

# NEUTRINO MASSES AND HUBBLE TENSION VIA A MAJORON IN MFV



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# Outline

- Introduction
- The Majoron Mechanism
- The Majoron and Axion from a MFV Setup
- Phenomenological Signatures
- Conclusions

# Introduction

- The Hubble Tension:

L. Verde, T. Treu, and A. Riess, 1907.10625

- Early Universe vs local measurements of  $H_0$  differ up to  $4 - 6 \sigma$

K. C. Wong et. al., H0LiCOW XIII, 1907.04869

- This may be solved by:

- Systematics

- New cosmological model

- **Particle physics. E.g.: a Majoron** M. Escudero and S. J. Witte, 1909.04044

- Study its compatibility with solutions to other SM problems

- Light neutrino masses  $\rightarrow$  Type-I Seesaw

- Flavour puzzle  $\rightarrow$  flavour continuous global symmetries

- Strong CP Problem  $\rightarrow$  Axion

# Introduction

- The Majoron,  $\omega$ , is the NGB associated to the breaking of LN
- For it to alleviate the  $H_0$  tension it needs:
  - A mass in the range of

$$m_\omega \in [0.1, 1] \text{ eV}$$

- Coupling to neutrinos of order

$$\lambda_{\omega\nu\nu} \in [5 \times 10^{-14}, 10^{-12}]$$

- Phenomenology of this Majoron in a Type-I Seesaw
  - **Collider signatures:**  $N_R$ , Higgs invisible decay, new scalar
  - Astrophysical effects: CAST and Red Giant observations
  - Majoron emission in  $0\nu\beta\beta$  decays

# The Majoron Mechanism

- SM extended with 3 RH neutrinos and a singlet scalar  $\chi$ , with LN  $-L_N$  and  $L_\chi$  respectively

$$-\mathcal{L}_\nu = \left(\frac{\chi}{\Lambda_\chi}\right)^{\frac{1+L_N}{L_\chi}} \bar{l}_L \tilde{H} y_\nu N_R + \frac{1}{2} \left(\frac{\chi}{\Lambda_\chi}\right)^{\frac{2L_N-L_\chi}{L_\chi}} \chi \bar{N}_R^c y_N N_R + \text{h. c.}, \quad \chi = \frac{\sigma + v_\chi}{\sqrt{2}} e^{i\frac{\omega}{v_\chi}}, \quad \varepsilon_\chi = \frac{v_\chi}{\sqrt{2}\Lambda_\chi}$$

- Heavy and light neutrino masses generated after LN SSB

$$m_\nu = \frac{\varepsilon_\chi^{\frac{2+L_\chi}{L_\chi}} v^2}{\sqrt{2}v_\chi} y_\nu y_N^{-1} y_\nu^T, \quad m_N = \varepsilon_\chi^{\frac{2L_N-L_\chi}{L_\chi}} \frac{v_\chi}{\sqrt{2}} y_N$$

- Axion coupling to light neutrinos:

$$\mathcal{L}_\omega^{\text{low-energy}} \supset i \frac{\lambda_{\omega\nu\nu}}{2} \omega \bar{\nu}_L \nu_L^c, \quad \lambda_{\omega\nu\nu} = 2 \frac{m_\nu}{L_\chi v_\chi}$$

# The Majoron Mechanism

- Combining those expressions with the bound on  $\lambda_{\omega\nu\nu}$

$$|L_\chi| \varepsilon_\chi^{\frac{2+L_\chi}{L_\chi}} \mathbf{y}_\nu \mathbf{y}_N^{-1} \mathbf{y}_\nu^T \in [1.2 \times 10^{-13}, 2.4 \times 10^{-12}]$$
$$\frac{\varepsilon_\chi^{\frac{2L_N-L_\chi}{L_\chi}}}{|L_\chi|} \mathbf{y}_N \gg 3.5 \times 10^{-14}$$

- A renormalizable scenario is possible, but it is very fine-tuned

$$L_N = -1, L_\chi = -2$$

$$\mathbf{y}_\nu \mathbf{y}_N^{-1} \mathbf{y}_\nu^T \in [1.2 \times 10^{-13}, 2.4 \times 10^{-12}]$$

- Can fine-tuning be avoided exploiting  $\varepsilon_\chi$ ?

# The Majoron Mechanism

- Two phenomenologically interesting non-renormalizable scenarios:

	$L_N$	$L_\chi$	$v_\chi$	$\varepsilon_\chi$	$\langle M_N \rangle$	$\Lambda_\chi$
CASE NR1	1	1	[0.1, 2] TeV	$[0.49, 1.4] \times 10^{-4}$	[3.5, 200] MeV	$[1.4 - 11] \times 10^3$ TeV
CASE NR2	1	2	[0.05, 1] TeV	$[2.4, 11] \times 10^{-7}$	[35.4, 707] GeV	$[1.4 - 6.5] \times 10^5$ TeV

# The Majoron Mechanism

- Apart from a small coupling to neutrinos, the Majoron needs a specific mass
  - Wormhole effects fall short [R. Alonso and A. Urbano, 1706.07415](#)
  - Planck-suppressed operators provide a mass too large [E. K. Akhmedov et al., hep-ph/9209285](#)
  - Explicit breaking of LN via a Majorana mass term
- Additional scalar d.o.f. to the Majoron: the radial part of  $\chi$ ,  $\sigma$
- Through the quartic coupling  $gH^\dagger H\chi^*\chi$ ,  $h$  and  $\sigma$  mix with an angle  $\vartheta$

$$g = \frac{M_\sigma^2 - M_h^2}{2vv_\chi} \sin 2\vartheta$$

$$\sin^2 \vartheta \lesssim 0.11 \quad \text{ATLAS Collaboration, 1909.02845}$$

# The Majoron and Axion from a MFV setup

R. S. Chivukula and H. Georgi, PLB 188, 99-104 (1987)

- Minimal Flavour Violation assumption: only Yukawas violate flavour symmetry

- Flavour Symmetry Group identified in the limit of vanishing Yukawas D'Ambrosio et al., 020736  
Cirigliano et al., 0507001

$$\mathcal{G}_F = U(3)_{q_L} \times U(3)_{u_R} \times U(3)_{d_R} \times U(3)_{l_L} \times U(3)_{N_R} \times U(3)_{e_R}$$

$$\mathcal{G}_F \supset \mathcal{G}_F^A = U(1)_B \times U(1)_L \times U(1)_Y \times U(1)_{PQ} \times U(1)_{e_R} \times U(1)_{N_R}$$

- The PQ charges are chosen to explain  $m_b/m_t$  and  $m_\tau/m_t$

$$x_{q_L} = x_{l_L} = x_{u_R} = x_{N_R} = 0, x_{d_R} = x_{e_R} = 3 \quad \text{FAA \& Merlo, 1709.07039}$$

- As with LN, PQ is made an exact symmetry by the addition of a scalar field  $\Phi$  with  $x_\Phi = -1$

$$\Phi = \frac{\rho + v_\Phi}{\sqrt{2}} e^{i\frac{a}{v_\Phi}}$$

# The Majoron and Axion from a MFV setup

$$\begin{aligned}
 -\mathcal{L}_Y = & \bar{q}_L \tilde{H} \mathcal{Y}_u u_R + \left( \frac{\Phi}{\Lambda_\Phi} \right)^3 \bar{q}_L H \mathcal{Y}_d d_R + \left( \frac{\Phi}{\Lambda_\Phi} \right)^3 \bar{l}_L H \mathcal{Y}_e e_R \\
 & + \left( \frac{\chi}{\Lambda_\chi} \right)^{\frac{1+L_N}{L_\chi}} \bar{l}_L \tilde{H} \mathcal{Y}_\nu N_R + \frac{1}{2} \left( \frac{\chi}{\Lambda_\chi} \right)^{\frac{2L_N-L_\chi}{L_\chi}} \chi \bar{N}_R^c \mathcal{Y}_N N_R + \text{h.c.}
 \end{aligned}$$

- The matrices  $\mathcal{Y}_{u,d,e,\nu,N}$  must become spurions transforming under the non-Abelian part of  $\mathcal{G}_F$

$$\langle \mathcal{Y}_u \rangle = c_t V^\dagger \text{diag} \left( \frac{m_u}{m_t}, \frac{m_c}{m_t}, 1 \right), \langle \mathcal{Y}_d \rangle = c_b \text{diag} \left( \frac{m_d}{m_b}, \frac{m_d}{m_b}, 1 \right), \langle \mathcal{Y}_e \rangle = c_\tau \text{diag} \left( \frac{m_e}{m_\tau}, \frac{m_e}{m_\tau}, 1 \right)$$

- The PQ SSB explains the  $m_b/m_t$  and  $m_\tau/m_t$  ratios assuming

$$\frac{v_\Phi}{\sqrt{2}\Lambda_\Phi} \simeq 0.23$$

- Non-renormalizable flavour violating operators are Yukawa suppressed: 1 – 10 TeV scale, accessible at colliders

# The Majoron and Axion from a MFV setup

- MFV in the lepton sector:  $\mathcal{Y}_\nu$  and  $\mathcal{Y}_N$  cannot be directly identified in terms of neutrino masses or the PMNS elements.

- Two possible ways out:

Cirigliano et al., 0507001

- $G_L^{NA} = SU(3)_{l_L} \times SU(3)_{e_R} \times SO(3)_{N_R} \times CP \Rightarrow \mathcal{Y}_N \propto \mathbb{1}, \mathcal{Y}_\nu \in \mathbb{R}$  S. Davidson and F. Palorini, hep-ph/0607329

$$m_\nu = \frac{\varepsilon_\chi^{L_\chi} v^2}{\sqrt{2} v_\chi} \mathcal{Y}_\nu \mathcal{Y}_\nu^T$$

- $G_L^{NA} = SU(3)_{l_L+N_R} \times SU(3)_{e_R} \Rightarrow \mathcal{Y}_\nu \propto \mathbb{1}$  R. Alonso et al., 1103.5461

$$m_\nu = \frac{\varepsilon_\chi^{L_\chi} v^2}{\sqrt{2} v_\chi} \mathcal{Y}_N^{-1}$$

- The axion arising from the PQ SSB couples to gluons and behaves as the usual QCD Axion solving the Strong CP Problem

N. Viaux et al., 1311.1669

$$m_a \sim 6 \mu\text{eV} \left( \frac{10^{12} \text{GeV}}{f_a} \right), \quad f_a = \frac{v_\Phi}{9} \gtrsim 8 \times 10^8 \text{ GeV}$$

O. Straniero et al., 1802.10357

S. A. Díaz et al., 1910.10568

# Phenomenological Signatures

- Coupling to photons

$$\mathcal{L}_\omega^{low-energy} \supset \frac{1}{4} \lambda_{\omega\gamma\gamma} \omega F^{\mu\nu} \tilde{F}_{\mu\nu}, \quad \lambda_{\omega\gamma\gamma} \lesssim 10^{-10} \text{ GeV}^{-1} \quad \text{CAST Collaboration, 1705.02290}$$

- Matching the effective coupling with the 2 loop explicit expression yields [C. García-Cely and J. Heeck, 1701.07209](#)

$$\lambda_{\omega\gamma\gamma} = \frac{\alpha m_\omega^2}{384\sqrt{2}\pi^3 m_e^2 v_\chi} \epsilon_\chi^{\frac{2+2L_N}{L_\chi}} \text{Tr}(y_\nu y_\nu^\dagger)$$

- Coupling to electrons

$$\mathcal{L}_\omega^{low-energy} \supset i\lambda_{\omega ee} \omega \bar{e}e, \quad \lambda_{\omega ee} \lesssim 4.3 \times 10^{-13} \quad \text{N. Viaux et al., 1311.1669}$$

- The explicit expression can be found at the 1 loop level [C. García-Cely and J. Heeck, 1701.07209](#)

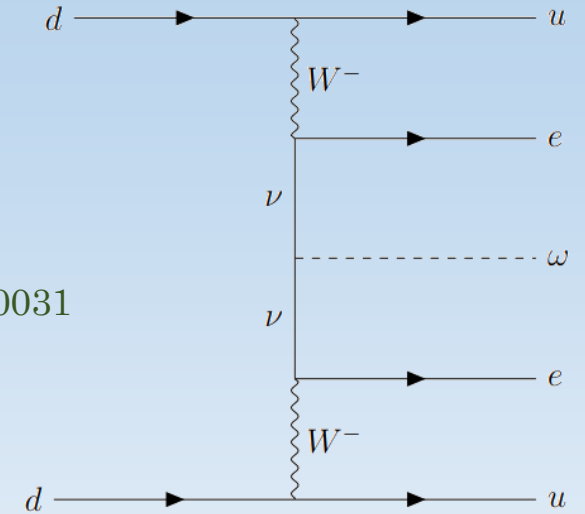
$$\lambda_{\omega ee} = \frac{1}{16\pi^2} \frac{m_e}{v_\chi} \epsilon_\chi^{\frac{2+2L_N}{L_\chi}} \left( (y_\nu y_\nu^\dagger)_{11} - \text{Tr}(y_\nu y_\nu^\dagger) \right)$$

# Phenomenological Signatures

- Coupling to neutrinos

- Constrained by Majoron emission in  $0\nu\beta\beta$  decays

$$\lambda_{\omega\nu\nu} < 10^{-5} \quad \text{R. Cepedello et al., 1811.00031}$$



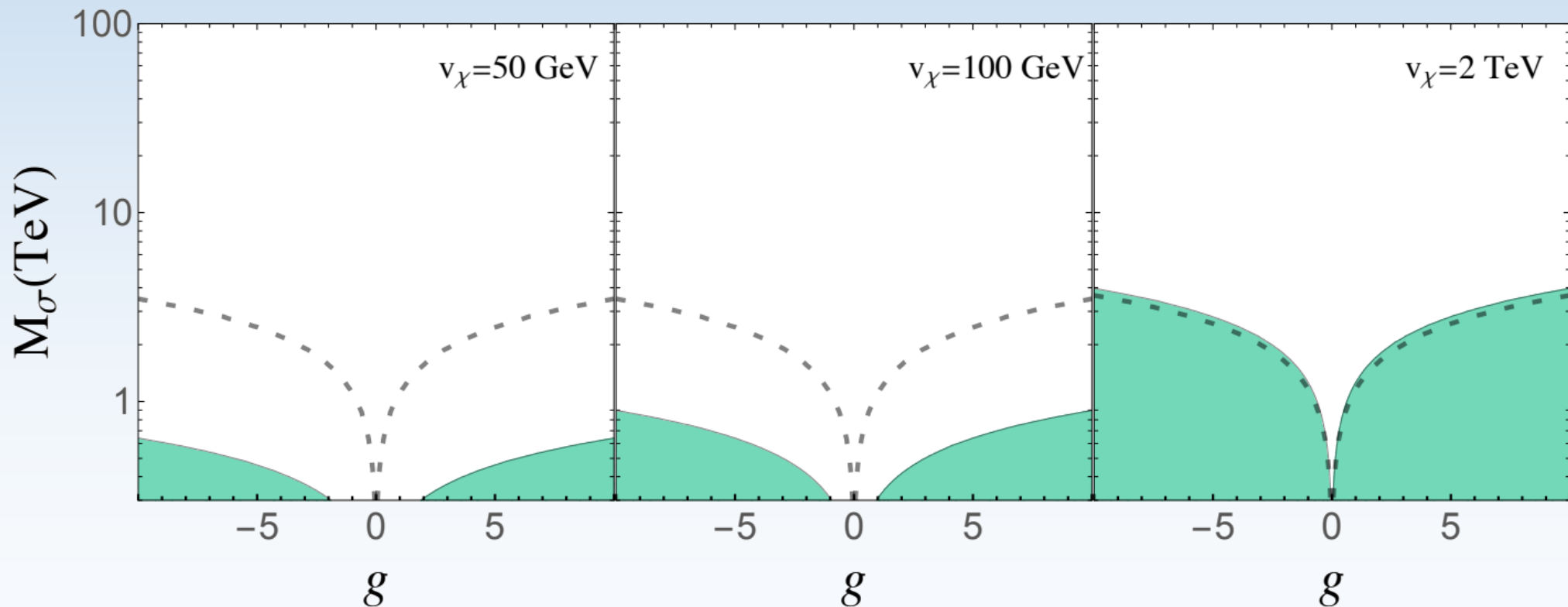
	$\lambda_{\omega\gamma\gamma}$	$\lambda_{\omega ee}$	$\lambda_{\omega\nu\nu}$
CASE NR1	$[10^{-39}, 10^{-36}] \text{ GeV}^{-1}$	$[10^{-25}, 10^{-24}]$	$[10^{-14}, 10^{-12}]$
CASE NR2	$[10^{-34}, 10^{-32}] \text{ GeV}^{-1}$	$10^{-20}$	
Exp. Upper bounds	$10^{-10} \text{ GeV}^{-1}$	$10^{-13}$	$10^{-5}$

# Phenomenological Signatures

- Coupling with the Higgs

- Apart from the  $h - \sigma$  mixing angle  $\vartheta$ , the Higgs invisible decay  $h \rightarrow \omega\omega$  is constrained

CMS collaboration, 1809.05937  $\Gamma_{h \rightarrow \omega\omega} = \frac{\sin^2 \vartheta M_h^3}{32\pi v_\chi^2} \lesssim 0.8 \text{ MeV} \Rightarrow \frac{v_\chi}{|\sin \vartheta|} \gtrsim 5 \text{ TeV}$



# Phenomenological Signatures

- Heavy neutrinos
  - Case NR1 testable at beam dump experiments or near detectors at oscillation experiments like DUNE or SHiP
  - Case NR2 interesting for production at LHC or future colliders
- $N \rightarrow 3\nu$  in the early universe may disfavour some scenarios
  - If it happens after BBN, as it may happen in Case NR1 with  $\langle M_N \rangle \in [3.5, 200]$  MeV, the light-heavy neutrino mixing  $\theta_s$  is bound by

$$\sin^2 \theta_s \equiv \frac{\langle m_\nu \rangle}{\langle M_N \rangle} \lesssim 10^{-15} - 10^{-17} \quad \text{A. C. Vincent et al., 1408.1956}$$

- The heavier masses in Case NR2 allow for decay before BBN, evading that cosmological bound

	$\langle M_N \rangle$	$\sin^2 \theta_s$	$\Gamma_{N \rightarrow 3\nu}^Z$	$\Gamma_{N \rightarrow 3\nu}^\omega$
CASE NR1	[3.5, 200] MeV	$[2.5 \times 10^{-10}, 1.4 \times 10^{-8}]$	$\mathcal{O}(10^{-38})$	$\mathcal{O}(10^{-68})$
CASE NR2	[35.4, 707] GeV	$[7.1 \times 10^{-14}, 1.4 \times 10^{-12}]$	$\mathcal{O}(10^{-27})$	$\mathcal{O}(10^{-66})$

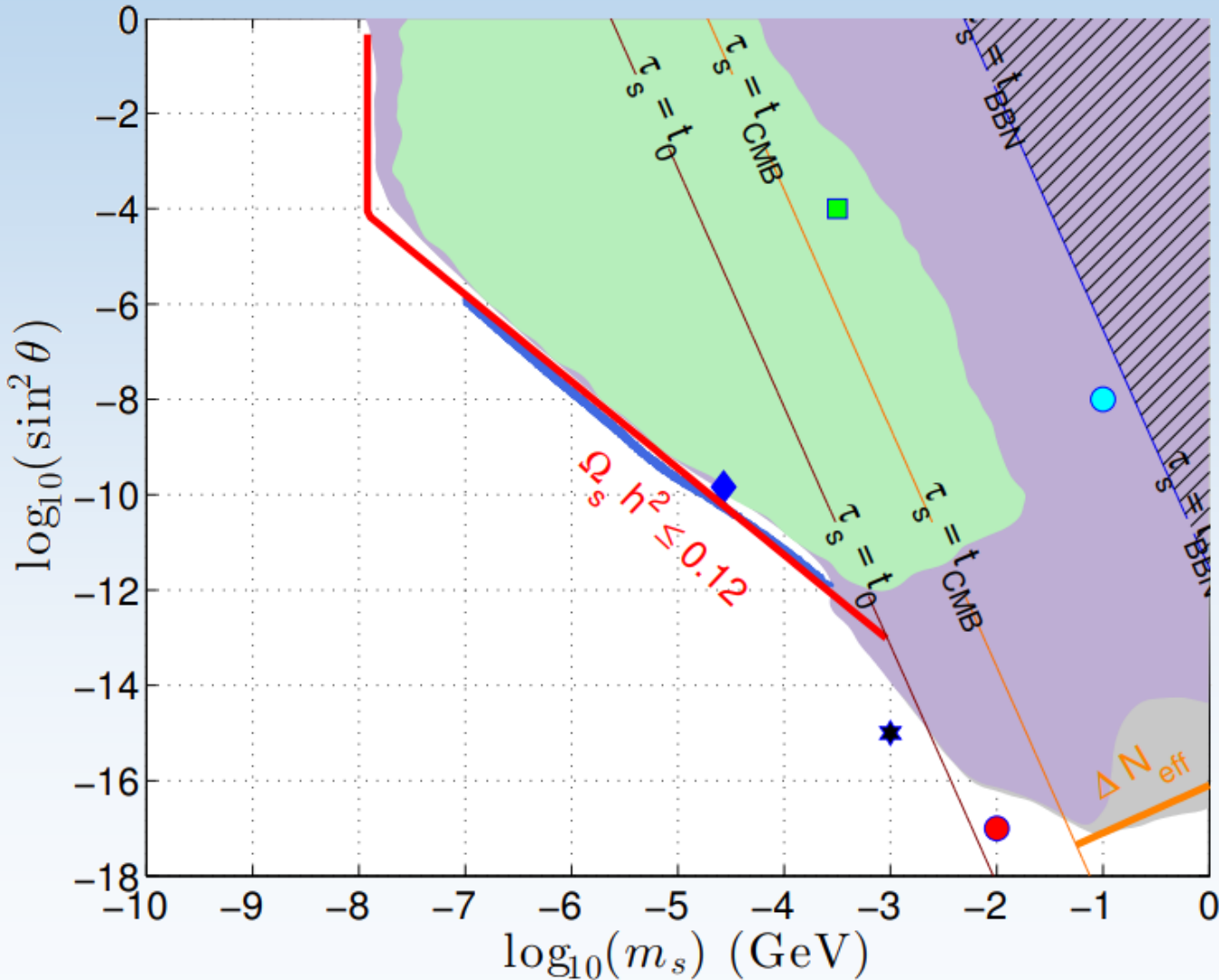
# Conclusions

- Majorons can alleviate the Hubble tension
- The smallness of neutrino masses was addressed here with a Majoron
- This Majoron can easily be embedded in MFV, where also a QCD axion can arise
- Cosmology sets strong bounds
- Colliders may see several signals: “Light” Heavy neutrinos, new scalar or Higgs invisible decay

THANK YOU FOR  
YOUR ATTENTION

# BACKUP SLIDES

# Phenomenological Signatures



Plot from A. C. Vincent, E. F. Martínez, P. Hernández, M. Lattanzi, and O. Mena, 1408.1956

	$\langle M_N \rangle$	$\sin^2 \theta_s$
CASE NR1	[3.5, 200] MeV	$[2.5 \times 10^{-10}, 1.4 \times 10^{-8}]$

# The Majoron Mechanism

- Two phenomenologically interesting non-renormalizable scenarios:

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- Other possibilities
  - $L_N > 0, L_\chi < 0 \Rightarrow \chi \leftrightarrow \chi^\dagger$
  - $L_N < 0, L_\chi > 0 \Rightarrow$  non-local
  - $L_N = L_\chi = -1 \Rightarrow m_\nu \propto \varepsilon_\chi^{-1}$ , highly fine-tuned