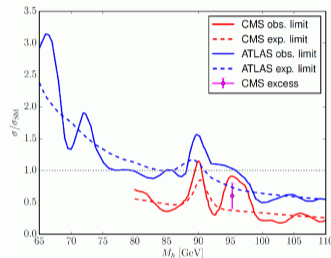
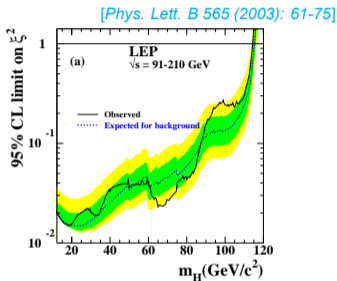


# A 96 GeV Higgs Boson in the 2HDMS

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# Motivation

[T. Stefaniak et al. arxiv.1812.05864]  
[CMS-PAS-HIG-17-013]  
[ATLAS-CONF-2018-025]



- 1 Alternative model interpret the 96 GeV "excess" in experiment
- 2 Extend the 2HDM to the NMSSM-like Higgs structure (complex singlet and  $\mathbb{Z}_3$  symmetry)
- 3 Search the 96 GeV Higgs boson at the future linear colliders (e.g. ILC)
- 4 Cosmological features like baryogenesis, gravitational waves.

# Overview

- > Scan intervals
- > Interpretation of 96 GeV excess
- > Experimental observable at ILC
- > Summary



# Scanning for the parameter space

We focus on Type II Yukawa structure first.

- > Implement the 2HDMS into the SARAH 4.14.3 and obtain the model file for SPheno 4.0.4
- > Use SPheno 4.0.4 to generate the spectra with 2-loop correction ( $\overline{\text{MS}}$  scheme)
- > Find the points in the following parameter space (low  $\tan \beta$ ):

$$\begin{aligned} m_{h_1} &\in \{80, 93\} \text{GeV}, & m_{h_2} &\in \{110, 126\} \text{GeV}, & m_{a_1} &\in \{200, 500\} \text{GeV} \\ m_{h_{\pm}} &\in \{650, 1000\} \text{GeV}, & m_{a_2} &\in \{650, 1000\} \text{GeV}, & m_{h_3} &\in \{650, 1000\} \text{GeV} \\ v_S &\in \{100, 2000\} \text{GeV} & \tan \beta &\in \{1, 4\}, & \alpha_1 &\in \{0.84, \frac{\pi}{2}\} \\ \alpha_2 &\in \{\pm 0.93, \pm 1.27\}, & \alpha_3 &\in \{\pm 1.2, \pm 1.5\}, & \alpha_4 &\in \{1.25, \frac{\pi}{2}\} \end{aligned}$$

- > Testing for theoretical and experimental constraints

## 96 GeV "excess"

LEP signal strengths:

$$\mu_{\text{LEP}} = \frac{\sigma(e^+e^- \rightarrow Zh_1 \rightarrow Zb\bar{b})}{\sigma(e^+e^- \rightarrow ZH_{\text{SM}} \rightarrow Zb\bar{b})} = |c_{h_1VV}|^2 \frac{\text{BR}(h_1 \rightarrow b\bar{b})}{\text{BR}_{\text{SM}}(h \rightarrow b\bar{b})} = 0.117 \pm 0.057 \quad (1)$$

CMS signal strengths:

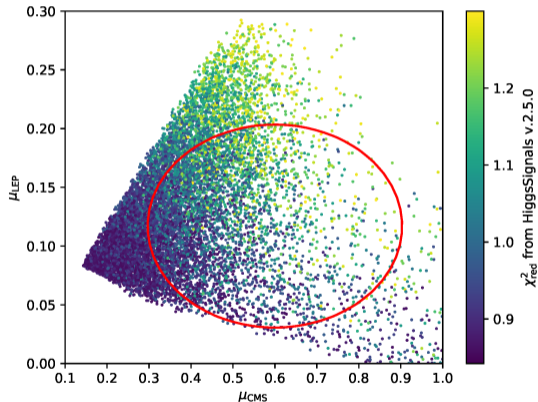
$$\mu_{\text{CMS}} = \frac{\sigma(pp \rightarrow h_1 \rightarrow \gamma\gamma)}{\sigma(pp \rightarrow H_{\text{SM}} \rightarrow \gamma\gamma)} = |c_{h_1tt}|^2 \frac{\text{BR}(h_1 \rightarrow \gamma\gamma)}{\text{BR}_{\text{SM}}(h \rightarrow \gamma\gamma)} = 0.6 \pm 0.2 \quad (2)$$

Fitting to the "excess":

$$\chi^2 = \left( \frac{\mu_{\text{LEP}} - 0.117}{0.057} \right)^2 + \left( \frac{\mu_{\text{CMS}} - 0.6}{0.2} \right)^2 < 2.3 \quad (3)$$

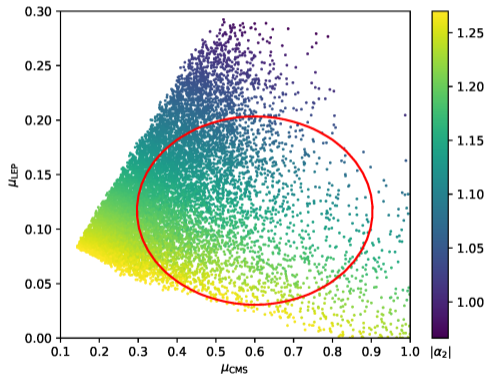
# Scan result for $\tan \beta = 1 \sim 4$

> Accept the points with  $m_{h_1} = (96 \pm 2)$  GeV

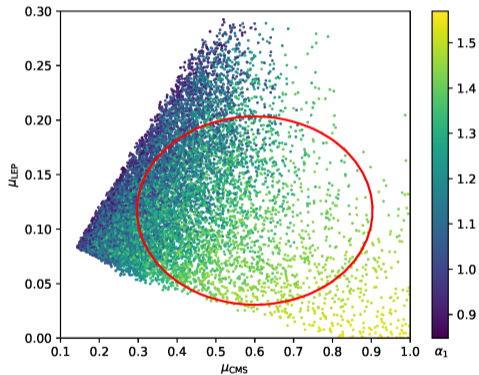


> Lots of "best-fit" points

# Scan result for $\tan \beta = 1 \sim 4$



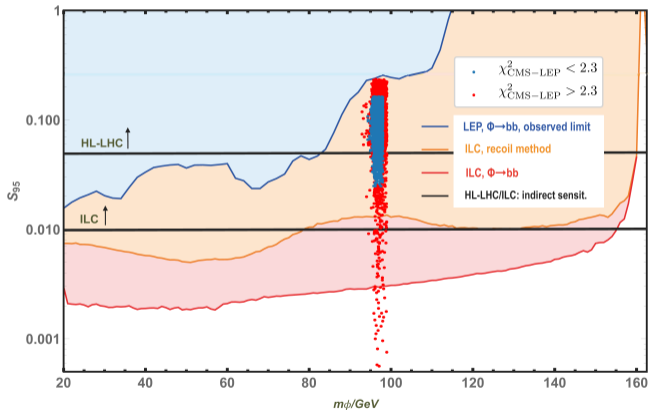
$$c_{h_1 VV} \sim \text{COS } \alpha_2 \text{ COS}(\beta - \alpha_1)$$



$$c_{h_1 bb} \sim \text{COS } \alpha_1 \text{ COS } \alpha_2$$

# Experimental observation

Experimental limit from [G. Moortgat-Pick et al. arXiv.1801.09662]

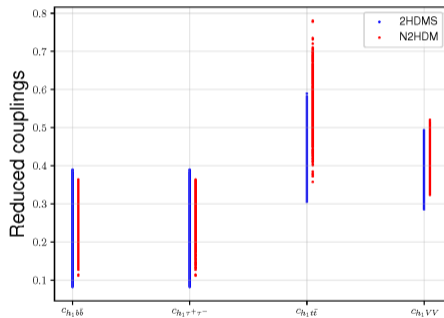
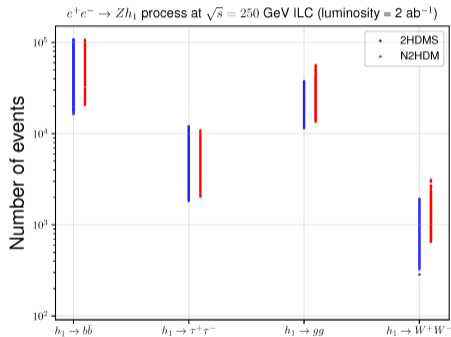


> The light 96 GeV Higgs can be detected at ILC

# Observable and Comparison to N2HDM

How to distinguish the 2HDMS and N2HDM?

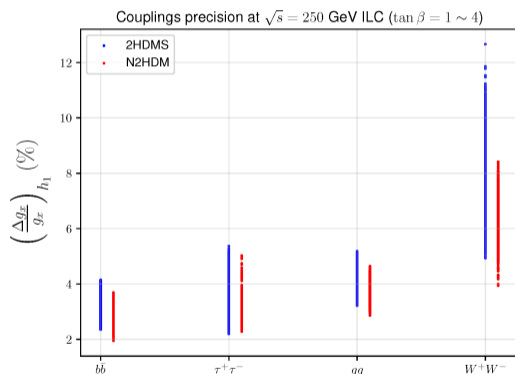
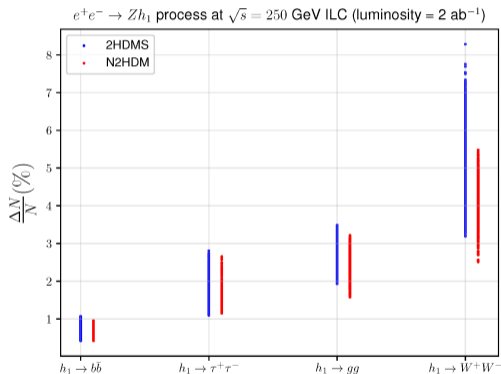
N2HDM data from *T.Biekoetter et al.*



- > 2HDMS could have the number of  $W^+W^-$  events slightly less than N2HDM
- > 2HDMS could have the  $c_{h_1 t\bar{t}}$  coupling smaller than N2HDM

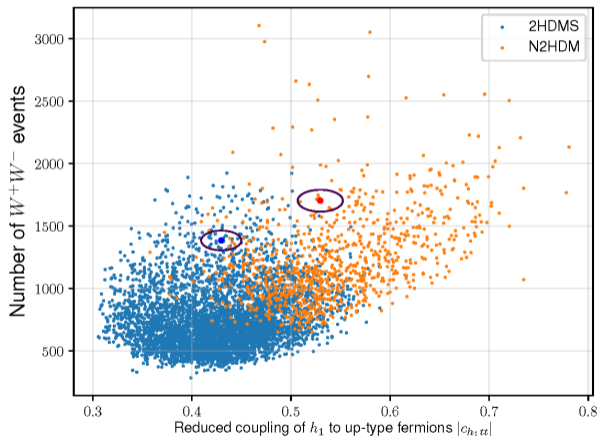
# Observable and Comparison to N2HDM

Method of uncertainties calculation from [T. Barklow et al. arXiv.1708.08912]



> Most of the uncertainties are below 10% at ILC

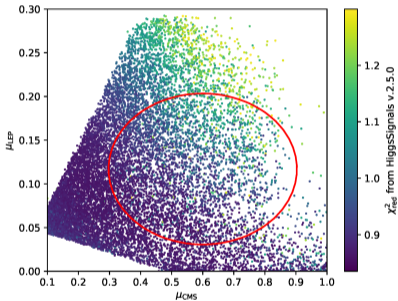
# Observable and Comparison to N2HDM



> One could potentially distinguish the 2HDMS and N2HDM at ILC

# Results for higher $\tan \beta$ range

$\tan \beta = \{4, 10\}$ ,  $m_{h^\pm} = \{650, 1500\}$  GeV

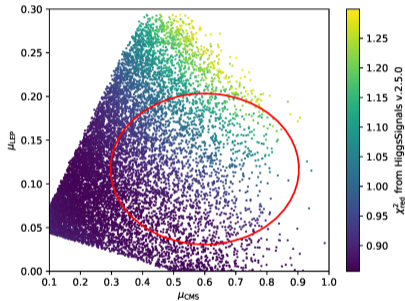


N2HDM: More rigid at higher  $\tan \beta$  range

$$M_{S13}^2 = \lambda_7 v v_S \cos \beta$$

$$M_{S23}^2 = \lambda_8 v v_S \sin \beta$$

$\tan \beta = \{10, 50\}$ ,  $m_{h^\pm} = \{1000, 2500\}$  GeV

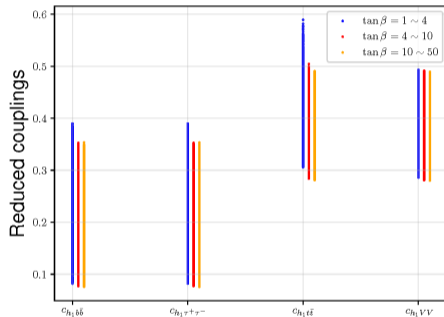
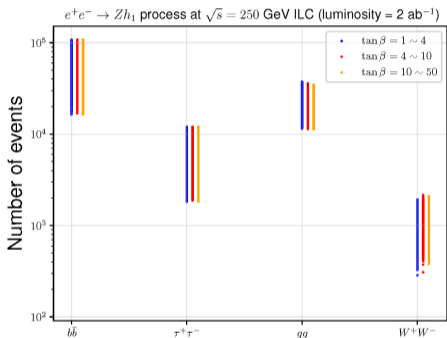


THDMs: Still flexible at higher  $\tan \beta$  range

$$M_{S13}^2 = (2\lambda'_1 v_S \cos \beta + \mu_{12} \sin \beta) v$$

$$M_{S23}^2 = (2\lambda'_2 v_S \sin \beta + \mu_{12} \cos \beta) v$$

# Results for higher $\tan\beta$ range



- > Number of events for different  $\tan\beta$  are almost the same
- > The higher  $\tan\beta$  could suppressed the upper limit of couplings for  $h_1$

# Summary

## Conclusions

- > We performed the scan and obtained lots of points that nicely fit to the 96 GeV "excess"
- > We found some theoretical and experimental distinction between 2HDMS and N2HDM
- > We evaluated number of events for some processes and couplings measurement precision at ILC

## Outlook

- > We will study more about the couplings determination of 2HDMS
- > We could study the light CP-odd Higgs sector of 2HDMS
- > We could also study the baryogenesis based on 2HDMS

# Thank you!

## Contact

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# Backup



# Theoretical framework of 2HDMS

Two Higgs doublets

$$\Phi_1 = \begin{pmatrix} \chi_1^+ \\ v_1 + \frac{\rho_1 + i\eta_1}{\sqrt{2}} \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \chi_2^+ \\ v_2 + \frac{\rho_2 + i\eta_2}{\sqrt{2}} \end{pmatrix},$$

Additional complex singlet

$$S = v_S + \frac{\rho_S + i\eta_S}{\sqrt{2}} \quad (4)$$

Convention of vacuum expectation values

$$\tan \beta = \frac{v_2}{v_1}, \quad v = \sqrt{v_1^2 + v_2^2} = 174 \text{ GeV} \quad (5)$$

$\mathbb{Z}_2$  Symmetry:

$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \\ S \end{pmatrix} \rightarrow \begin{pmatrix} \Phi_1 \\ -\Phi_2 \\ S \end{pmatrix} \quad (6)$$

$\mathbb{Z}_3$  Symmetry:

$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \\ S \end{pmatrix} \rightarrow \begin{pmatrix} \Phi_1 \\ e^{i\frac{2\pi}{3}} \Phi_2 \\ e^{-i\frac{2\pi}{3}} S \end{pmatrix} \quad (7)$$

# Theoretical framework of 2HDMS

Higgs potential [S. Baum, N. Shah arXiv:1808.02667]:

$$\begin{aligned} V = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ & + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) - m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \\ & + m_S^2 S^\dagger S + \lambda'_1 (S^\dagger S) (\Phi_1^\dagger \Phi_1) + \lambda'_2 (S^\dagger S) (\Phi_2^\dagger \Phi_2) \\ & + \frac{\lambda_3''}{4} (S^\dagger S)^2 + \left( \frac{\mu_{S1}}{6} S^3 + \mu_{12} S \Phi_1^\dagger \Phi_2 + \text{h.c.} \right) \end{aligned} \quad (8)$$

12 free parameters:

$$\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda'_1, \lambda'_2, \lambda_3'', m_{12}, \mu_{S1}, \mu_{12}, v_S, \tan \beta \quad (9)$$

- >  $m_{12}$  softly break the  $\mathbb{Z}_2, \mathbb{Z}_3$  symmetry
- >  $\mu_{12}$  softly break the  $\mathbb{Z}_2$  symmetry



# Theoretical framework of 2HDMS

Tree level Higgs mass matrices:

$$M_{S11}^2 = 2\lambda_1 v^2 \cos^2 \beta + (m_{12}^2 - \mu_{12} v_S) \tan \beta$$

$$M_{S22}^2 = 2\lambda_2 v^2 \sin^2 \beta + (m_{12}^2 - \mu_{12} v_S) \cot \beta$$

$$M_{S12}^2 = (\lambda_3 + \lambda_4) v^2 \sin 2\beta - (m_{12}^2 - \mu_{12} v_S)$$

$$M_{S13}^2 = (2\lambda'_1 v_S \cos \beta + \mu_{12} \sin \beta) v$$

$$M_{S23}^2 = (2\lambda'_2 v_S \sin \beta + \mu_{12} \cos \beta) v$$

$$M_{S33}^2 = \frac{\mu_{S1}}{2} v_S + \lambda_3'' v_S^2 - \mu_{12} \frac{v^2}{2v_S} \sin 2\beta$$

$$M_{P11}^2 = (m_{12}^2 - \mu_{12} v_S) \tan \beta$$

$$M_{P22}^2 = (m_{12}^2 - \mu_{12} v_S) \cot \beta$$

$$M_{P12}^2 = -(m_{12}^2 - \mu_{12} v_S)$$

$$M_{P13}^2 = \mu_{12} v \sin \beta$$

$$M_{P23}^2 = -\mu_{12} v \cos \beta$$

$$M_{P33}^2 = -\frac{3}{2} \mu_{S1} v_S - \mu_{12} \frac{v^2}{2v_S} \sin 2\beta$$

$$M_C^2 = 2(m_{12}^2 - \mu_{12} v_S) \csc 2\beta - \lambda_4 v^2$$

(10)

# Theoretical framework of 2HDMS

$$\tilde{\mu}^2 = \cos^2 \alpha_4 m_{a1}^2 + \sin^2 \alpha_4 m_{a2}^2$$

$$\lambda_1 = \frac{1}{2v^2 \cos^2 \beta} \left[ \sum_i m_{h_i}^2 R_{i1}^2 - \tilde{\mu}^2 \sin^2 \beta \right]$$

$$\lambda_2 = \frac{1}{2v^2 \sin^2 \beta} \left[ \sum_i m_{h_i}^2 R_{i2}^2 - \tilde{\mu}^2 \cos^2 \beta \right]$$

$$\lambda_3 = \frac{1}{v^2} \left[ \frac{1}{\sin 2\beta} \sum_i m_{h_i}^2 R_{i1} R_{i2} + m_{h^\pm}^2 - \tilde{\mu}^2 \right]$$

$$\lambda_4 = \frac{\tilde{\mu}^2 - m_{h^\pm}^2}{v^2}$$

$$m_{12}^2 = \mu_{12} v_S + \tilde{\mu}^2 \sin \beta \cos \beta$$

$$\mu_{12} = \frac{m_{a1}^2 - m_{a2}^2}{v} \sin \alpha_4 \cos \alpha_4$$

$$\lambda'_1 = \frac{1}{2v_S v \cos \beta} \left[ \sum_i m_{h_i}^2 R_{i1} R_{i3} - \mu_{12} v \sin \beta \right]$$

$$\lambda'_2 = \frac{1}{2v_S v \sin \beta} \left[ \sum_i m_{h_i}^2 R_{i2} R_{i3} - \mu_{12} v \cos \beta \right]$$

$$\lambda''_3 = \frac{1}{v_S^2} \left[ \sum_i m_{h_i}^2 R_{i3}^2 + \mu_{12} \frac{v^2}{2v_S} \sin 2\beta - \frac{\mu_{S1}}{2} v_S \right]$$

$$\mu_{S1} = -\frac{2}{3v_S} \left[ \sin^2 \alpha_4 m_{a1}^2 + \cos^2 \alpha_4 m_{a2}^2 + \frac{v}{2v_S} \sin 2\beta \mu_{12} \right]$$

# Theoretical framework of 2HDMS

Scalar potential  $\xrightarrow{\text{second derivative}}$  mass matrix  $\xrightarrow{\text{diagonalization}}$  mass eigenvalues & mixing matrix

Parameterize the CP-even and CP-odd mixing matrices by 4 mixing angles  $\alpha_{1,2,3,4}$ :

$$R = \begin{pmatrix} c_{\alpha_1} c_{\alpha_2} & s_{\alpha_1} c_{\alpha_2} & s_{\alpha_2} \\ -s_{\alpha_1} c_{\alpha_3} - c_{\alpha_1} s_{\alpha_2} s_{\alpha_3} & c_{\alpha_1} c_{\alpha_3} - s_{\alpha_1} s_{\alpha_2} s_{\alpha_3} & c_{\alpha_2} s_{\alpha_3} \\ s_{\alpha_1} s_{\alpha_3} - c_{\alpha_1} s_{\alpha_2} c_{\alpha_3} & -s_{\alpha_1} s_{\alpha_2} c_{\alpha_3} - c_{\alpha_1} s_{\alpha_3} & c_{\alpha_2} c_{\alpha_3} \end{pmatrix} \quad (11)$$

$$R_A = \begin{pmatrix} c_{\beta} & s_{\beta} & 0 \\ -s_{\beta} c_{\alpha_4} & c_{\beta} c_{\alpha_4} & s_{\alpha_4} \\ s_{\beta} s_{\alpha_4} & -c_{\beta} s_{\alpha_4} & c_{\alpha_4} \end{pmatrix} \quad (12)$$

The mass matrices can be written in terms of the masses and mixing angles

$$M_S^2 = R^T \text{diag}\{m_{h_1}^2, m_{h_2}^2, m_{h_3}^2\} R, \quad M_P^2 = R_A^T \text{diag}\{0, m_{a_1}^2, m_{a_2}^2\} R_A \quad (13)$$

Inputs of mass basis (12 parameters):

$$m_{h_{1,2,3}}, m_{a_{1,2}}, m_{h^{\pm}}, \alpha_{1,2,3,4}, v_S, \tan \beta \quad (14)$$

# Testing for constraints

## Theoretical constraints

- > Perturbative unitarity  $\longrightarrow$   $2 \rightarrow 2$  scattering matrix [*J. Horejsi, M. Kladiva arXiv.0510154*]
- > Vacuum stability  $\longrightarrow$  Boundedness from below and Evade [*K.G. Klimenko Theor. Math. Phys. 62, 58–65 (1985)*]

## Experimental constraints

- > LEP, Tevatron & LHC Higgs searches  $\longrightarrow$  HiggsBounds 5.9.0
- > SM Higgs couplings  $\longrightarrow$  HiggsSignals 2.5.0
- > Electroweak precision observable  $\longrightarrow$   $S, T, U$  parameters [*M. Baak et al. arXiv.1209.2716*]
- > Flavor physics  $B \rightarrow X_s \gamma$  limit  $\longrightarrow$  Lower bound of the  $m_{h^\pm}$  [*O. Deschamps et al. arXiv.0907.5135*]

# Backup

N2HDM scalar potential:

$$\begin{aligned} V = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) \\ & + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[ \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 - m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] \\ & + \frac{1}{2} m_S^2 S^2 + \frac{\lambda_6}{8} S^4 + \frac{\lambda_7}{2} S^2 (\Phi_1^\dagger \Phi_1) + \frac{\lambda_8}{2} S^2 (\Phi_2^\dagger \Phi_2) \end{aligned} \quad (15)$$

N2HDM CP-even Higgs mass matrix:

$$M_S^2 = \begin{pmatrix} \lambda_1 c_\beta^2 v^2 + t_\beta m_{12}^2 & \lambda_{345} c_\beta s_\beta v^2 - m_{12}^2 & \lambda_7 c_\beta v v_S \\ \lambda_{345} c_\beta s_\beta v^2 - m_{12}^2 & \lambda_2 s_\beta^2 v^2 + m_{12}^2 / t_\beta & \lambda_8 s_\beta v v_S \\ \lambda_7 c_\beta v v_S & \lambda_8 s_\beta v v_S & \lambda_6 v_S^2 \end{pmatrix} \quad (16)$$

# Scan result for $\tan \beta = 1 \sim 4$

