measure Higgs self-couplings precisely

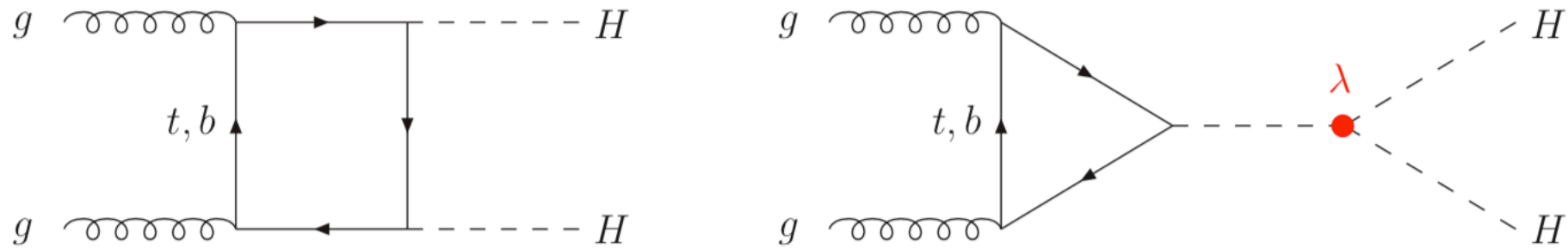


$$V(h) = m_h^2 h^\dagger h + \frac{1}{2} \lambda (h^\dagger h)^2,$$



$$V(h) = ?$$

Main Channel to measure Higgs self-couplings at LHC: $gg \rightarrow HH$



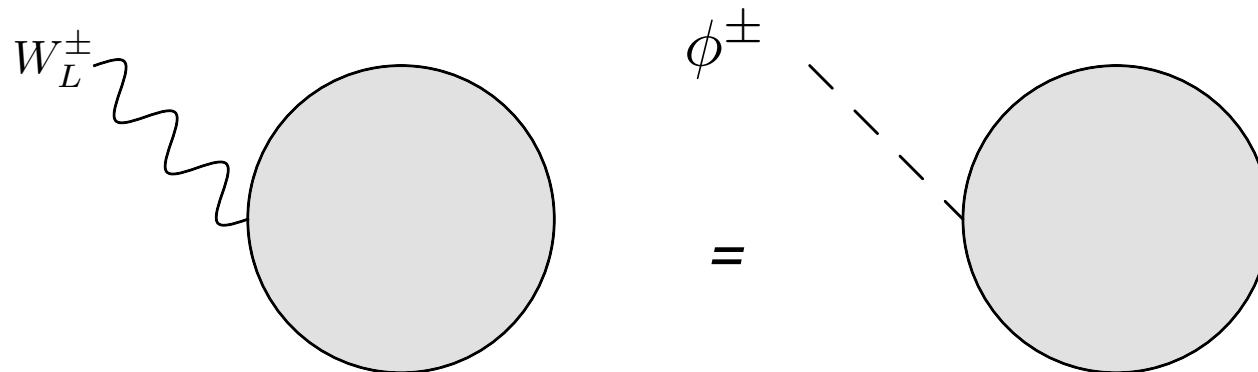
Feynman diagrams in SM

New channels and new approaches?

1. Higgs field in SM: Higgs boson and would-be Goldstone bosons form a SU(2) doublet:

$$\Phi^\pm = \begin{pmatrix} \phi^\pm \\ \frac{1}{\sqrt{2}}(h + i\phi^0) \end{pmatrix}$$

2. Goldstone equivalence theorem



- Parameterization scheme: SMEFT.

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i + \dots$$

- Related to Higgs physics

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} - c_6(\Phi^\dagger\Phi)^3 + c_{\Phi_1}\partial^\mu(\Phi^\dagger\Phi)\partial_\mu(\Phi^\dagger\Phi) + c_{\Phi_2}(\Phi^\dagger\overleftrightarrow{D}^\mu\Phi)^*(\Phi^\dagger\overleftrightarrow{D}_\mu\Phi) \\ & + c_{W^3}\epsilon^{abc}W_\mu^{a\nu}W_\nu^{b\rho}W_\rho^{b\mu} + c_{\Phi^2W^2}\Phi^\dagger\Phi W_{\mu\nu}^a W^{a\mu\nu} + c_{\Phi^2B^2}\Phi^\dagger\Phi B_{\mu\nu}B^{\mu\nu} \\ & + c_{\Phi^2WB}\Phi^\dagger\tau^a\Phi W_{\mu\nu}^a B^{\mu\nu} \end{aligned} \tag{1}$$

- c_6 and c_{Φ_1} modify Higgs potential

- Measuring Higgs couplings with longitudinal external states.

Higgs Couplings without the Higgs

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$$\kappa_t : pp \rightarrow jt + V_L V_L' \quad (4)$$

$$(e^+ e^- \rightarrow ll + \{tbW_L, tbZ_L, ttW_L, ttZ_L\})$$

$$\kappa_\lambda : pp \rightarrow jjh + V_L V_L', (e^+ e^- \rightarrow llhV_L V_L') \quad (5)$$

$$pp \rightarrow jj + 4V_L, (e^+ e^- \rightarrow ll4V_L) \quad (6)$$

$$\kappa_{\gamma\gamma, Z\gamma} : pp \rightarrow jj + V'V, (e^+ e^- \rightarrow llV'V) \quad (7)$$

$$\kappa_V : pp \rightarrow jj + V_L V_L', (e^+ e^- \rightarrow llV_L V_L') \quad (8)$$

$$\kappa_g : pp \rightarrow W_L^+ W_L^-, Z_L Z_L, (e^+ e^- \rightarrow lljj) \quad (9)$$

		HC	HwH	Growth
κ_t	\mathcal{O}_{yt}			$\sim \frac{E^2}{\Lambda^2}$
κ_λ	\mathcal{O}_6			$\sim \frac{vE}{\Lambda^2}$
$\kappa_{Z\gamma}$ $\kappa_{\gamma\gamma}$ κ_V	\mathcal{O}_{WW} \mathcal{O}_{BB} \mathcal{O}_r			$\sim \frac{E^2}{\Lambda^2}$
κ_g	\mathcal{O}_{gg}			$\sim \frac{E^2}{\Lambda^2}$

Kinda follow-up to this paper.

2 \rightarrow 3 Vector Boson Scattering:

- 1. $V_L V_L \rightarrow V_L V_L h : W_L^+ W_L^- \rightarrow W_L^+ W_L^- h$

- $V_L V_L \rightarrow h h h : W_L^+ W_L^- \rightarrow h h h$

- 2. Next: a). Amplitudes in high energy limit

- b). Simulation: cross sections in colliders

2 Amplitudes

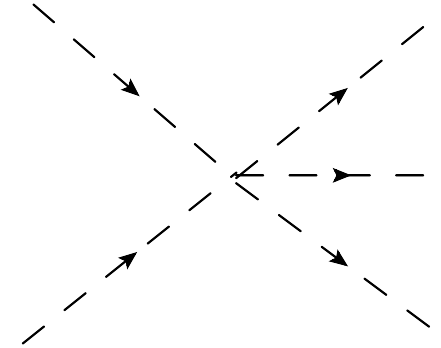
$$M(W_L W_L \rightarrow W_L W_L h) \simeq M(\phi\phi \rightarrow \phi\phi h)$$

(Focus on c6)

- 1. No propagator $(\Phi^\dagger\Phi)^3$ operator:

$$\mathcal{A}_0^{\phi^+\phi^- \rightarrow \phi^+\phi^- h} = \lambda_{(\phi^+\phi^-)^2 h} = -12C_6 v i$$

Since C_6 is suppressed by $\frac{1}{\Lambda^2}$, $\mathcal{A}_0 \sim \frac{v}{\Lambda^2}$.



Main entrance to modify Higgs coupling, the effect has to be strong.
(Amplitude sensitive to .)

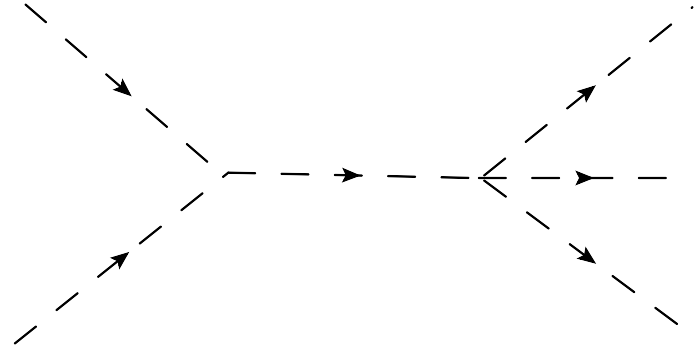
Same for $\phi^+\phi^- \rightarrow hhh$ ($W_L^+ W_L^- \rightarrow hhh$)

2. Amplitudes

Feynman diagrams

- 2. One propagator. 8 diagrams.

$$A_1 = \mathcal{M}'_4 \frac{i}{q^2 - m^2} \mathcal{M}'_3$$



$$\mathcal{A}_1^{BSM} \simeq -i2C_{\Phi_1} \frac{m_h^2}{v} \left(\frac{(p_1 + p_2)^2}{(p_4 + p_5)^2 - m_W^2} + \frac{(p_1 + p_2)^2}{(p_3 + p_5)^2 - m_W^2} + \frac{(p_1 - p_3)^2}{(p_2 - p_5)^2 - m_W^2} + \frac{(p_2 - p_4)^2}{(p_1 - p_5)^2 - m_W^2} \right) - iC_{\Phi_1} \frac{m_h^2}{v} \left(\frac{(p_1 + p_2)^2}{(p_3 + p_4)^2 - m_h^2} + \frac{(p_3 + p_4)^2}{(p_1 + p_2)^2 - m_h^2} + \frac{(p_1 - p_3)^2}{(p_2 - p_4)^2 - m_h^2} + \frac{(p_2 - p_4)^2}{(p_1 - p_3)^2 - m_h^2} \right) \quad (8)$$

So we have $\mathcal{A}_1^{BSM} \sim \frac{v}{\Lambda^2}$. $\mathcal{A}_1^{SM} \sim \frac{v}{E^2}$.

$\phi^+ \phi^- \rightarrow hhh$: effective number of diagrams = 4.

2 Amplitudes

Feynman diagrams

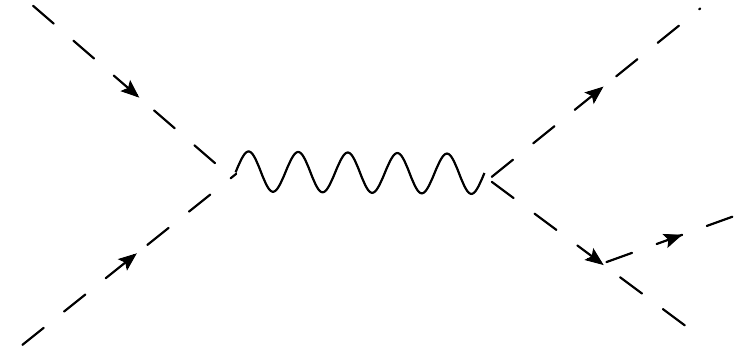
- 3. Two propagators. Full amplitude complicated, scaling simple.

$$A_2 \simeq A_2^a + A_2^b + A_2^c \sim \frac{v}{\Lambda^2} + \frac{v}{E^2}$$

- 47 diagrams (not conclusive).

-

- Effective no. of diagrams for $\phi^+ \phi^- \rightarrow hhh$: 8



2 Amplitudes

Summary of the amplitude

$$\mathcal{A}(W_L^+ W_L^- \rightarrow W_L^+ W_L^- h) = \mathcal{A}^{\text{SM}} + \mathcal{A}^{\text{BSM}} \quad (13)$$

with

$$\mathcal{A}^{\text{SM}} \simeq \frac{v}{E^2} \quad \mathcal{A}^{\text{BSM}} \simeq \frac{v}{\Lambda^2} \quad (14)$$

The ratio between BSM and SM is approximately

$$\frac{\mathcal{A}^{\text{BSM}}}{\mathcal{A}^{\text{SM}}} \sim \frac{E^2}{\Lambda^2} \quad (15)$$

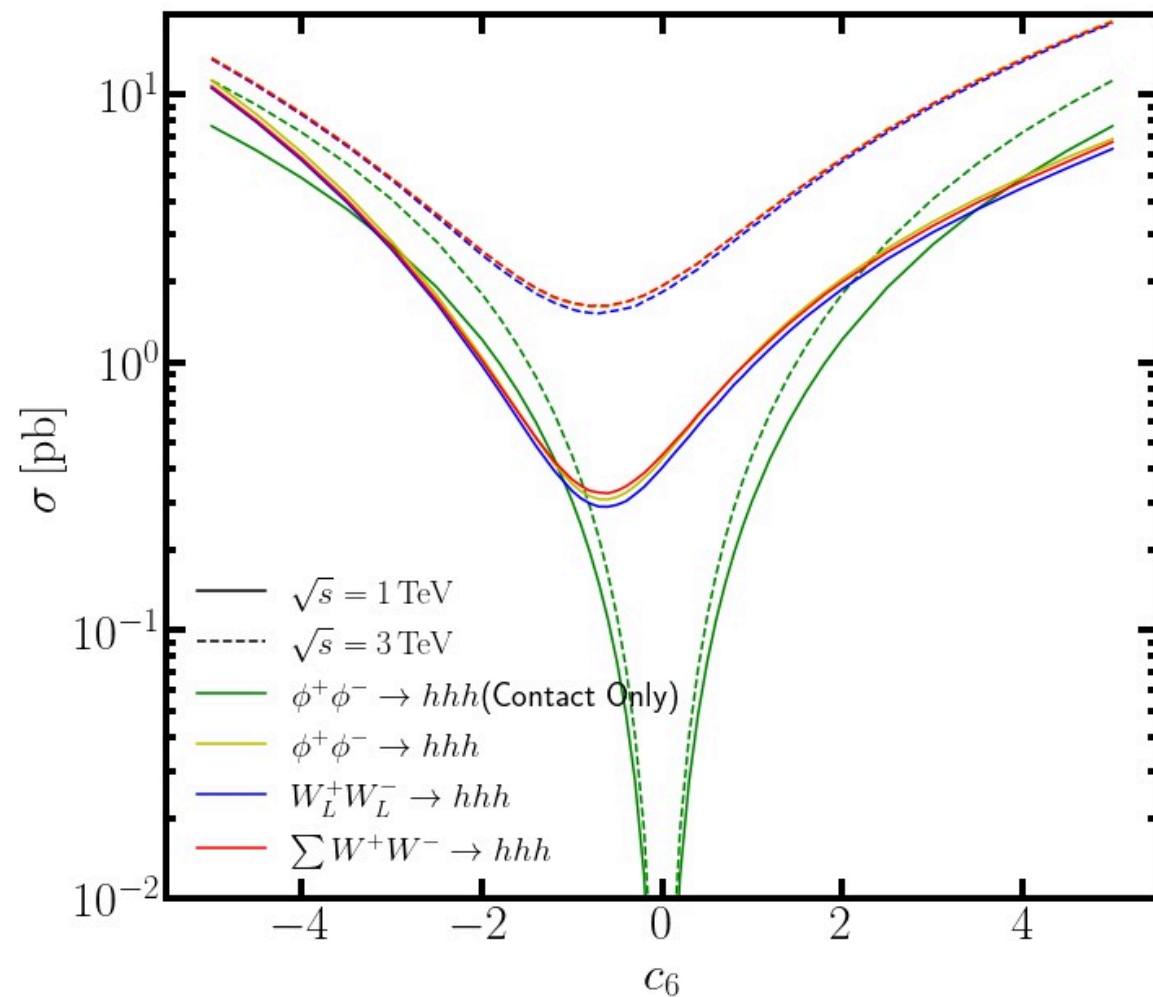
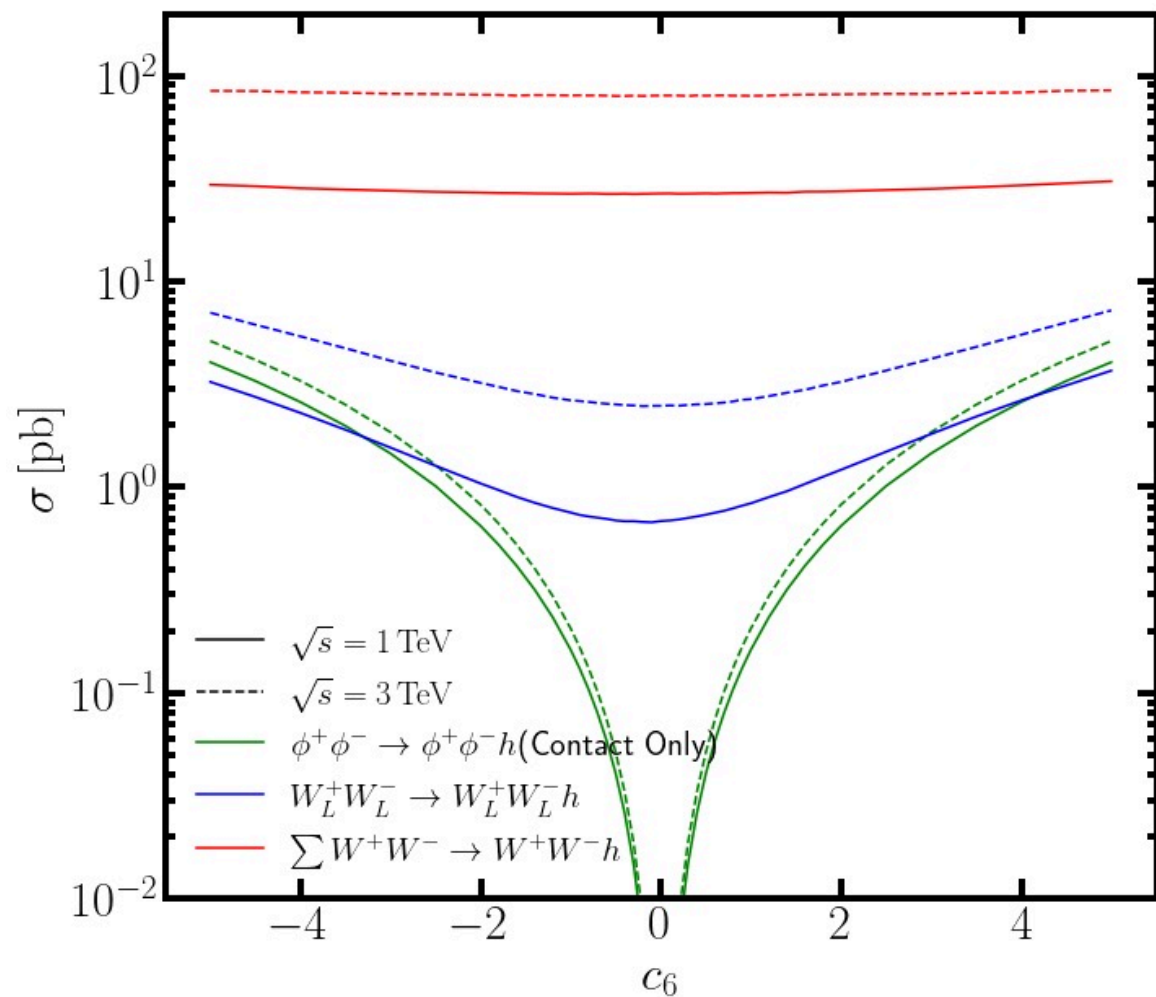
3. Cross section

- Amplitudes: $\frac{\mathcal{A}^{BSM}}{\mathcal{A}^{SM}} \sim \frac{E^2}{\Lambda^2}$
- Additional factors:
 - 1) Log enhancement from infrared singularities (soft, and collinear)
- Sensitivity to new physics don't necessary translate to cross sections

3 Cross section

Cross section: $V_L V_L \rightarrow V_L V_L h$ & $V_L V_L \rightarrow h h h$

- Plots with c_6 ($C_6 = c_6/\Lambda^2$), $\Lambda = 1\text{TeV}$



4. Full Simulation:

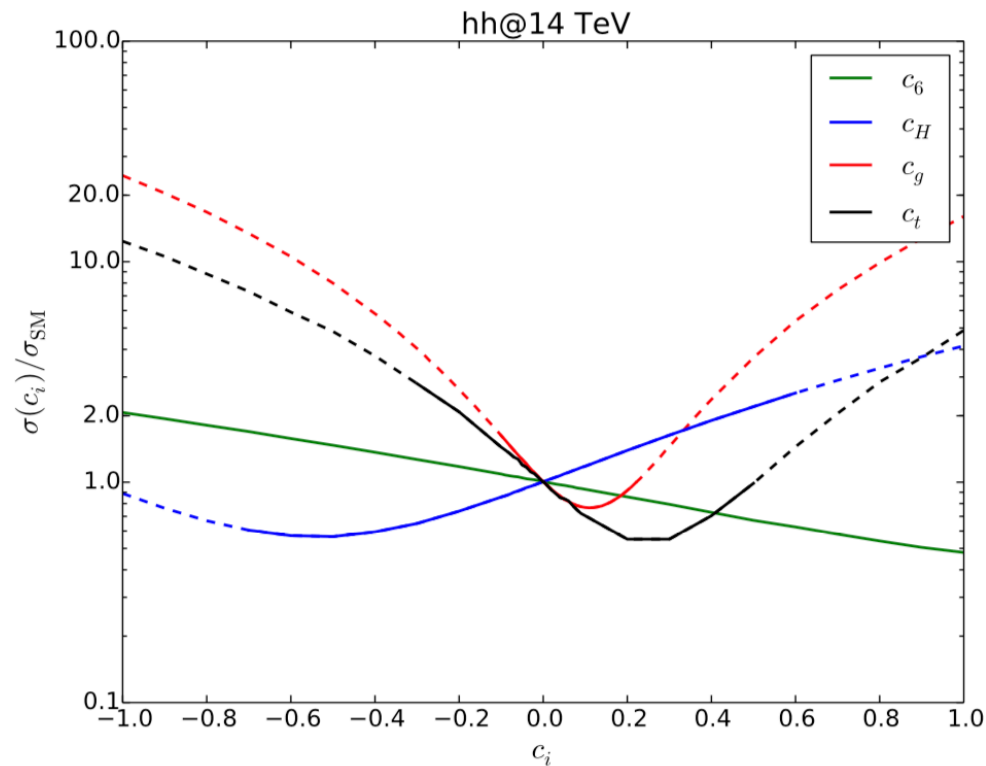
- 1. Processes on lepton colliders and proton colliders:

$$l^+l^- \rightarrow \nu_l \bar{\nu}_l W_L^+ W_L^- h \quad l^+l^- \rightarrow \nu_l \bar{\nu}_l h h h \quad (4.1)$$

$$pp \rightarrow jj W_L^\pm W_L^\pm h \quad pp \rightarrow jj h h h \quad (4.2)$$

- 2. Select for longitudinal polarizations

4. Full Simulation: Comparison with $pp > hh$



$$c'_6 \in [-1.0, 1.0], c'_H \in [-0.8, 0.6],$$

Translate to

$$c_6 \in [-1.8, 1.8] \quad c_{\Phi_1} \in [-6.6, 5.0]$$

Choice of range

$$c_6 \in [-2, 2] \quad c_{\Phi_1} \in [-2, 2]$$

Taken from arxiv: 1910.00012v2

4. Full Simulation: $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu W_L^+ W_L^- h$

Dependence on c_6 :

Cross sections (pb) for $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu W_L^+ W_L^- h$ ($c_{\Phi_1} = 0$, Scheme 2)					
c_6	-2	-1	0	1	2
1 TeV, cut 1	$4.17 \cdot 10^{-9}$	$1.57 \cdot 10^{-9}$	$8.22 \cdot 10^{-10}$	$1.93 \cdot 10^{-9}$	$4.90 \cdot 10^{-9}$
3 TeV, cut 1	$1.79 \cdot 10^{-6}$	$6.98 \cdot 10^{-6}$	$3.71 \cdot 10^{-7}$	$8.01 \cdot 10^{-7}$	$2.00 \cdot 10^{-6}$
5 TeV, cut 1	$6.10 \cdot 10^{-6}$	$2.43 \cdot 10^{-6}$	$1.32 \cdot 10^{-6}$	$2.74 \cdot 10^{-6}$	$6.72 \cdot 10^{-6}$
10 TeV, cut 1	$1.94 \cdot 10^{-5}$	$7.98 \cdot 10^{-6}$	$4.38 \cdot 10^{-6}$	$8.74 \cdot 10^{-6}$	$2.09 \cdot 10^{-5}$
14 TeV, cut 1	$2.99 \cdot 10^{-5}$	$1.25 \cdot 10^{-5}$	$7.11 \cdot 10^{-6}$	$1.36 \cdot 10^{-5}$	$3.22 \cdot 10^{-5}$
30 TeV, cut 1	$6.45 \cdot 10^{-5}$	$2.82 \cdot 10^{-5}$	$1.58 \cdot 10^{-5}$	$2.95 \cdot 10^{-5}$	$6.68 \cdot 10^{-5}$

Dependence on : C_{Φ_1}

Cross sections (pb) for $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu W_L^+ W_L^- h$ ($c_6 = 0$, Scheme 2)					
c_{Φ_1}	-2	-1	0	1	2
1 TeV, cut 0	$6.23 \cdot 10^{-7}$	$6.70 \cdot 10^{-7}$	$7.69 \cdot 10^{-7}$	$9.27 \cdot 10^{-7}$	$1.14 \cdot 10^{-6}$
3 TeV, cut 0	$2.65 \cdot 10^{-5}$	$2.34 \cdot 10^{-5}$	$2.47 \cdot 10^{-5}$	$2.96 \cdot 10^{-5}$	$3.95 \cdot 10^{-5}$
5 TeV, cut 0	$8.85 \cdot 10^{-5}$	$6.71 \cdot 10^{-5}$	$6.43 \cdot 10^{-5}$	$8.13 \cdot 10^{-5}$	$1.17 \cdot 10^{-4}$
10 TeV, cut 0	$4.09 \cdot 10^{-4}$	$2.22 \cdot 10^{-4}$	$1.71 \cdot 10^{-4}$	$2.61 \cdot 10^{-4}$	$4.72 \cdot 10^{-4}$
14 TeV, cut 0	$8.63 \cdot 10^{-4}$	$3.95 \cdot 10^{-4}$	$2.56 \cdot 10^{-4}$	$4.38 \cdot 10^{-4}$	$9.39 \cdot 10^{-4}$
30 TeV, cut 0	$4.97 \cdot 10^{-3}$	$1.60 \cdot 10^{-3}$	$5.07 \cdot 10^{-4}$	$1.66 \cdot 10^{-3}$	$5.04 \cdot 10^{-3}$

Dependence on c_6 :

- $\sigma/\sigma_{\text{SM}} > 4$

2. Requires PT cuts to reduce SM cross sections:

$$p_T(W^\pm) > 150 \text{ GeV} \text{ and } p_T(h) > 150 \text{ GeV.}$$

- $\sigma_{\text{SM}} < 10^{-5} \text{ pb}$ until 30 TeV

Dependence on C_{Φ_1} :

- $\sigma/\sigma_{\text{SM}} > 10$

2. No pT cuts required

- $\sigma_{\text{SM}} < 10^{-5} \text{ pb}$ until 3 TeV

$$\sigma_{\text{SM}} < 10^{-4} \text{ pb} \text{ until 10 TeV}$$

4. Full Simulation: $pp \rightarrow jjW_L^\pm W_L^\pm h$

Dependence on c_6 :

- $\sigma/\sigma_{\text{SM}} > 3$

- Requires PT cuts to reduce SM cross sections:

$$p_T(W^\pm) > 150 \text{ GeV} \text{ and } p_T(h) > 150 \text{ GeV. } \uparrow$$

- $\sigma_{\text{SM}} < 10^{-5} \text{ pb}$ until 100 TeV

Cross sections (pb) for $pp \rightarrow j_F j_F W_L^\pm W_L^\pm h$ (Scheme 2, $c_{\Phi_1} = 0$)					
c_6	-2	-1	0	1	2
14 TeV, cut 2	$6.35 \cdot 10^{-7}$	$2.81 \cdot 10^{-7}$	$1.68 \cdot 10^{-7}$	$3.01 \cdot 10^{-7}$	$6.79 \cdot 10^{-7}$
27 TeV, cut 2	$3.58 \cdot 10^{-6}$	$1.68 \cdot 10^{-6}$	$1.09 \cdot 10^{-6}$	$1.78 \cdot 10^{-6}$	$3.76 \cdot 10^{-6}$
100 TeV, cut 2	$3.28 \cdot 10^{-5}$	$1.82 \cdot 10^{-5}$	1.38×10^{-5}	1.87×10^{-5}	$3.34 \cdot 10^{-5}$

Cross sections (pb) for $pp \rightarrow j_F j_F W_L^\pm W_L^\pm h$ (Scheme 2, $c_6 = 0$)					
c_{Φ_1}	-2	-1	0	1	2
14 TeV, cut 3	$2.58 \cdot 10^{-5}$	$2.65 \cdot 10^{-5}$	$2.88 \cdot 10^{-5}$	$3.29 \cdot 10^{-5}$	$3.90 \cdot 10^{-5}$
27 TeV, cut 3	$1.27 \cdot 10^{-4}$	$1.20 \cdot 10^{-4}$	$1.27 \cdot 10^{-4}$	$1.49 \cdot 10^{-4}$	$1.83 \cdot 10^{-4}$
100 TeV, cut 3	$1.26 \cdot 10^{-3}$	$9.91 \cdot 10^{-4}$	$9.70 \cdot 10^{-4}$	$1.23 \cdot 10^{-3}$	$1.72 \cdot 10^{-3}$

4. Full Simulation: $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu hhh$

Cross sections (pb) for $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu hhh$ ($c_{\Phi_1} = 0$, Scheme 2)					
c_6	-2	-1	0	1	2
1 TeV, cut 0	$4.42 \cdot 10^{-8}$	$1.06 \cdot 10^{-8}$	$3.39 \cdot 10^{-9}$	$2.25 \cdot 10^{-8}$	$6.76 \cdot 10^{-8}$
3 TeV, cut 0	$1.93 \cdot 10^{-6}$	$5.66 \cdot 10^{-7}$	$2.78 \cdot 10^{-7}$	$1.08 \cdot 10^{-6}$	$2.94 \cdot 10^{-6}$
5 TeV, cut 0	$4.91 \cdot 10^{-6}$	$1.57 \cdot 10^{-6}$	$9.50 \cdot 10^{-7}$	$3.03 \cdot 10^{-6}$	$7.74 \cdot 10^{-6}$
10 TeV, cut 0	$1.25 \cdot 10^{-5}$	$4.59 \cdot 10^{-6}$	$3.46 \cdot 10^{-6}$	$8.75 \cdot 10^{-6}$	$1.95 \cdot 10^{-5}$
14 TeV, cut 0	$1.80 \cdot 10^{-5}$	$6.70 \cdot 10^{-6}$	$5.38 \cdot 10^{-6}$	$1.30 \cdot 10^{-5}$	$2.88 \cdot 10^{-5}$
30 TeV, cut 0	$3.50 \cdot 10^{-5}$	$1.77 \cdot 10^{-5}$	$1.41 \cdot 10^{-5}$	$2.92 \cdot 10^{-5}$	$5.42 \cdot 10^{-5}$

Cross sections (pb) for $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu hhh$ ($c_6 = 0$, Scheme 2)				
c_{Φ_1}	-2	-1	1	2
1 TeV, cut 0	$2.78 \cdot 10^{-8}$	$1.08 \cdot 10^{-8}$	$5.56 \cdot 10^{-9}$	$1.73 \cdot 10^{-8}$
3 TeV, cut 0	$3.01 \cdot 10^{-6}$	$1.11 \cdot 10^{-6}$	$5.43 \cdot 10^{-7}$	$1.89 \cdot 10^{-6}$
5 TeV, cut 0	$1.33 \cdot 10^{-5}$	$4.47 \cdot 10^{-6}$	$2.38 \cdot 10^{-6}$	$8.76 \cdot 10^{-6}$
10 TeV, cut 0	$7.83 \cdot 10^{-5}$	$2.38 \cdot 10^{-5}$	$1.50 \cdot 10^{-5}$	$5.97 \cdot 10^{-5}$
14 TeV, cut 0	$1.77 \cdot 10^{-4}$	$4.97 \cdot 10^{-5}$	$3.73 \cdot 10^{-5}$	$1.44 \cdot 10^{-4}$
30 TeV, cut 0	$1.07 \cdot 10^{-3}$	$2.77 \cdot 10^{-4}$	$2.44 \cdot 10^{-4}$	$9.86 \cdot 10^{-4}$

Table 2: The same as Table 1 except for the $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu hhh$ process.

Dependence on c_6 and c_{Φ_1} :

1. $\sigma / \sigma_{\text{SM}} > 3$
2. No PT cuts required
3. $\sigma_{\text{SM}} < 10^{-5} \text{ pb}$ until 30 TeV

4. Full Simulation: $pp \rightarrow jjhhh$

Cross sections (pb) for $pp \rightarrow j_F j_F hhh$ (Scheme 2, $c_{\Phi_1} = 0$).					
c_6	-2	-1	0	1	2
14 TeV, cut 3	$1.99 \cdot 10^{-6}$	$5.77 \cdot 10^{-7}$	$2.97 \cdot 10^{-7}$	$1.16 \cdot 10^{-6}$	$3.12 \cdot 10^{-6}$
27 TeV, cut 3	$9.46 \cdot 10^{-6}$	$2.93 \cdot 10^{-6}$	$1.50 \cdot 10^{-6}$	$5.48 \cdot 10^{-6}$	$1.45 \cdot 10^{-5}$
100 TeV, cut 3	$7.91 \cdot 10^{-5}$	$2.65 \cdot 10^{-5}$	$1.48 \cdot 10^{-5}$	$4.30 \cdot 10^{-5}$	$1.13 \cdot 10^{-4}$

Cross sections (pb) for $pp \rightarrow j_F j_F hhh$ (Scheme 2, $c_6 = 0$).				
c_{Φ_1}	-2	-1	1	2
14 TeV, cut 3	$2.94 \cdot 10^{-6}$	$1.10 \cdot 10^{-6}$	$5.33 \cdot 10^{-7}$	$1.83 \cdot 10^{-6}$
27 TeV, cut 3	$1.97 \cdot 10^{-5}$	$6.99 \cdot 10^{-6}$	$3.75 \cdot 10^{-6}$	$1.35 \cdot 10^{-5}$
100 TeV, cut 3	$3.31 \cdot 10^{-4}$	$1.02 \cdot 10^{-4}$	$7.04 \cdot 10^{-5}$	$2.69 \cdot 10^{-4}$

Table 4: The same as Table 3 except for the $pp \rightarrow j_F j_F hhh$ process.

Dependence on c_6 and c_{Φ_1} :

- $\sigma / \sigma_{\text{SM}} > 6$

- No PT cuts required

- $\sigma_{\text{SM}} < 10^{-5} \text{ pb}$ until 100 TeV

Conclusions

- In high energy, Amplitudes of $V_L V_L \rightarrow V_L V_L$ or hhh $\frac{\mathcal{A}^{BSM}}{\mathcal{A}^{SM}} \sim \frac{E^2}{\Lambda^2}$
- Origin: 5-point scalar vertices from c_6 operator.
- Behavior of cross section follows for $pp \rightarrow jjhhh$ $l^+ l^- \rightarrow \nu_l \bar{\nu}_L hhh$
- Cuts are needed for $pp \rightarrow jjW_L^\pm W_L^\pm h$ $l^+ l^- \rightarrow \nu_l \bar{\nu}_l W_L^+ W_L^- h$
- Cross sections only large enough for future muon colliders and 100 TeV pp colliders for c_6 dependence