

# Probing extended Higgs sectors by the synergy between the LHC and the ILC

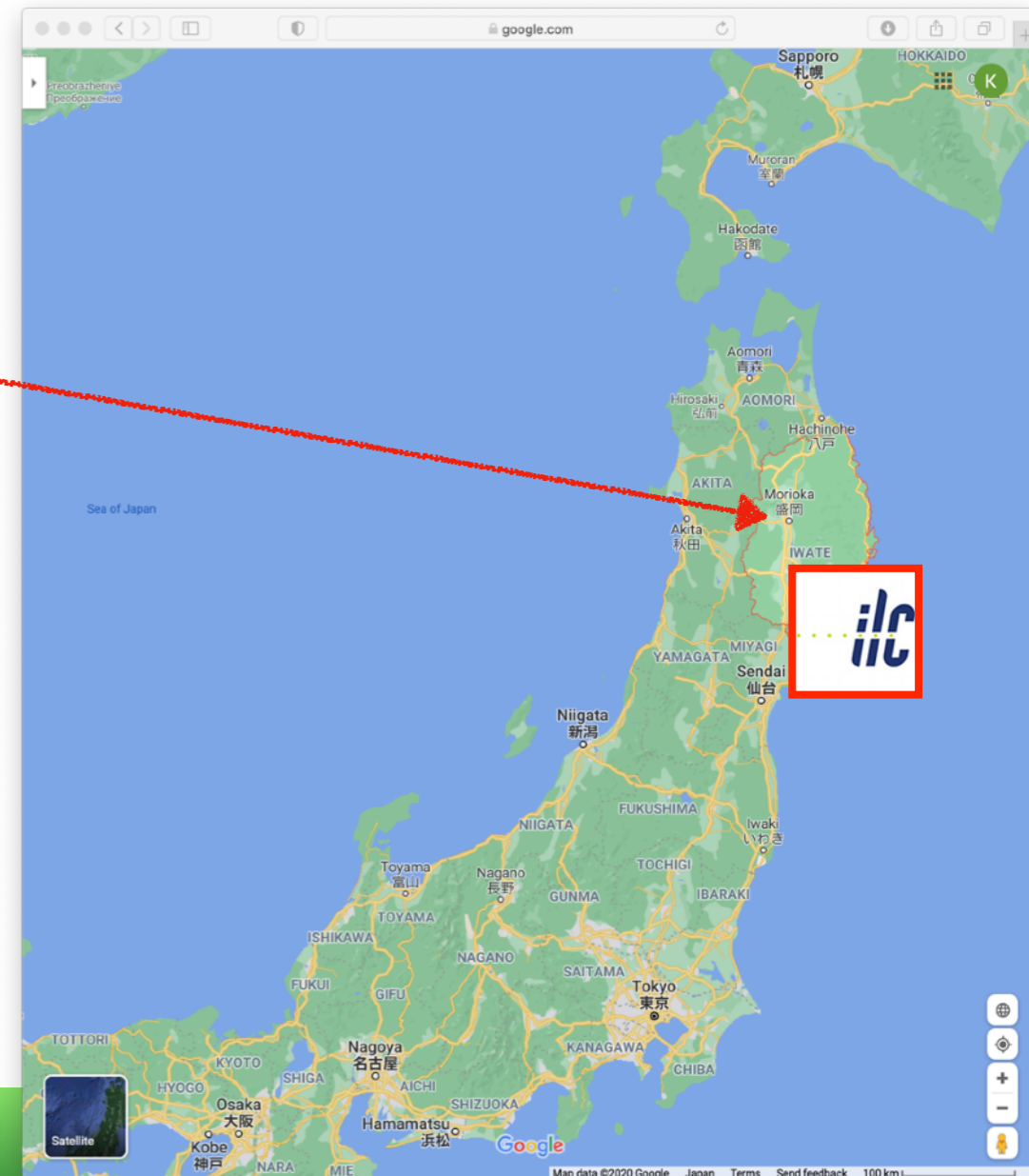
Kentarou Mawatari



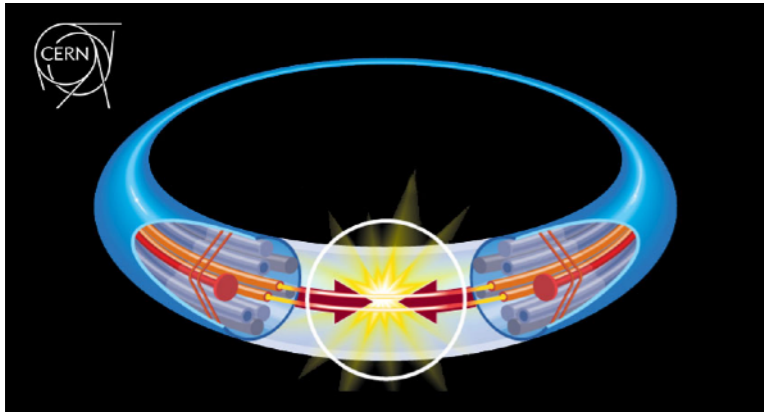
[\[arXiv: 2010.15057, appear in NPB\]](#)

in collaboration with

Masashi Aiko (Osaka U.)  
Shinya Kanemura (Osaka U.)  
Mariko Kikuchi (Kitakyushu College)  
Kodai Sakurai (Karlsruhe)  
Kei Yagyu (Osaka U.)



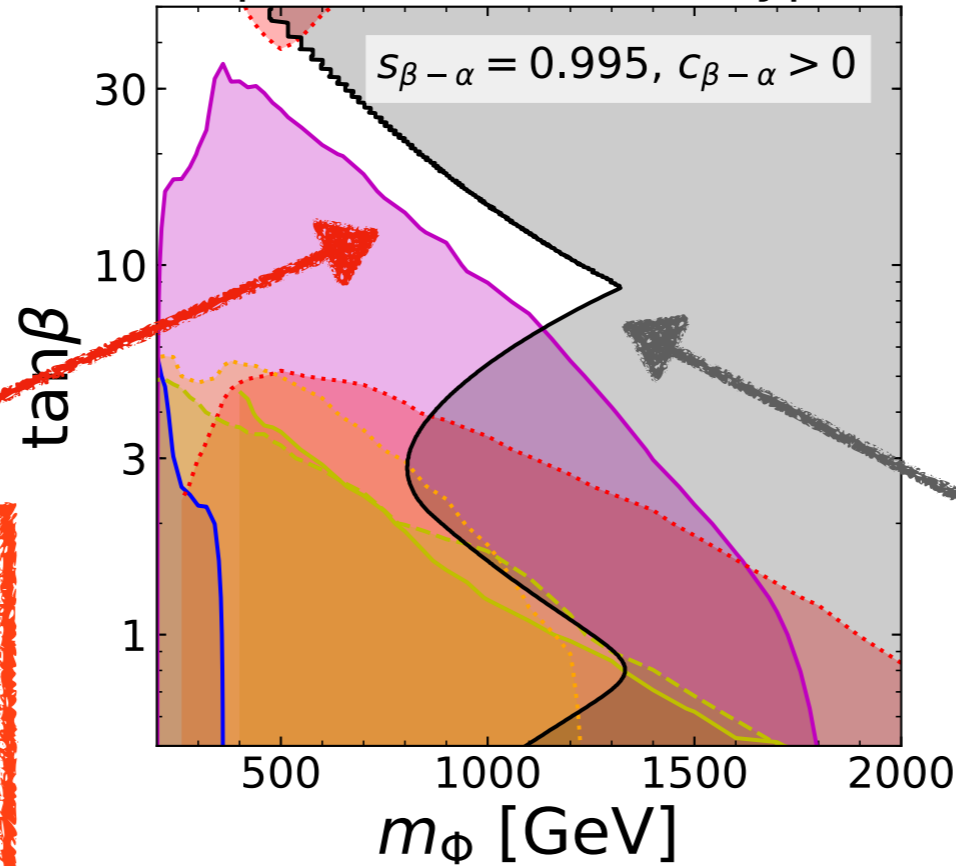
# Contents of my talk



synergy



Expected exclusion; Type-I



The direct searches for additional Higgs bosons give lower limits of the masses.

The precision measurements for the SM-like Higgs boson set upper limits of the masses.

# Introduction

- We are seeking for **BSM** physics.
  - Many BSM models require some **extensions of the Higgs sector**, e.g. MSSM.
  - **Two Higgs doublet models** (THDMs) are one of the simplest extensions, but immediately provides us rich theoretical and experimental discussions.
- ➡ Let's take THDMs as our benchmark model to explore BSM physics!

# THDM: Two Higgs doublet model

$$V(\Phi_1, \Phi_2) = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_3^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} \lambda_5 [(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}]$$

$$\Phi_i = \begin{pmatrix} w_i^+ \\ \frac{1}{\sqrt{2}}(v_i + h_i + iz_i) \end{pmatrix} \quad v = (v_1^2 + v_2^2)^{1/2} \\ \tan \beta = v_2/v_1$$

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R(\alpha) \begin{pmatrix} H \\ h \end{pmatrix}, \quad \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = R(\beta) \begin{pmatrix} G^0 \\ A \end{pmatrix}, \quad \begin{pmatrix} w_1^\pm \\ w_2^\pm \end{pmatrix} = R(\beta) \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

$$m_{H^\pm}^2 = M^2 - \frac{1}{2} v^2 (\lambda_4 + \lambda_5),$$

$$m_A^2 = M^2 - v^2 \lambda_5,$$

$$m_H^2 = M_{11}^2 c_{\beta-\alpha}^2 + M_{22}^2 s_{\beta-\alpha}^2 - M_{12}^2 s_{2(\beta-\alpha)}, \quad M_{11}^2 = v^2 (\lambda_1 c_\beta^4 + \lambda_2 s_\beta^4 + \lambda_{345} s_\beta^2 c_\beta^2),$$

$$m_h^2 = M_{11}^2 s_{\beta-\alpha}^2 + M_{22}^2 c_{\beta-\alpha}^2 + M_{12}^2 s_{2(\beta-\alpha)}, \quad M_{22}^2 = M^2 + \frac{1}{2} v^2 s_{2\beta}^2 (\lambda_1 + \lambda_2 - 2\lambda_{345}),$$

$$\tan 2(\beta - \alpha) = -\frac{2M_{12}^2}{M_{11}^2 - M_{22}^2},$$

$$M_{12}^2 = \frac{1}{2} v^2 s_{2\beta} (-\lambda_1 c_\beta^2 + \lambda_2 s_\beta^2 + \lambda_{345} c_{2\beta}),$$

Decoupling limit:  $M \rightarrow \infty$

- Masses of  $H, A, H^\pm$  become infinity.

6 free parameters in the THDMs:

$$m_H, m_A, m_{H^\pm}, M^2, \tan \beta, s_{\beta-\alpha},$$

# THDM : Feynman rules

$$\kappa_X^\phi \equiv \frac{g_{\phi X \bar{X}}}{g_{h_{\text{SM}} X \bar{X}}}, \quad \phi = h, H, A$$

$$\kappa_V^h = s_{\beta-\alpha}, \quad \kappa_V^H = c_{\beta-\alpha}, \quad \kappa_V^A = 0,$$

$$\kappa_f^h = s_{\beta-\alpha} + c_{\beta-\alpha} \zeta_f, \quad \kappa_f^H = c_{\beta-\alpha} - s_{\beta-\alpha} \zeta_f, \quad \kappa_f^A = -2i I_f \zeta_f,$$

$Z_2$  charge assignment (to avoid the tree-level FCNCs)

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$	$\zeta_u$	$\zeta_d$	$\zeta_e$
Type-I	+	-	+	+	-	-	-	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type-II	+	-	+	+	-	+	+	$\cot \beta$	$-\tan \beta$	$-\tan \beta$
Type-X (lepton-specific)	+	-	+	+	-	-	+	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type-Y (flipped)	+	-	+	+	-	+	-	$\cot \beta$	$-\tan \beta$	$\cot \beta$

**Alignment limit (SM-like limit):**  $s_{\beta-\alpha} \rightarrow 1$

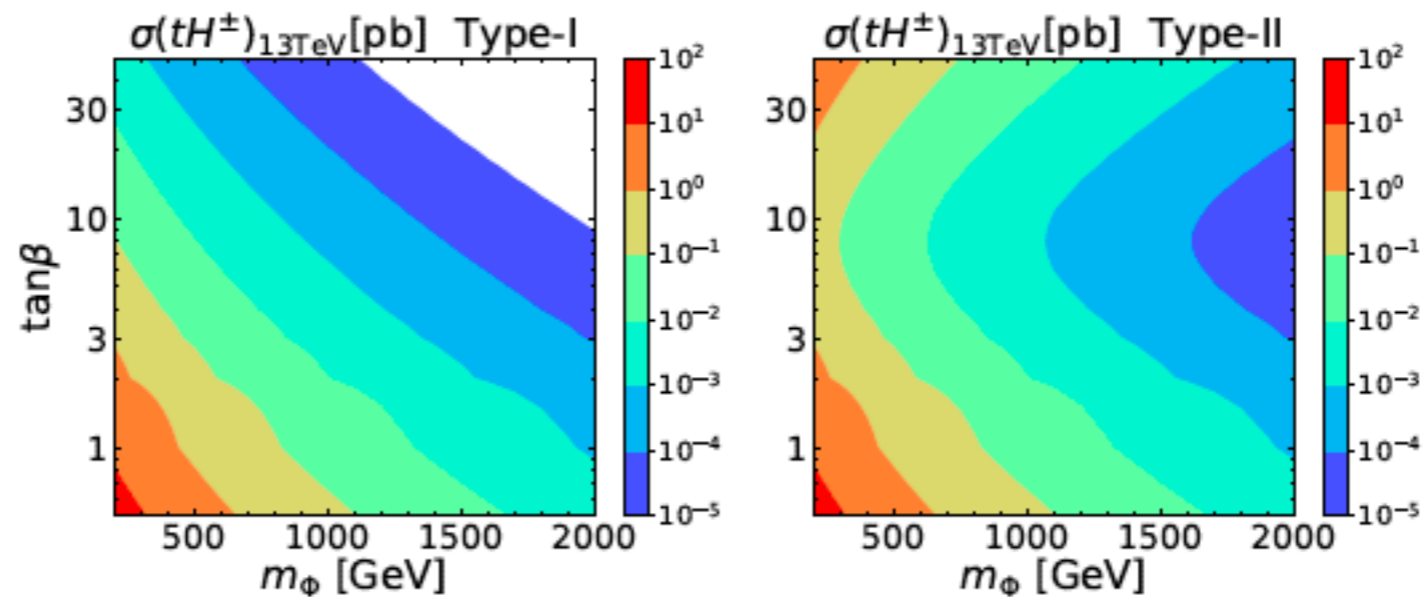
- $h$  behaves like the SM Higgs boson.
- $H, A, H^\pm$  only couple to the fermions.

- How and how much are the extra Higgs bosons produced at the LHC ?

# Production: charged Higgs bosons ( $H^\pm$ )

$b g \rightarrow t H^\pm$

[HXS WG (Higgs cross section working group)]



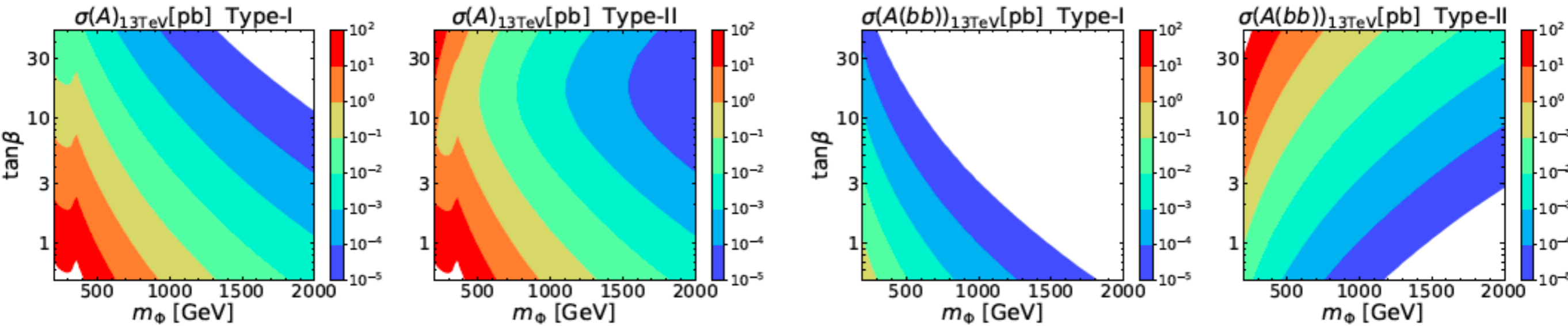
$$\mathcal{L}_Y^{H^\pm} = \frac{\sqrt{2}}{v} [\bar{u}_i (m_{u_i} V_{ij} \zeta_u P_L - V_{ij} m_{d_j} \zeta_d P_R) d_j H^\pm + \text{h.c.}]$$

	$Q_L$	$u_R$	$d_R$	$\zeta_u$	$\zeta_d$
Type-I	+	-	-	$\cot \beta$	$\cot \beta$
Type-II	+	-	+	$\cot \beta$	$-\tan \beta$

# Production: CP-odd Higgs boson (A)

gluon fusion via heavy-quark loops

b-quark fusion (b-quark associated)



[Sushi-1.7.0]

$$\kappa_f^A = -2iI_f\zeta_f$$

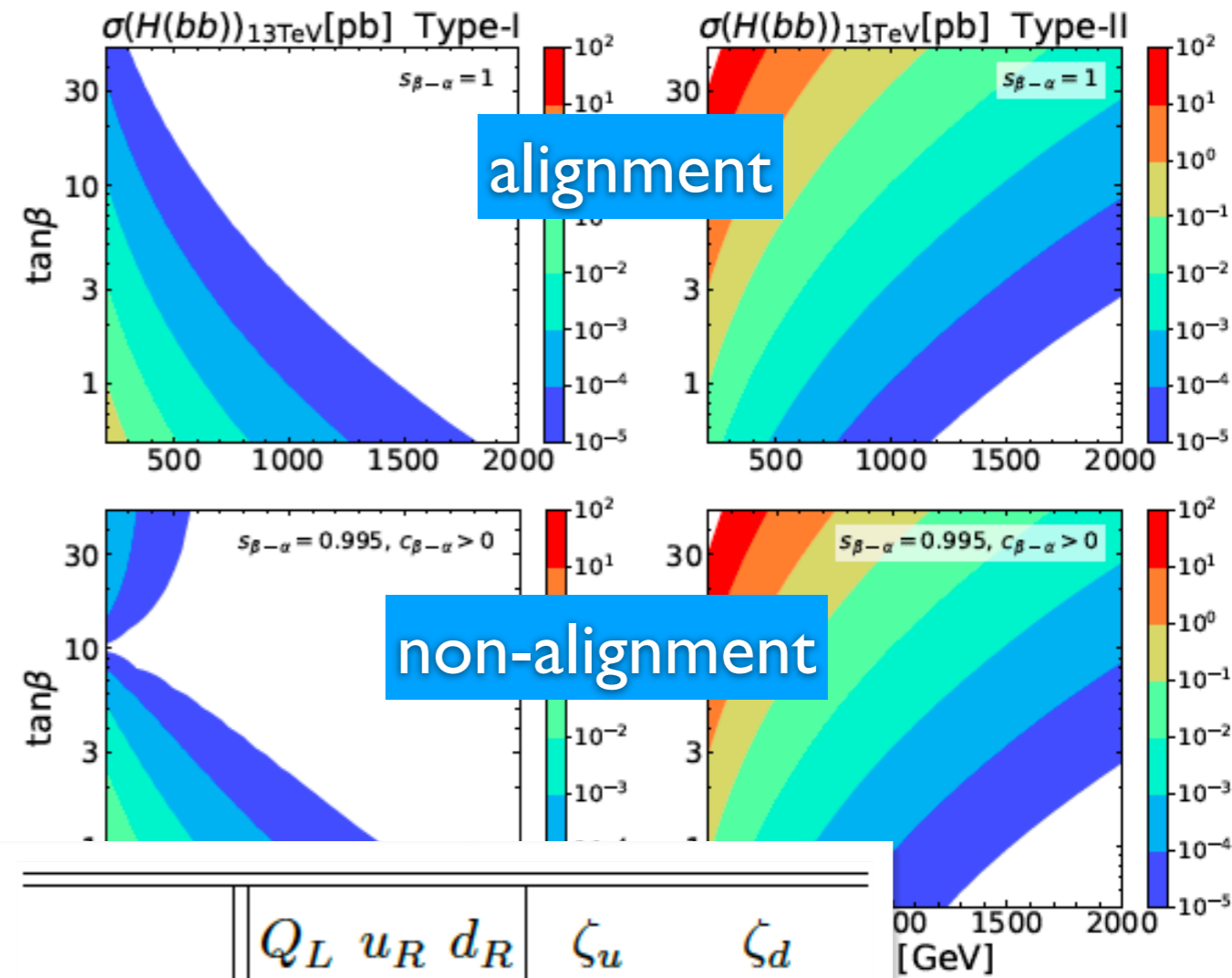
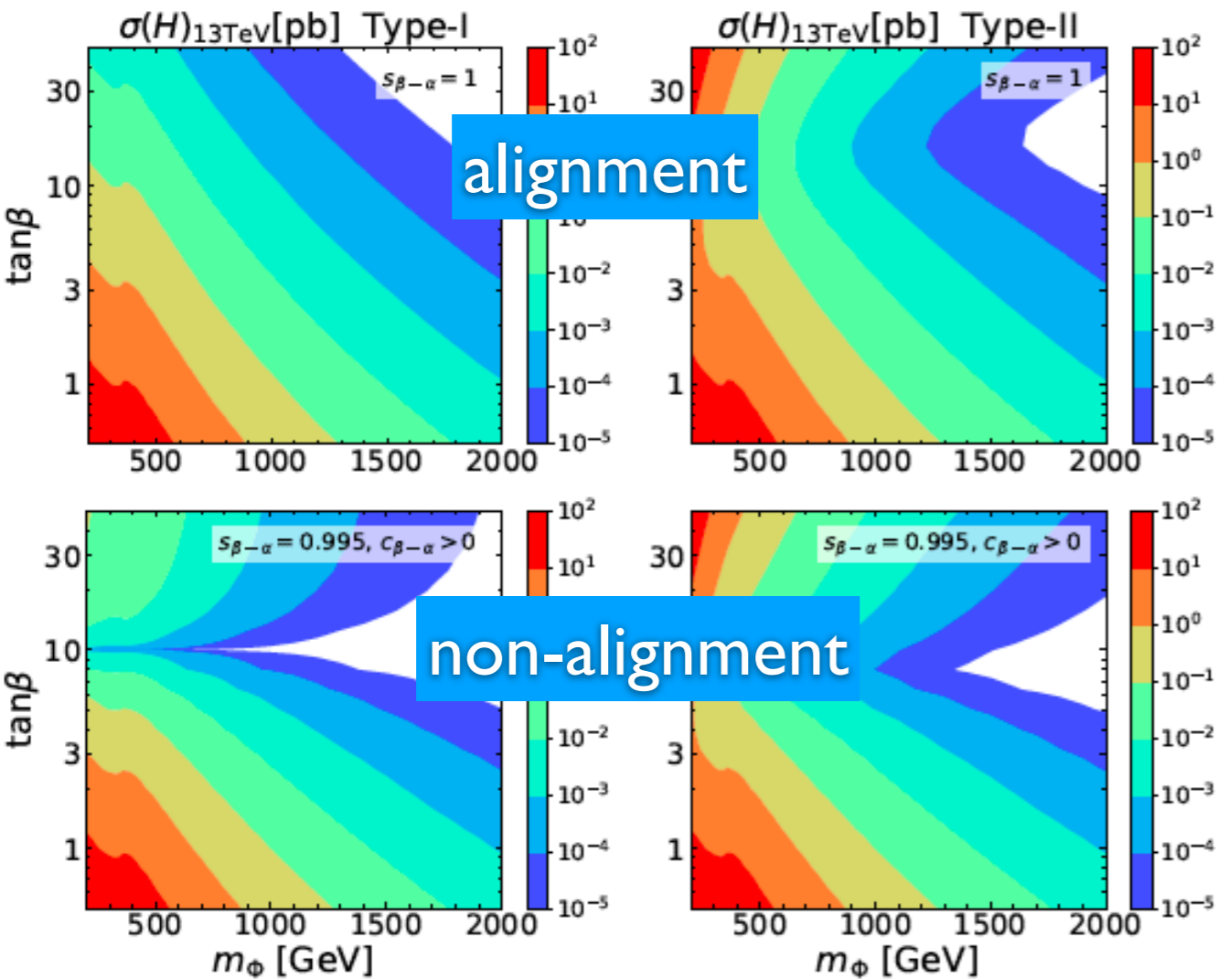
	$Q_L$	$u_R$	$d_R$	$\zeta_u$	$\zeta_d$
Type-I	+	-	-	$\cot \beta$	$\cot \beta$
Type-II	+	-	+	$\cot \beta$	$-\tan \beta$



# Production: CP-even Higgs boson (H)

gluon fusion via heavy-quark loops

b-quark fusion (b-quark associated)



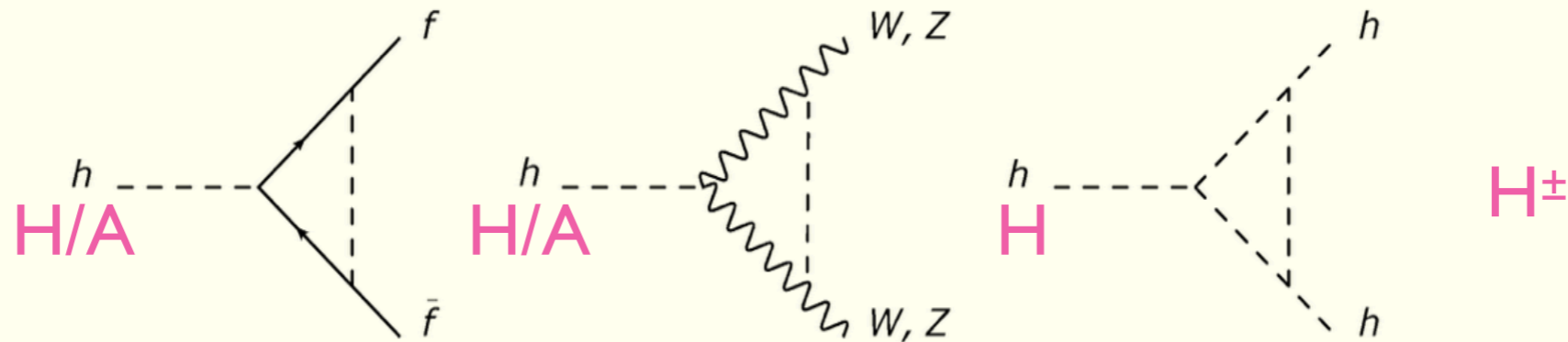
$$\kappa_f^H = c_{\beta-\alpha} - s_{\beta-\alpha} \zeta_f$$

	$Q_L$	$u_R$	$d_R$	$\zeta_u$	$\zeta_d$
Type-I	+	-	-	$\cot \beta$	$\cot \beta$
Type-II	+	-	+	$\cot \beta$	$-\tan \beta$

[Sushi-1.7.0]

- How do the Higgs bosons decay ?

# H-COUP



**NEW!! H-COUP version 2.3 was released (30 Apr. 2020)**

H-COUP version 2 (1 Sep. 2019) is a calculation tool composed of a set of Fortran codes to compute the Higgs boson decay rates and the branching ratios with radiative corrections (NNLO for QCD and NLO for EW) in various non-minimal Higgs models, such as the Higgs singlet model, four types of two Higgs doublet models and the inert doublet model. H-COUP ver. 2 contains all the functions in H-COUP ver. 1.

→ **version 3 (beta)**

Authors:

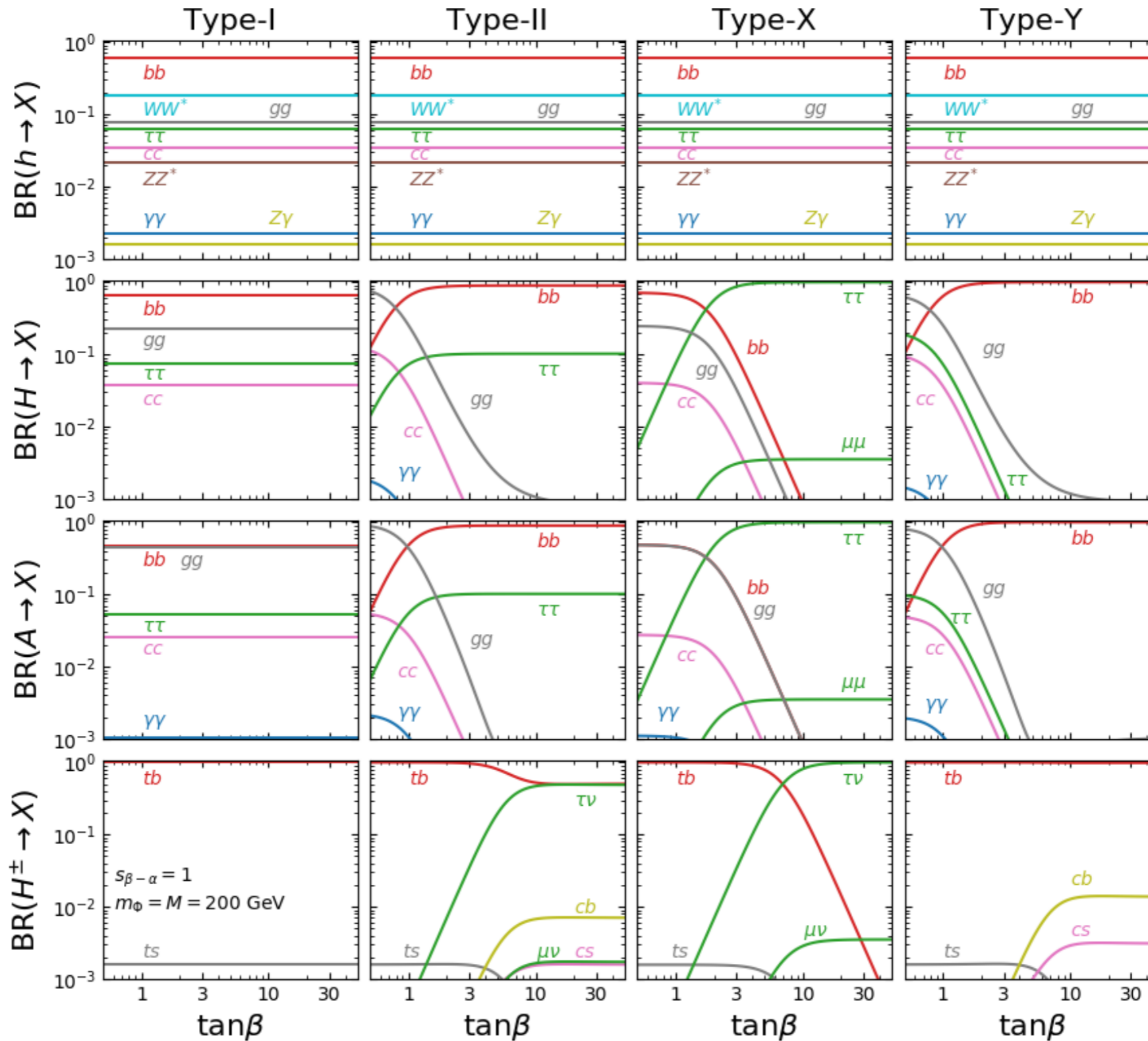
Shinya Kanemura, Mariko Kikuchi, Kentarou Mawatari, Kodai Sakurai and Kei Yagyu + **Aiko**

The manual for H-COUP version 2 can be taken on [arXiv:1910.12769 \[hep-ph\]](https://arxiv.org/abs/1910.12769).

# Decay: alignment, $m=200\text{GeV}$

[H-COUP v2]

[H-COUP v3 beta]



	$\zeta_u$	$\zeta_d$	$\zeta_e$
Type-I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type-II	$\cot \beta - \tan \beta$	$\cot \beta - \tan \beta$	$-\tan \beta$
Type-X (lepton-specific)	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type-Y (flipped)	$\cot \beta - \tan \beta$	$\cot \beta - \tan \beta$	$\cot \beta$

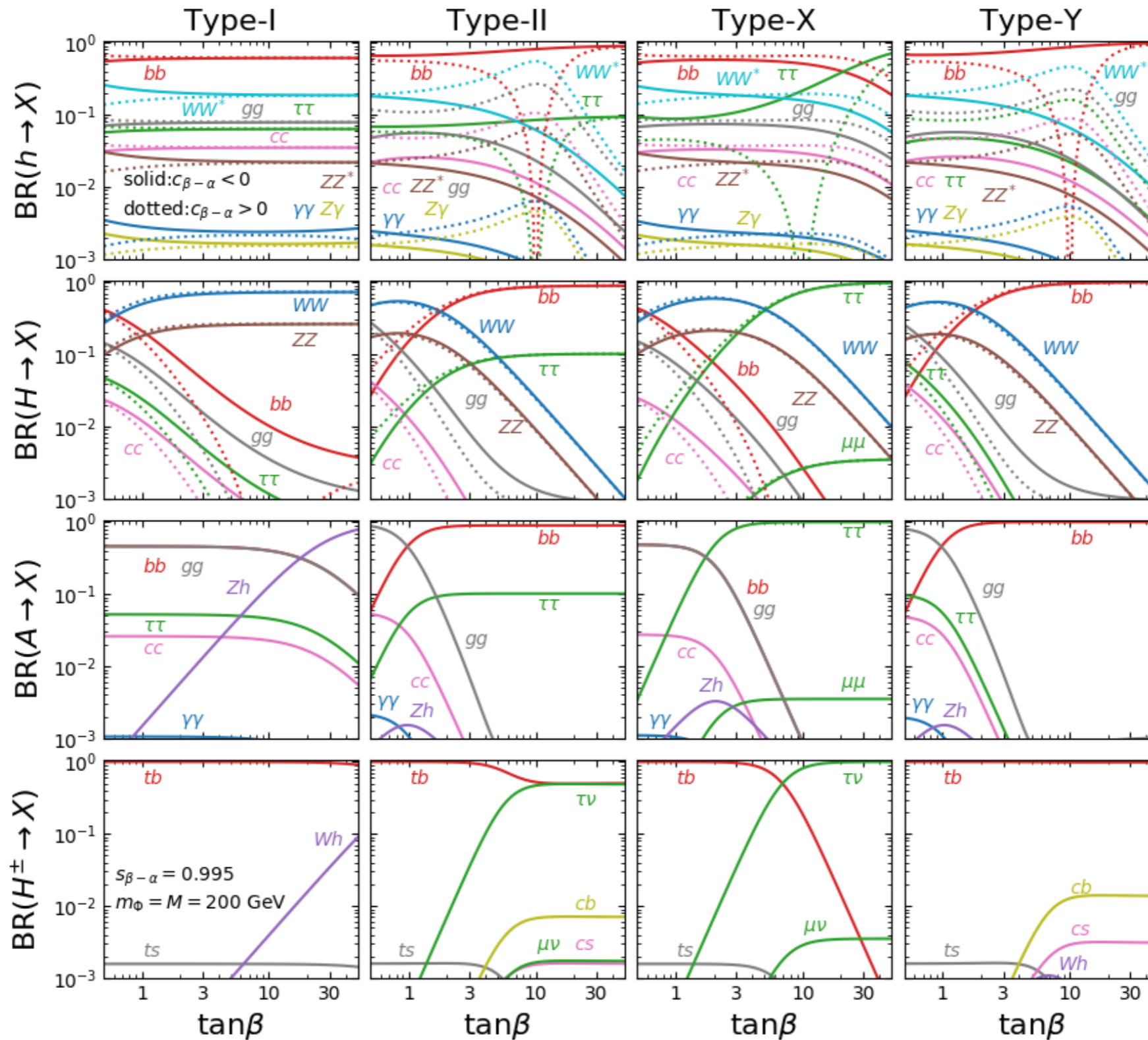
  

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	+	-	+	+	-	-	-
Type-II	+	-	+	+	-	+	+
Type-X (lepton-specific)	+	-	+	+	-	-	+
Type-Y (flipped)	+	-	+	+	-	+	-

# Decay: non-alignment, $m=200\text{GeV}$

[H-COUP v2]

[H-COUP v3 beta]



	$\zeta_u$	$\zeta_d$	$\zeta_e$
Type-I	$\cot\beta$	$\cot\beta$	$\cot\beta$
Type-II	$\cot\beta$	$-\tan\beta$	$-\tan\beta$
Type-X (lepton-specific)	$\cot\beta$	$\cot\beta$	$-\tan\beta$
Type-Y (flipped)	$\cot\beta$	$-\tan\beta$	$\cot\beta$

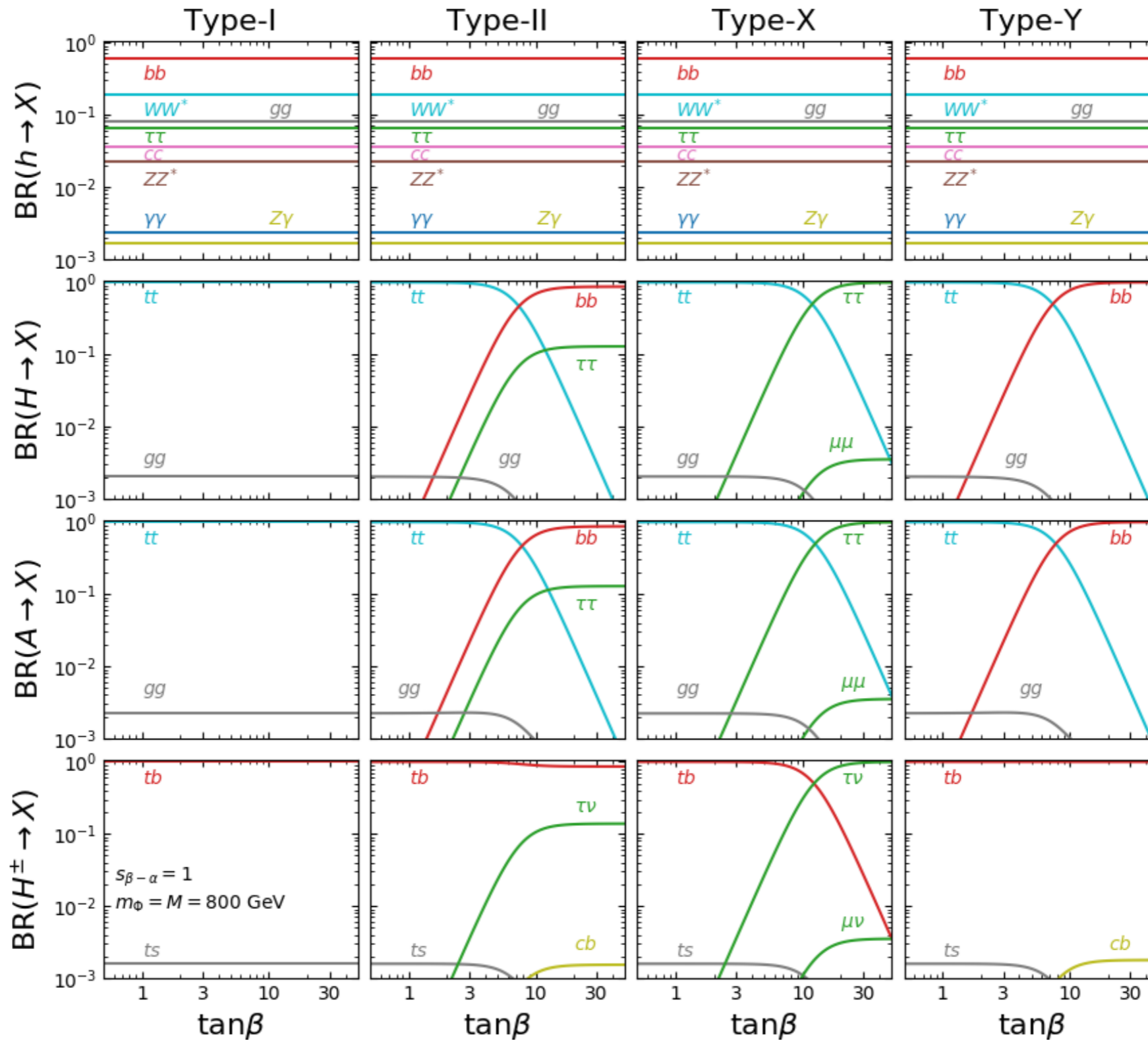
  

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	+	-	+	+	-	-	-
Type-II	+	-	+	+	-	+	+
Type-X (lepton-specific)	+	-	+	+	-	-	+
Type-Y (flipped)	+	-	+	+	-	+	-

# Decay: alignment, $m=800\text{GeV}$

[H-COUP v2]

[H-COUP v3 beta]



	$\zeta_u$	$\zeta_d$	$\zeta_e$
Type-I	$\cot\beta$	$\cot\beta$	$\cot\beta$
Type-II	$\cot\beta$	$-\tan\beta$	$-\tan\beta$
Type-X (lepton-specific)	$\cot\beta$	$\cot\beta$	$-\tan\beta$
Type-Y (flipped)	$\cot\beta$	$-\tan\beta$	$\cot\beta$

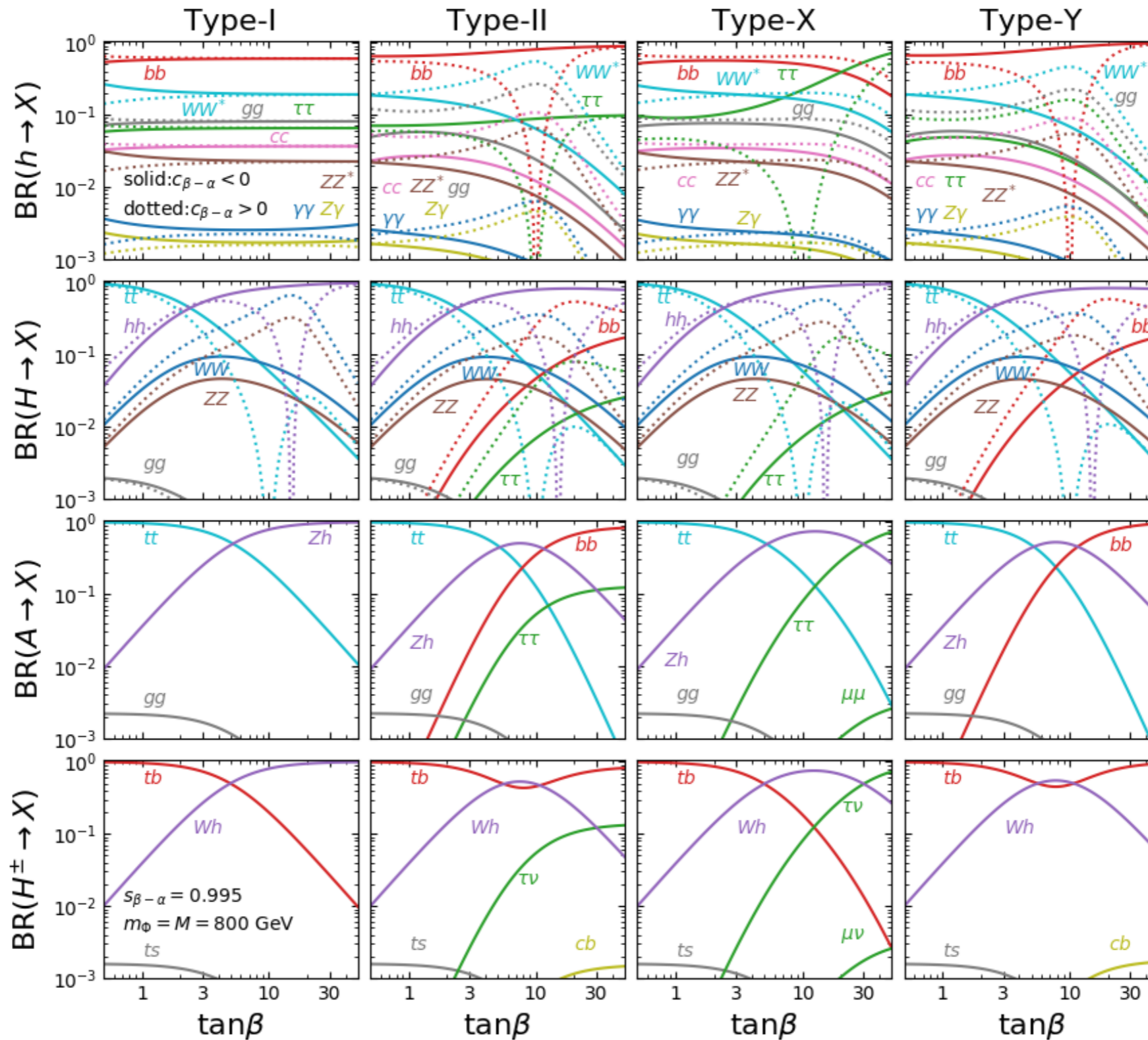
  

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	+	-	+	+	-	-	-
Type-II	+	-	+	+	-	+	+
Type-X (lepton-specific)	+	-	+	+	-	-	+
Type-Y (flipped)	+	-	+	+	-	+	-

# Decay: non-alignment, $m=800\text{GeV}$

[H-COUP v2]

[H-COUP v3 beta]



	$\zeta_u$	$\zeta_d$	$\zeta_e$
Type-I	$\cot\beta$	$\cot\beta$	$\cot\beta$
Type-II	$\cot\beta$	$-\tan\beta$	$-\tan\beta$
Type-X (lepton-specific)	$\cot\beta$	$\cot\beta$	$-\tan\beta$
Type-Y (flipped)	$\cot\beta$	$-\tan\beta$	$\cot\beta$

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	+	-	+	+	-	-	-
Type-II	+	-	+	+	-	+	+
Type-X (lepton-specific)	+	-	+	+	-	-	+
Type-Y (flipped)	+	-	+	+	-	+	-

- So far, unfortunately, there is no report on new particle discovery from the LHC...

➡ constraints on the parameters of the models.

6 free parameters in the THDMs:

$$m_H, m_A, m_{H^\pm}, M^2, \tan \beta, s_{\beta-\alpha},$$

In our study, we take

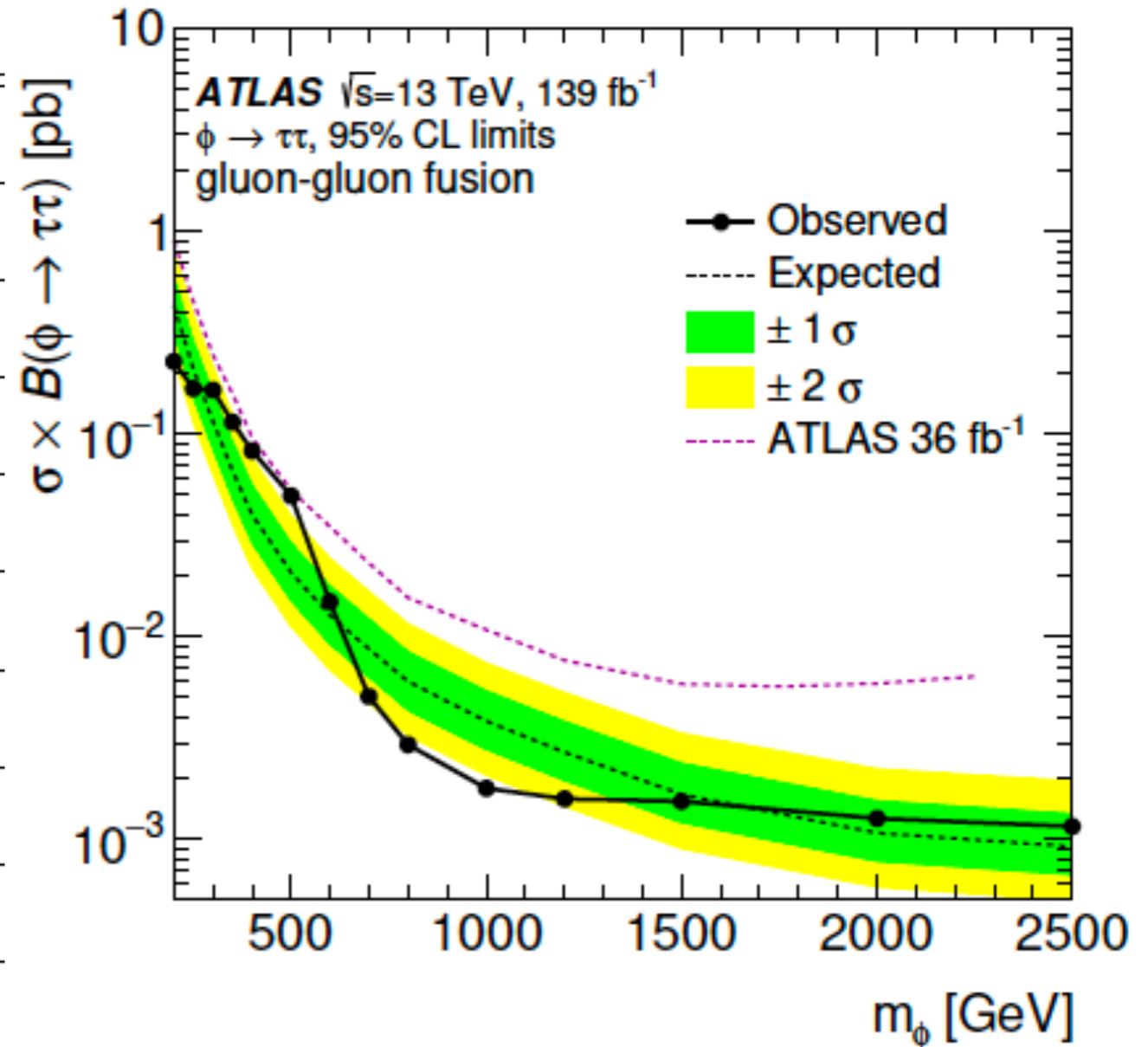
$$m_H = m_A = m_{H^\pm} (\equiv m_\Phi)$$



# List of LHC constraints used in our study

LHC Run-II 36 fb<sup>-1</sup> data

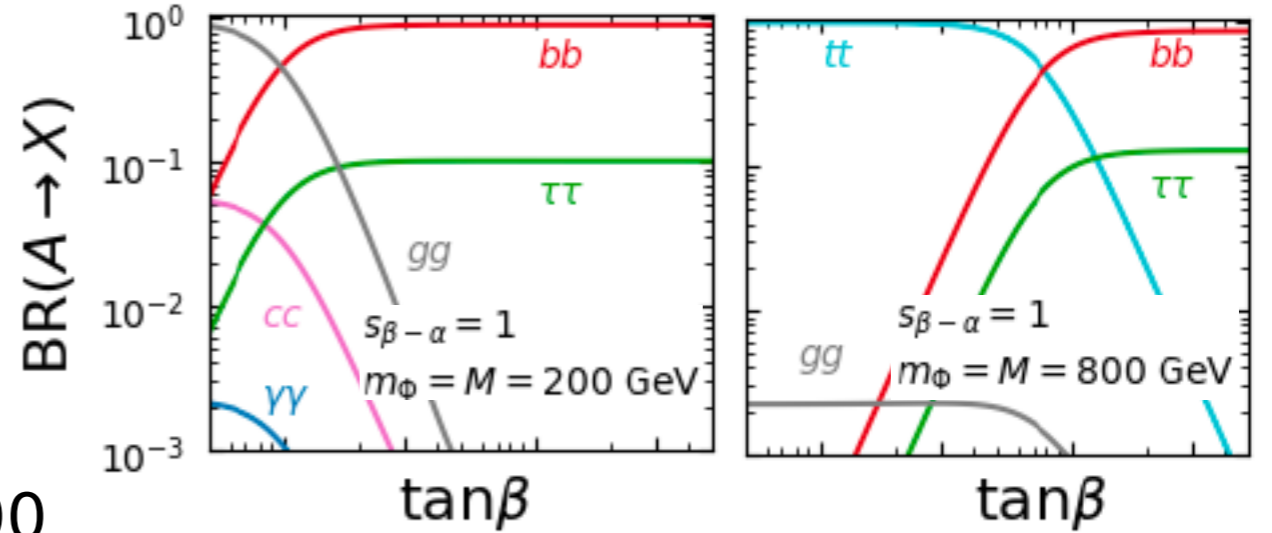
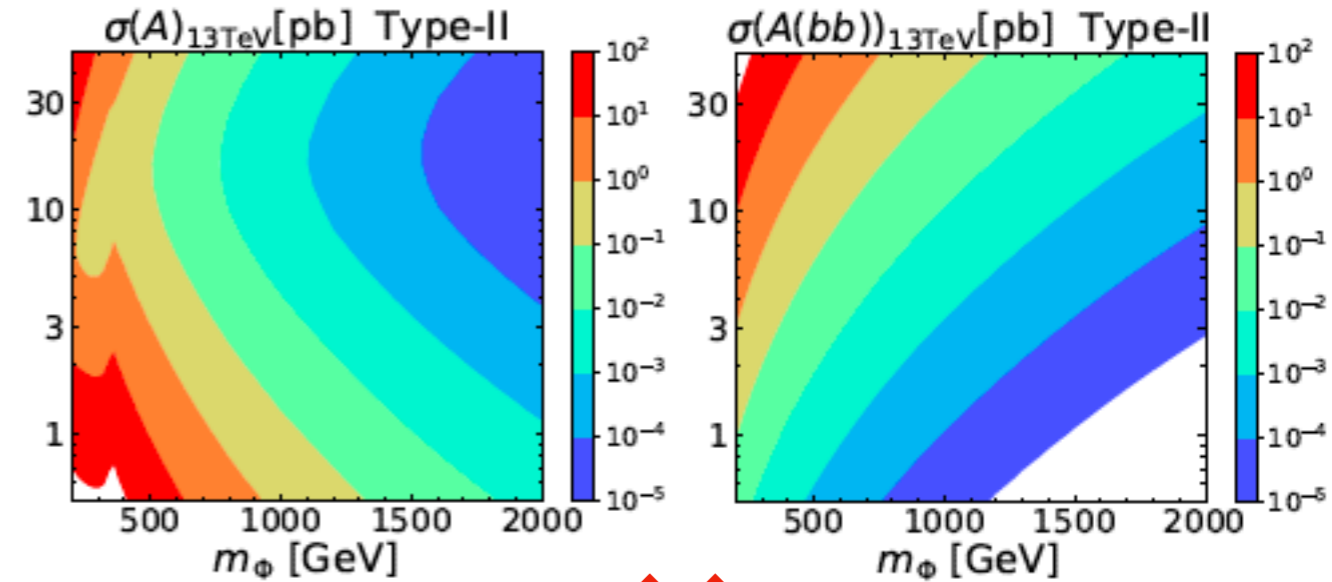
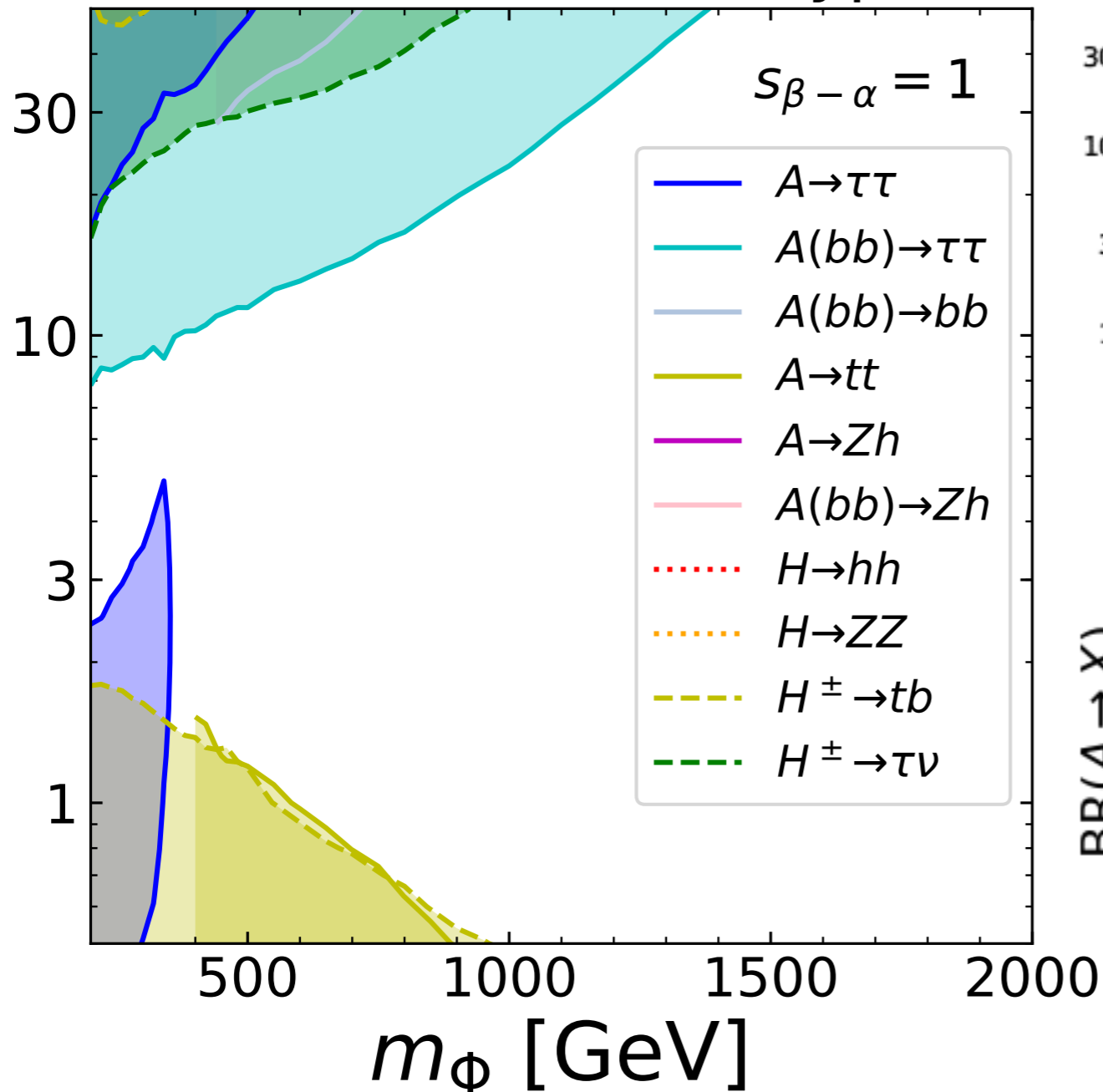
Constrained quantity
$\sigma(\phi) \times \text{BR}(\phi \rightarrow \tau\tau)$
$\sigma(\phi(bb)) \times \text{BR}(\phi \rightarrow \tau\tau)$
$\sigma(\phi(bb)) \times \text{BR}(\phi \rightarrow bb)$
$\sigma(\phi) \times \text{BR}(\phi \rightarrow tt)$
$\sigma(H) \times \text{BR}(H \rightarrow hh) \times \text{BR}(h \rightarrow bb)^2$
$\sigma(H) \times \text{BR}(H \rightarrow WW)$
$\sigma(H) \times \text{BR}(H \rightarrow ZZ)$
$\sigma(A) \times \text{BR}(A \rightarrow Zh) \times \text{BR}(h \rightarrow bb)$
$\sigma(A(bb)) \times \text{BR}(A \rightarrow Zh) \times \text{BR}(h \rightarrow bb)$
$\sigma(tH^\pm) \times \text{BR}(H^\pm \rightarrow tb)$
$\sigma(tH^\pm) \times \text{BR}(H^\pm \rightarrow \tau\nu)$



200 < m<sub>ϕ</sub> < model-independent constraints  
 → interpretation to THDMs

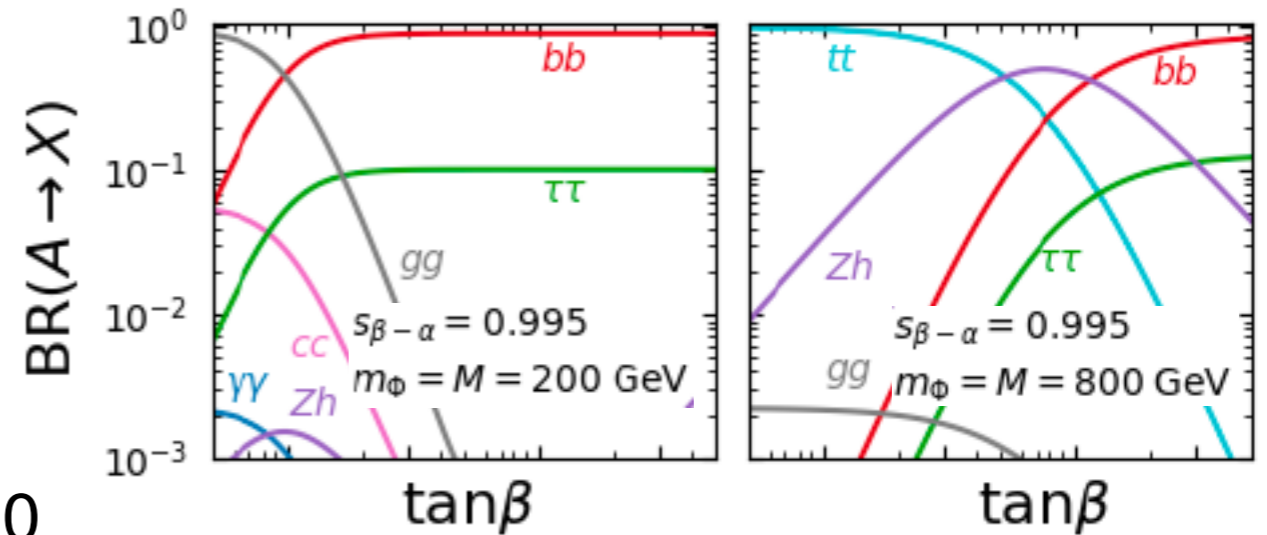
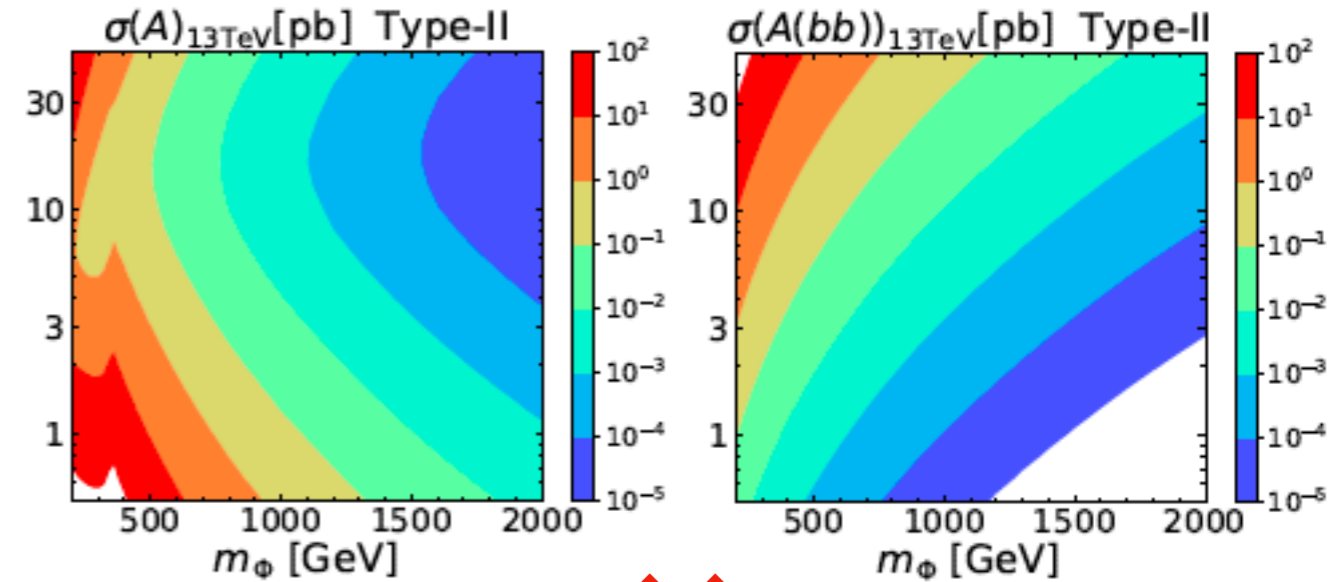
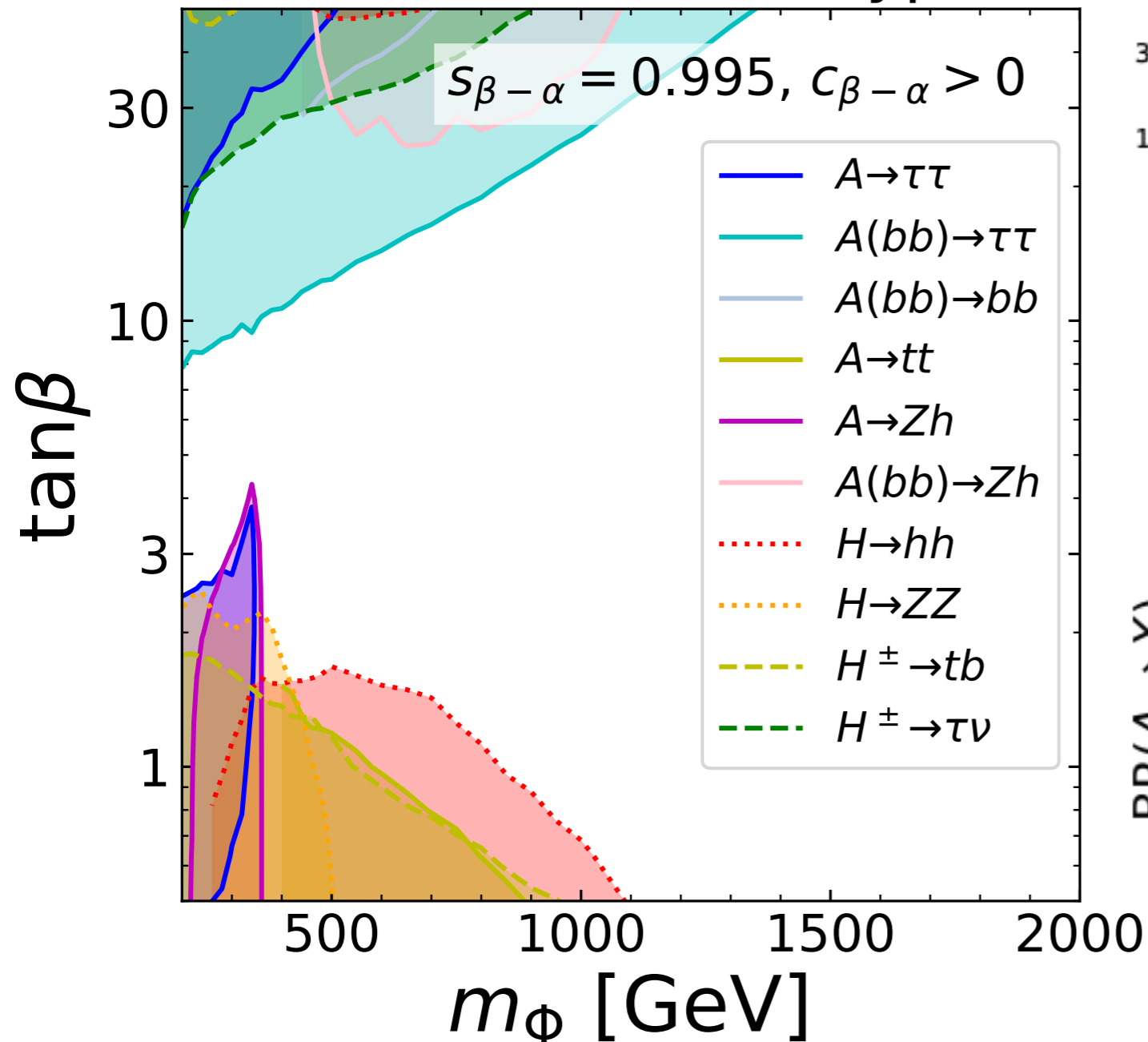
# Exclusion region (e.g. Type-II, alignment)

Current exclusion; Type-II



# Exclusion region (e.g. Type-II, non-alignment)

Current exclusion; Type-II



Current exclusion; Type-I

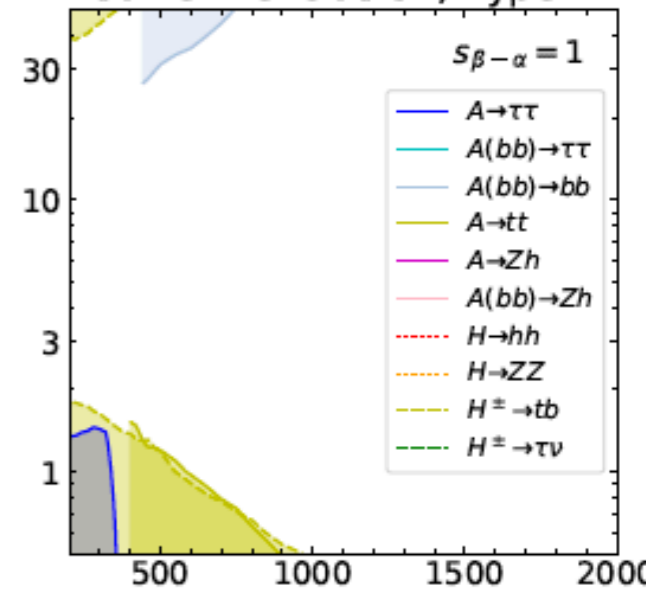
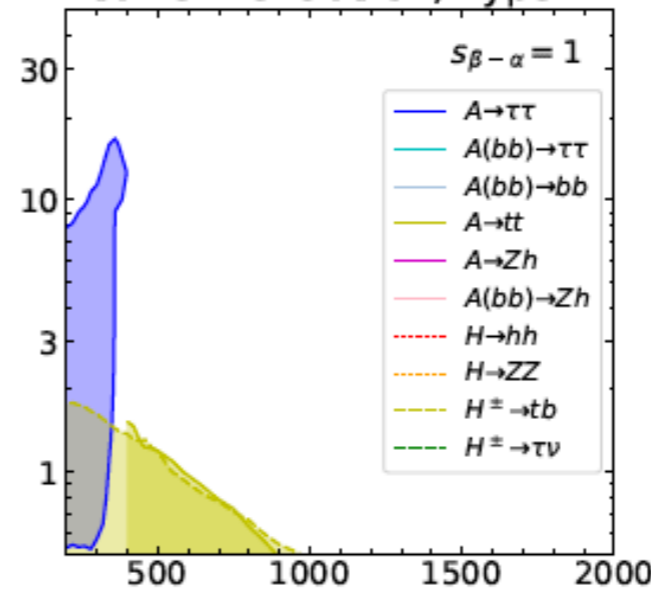
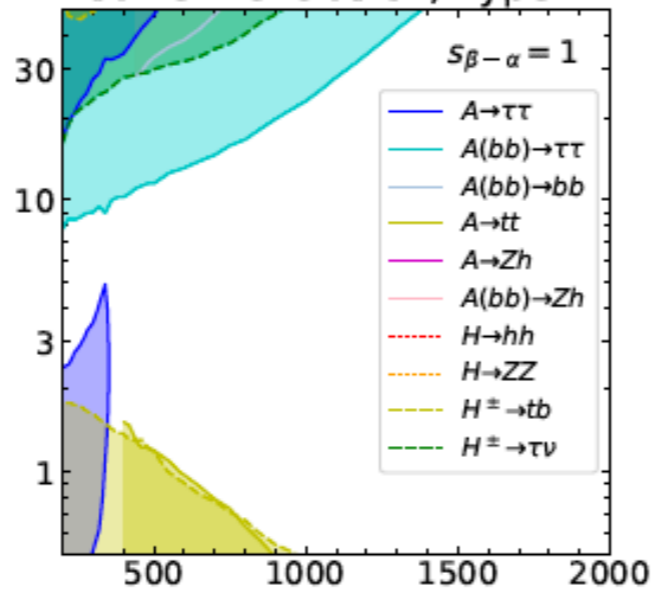
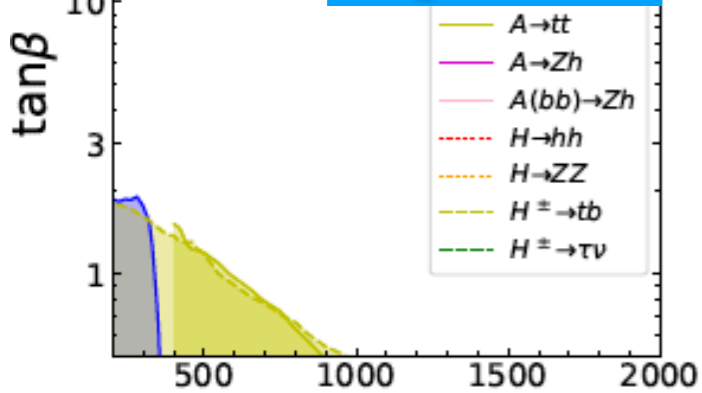
Current exclusion; Type-II

Current exclusion; Type-X

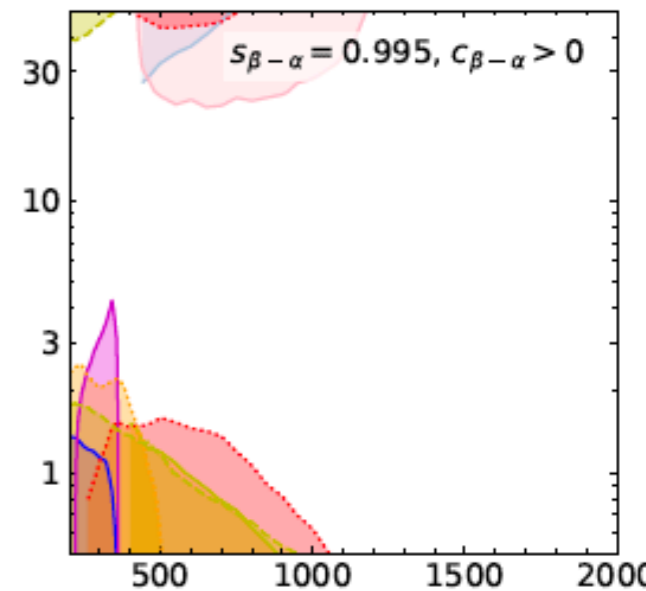
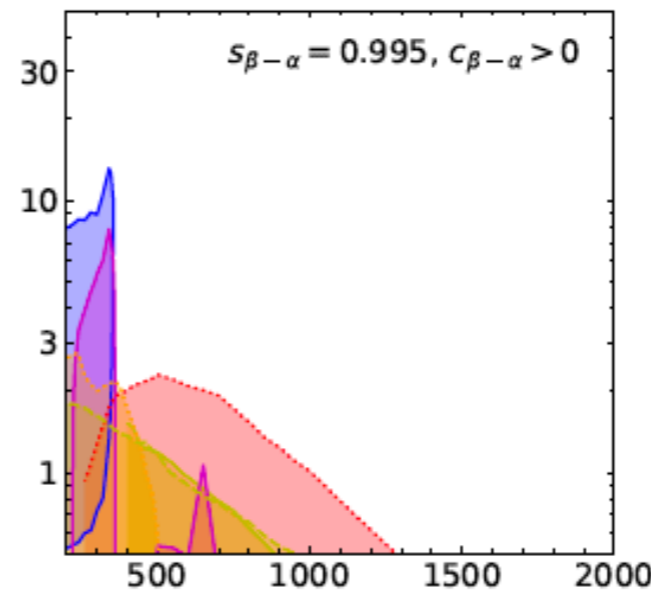
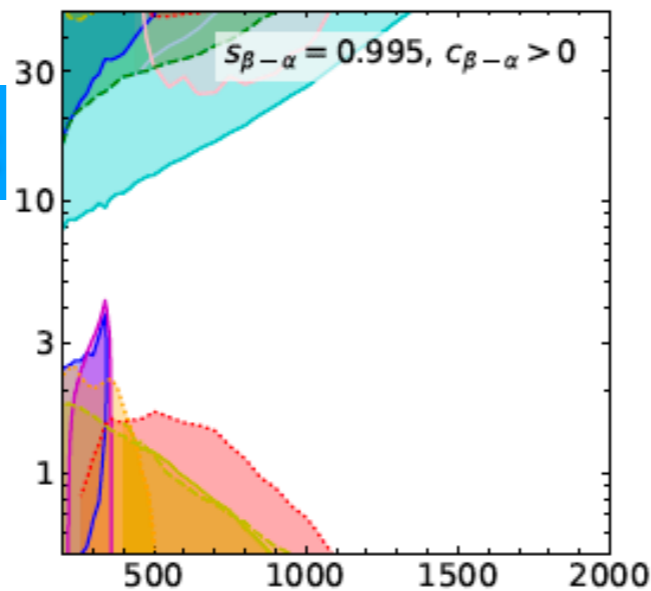
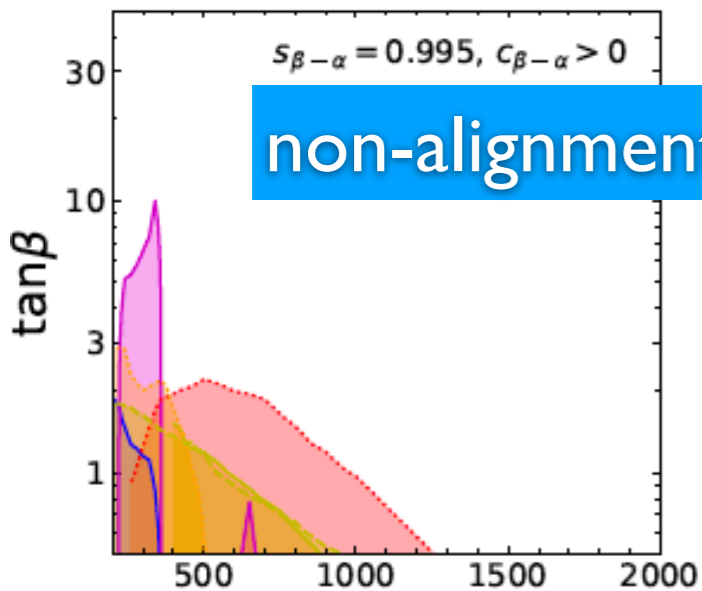
Current exclusion; Type-Y

LHC Run2 (36fb<sup>-1</sup>)

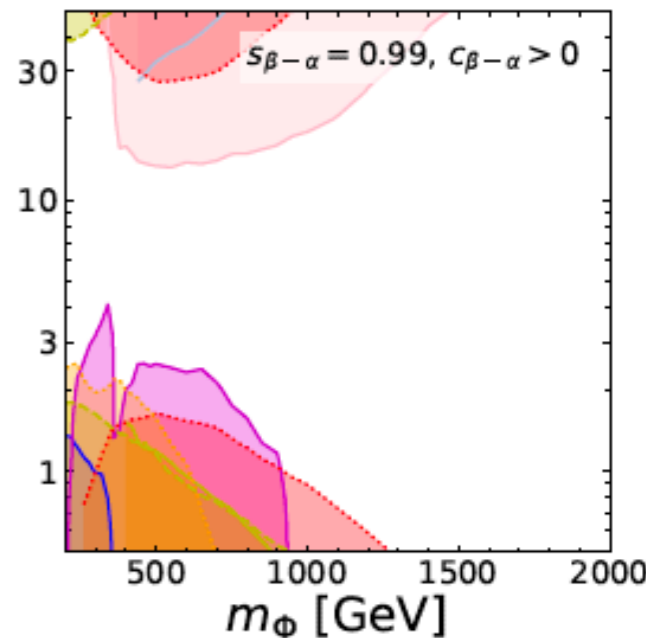
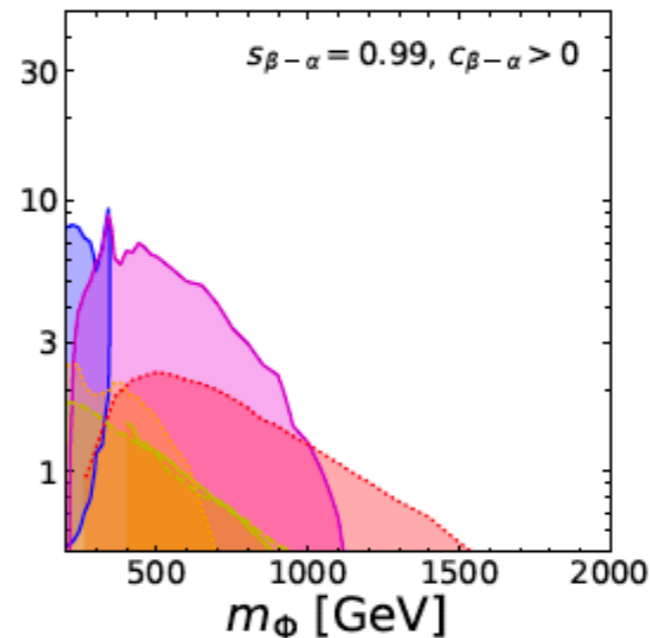
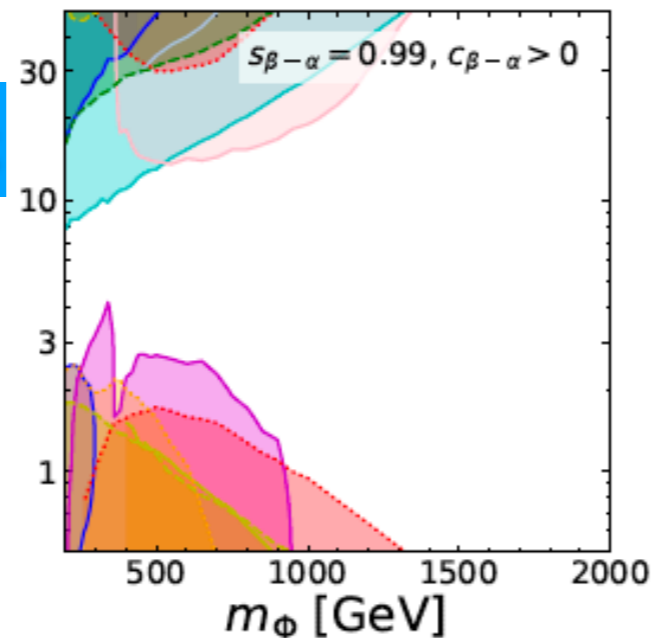
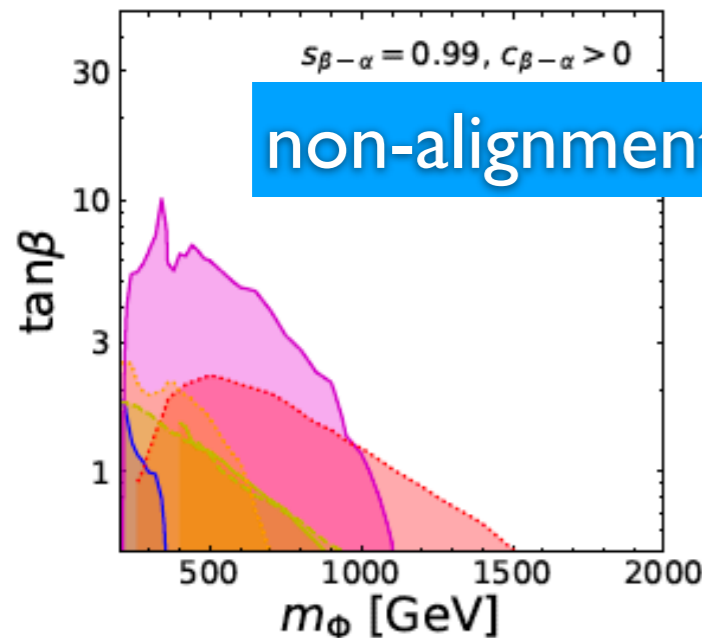
alignment

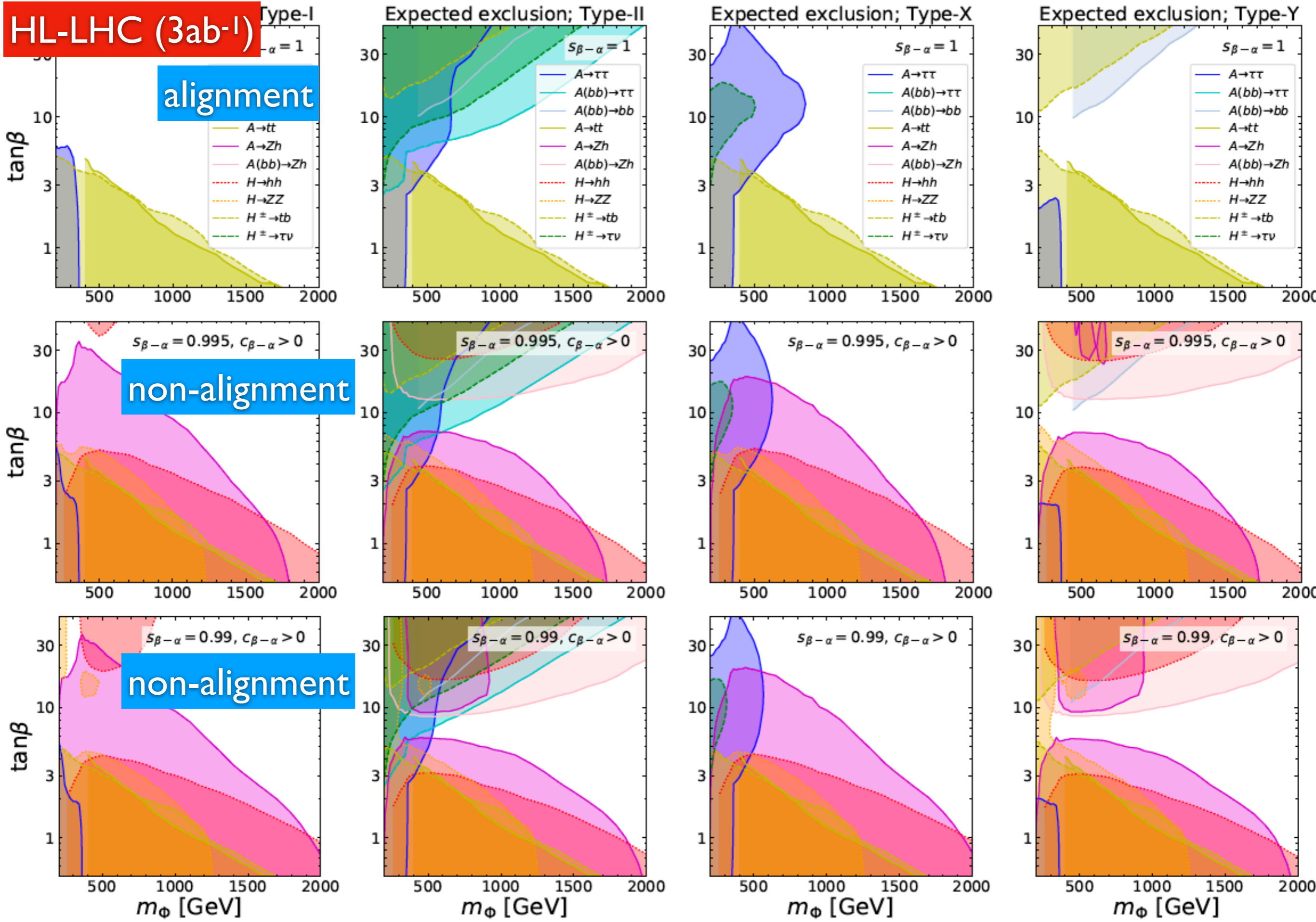


non-alignment

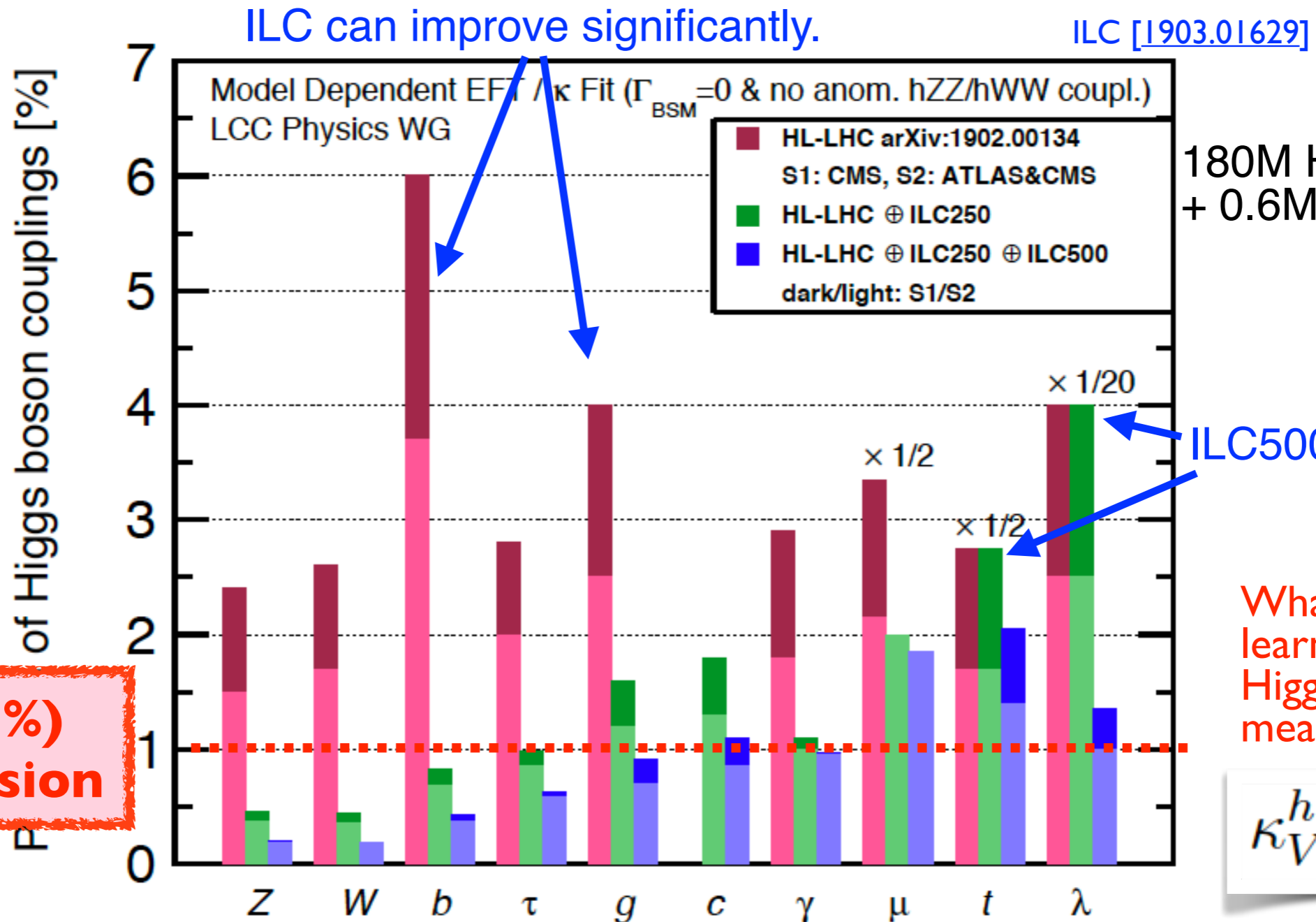


non-alignment





# Higgs precision measurements @ HL-LHC + ILC



180M Higgs (HL-LHC) + 0.6M (ILC250)

ILC500 is necessary.

What can we learn from the Higgs precision measurements?

$$\kappa_V^h = s_{\beta-\alpha}$$

$O(1\%)$  precision

relatively clean even at the LHC. Only ILC can measure.

# Decoupling without alignment

- Can we take  $M \rightarrow \infty$  with  $\sin(\beta - \alpha) \neq 1$  ?

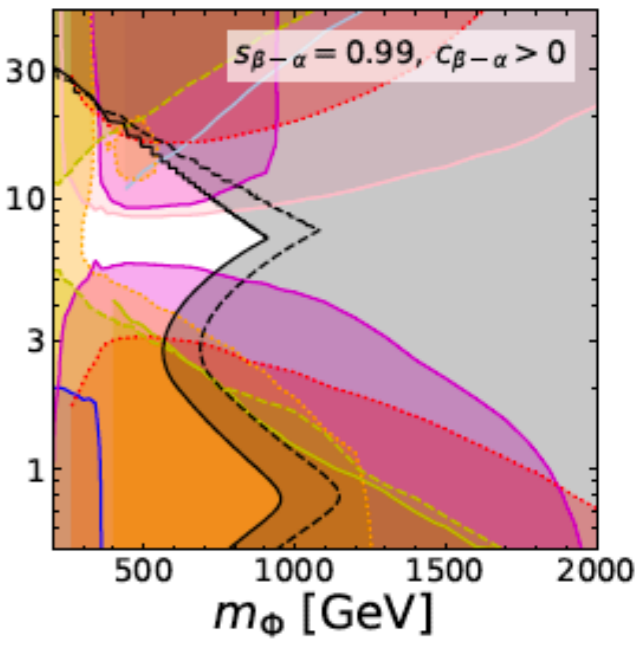
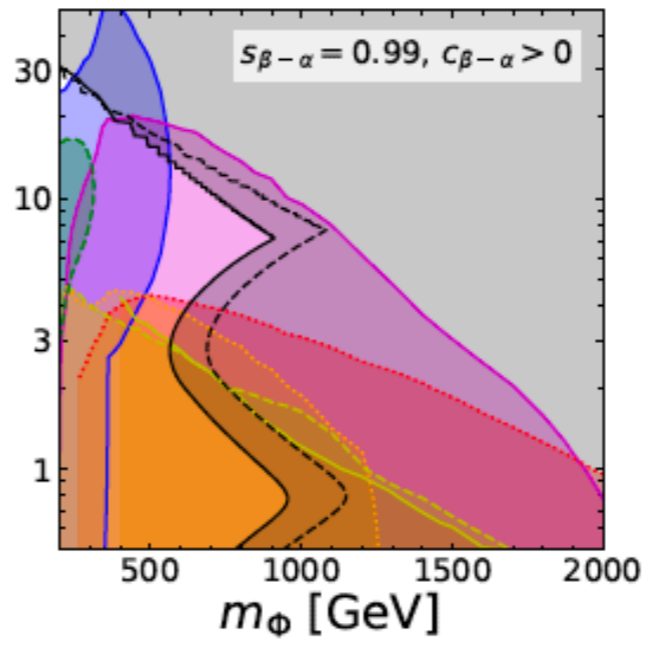
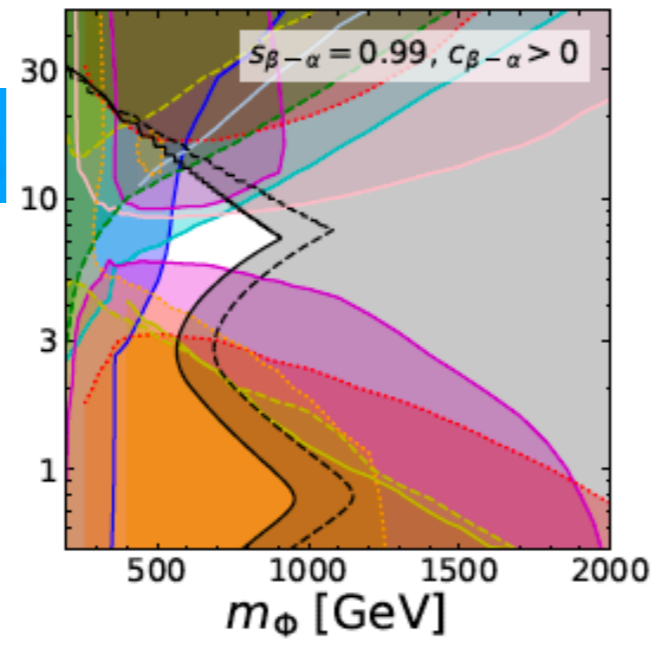
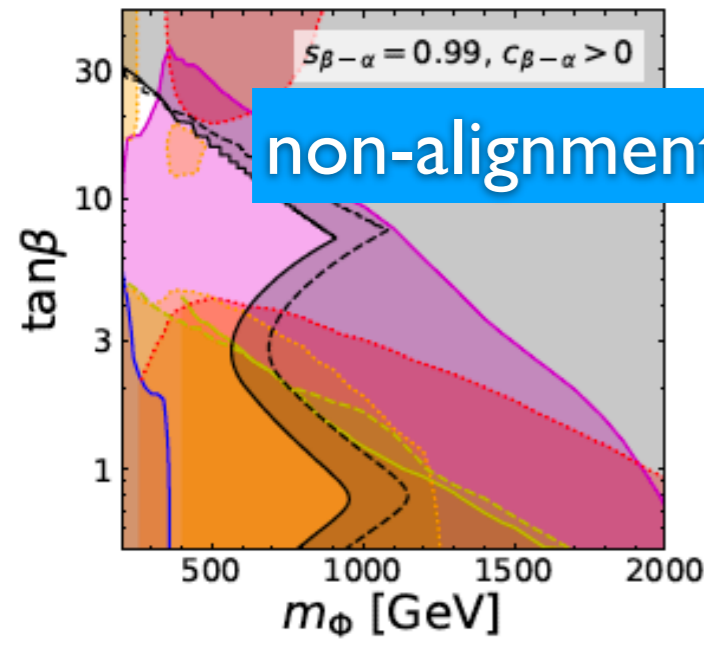
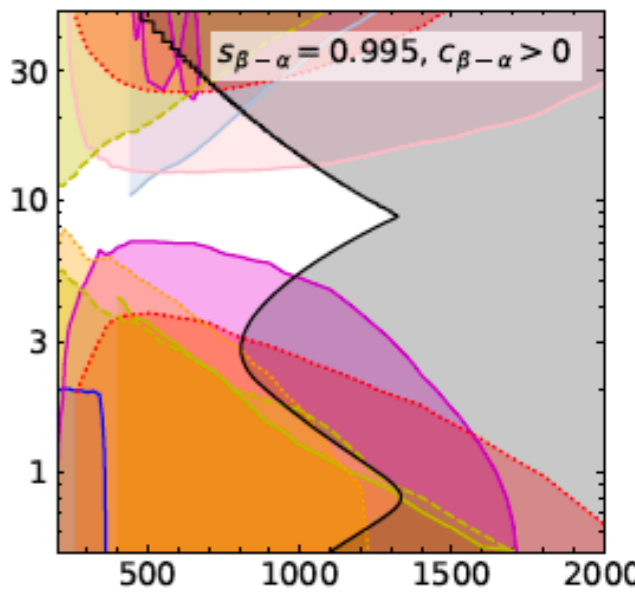
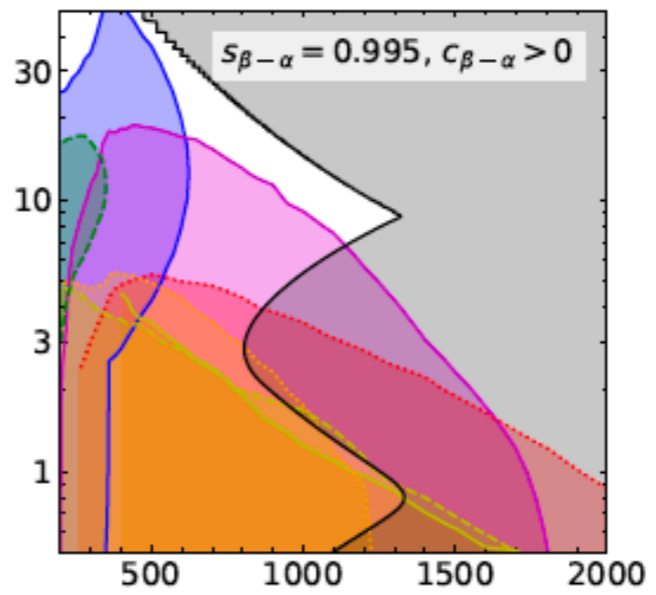
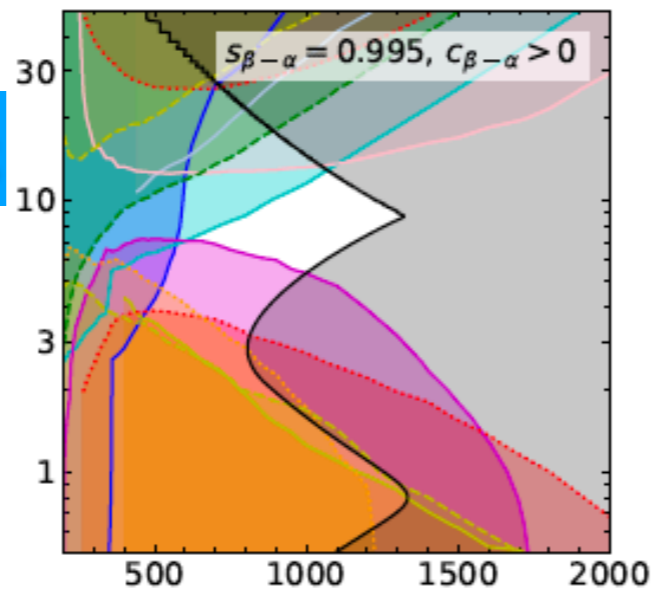
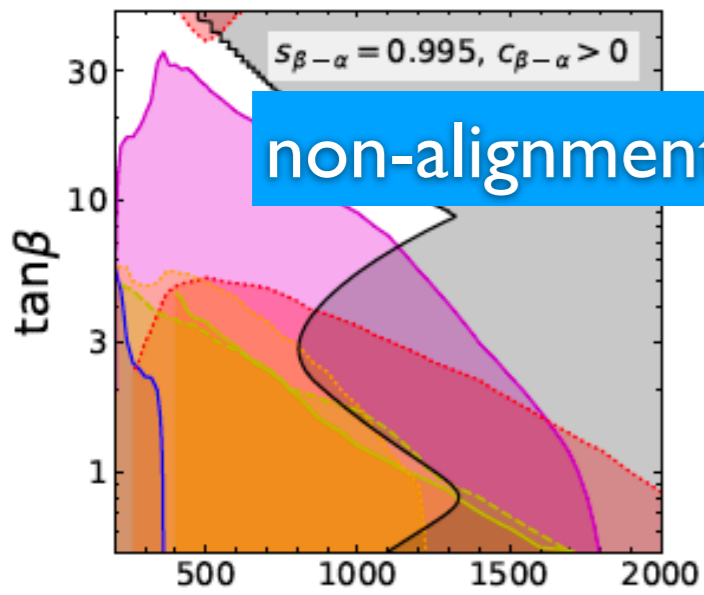
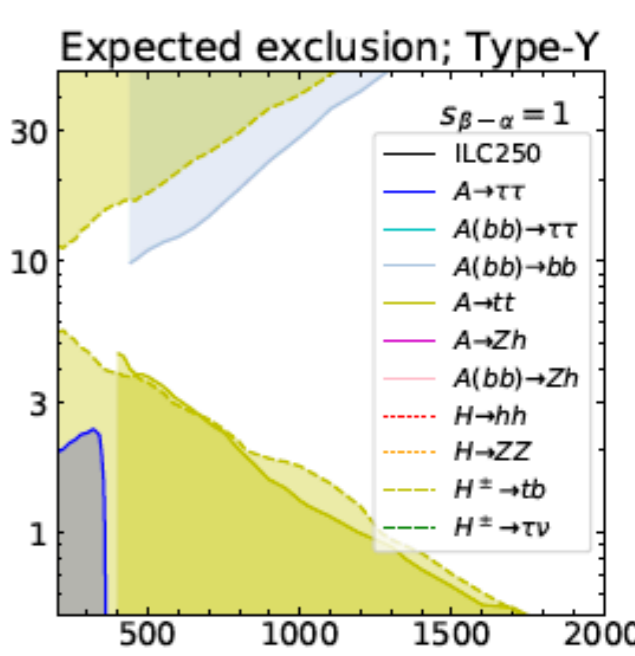
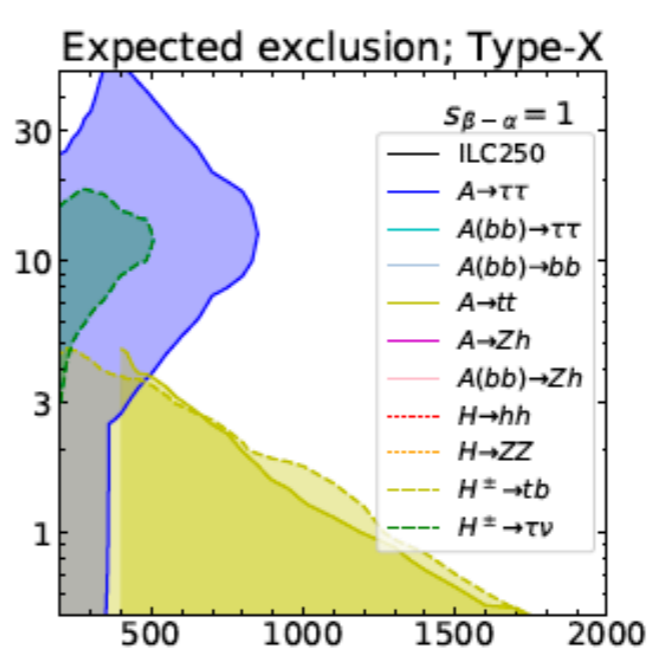
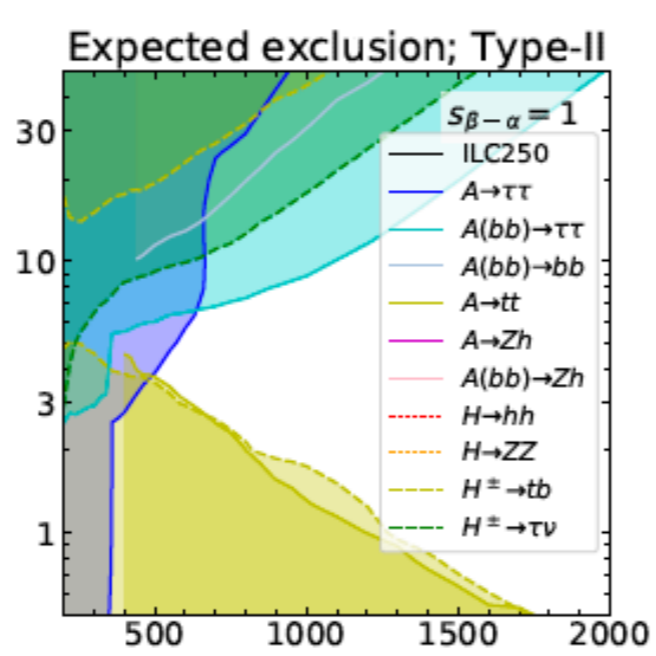
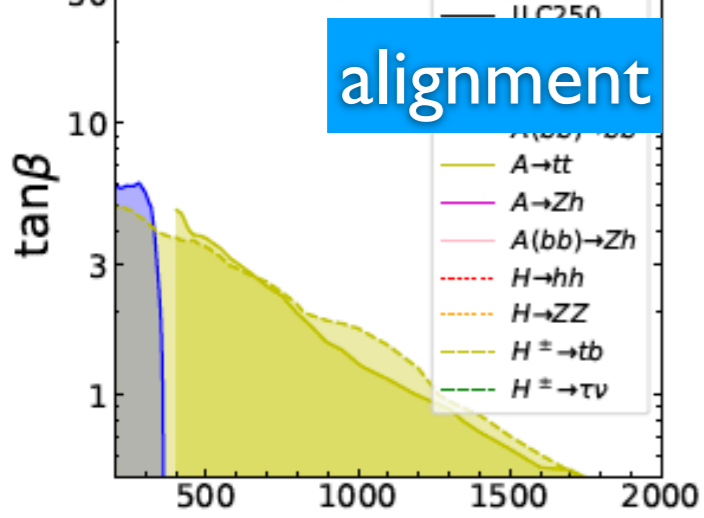
▶ NO !  $m_h^2 = \lambda v^2 + \cos^2(\beta - \alpha)M^2 = (125 \text{ GeV})^2$

➡ If  $\sin(\beta - \alpha) \neq 1$ , the upper limit on  $M$  is set.

➡ When ILC observes the deviation of the Higgs couplings, we are able to know the mass scale of the extra scalars.

ILC [1903.01629]

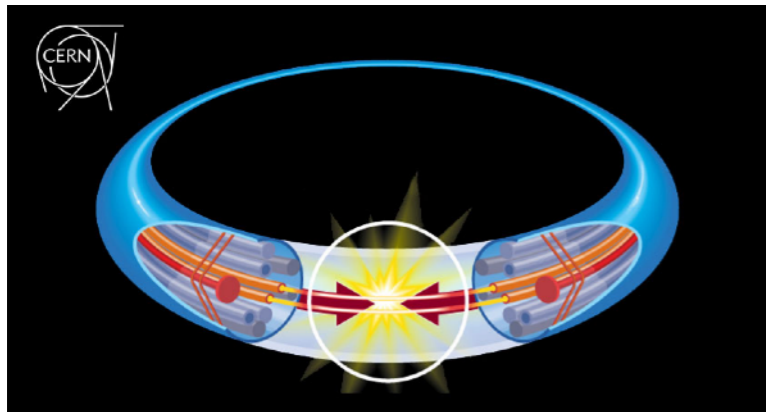
$$\kappa_V^h = [0.995, 0.99, 0.98] \pm 0.0038 \text{ (0.0076)}$$



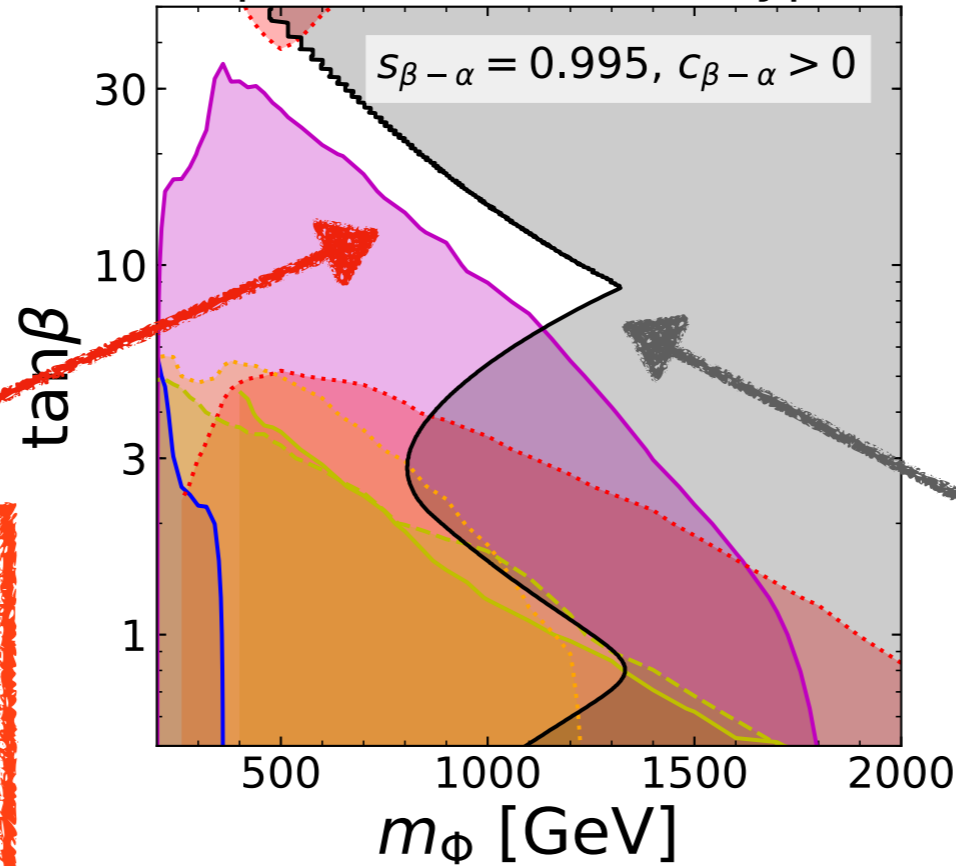


# Summary

synergy



Expected exclusion; Type-I



The direct searches for additional Higgs bosons give lower limits of the masses.

The precision measurements for the SM-like Higgs boson set upper limits of the masses.



@ aiina (next to Morioka station in Iwate)