

# Importance of Fermion Loops in VBS

## Carlos Quezada Calonge

Universidad Complutense de Madrid & IPARCOS

[cquezada@ucm.es](mailto:cquezada@ucm.es)

LCWS 2021

A. Dobado, JJ. Sanz-Cillero



# 1. Introduction

- Higgs couplings to gauge bosons and **top quark** are still compatible with the SM with deviations of  $\mathcal{O}$  (**10%**). For other fermions (e.g **bottom**) and the triple-Higgs coupling **larger** deviations are not excluded .[1]
- These deviations may come **from strongly interacting new physics**, where the Higgs boson and the Goldstone Bosons are composite states.
- We will focus on heavy fermion loop corrections to **VBS** (imaginary part) with **top quark** because of its large mass, 175 GeV. Fermion corrections are often neglected because the bosons ones dominate at high energy. ( $\sim 3$  TeV)

**But how important are fermion loops?**

The imaginary parts enter in the NLO counting

Is it possible to find values for the modified couplings that lead to a significant contribution?

## 2. Electroweak Chiral Lagrangian (EFT)

- Electroweak Chiral Lagrangian : EW GB **transform non-linearly** and a **Higgs-like** field which **transforms linearly** under  $SU(2)_L \times SU(2)_R$  which breaks to the **Custodial Symmetry**  $SU(2)_{L+R}$ .

$$SU(2)_L \times SU(2)_R \xrightarrow{SSB} SU(2)_{L+R}$$

- Systematic expansion in **chiral power counting** (different to the SMEFT canonical expansion). **Renormalizable order by order.**

$$\mathcal{L}_{EChL} = \mathcal{L}_2 + \mathcal{L}_4 + \dots$$

- It is often used the Equivalence Theorem [2], where we relate the gauge bosons with the would-be-Goldstones at high energies.

$$\mathcal{A}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \mathcal{A}(\omega^a \omega^b \rightarrow \omega^c \omega^d) + O\left(\frac{M_W}{\sqrt{s}}\right)$$

- Because of exact cancellations of some amplitudes we need go beyond the ET.

[2] P.B. Pal, What is the equivalence theorem really? (1994)

## The lagrangian at lowest order (chiral dimension 2)

$$\mathcal{L}_2 = \frac{v^2}{4} \mathcal{F}(h) \text{Tr} \left[ (D_\mu U)^\dagger D^\mu U \right] + \frac{1}{2} \partial_\mu h \partial^\mu h - V(h) + i \bar{Q} \partial Q - v \mathcal{G}(h) \left[ \bar{Q}'_L U H_Q Q'_R + \text{h.c.} \right]$$

**GB + h**  
**+ Yukawa sector**

Just the top for this case

**Spherical parametrization**

$$U = \sqrt{1 - \frac{\omega^2}{v^2}} + i \frac{\bar{\omega}}{v}$$

**GB**

$$\bar{\omega} = \tau^a \omega^a$$

$$Q^{(l)} = \begin{pmatrix} \mathcal{U}^{(l)} \\ \mathcal{D}^{(l)} \end{pmatrix}$$

$$\mathcal{U}' = (u, c, t)'$$

$$\mathcal{D}' = (d, s, b)'$$

**Quarks**

**Analytic functions of powers of the Higgs field.** Inspired by most of low energy HEFT models.

$$V(h) = v^4 \sum_{n=3}^{\infty} V_n \left( \frac{h}{v} \right)^n \quad \text{for} \quad V_2 = V_3 = \frac{M_h^2}{2v^2}, \quad V_4 = \frac{M_h^2}{8v^4}, \quad V_{n>4} = 0$$

**Recover the SM**

$$\mathcal{F}(h) = 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + \dots \quad \mathcal{G}(h) = 1 + c_1 \frac{h}{v} + c_2 \frac{h^2}{v^2} + \dots$$



$$a = b = 1$$

$$c_1 = 1$$

$$c_2 = c_3 = \dots c_n = 0$$

**Modifications on the Higgs SM couplings and beyond!**

### 3. Loops

We have calculated the contribution of top quark loops to VBS via the generating functional, obtaining the scattering for gauge bosons. Renormalized the relevant couplings and fields and compared to the existing literature [3].

We have obtained the real and imaginary part of the PWA.

But how important are fermion loops?

The imaginary parts enter in the NLO counting.

In general the bosons dominate at high energy. ( $\sqrt{s} \sim 3 \text{ TeV}$ )

$$\begin{aligned} \text{Im}[Bosons] &= \text{Im}[a_J] \Big|_{W^+W^-, ZZ, HH, \gamma\gamma} \\ \text{Im}[Fermions] &= \text{Im}[a_J] \Big|_{t\bar{t}, b\bar{b}} \end{aligned}$$

$$R_J = \frac{\text{Im}[Fermions]}{\text{Im}[Boson] + \text{Im}[Fermions]}$$

$R \sim 1 \rightarrow$  Fermions dominate

$R \sim 0 \rightarrow$  Bosons dominate

We will inspect this ratio for the PWA of the process  $W^+W^- \rightarrow W^+W^-$

[3] G. Buchalla et al. LMU-ASC 13/20 [4] D. Espriu and J. Matías Phys. Rev. D **52**, 6530

[5] T. Bahnik [hep-ph/9710265](https://arxiv.org/abs/hep-ph/9710265) [6] A. Denner et al Phys. Rev. D **51**, 4738

[7] E. Arganda, C. Garcia-Garcia and M.J Herrero Nucl.Phys.B 945 (2019) 114687

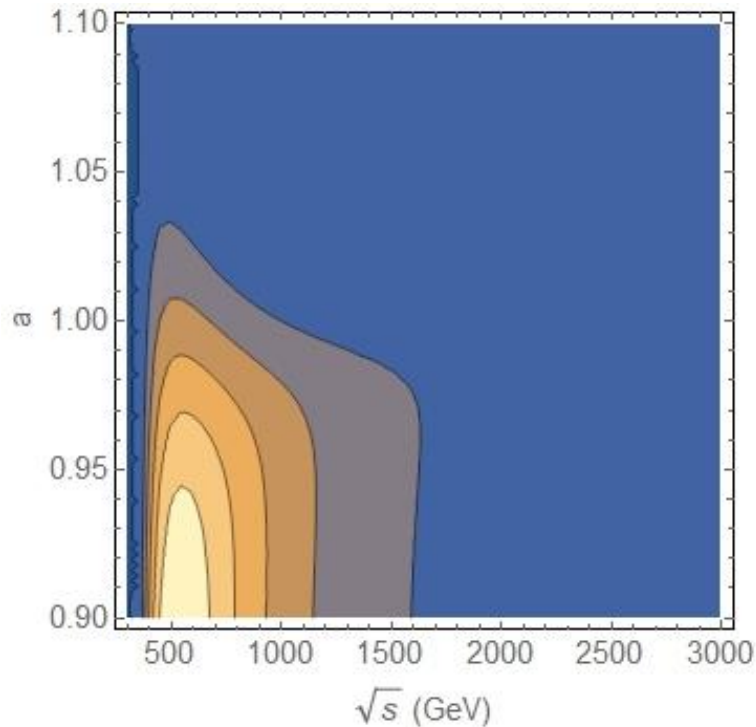
$Im[Bosons]$  depend on  $a$ ,  $b$  and  $d_3$

$Im[Fermions]$  depend on  $a$  and  $c_1$

We will allow a 10% deviation  
from 1

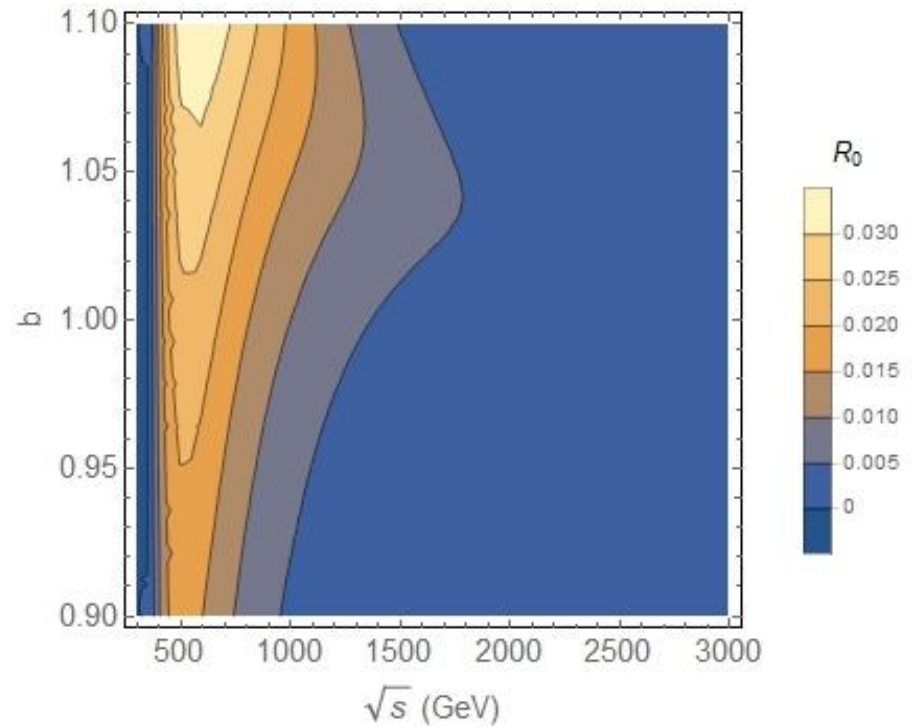
# 4. Results for $W^+W^- \rightarrow W^+W^-$

## 4.1 Partial wave $a_0$ (J=0)



$$b = c_1 = 1$$

5 % corrections at 500 GeV  
máximo for  $a$  around 0.9

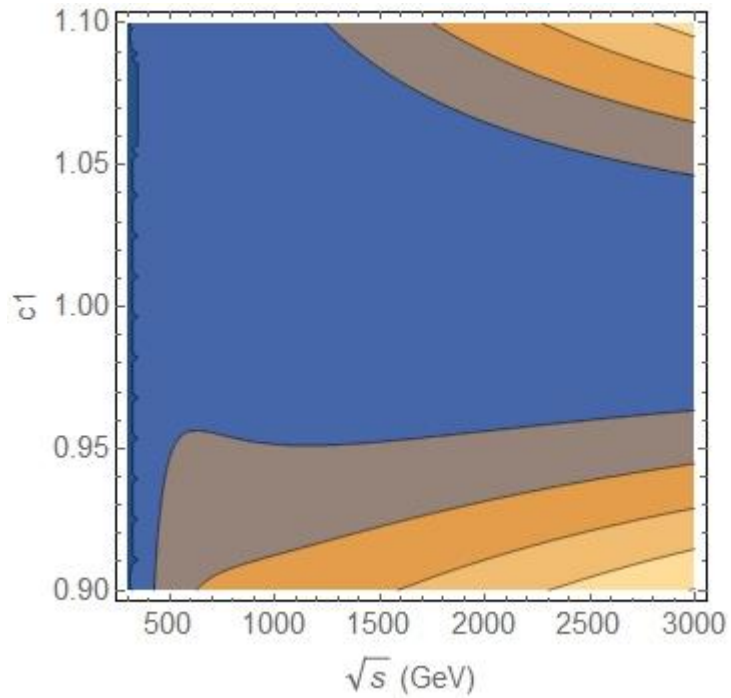


$$a = c_1 = 1$$

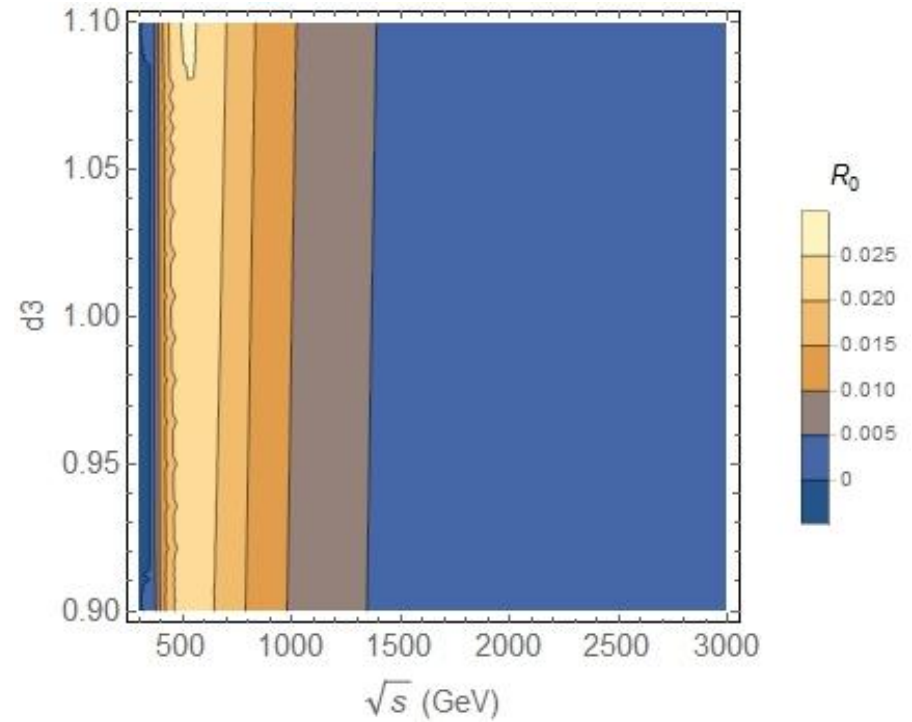
3 % correction at 500 GeV  
for  $b$  around 1.1

Bosons completely dominate over 1 TeV for  $a$  and  $b$

$$a = b = 1$$



We find corrections of 25% at high energies around  $c_1=0.90$  and  $c_1=1.1$



Again 2% corrections. Negligible



# Parameter scan for $a_0$

We inspect  $a$ ,  $b$ ,  $c_1$  and  $d_3 \in [0.90, 1.10]$  [1]

$\sqrt{s}$ ( Tev)	$a$	$b$	$c_1$	$d_3$	$R_0$
1.5	0.95	0.95	0.9	0.95	0.07
1.5	1.05	1.1	1.1	1.1	0.16
3.0	1.0	1.0	0.9	1.0	0.25
3.0	1.0	1.0	1.1	1.0	0.22

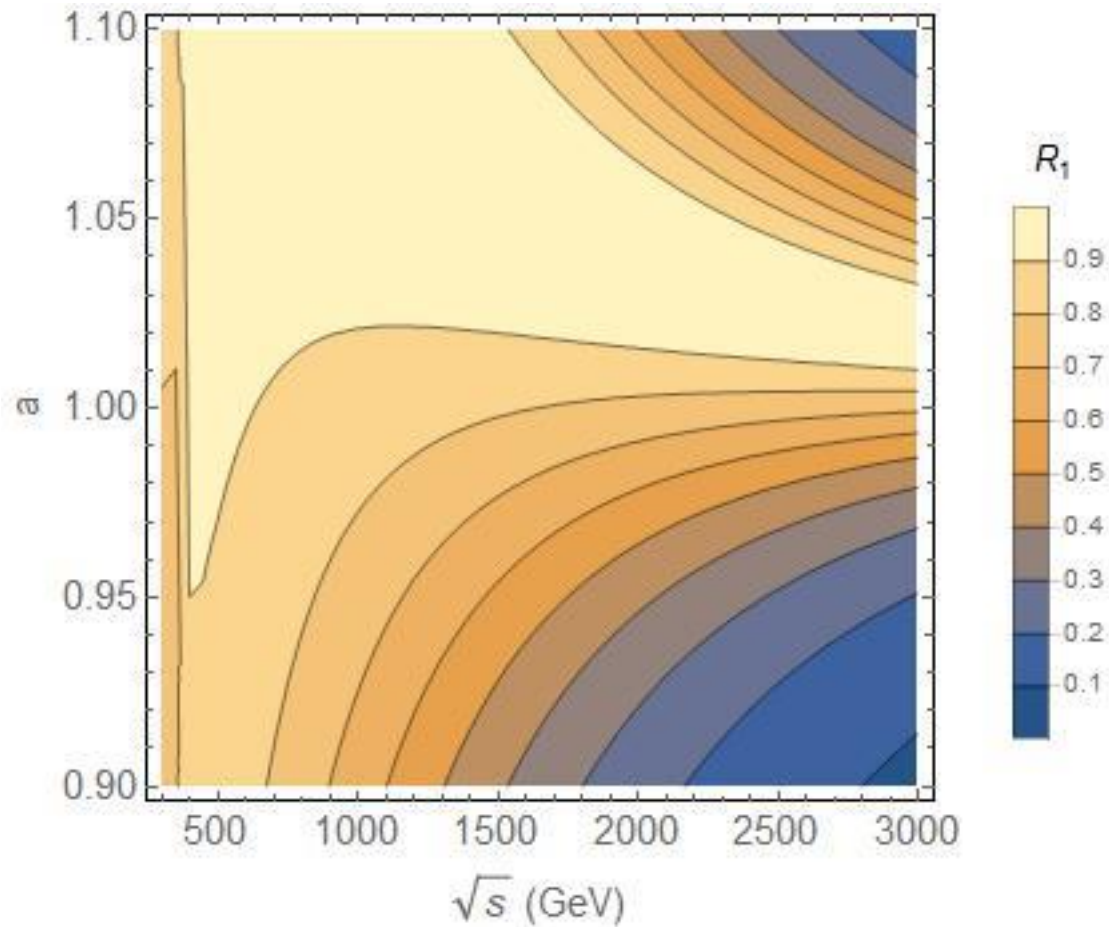


Highest R

Clearly  $c_1$  is the most important parameter for  $J=0$

[1] Handbook of LHC Higgs Cross Sections: 4. - LHC Higgs Cross Section Working Group

## 4.2 Partial wave $a_1$ ( $J=1$ )



$$\text{Im}[\text{Bosons}] = f(a) \approx \left[ \frac{(1-a^2)^{2s}}{96 \pi v^2} \right]^2$$

$$\text{Im}[\text{Fermions}] = \text{Im}[\text{Fermions}]_{SM}$$

Does not depend on  $b, c_1$  or  $d_3$ , just  $a$

High corrections for  $a$  close to 1

# 4. Specific Scenarios: Minimal Composite Higgs Model

Agashe, Contino, Pomarol *Nucl.Phys.B* 719 (2005) 165-187

$$\xi = v^2 / f^2$$

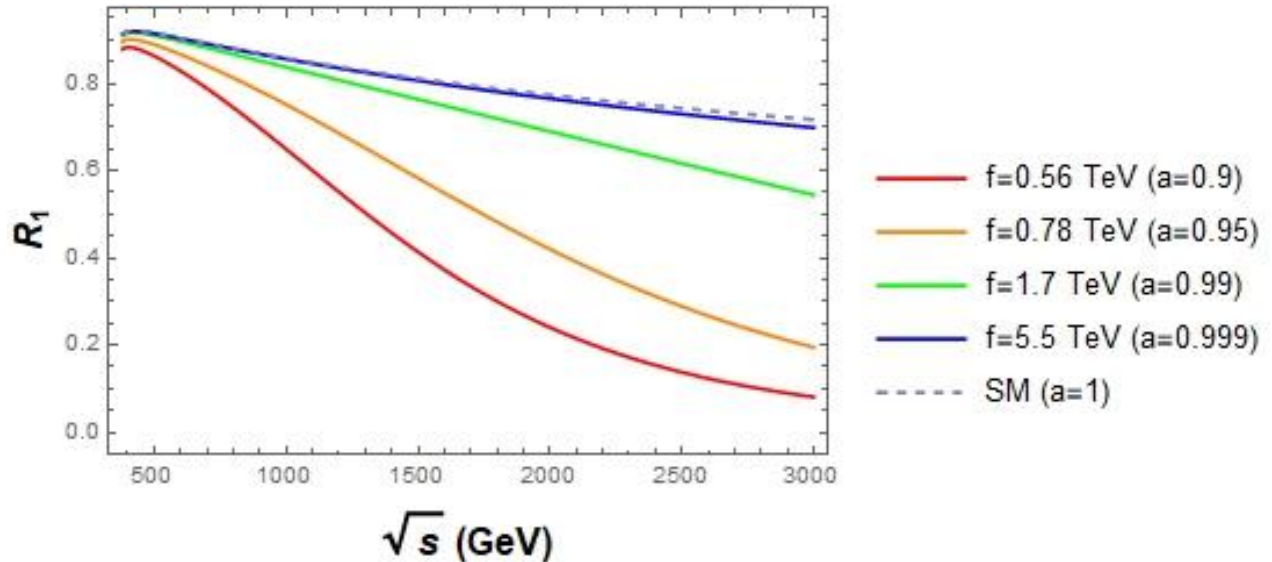
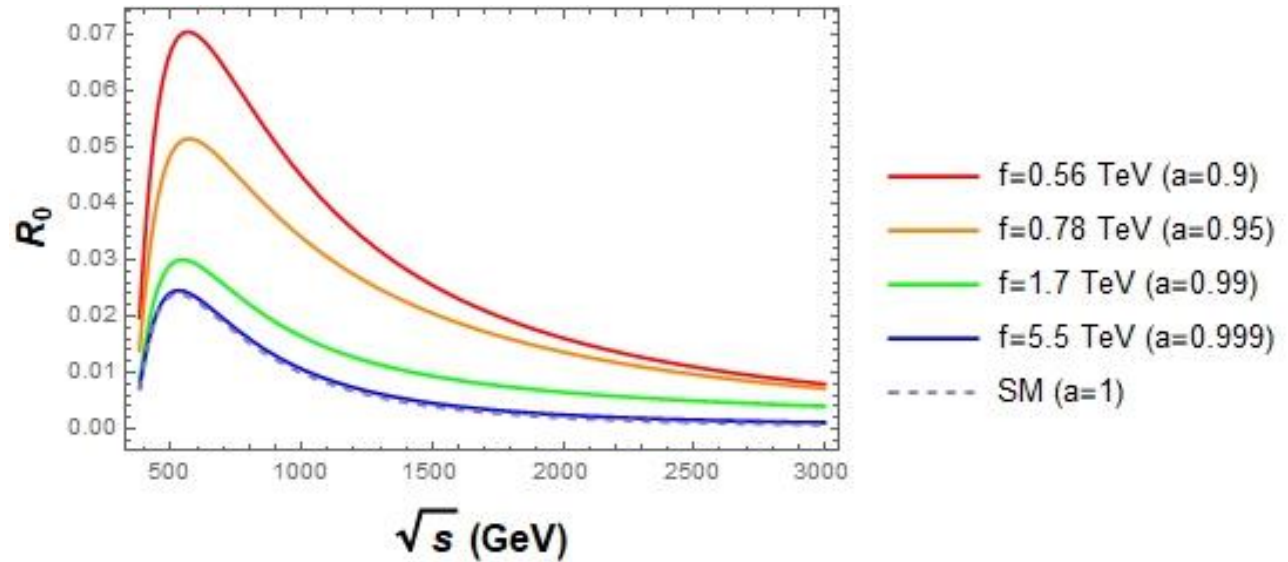
$$b^* = 1 - 2\xi$$

$$a^* = c_1^* = \sqrt{1 - \xi}$$

R1 is significantly larger than R0

a1 more sensitive to fermion corrections

80% corrections at Low energy and for values close to SM



## 5. Conclusions

- We estimate fermion corrections to WW scattering: negligible in most of the parameter space in some cases but not always.
- For instance, the PWA's:

$R_0$	1.5 - 3 TeV	$a = b = d_3 = 1$ and $c_1 = 0.9$	15-25%
$R_1$	1.5- 3 TeV	$a \in [0.95, 1.95]$	60-90%

- The MCHM shows R1 than R0 hence its more sensitive to the fermion corrections.
- Future work: considering the whole amplitude (real and imaginary) and unitarizing.

Thank you.