



Integrated luminosity measurement at CEPC

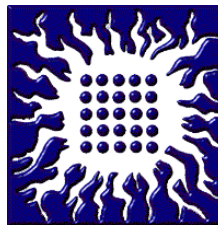
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On behalf of the CEPC Collaboration

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- Reminder on luminosity measurement as a counting experiment
- MDI layout (see Haoyu Shi's talk in MDI session)
- Luminometer at CEPC
- Systematics in luminosity measurement at CEPC
 - Effects from mechanical uncertainties and MDI
 - Data-driven correction of the uncertainty of the effective center-of-mass energy
 - Discussion on EMD
 - Physics processes as background to the Bhabha count
- Summary



Reminder on luminosity measurement as a counting experiment



- Integrated luminosity measurement based on Bhabha scattering is a counting experiment

$$\mathcal{L} = \frac{N_{Bh}}{\sigma}$$

- N_{Bh} is Bhabha count in the certain phase space of physics parameters including the detector acceptance (fiducial) region
- σ is the theoretical cross-section in the same geometrical and phase space
- Both N_{Bh} and σ have to be known at the luminosity uncertainty level (10^{-3} (or -4))

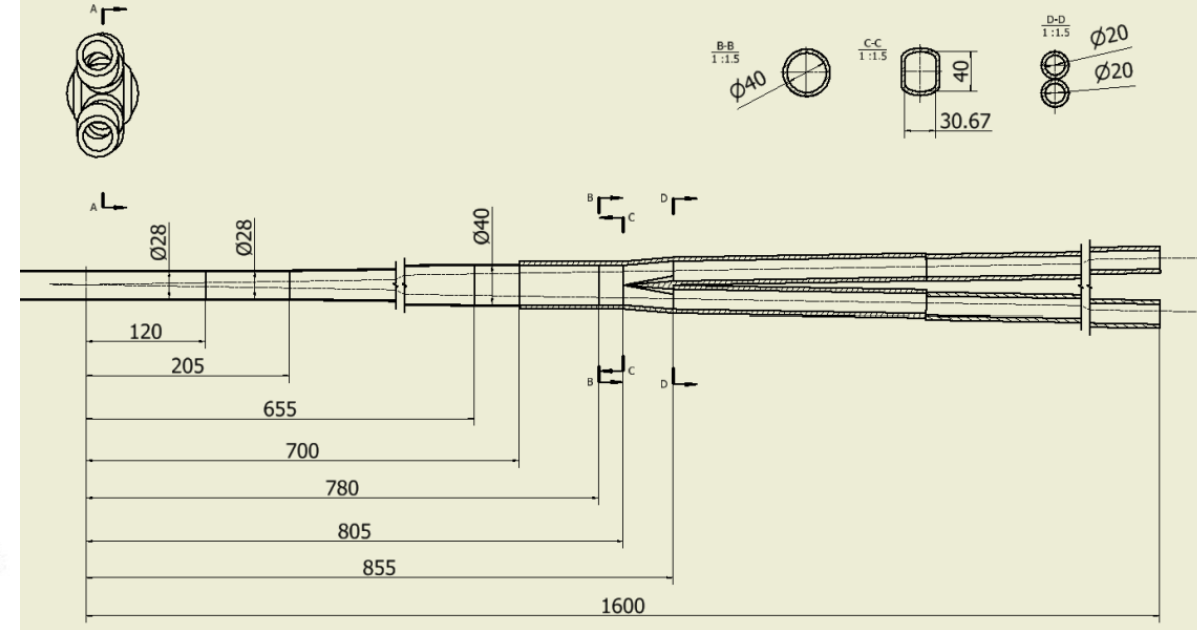
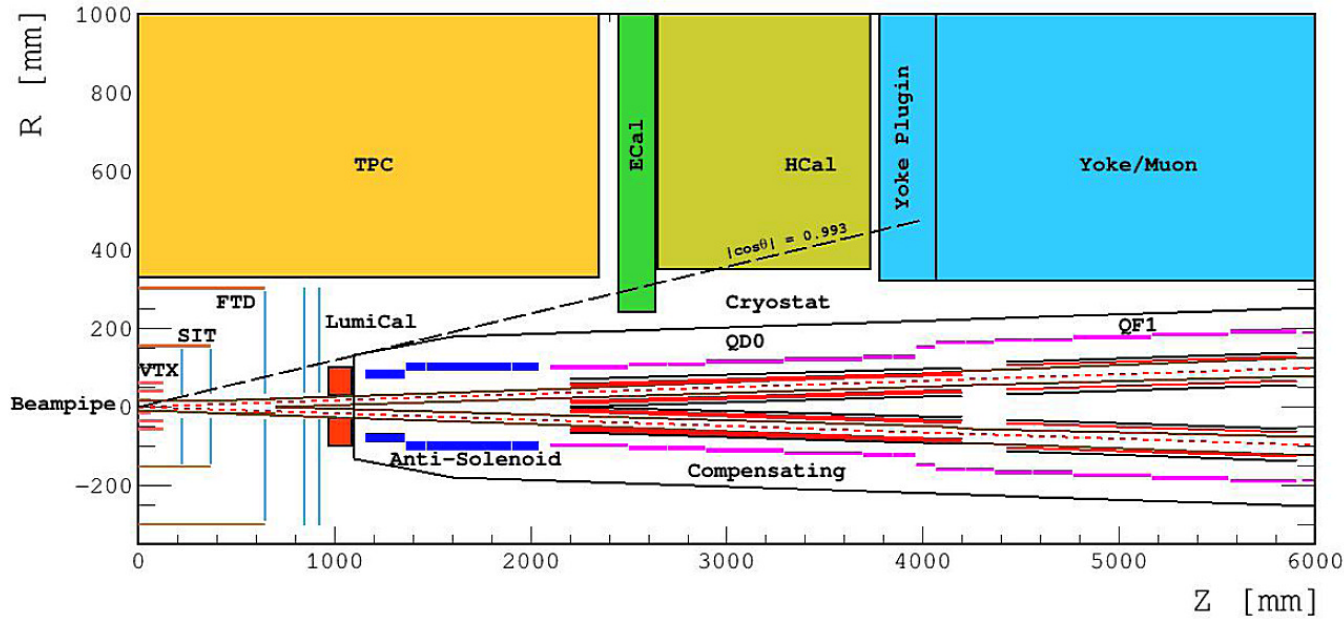
In experiment, $N_{Bh} \rightarrow N_x$

- N_x , effected by miscounts due to various effects:
 - detector resolution
 - mechanics (positioning and alignment) ✓
 - center-of-mass energy, beam synchronization, IP displacements ✓
 - physics background ✓
 - beam-induced processes (EMD) ✓
 - off-momentum electrons (addressed in the [[CEPC CDR](#)])

To correct for it (recover N_{Bh}) implies that effects have to be known at 10^{-3} (or -4) level



MDI layout and IR design



Revised beampipe design

- The Machine Detector Interface(MDI) of CEPC is about 6m long from the IP.
- The accelerator components inside the detector without shielding are within a conical space with an opening angle of $\arccos 0.993$.
- The two beams collide at the IP with a crossing angle of 33 mrad in horizontal plane, and the final focus length is 2.2m
- Lumical will be installed in longitudinal 0.95-1.11 m, with inner radius 28.5 mm and outer radius 100 mm.

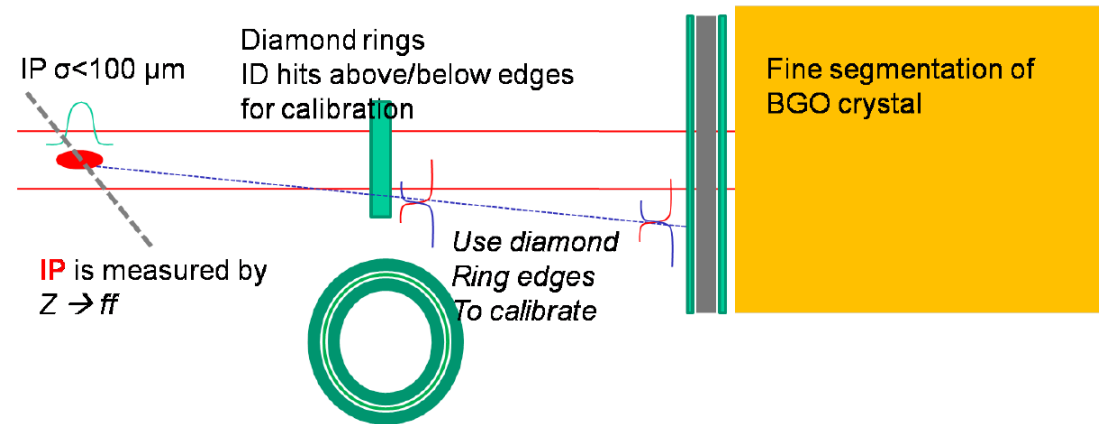
[Haoyu Shi, Status on CEPC MDI IR design]



- Luminometer technology options are open
- Coarse segmentation, compact electronics, search feasible readout chips
- Performance in terms **of energy and polar angle measurement** will play a key role in the control of systematics.

- **Si-W 'ILC-like' – used in our studies**

- BGO (bunch spacing of 25 ns is an issue at Z^0 pole CEPC);
- Lutetium Yttrium Orthosilicate ($\text{Lu}_2\text{SiO}_5:\text{Ce}$) may work in a CMS-like shashlik type of calorimeter
- SciFi spaghetti calorimeter with individually read-out fibers (prototyped for J-PARC K_L experiment)

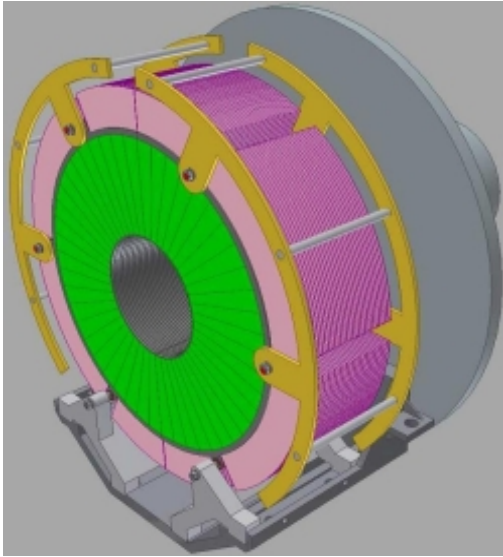


Si or diamond layer in front of the luminometer seems to be a viable option to enable:

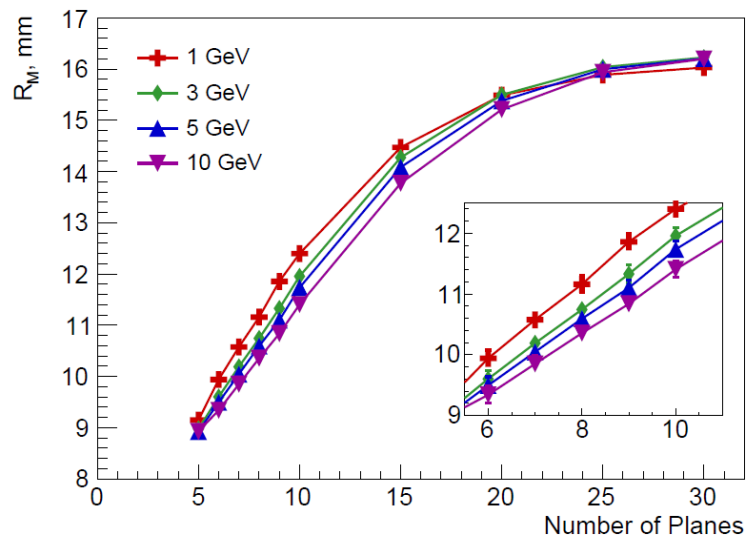
- calibration
- e/γ separation
- polar angle measurement with precision equivalent to $1 \mu\text{m}$ radial uncertainty

[Courtesy: S. Hou]





- Si-W sandwich type of calorimeter, over $20 X_0$ (longitudinal, not larger than 10 cm)
- distance from IP: ~ 100 cm
- polar angle coverage: 26 mrad – 105 mrad
- fiducial volume: 53 mrad – 79 mrad
- Sensors placed in 2 mm air gaps
- Fine Si-pixel segmentation (i.e 48/64 azimuthal/radial)
- Small (effective) Moliere radius (~ 2 cm)
- -> **Excellent resolution in E and θ** : 20% sampling term, 10^{-3} mrad in θ



[arXiv:1812.11426v1 \[physics.ins-det\]](https://arxiv.org/abs/1812.11426v1)

Existing and proven technology in a test-beam (FCAL Collaboration) - see FCAL talk by Alina

[arXiv:1812.11426v1 \[physics.ins-det\]](https://arxiv.org/abs/1812.11426v1), [Eur.Phys.J. C78 \(2018\) no.2, 135](https://arxiv.org/abs/1411.4431),
[arXiv:1411.4431 \[physics.ins-det\]](https://arxiv.org/abs/1411.4431)

Goal: relative uncertainty of the integrated luminosity measurement:

$\sim 10^{-4}$ at Z^0 pole and $\sim 10^{-3}$ at 240 GeV

$$\mathcal{L} = \frac{N_{Bh}}{\sigma}$$

Uncertainty of \mathcal{L} :

- **Modification of the acceptance region** (either directly or through the loss of colinearity of Bhabha events via longitudinal boost)
- **Effect on the Bhabha cross-section calculation** (modification of the phase space and E_{CM})
- **Sensitivity of selection based observables** (reconstructed energy, polar and azimuthal angles)

A long list of sources of integrated luminosity systematic uncertainties:

1. Beam related:

- Uncertainty of the average net CM energy
- Uncertainty of the asymmetry in energy of the e^+ and e^- beam
- Uncertainty of the beam energy spread
- IP position displacement and fluctuations w.r.t. the LumiCal, finite beam sizes at the IP

2. Detector related:

- Uncertainty of the LumiCal inner radius
- Positioning of the LumiCal (longitudinal L-R distance)
- Mechanical fluctuations of the LumiCal position w.r.t the IP (vibrations, thermal stress)
- Tilt and twist of the calorimeters
- Uncertainty of the sampling term
- Detector performance: energy and polar angle resolution

3. Physics interactions:

- Bhabha and physics background cross-section (uncertainty of the count)
- Bhabha acolinearity – other sources of the acceptance losses (ISR and FSR, Beamstrahlung)
- Machine-related backgrounds – EMD
- Off-momentum electrons from the beam-gas scattering



- **Simulation:**

- 10^{-7} Bhabha scattering events generated using BHLUMI Bhabha event generator, at two CEPC center-of-mass energies: 240 GeV and Z^0 production threshold
- The effective Bhabha cross-section in fiducial volume is of order of a few nb
- Final state particles are accepted in the polar angle range from 45 mrad to 85 mrad that is slightly wider than the fiducial volume, to allow events with non-collinear FSR to contribute
- Close-by particles are summed up to imitate cluster merging
- We assumed that the shower leakage from the luminometer is negligible

- **Event selection:**

- asymmetric in polar angle acceptance on the left and right arm of the detector (like at OPAL) - at one side we consider the full fiducial volume, while at the other side we shrink the radial acceptance for Δr ; this has been done subsequently to the left (L) and right (R) side of the luminometer, event by event
- high-energy electrons carry more than 50% of the available beam energy



Systematic uncertainties from mechanics and MDI

Considered detector-related uncertainties arising from manufacturing, positioning and alignment:

- uncertainty of the luminometer inner radius (Δr_{in}),
- spread of the measured radial shower position w.r.t. to the true impact position on the luminometer front plane (σ_r),
- uncertainty of the longitudinal distance between left and right halves of the luminometer (Δd),
- mechanical fluctuations of the luminometer position with respect to the IP caused by vibrations and thermal stress, radial and axial ($\sigma_{X_{ip}}$, $\sigma_{Z_{ip}}$),
- twist of the calorimeters corresponding to different rotations of the left and right detector axis with respect to the outgoing beam ($\Delta\phi$)

Considered MDI related effects:

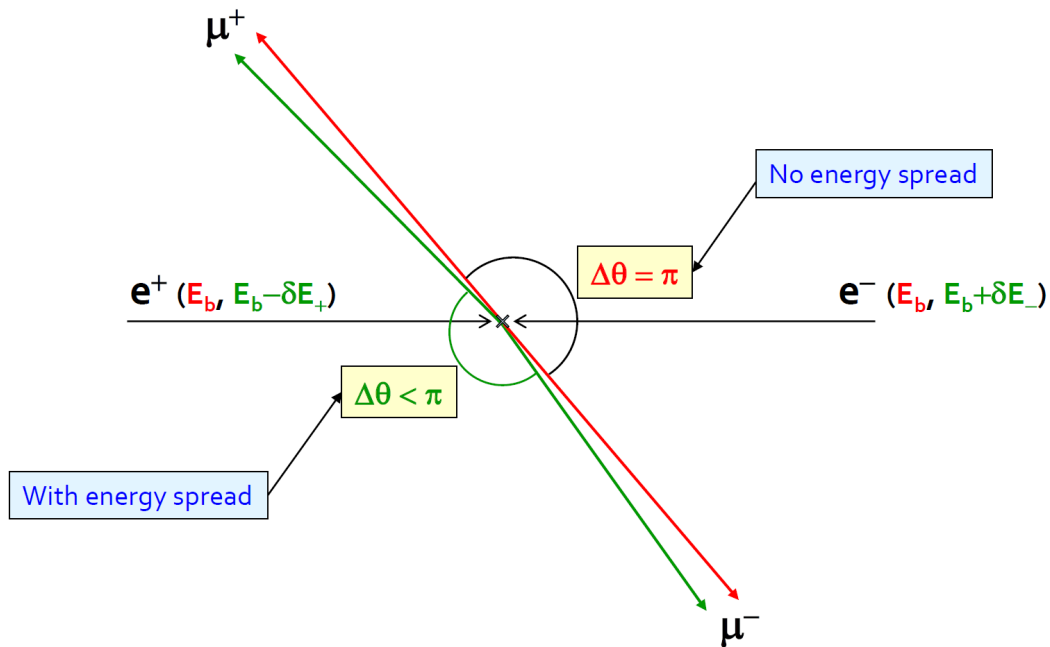
- uncertainty of the average net center-of-mass energy (ΔE_{CM}),
- uncertainty of the asymmetry in energy of the e^+ and e^- beams, ($|E_{e^+} - E_{e^-}|$),
- IP position displacements with respect to the luminometer, radial and axial (Δx_{IP} , Δz_{IP}), caused by the finite beam transverse sizes and beam synchronization, respectively.

parameter	limit@240 GeV $\Delta L/L=10^{-3}$	limit@91 GeV $\Delta L/L=10^{-4}$
ΔE_{CM} (MeV)	120	5
$ E_{e^+} - E_{e^-} $ (MeV)	240	11
Δx_{IP} (mm)	1.0	0.5
Δz_{IP} (mm)	10.0	2.0
beam synch. (ps)	15	3
Δr_{in} (μm)	10	1
σ_r (mm)	1.00	0.20
Δd (mm)	1.00	0.08
$\sigma_{X_{ip}}$ (mm)	1.0	0.5
$\sigma_{Z_{ip}}$ (mm)	10	7
$\Delta\phi$ (mrad)	6.0	0.8

Main systematic effects are coming from the uncertainty of the luminometer inner radius and the effective center-of-mass energy



Systematic uncertainty from the uncertainty of effective center-of-mass energy



- CEPC CDR: beam-energy spread will not exceed 0.134% of the E_{beam} @240 GeV and 0.08% of the E_{beam} @ 91.2 GeV
- Non-zero beam-spread will result in acollinearity of final state muons produced in $e^+e^- \rightarrow \mu^+\mu^-$
- CEPC: muon polar angle resolution over the whole tracking volume foreseen be 0.1 mrad, which corresponds to 100 μm position resolution in TPC
- The effective center-of-mass energy s' can be calculated from the reconstructed muons' polar angles from the TPC:

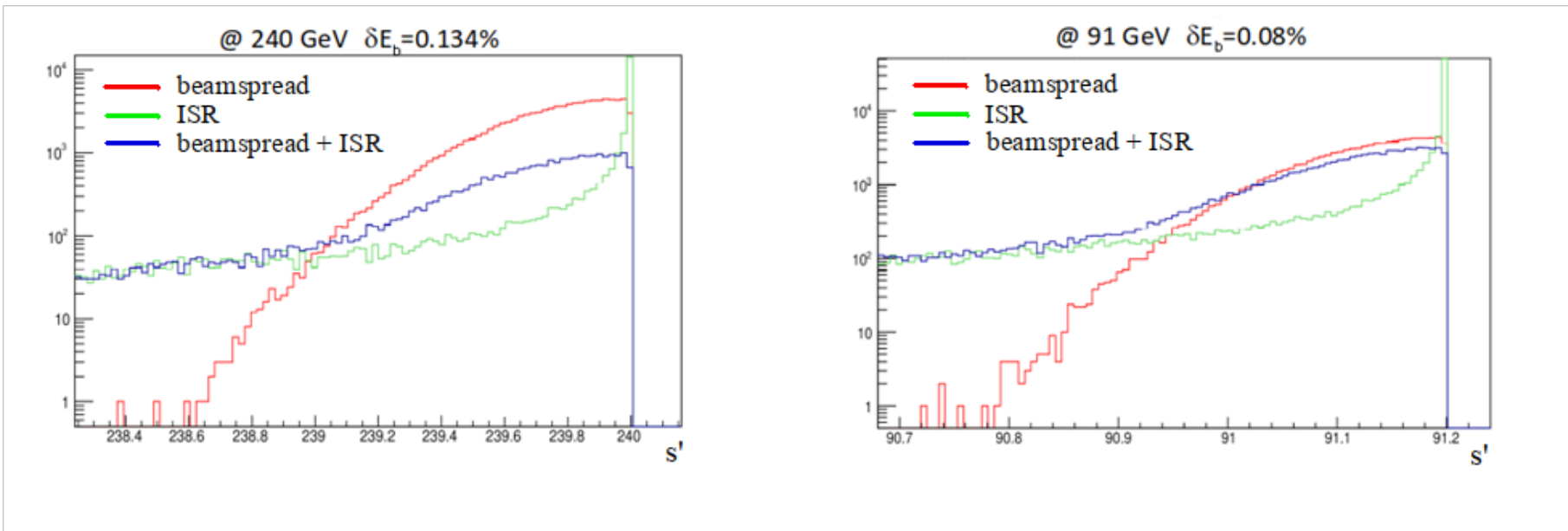
$$\frac{s'}{s} = \frac{\sin\theta^+ + \sin\theta^- - |\sin(\theta^+ + \theta^-)|}{\sin\theta^+ + \sin\theta^- + |\sin(\theta^+ + \theta^-)|}$$

[P. Janot, Beam Energy Spread Measurement @ FCC-ee]



Systematic uncertainty from the uncertainty of effective center-of-mass energy

- In WHIZARD 2.6.2 we generated between 100K and 250K $e^+e^- \rightarrow \mu^+\mu^-$ events at 91.2 GeV and 240 GeV, in polar angle range 8° - 172° , which is the angular acceptance of the TPC at CEPC
- Events are generated without any additional effects, in order to study individual effects of ISR, beamstrahlung and muon angular resolution competing with the beam-spread
- Detector energy resolution is simulated by performing Gaussian smearing of the muons' polar angles in case of a few different central tracker reconstruction capabilities

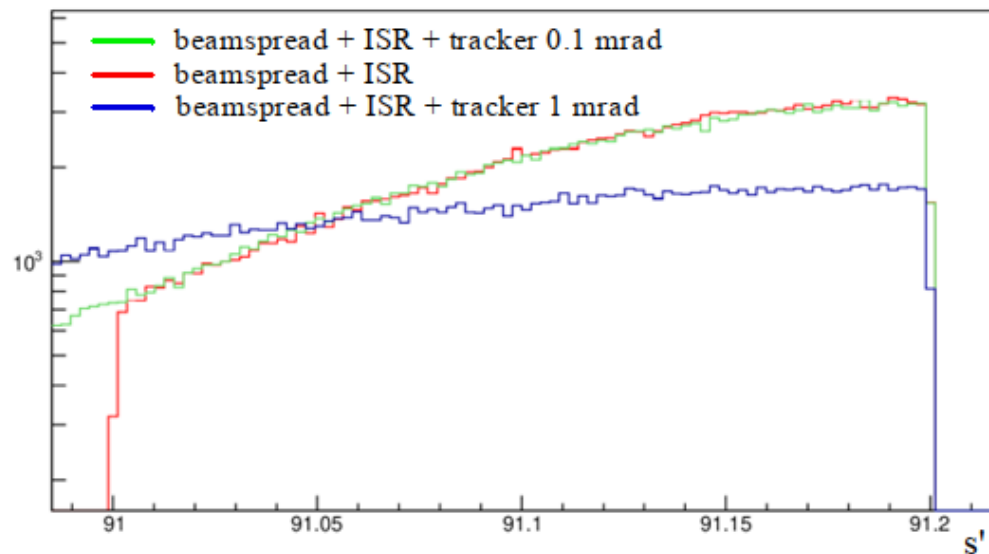


- Tracker (muon polar angle) resolution is not considered
- At both energies the beam-spread dominates the s' shape at energies close to the nominal center-of-mass energy
- In order to rely on this method, excellent theoretical description of ISR effect is required

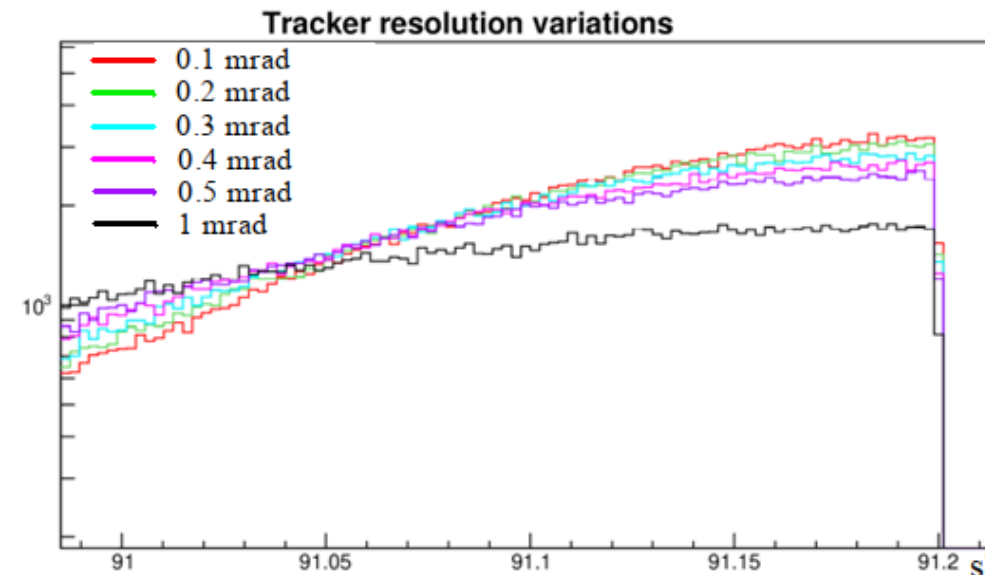
s' distribution in the presence of ISR and the beam-spread



Systematic uncertainty from the uncertainty of effective center-of-mass energy



s' sensitivity to 0.1 mrad and 1 mrad tracker resolutions at 91.2 GeV

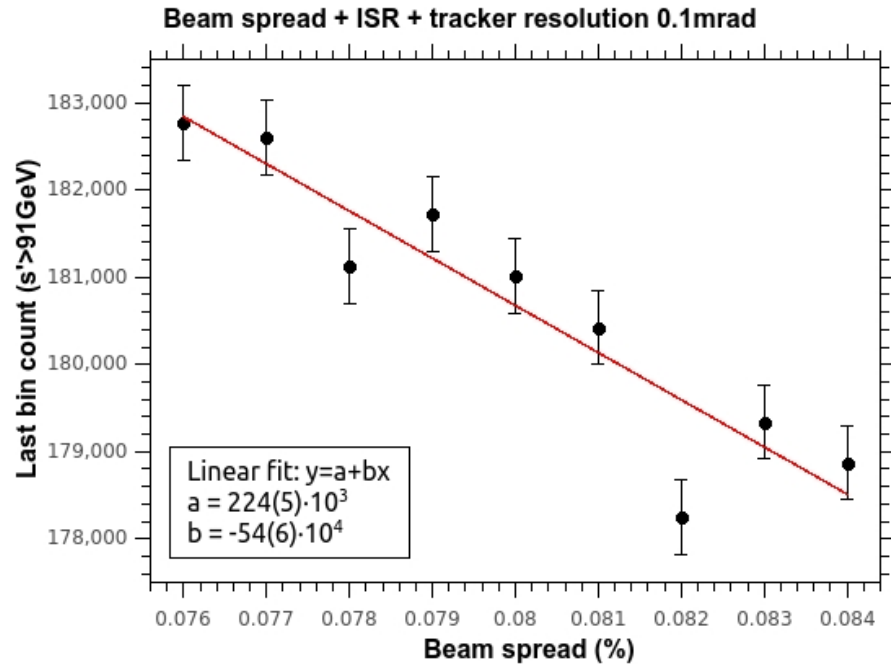


s' sensitivity to the different tracker resolutions at 91.2 GeV

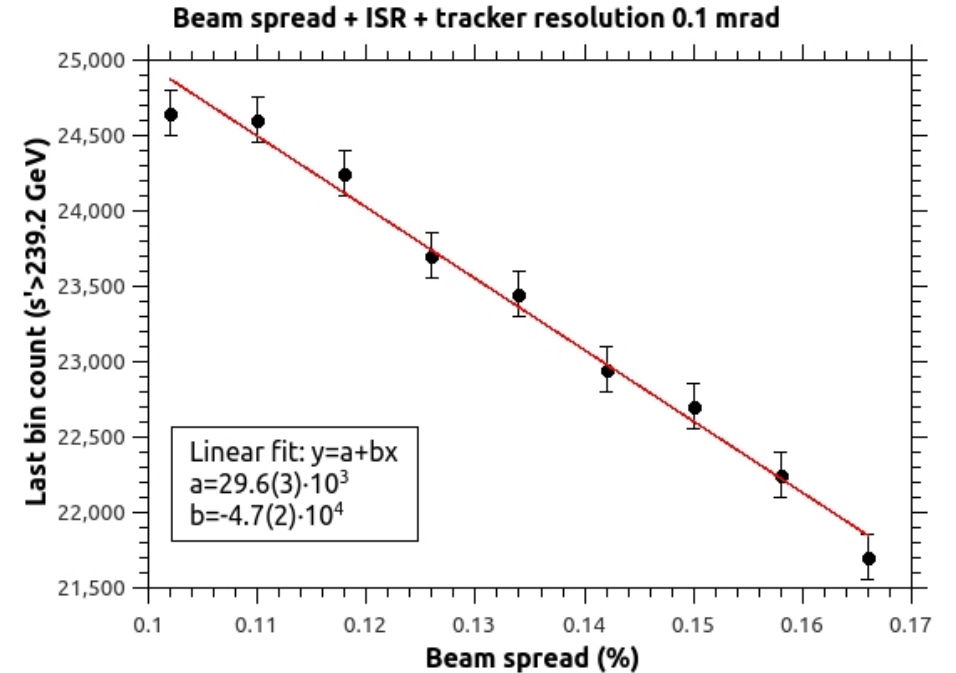
- Foreseen 0.1 mrad central tracker resolution of muons' θ reconstruction does not affect the s' distribution at the Z-pole
- The same stands for 240 GeV



Systematic uncertainty from the uncertainty of effective center-of-mass energy



Most energetic muons count dependence on the beam-spread @ Z^0 pole



Most energetic muons count dependence on the beam-spread @ 240 GeV

- The effective beam-spread can be determined from the count of the top-part of the s' distribution
- Increase of the beam-spread leads to increase of acolinearity of outgoing muons, and the corresponding reduction of the center-of-mass energy available for a collision
- The muon count dependence on the beam-spread can be fitted using a simple linear fit where statistical uncertainty of the muon count corresponds to the uncertainty of the beam-spread (effective center of mass determination)



Systematic uncertainty from the uncertainty of effective center-of-mass energy

CEPC	Luminosity @ IP ($\text{cm}^{-2} \text{s}^{-1}$) CDR/post-CDR	Nominal beam-spread δE_b (%)	Number of events	σ $e^+e^- \rightarrow \mu^+\mu^-$	Collecting time (approximate)	Beam-spread variation (δE_b)	s' uncertainty (MeV)
Z^0 pole	$3.2 \cdot 10^{35} / 1.02 \cdot 10^{36}$	0.080	250 kEvt.	1.5 nb	9 min/3 min	$1.4 \cdot 10^{-2} \cdot \delta E_b$	1.8
					3 min/<1 min for 10^{-4} of $\Delta L/L$	$7.0 \cdot 10^{-2} \cdot \delta E_b$	5
240 GeV	$3.0 \cdot 10^{34} / 5.2 \cdot 10^{34}$	0.134	100 kEvt.	4.1 pb	9.4 days/5.2 days	$4.7 \cdot 10^{-2} \cdot \delta E_b$	15
					1.2 days/16h for 10^{-3} of $\Delta L/L$	$37.6 \cdot 10^{-2} \cdot \delta E_b$	120

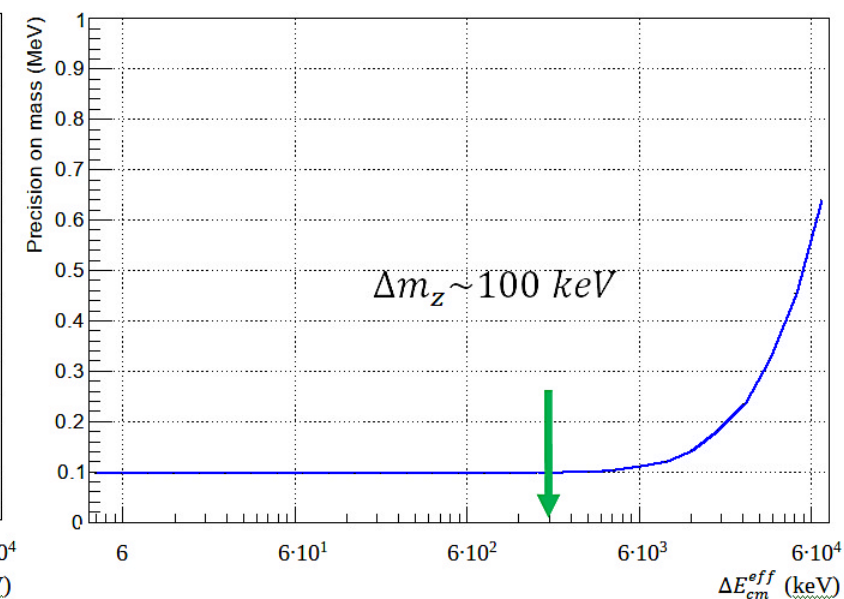
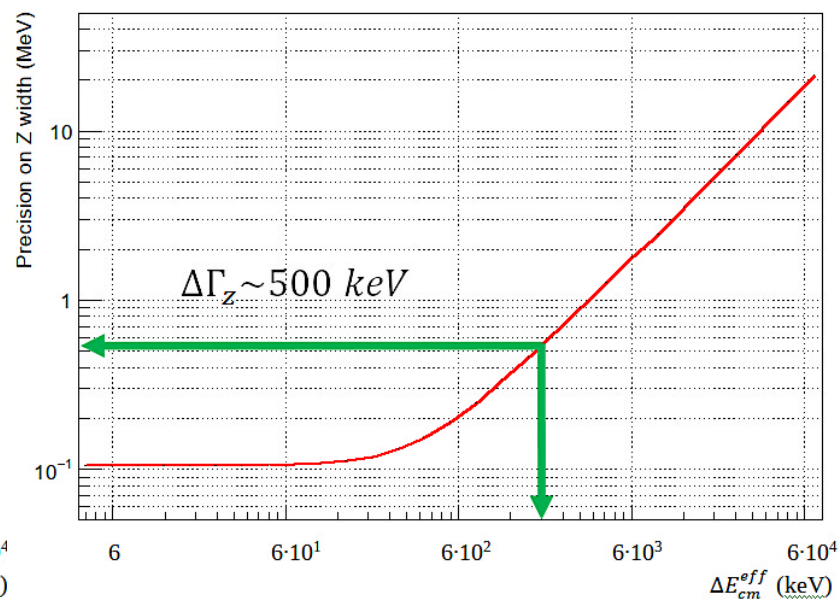
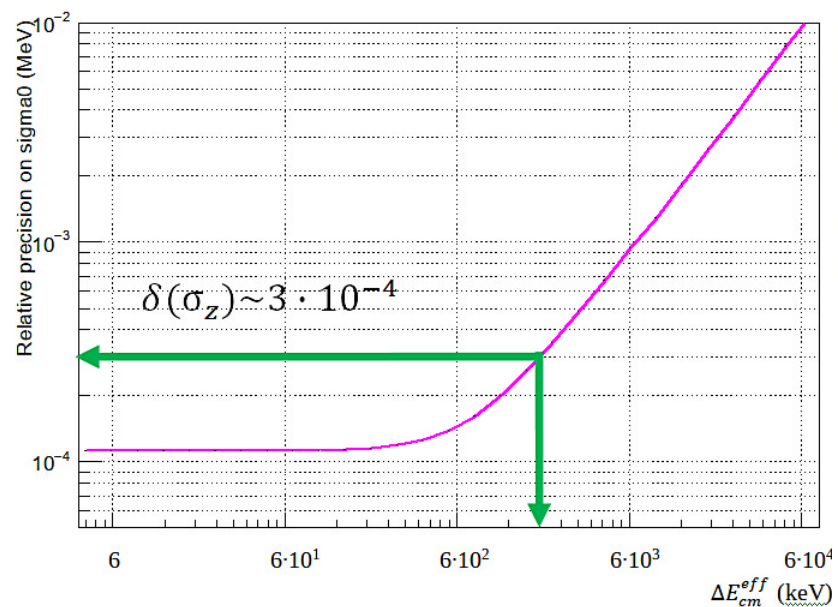
- With a statistics of 250K events at Z^0 pole and 100K events at 240 GeV, relative variations of the nominal beam-spread of 2.5% (1.5%) can be measured, respectively
- For such relative precision in determination of the effective beam-spread, only ~ 3 minutes of collecting the most energetic muons are needed at the Z^0 pole which corresponds to the uncertainty of the effective center-of-mass energy of 1.8 MeV

To control the relative uncertainty of the integrated luminosity at the level of 10^{-4} , less than 1 minute of collecting muons are needed at the Z^0 pole



Systematic uncertainty from the uncertainty of effective center-of-mass energy

Impact of s' precision on other EW observables at CEPC



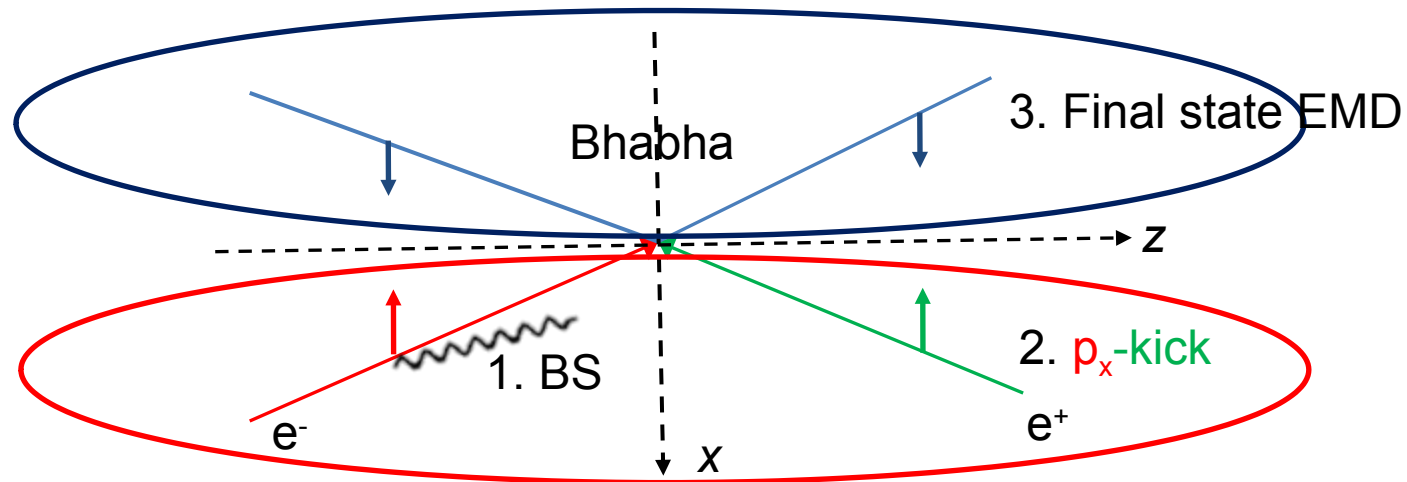
Discussion on electromagnetic deflection (EMD)

General facts

- Interaction of beams happens prior to the physics interaction at the IP (1 and 2) and final state particles may interact with incoming beam (3)
- 1. EM field of the incoming bunch of the opposite charge induces radiation (*Beamstrahlung*) of the **initial state**
- 2. EM field of the outgoing (opposite-charged) beam impacts the **initial state** leading to effective reduction of the crossing angle (**p_x kick**)
- 3. Similar deflection affects the Bhabha **final state** by the EM field of the incoming bunches

We are going to discuss 2 and touch 3.

- Both 2 and 3 contribute to *Electromagnetic deflection (EMD)* effect in luminosity measurement

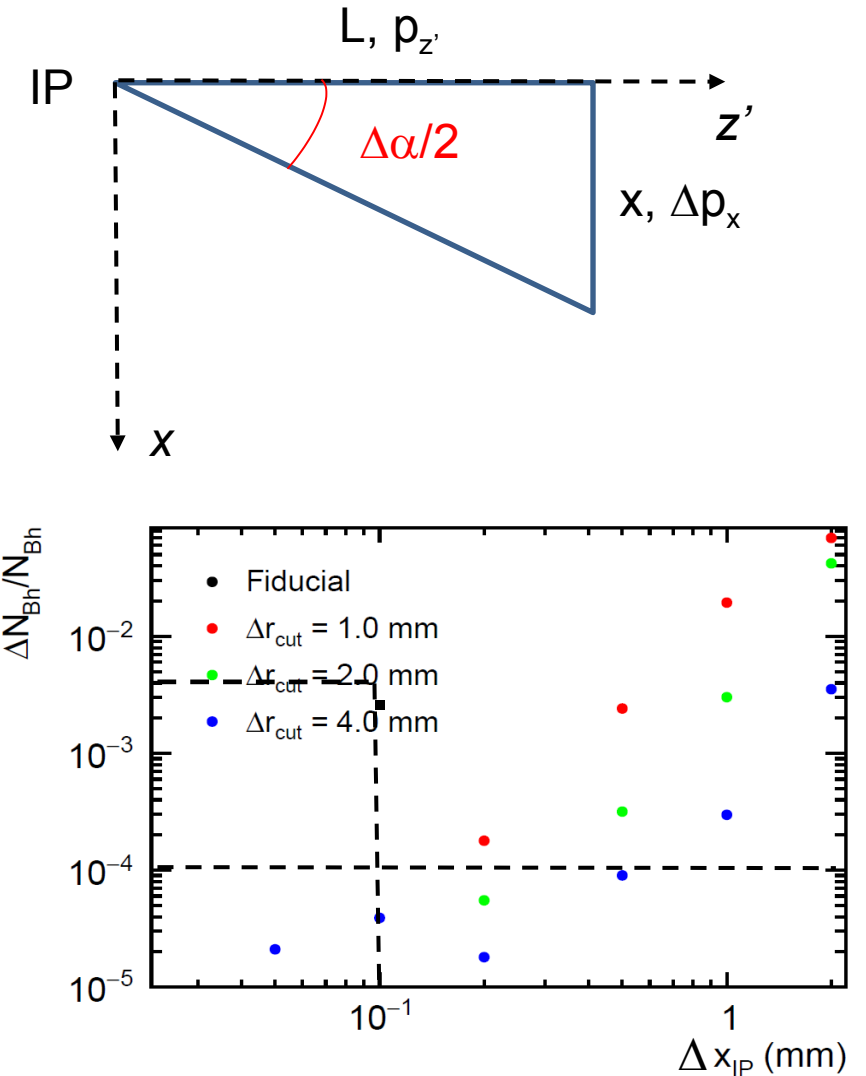


Discussion on electromagnetic deflection (EMD)

What is the impact of the initial state p_x kick ($2 \cdot \Delta p_x$) on integrated luminosity measurement?

- Knowing that Δp_x is equivalent to $\Delta\alpha/2$, we can describe the p_x kick of the initial state as the effective shift (x) of the luminometer along the ($-x$)-axis, positioned at the distance L from the IP, **along the outgoing beam-pipe z'**
- From the relations between the sides of the triangle it follows:
 $x = L \cdot (\Delta p_x / p_{z'}) = L \cdot \text{tg}(\Delta\alpha/2)$
- Assuming that $p_{z'} \approx E_{\text{beam}}$ and $L = 0.95\text{m}$, for $(2 \cdot \Delta p_x): 5\text{-}10\text{ MeV}$ at Z-pole CEPC

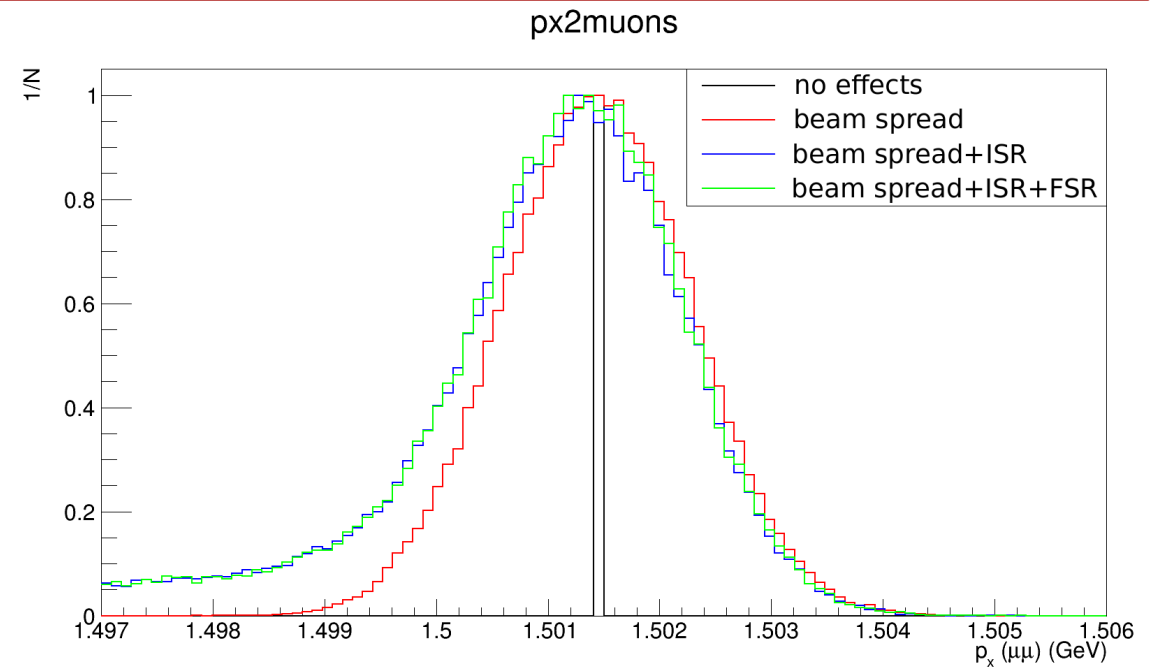
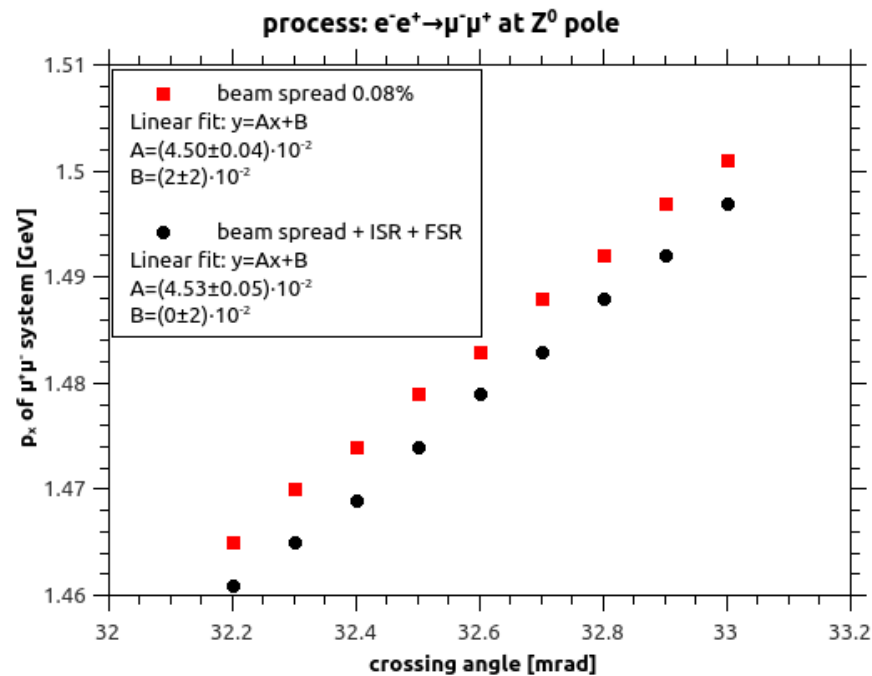
With detector is at the outgoing beam, asymmetric selection can be tuned to keep luminosity insensitive ($\Delta L/L \approx 10^{-4}$) to the x -shift almost up to 1 mm



Discussion on electromagnetic deflection (EMD)

Can we measure the effective x-angle from the p_x kick?

- 10^5 simulated di-muon events (1 min of integrated L at Z^0 pole – post CDR design),
- TPC acceptance $|\cos\theta| < 0.78$, $\Delta p_t/p_t^2 \sim 10^{-5}$
- Detector resolution contributes insignificantly (10s of keV) to the p_x width.
- Beam-spread and ISR widen the p_x distribution
- p_x mean remains linearly proportional to the effective crossing angle (calibration plot)
- **Effective crossing angle can be measured with 1% uncertainty**



Discussion on electromagnetic deflection (EMD)

What about EMD of the final state?

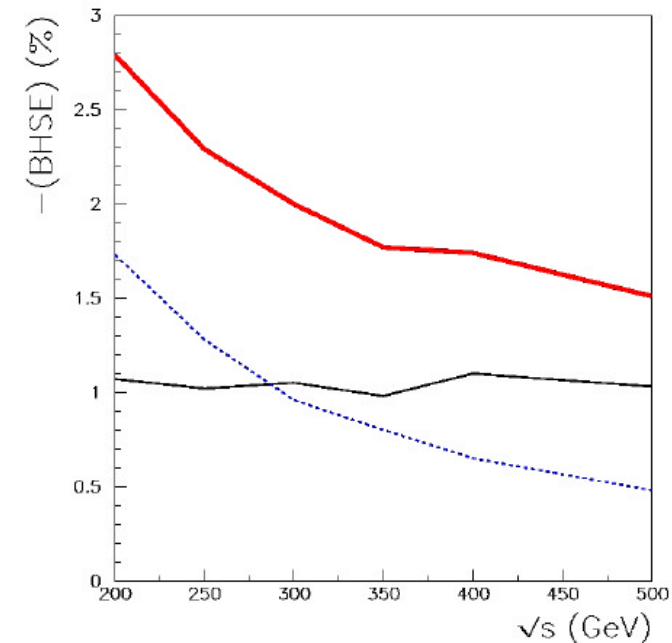
1. We can talk about the overall focusing effect on the final state that will include p_x kick + final state EMD
2. The net effect will be effective shift of the luminometer along $-x$ axis for $\Delta\theta_{\text{EMD}}$
3. The count will become asymmetric for different φ
4. 2. and 3. can be exploited to define observable(s) describing the effect

[[S. Lukic, et al., 2013 JINST 8 P08012](#)]

[[Y. Voutsinas, 34 FCAL WS, CERN, 2019](#)]

With detector is at the outgoing beam, asymmetric selection can be tuned to keep luminosity insensitive ($\Delta L/L \approx 10^{-4}$) to the x-shift almost up to 1 mm

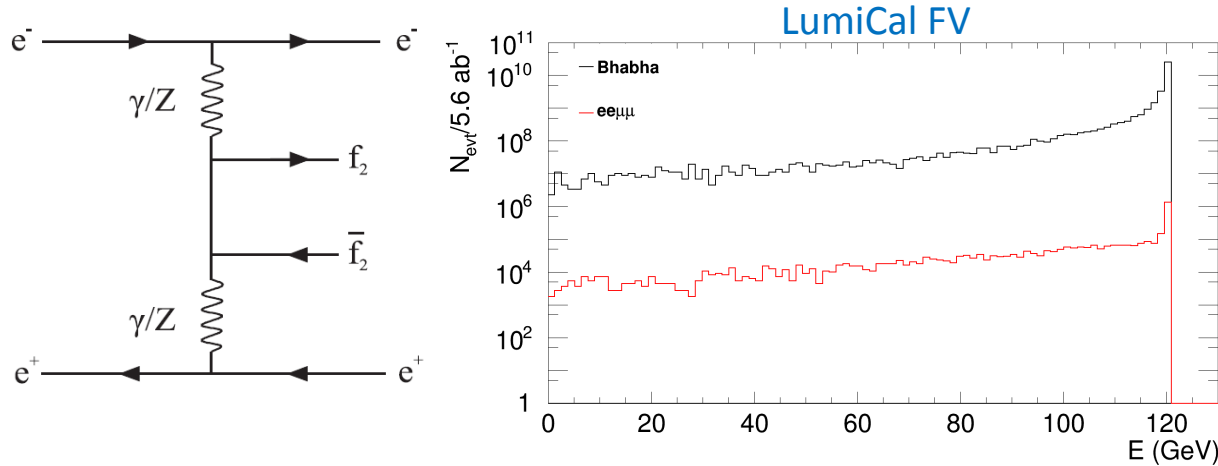
The effect is smaller at larger center-of-mass energies (i.e. for the CLIC beam we have estimated $\Delta\theta_{\text{EMD}}$ to be 43 μrad @ 500 GeV and 20 μrad @ 1 TeV [[JINST 8 P08012, 2013](#)], at FCCee Z^0 it amounts up to 150 μrad [[arXiv:1908.01698v3 \[hep-ex\]](#)])



Bhabha suppression due to beamstrahlung (black line) and electromagnetic deflections (blue line), as well as the combined effect (red line) [[2007 JINST 2 P09001](#)]



2-photon processes

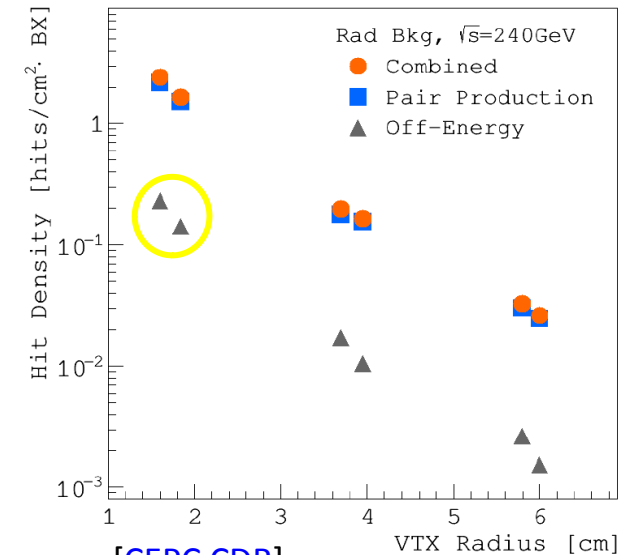


- Multi-peripheral process $\sim nb$ x-section
- High energy e⁻ spectators can fake the signal
- Most of spectators go below luminometer acceptance
- Initial contamination (without any selection) of the detector volume is $\sim 10^{-4}$ w.r.t. the signal at 240 GeV CEPC
- With the relative energy $(E_1 + E_2)/2E_{beam} = E_{rel} > 0.8$, B/S ratio is $\sim 8 \cdot 10^5$
- Even smaller at the Z⁰-pole since 2-photon x-section is scaling like $\ln^2(s)$

Off-momentum particles

- Can influence luminosity measurement by accidental overlapping to the Bhabha signal in both detector halves that happens at the same rate as the signal.
- Off-momentum particles from beam-gas interaction were the main source of systematics in luminosity measurement at LEP $(0.1-0.6) \cdot 10^{-4}$ [arXiv:hep-ex/9910066v2]. Nicely regulated by the (relative) energy cut.

CEPC simulations show that proper size collimators can be employed to suppress off-momentum particles in the first VTX detector layer to 0.22 hits/cm² per BX



[CEPC CDR]

240 GeV CEPC: first VTX layer-
2.4 particle/cm² per BX



- Several sources of the systematic uncertainty in integrated luminosity determination have been studied at CEPC (Z^0 -pole and 240 GeV)
- The uncertainty of the luminometer inner radius at the micron level together with the uncertainty of the available center-of-mass energy are posing the most challenging requirements
- The method of experimental determination of the effective center-of-mass energy based on di-muon production at Z^0 -pole CEPC, enables luminosity precision of 10^{-4} after less than 1 min of data taking
- At 240 GeV, 10^{-3} precision goal on integrated luminosity requires 16 hours of data taking, due to significantly smaller x-section for di-muon production
- Changes of the nominal crossing angle due to the EMD (p_x -kick and EMD of the Bhabha final state) can be relaxed with the asymmetric selection in polar angle (LEP-style) in integrated luminosity measurement
- Effective crossing angle can be determined with 1% relative uncertainty for < 1 min of collecting di-muon events at the Z^0 -pole, in a semi-dependent way from the simulation
- Physics processes (2-photon and off-momentum background) can be suppressed with the cut on relative energy



Thanks for your attention!



Backup

MDI parameters



CEPC parameters from CDR

	<i>Higgs</i>	<i>W</i>	<i>Z (3T)</i>	<i>Z (2T)</i>
Number of IPs	2			
Beam energy (GeV)	120	80	45.5	
Circumference (km)	100			
Synchrotron radiation loss/tum (GeV)	1.73	0.34	0.036	
Crossing angle at IP (mrad)	16.5×2			
Piwinski angle	2.58	7.0	23.8	
Number of particles/bunch N_e (10^{10})	15.0	12.0	8.0	
Bunch number (bunch spacing)	242 (0.68μs)	1524 (0.21μs)	12000 (25ns+10%gap)	
Beam current (mA)	17.4	87.9	461.0	
Synchrotron radiation power /beam (MW)	30	30	16.5	
Bending radius (km)	10.7			
Momentum compact (10^{-5})	1.11			
β function at IP β_x^*/β_y^* (m)	0.36/0.0015	0.36/0.0015	0.2/0.0015	0.2/0.001
Emittance ϵ_x/ϵ_y (nm)	1.21/0.0031	0.54/0.0016	0.18/0.004	0.18/0.0016
Beam size at IP σ_x/σ_y (μm)	20.9/0.068	13.9/0.049	6.0/0.078	6.0/0.04
Beam-beam parameters ξ_x/ξ_y	0.031/0.109	0.013/0.106	0.0041/0.056	0.0041/0.072
RF voltage V_{RF} (GV)	2.17	0.47	0.10	
RF frequency f_{RF} (MHz) (harmonic)	650 (216816)			
Natural bunch length σ_z (mm)	2.72	2.98	2.42	
Bunch length σ_z (mm)	3.26	5.9	8.5	
HOM power/cavity (2 cell) (kw)	0.54	0.75	1.94	
Natural energy spread (%)	0.1	0.066	0.038	
Energy acceptance requirement (%)	1.35	0.4	0.23	
Energy acceptance by RF (%)	2.06	1.47	1.7	
Photon number due to beamstrahlung	0.1	0.05	0.023	
Lifetime _simulation (min)	100			
Lifetime (hour)	0.67	1.4	4.0	2.1
F (hour glass)	0.89	0.94	0.99	
Luminosity/IP L ($10^{34}\text{cm}^{-2}\text{s}^{-1}$)	2.93	10.1	16.6	32.1

[Haoyu Shi, Status on CEPC MDI IR design]

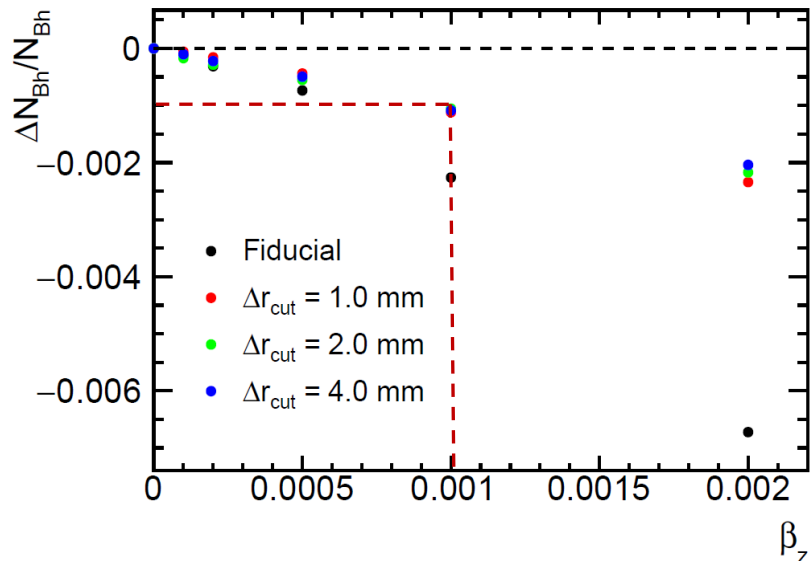


15-18 March 2021

International Workshop on Future Linear Colliders, LCWS2021

Uncertainty of the beam-asymmetry

- CEPC CDR: beam-energy spread will not exceed 0.134% of the E_{beam} @240 GeV and 0.08% of the E_{beam} @ 91.2 GeV
- Difference in energy of colliding particles can be as large as 322 MeV @240 GeV and up to 73 MeV @ Z^0 -pole
- Uncertainty of count of 10^{-4} implies knowledge of the asymmetry in beam energies at the level of 12.5% of the beam-spread at the Z^0 pole, which is below the natural energy-spread of the beam



- Longitudinal boost of the center-of-mass (CM) frame of colliding particles with respect to the lab frame, β_{coll}
- Leading to the **counting loss in luminometer, due to acolinearity of Bhabha final states**
- β_{coll} can be determined from the measured polar angles of Bhabha e^+ , e^- in the luminometer or from a di-muon system:

$$\beta_{\text{coll}} = \frac{\sin(\theta_1^{\text{lab}} + \theta_2^{\text{lab}})}{\sin \theta_1^{\text{lab}} + \sin \theta_2^{\text{lab}}} = \Delta E / \sqrt{s}$$

Determination of electromagnetic deflection of the Bhabha final state

Our method proposed for ILC/CLIC [JINST 8 P08012, 2013]

- $\Delta L/L = x_{\text{EMD}} \cdot \Delta\theta_{\text{EMD}}$
- Calibrate from experiment (measure slope x_{EMD})
- Determine from $\Delta\theta_{\text{EMD}}$ simulation - down-side, but
- $\Delta\theta_{\text{EMD}}$ is stable w.r.t. the variation of beam parameters (bunch size variations by ± 10 and $\pm 20\%$ of both bunches and one-sided variations by $+20\%$, of bunch charge and dimensions) \Rightarrow dissipation gives uncertainty of the method

