

Introduction

Motivations for Beyond Standard Model

Empirical

- dark matter
- origin of primordial density perturbations
- matter/antimatter asymmetry

Theoretical puzzles

- electroweak hierarchy
- strong CP problem
- flavor: pattern of masses and mixings

Theoretical opportunities

- low-dimension “portal” operators
(Higgs $|h|^2$, hypercharge $B_{\mu\nu}$, neutrino $h \cdot l$)

Motivations for Beyond Standard Model

Empirical

- dark matter
- origin of primordial density perturbations
- matter/antimatter asymmetry

Theoretical puzzles

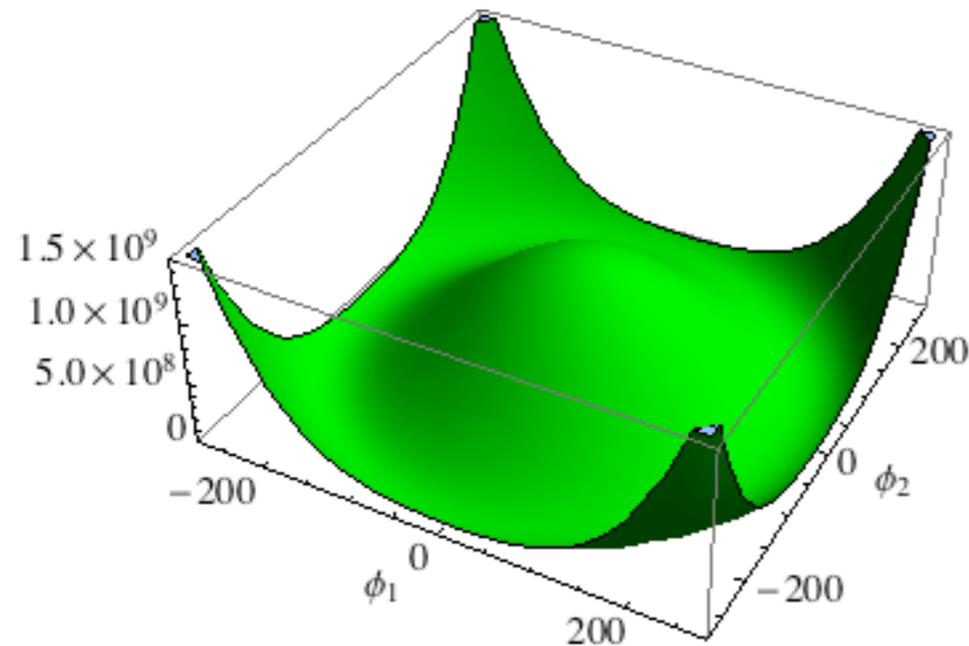
- ***electroweak hierarchy***
- strong CP problem
- flavor: pattern of masses and mixings

Theoretical opportunities

- low-dimension “portal” operators
(Higgs $|h|^2$, hypercharge $B_{\mu\nu}$, neutrino $h \cdot l$)

Higgs Potential

$$V(h) = -\mu^2 |h|^2 + \lambda |h|^4$$



The Standard Model *assumes* this potential and scale

$$\mu \sim 100 \text{ GeV}$$

but doesn't *explain* it.

(Also haven't *measured* it.)

Like Landau-Ginzburg or the London equations for superconductivity; still waiting for a ***microscopic, dynamical description***, a (very loose) analogue of BCS.

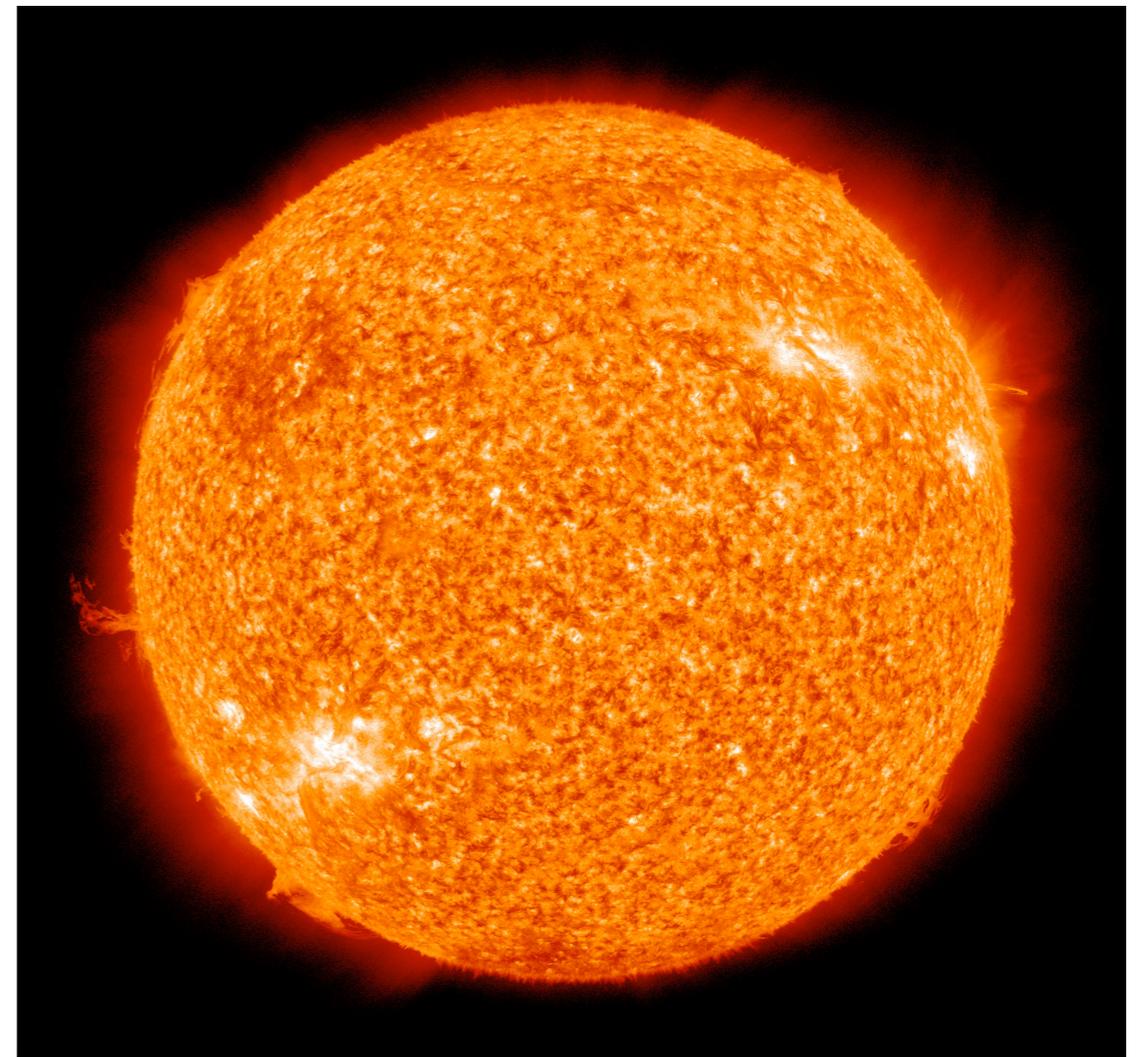
Hierarchies



$$M_{\text{Pl}} \sim 2 \times 10^{18} \text{ GeV}$$

$$\nu_{\text{EW}} \approx 246 \text{ GeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$



$$M_{\odot} \approx 2 \times 10^{30} \text{ kg}$$

$$\approx 1.1 \times 10^{57} \text{ GeV}$$

$$\approx 0.6 \left(\frac{M_{\text{Pl,unred}}}{m_{\text{proton}}} \right)^3 m_{\text{proton}}$$

[Details: V. Weisskopf, *Science* **187**(4177):605–612 (1975); Burrows and Ostriker, *PNAS* 111 (7):2409-2416 (2014).]

Hierarchies


$$M_{\text{Pl}} \sim 2 \times 10^{18} \text{ GeV}$$

Flat measure on \mathcal{L} parameters:

$$P(\text{EW hierarchy} | \text{SM}) \sim \left(\frac{v_{\text{EW}}}{M_{\text{Pl}}} \right)^2$$

$$\sim 10^{-32}$$

$$v_{\text{EW}} \approx 246 \text{ GeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

Hierarchies


$$M_{\text{Pl}} \sim 2 \times 10^{18} \text{ GeV}$$

Flat measure on \mathcal{L} parameters:

$$P(\text{QCD hierarchy} | \text{SM}) \sim \frac{1}{\log(M_{\text{Pl}}/\Lambda_{\text{QCD}})}$$

$$\sim 10^{-2}$$

$$v_{\text{EW}} \approx 246 \text{ GeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

Hierarchies


$$M_{\text{Pl}} \sim 2 \times 10^{18} \text{ GeV}$$

$$P(\text{QCD hierarchy} | \text{SM}) \sim \frac{1}{\log(M_{\text{Pl}}/\Lambda_{\text{QCD}})}$$
$$\sim 10^{-2}$$

$$v_{\text{EW}} \approx 246 \text{ GeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

The magic of running couplings:

$$\Lambda_{\text{QCD}} \sim \Lambda_{\text{UV}} e^{-8\pi^2/(bg^2)}$$

SUSY as an Example (More General Idea)


$$M_{\text{Pl}} \sim 2 \times 10^{18} \text{ GeV}$$

Dynamical SUSY breaking

$$P(\text{EW hierarchy} | \text{SUSY}) \sim \frac{1}{\log(M_{\text{Pl}}/M_{\text{SUSY}})}$$

$$\sim 10^{-2}$$

$$M_{\text{SUSY}} \sim v_{\text{EW}} \approx 246 \text{ GeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

(Witten, 1981)

Naturalness as Bayesian Guesswork

$$P(\text{EW hierarchy} | \text{SM}) \sim \left(\frac{v_{\text{EW}}}{M_{\text{Pl}}} \right)^2 \sim 10^{-32}$$

$$P(\text{EW hierarchy} | \text{SUSY}) \sim \frac{1}{\log(M_{\text{Pl}}/M_{\text{SUSY}})} \sim 10^{-2}$$

If you have no strong preconception about which theory is right, then the **data** that we live in a universe with a **vast hierarchy** suggests that we take **weak-scale** solutions to the hierarchy problem (not only SUSY!) very seriously.

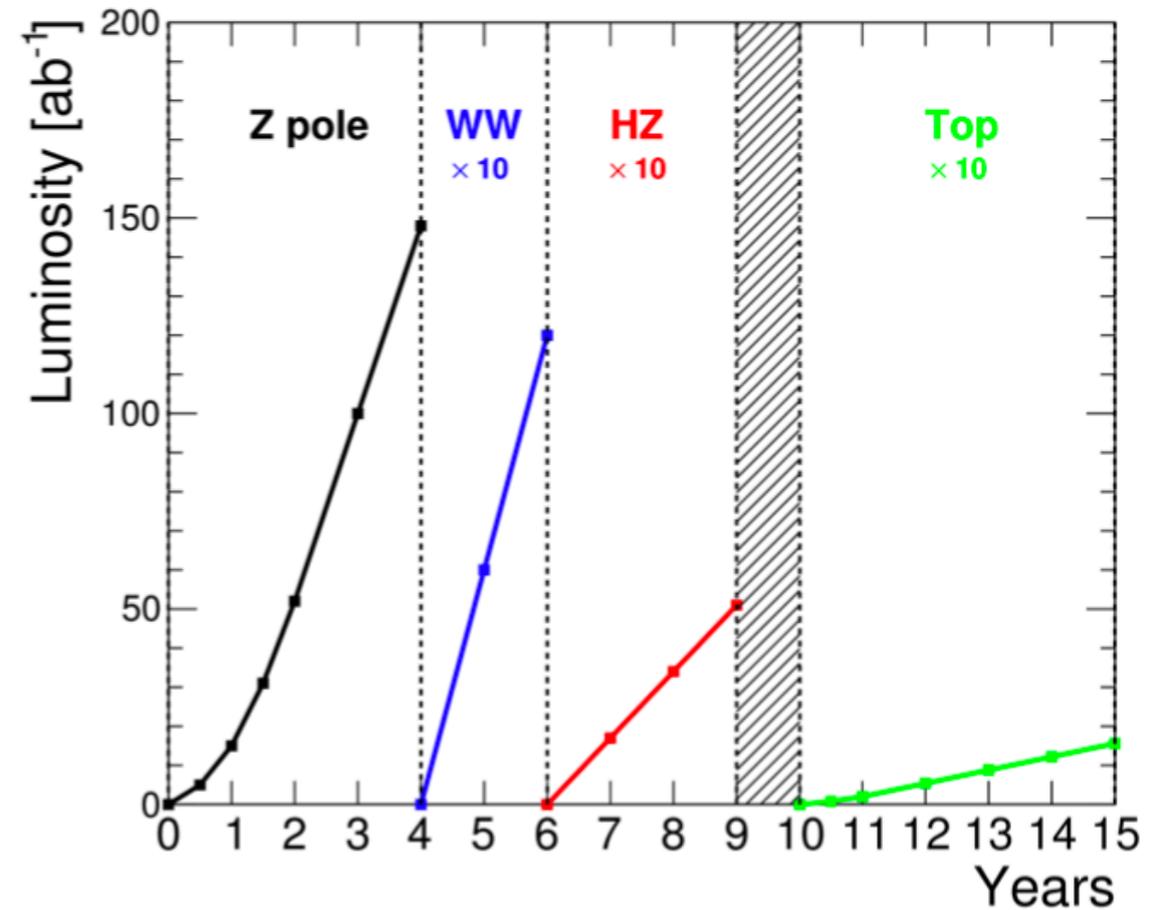
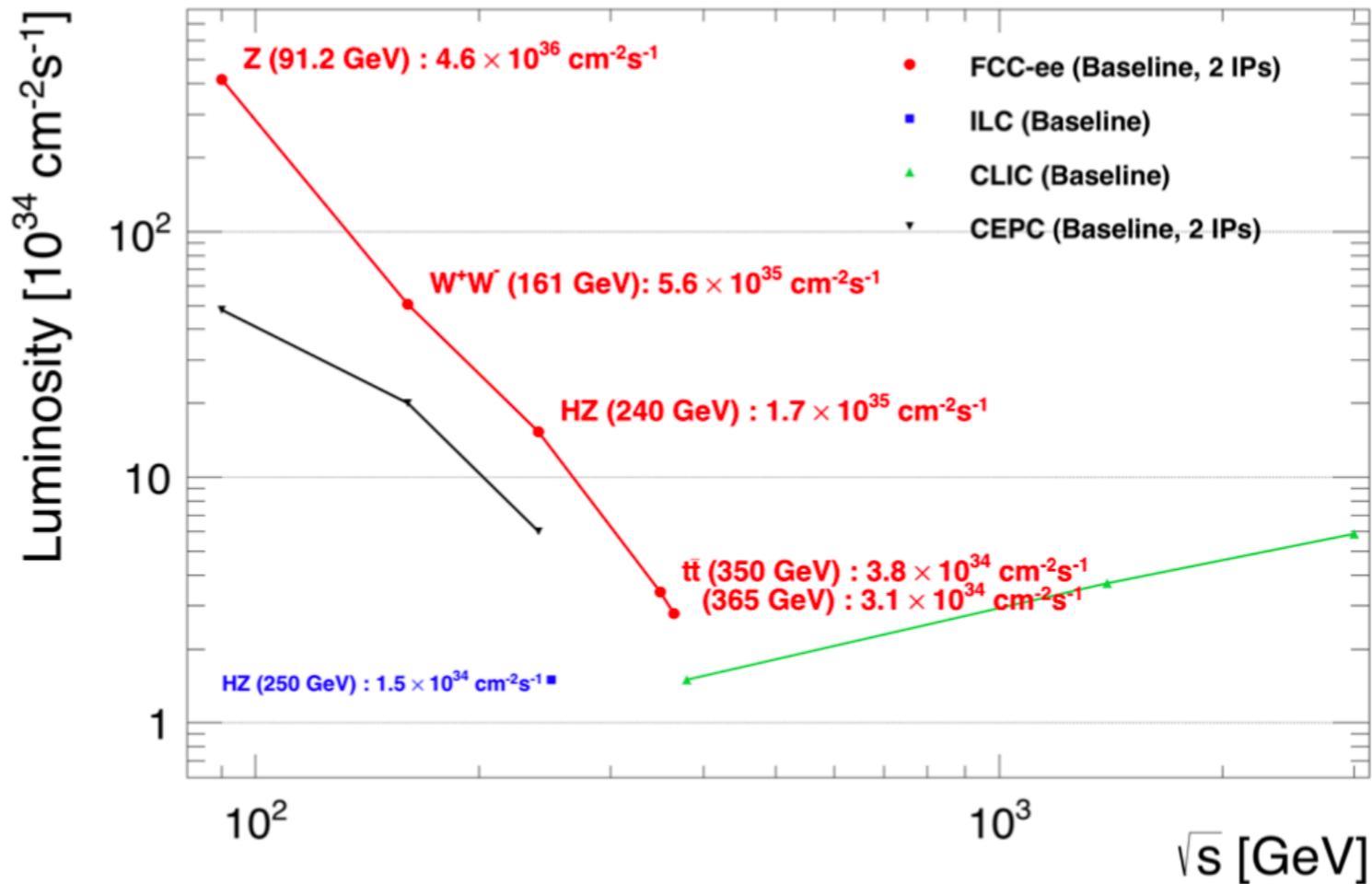
FCC-ee Physics Case

Circular e^+e^- , or Linear e^+e^- ?

Advantages and disadvantages to each.

- **Linear**: go to higher energy. **Higher direct discovery potential *if* new electroweak states exist.**
-
- **Linear**: easy to reach top threshold, **improve top mass as input to electroweak fits.** But FCC-ee also gets there.
- **Circular**: **resonant spin depolarization** gives precise energy calibration and **Z mass & width measurement**
- **Circular**: future as **high energy hadron machine.**
Important to build a large enough tunnel that foreseeable magnet technology can reach desired energies!

FCC-ee Studies the Weak Scale: Not *Just* a Higgs Factory



$\sim 5 \times 10^{12}$ Z bosons, $\sim 10^6$ Higgs bosons,
 $\sim 10^7$ W^+W^- pairs, $\sim 10^6$ $t\bar{t}$ pairs

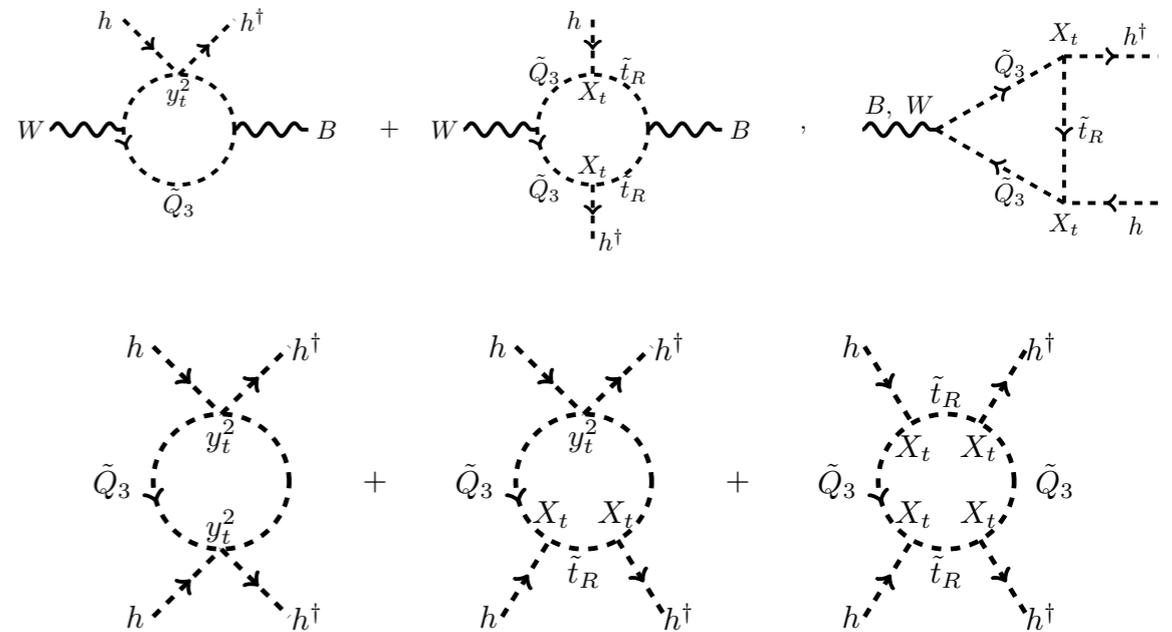
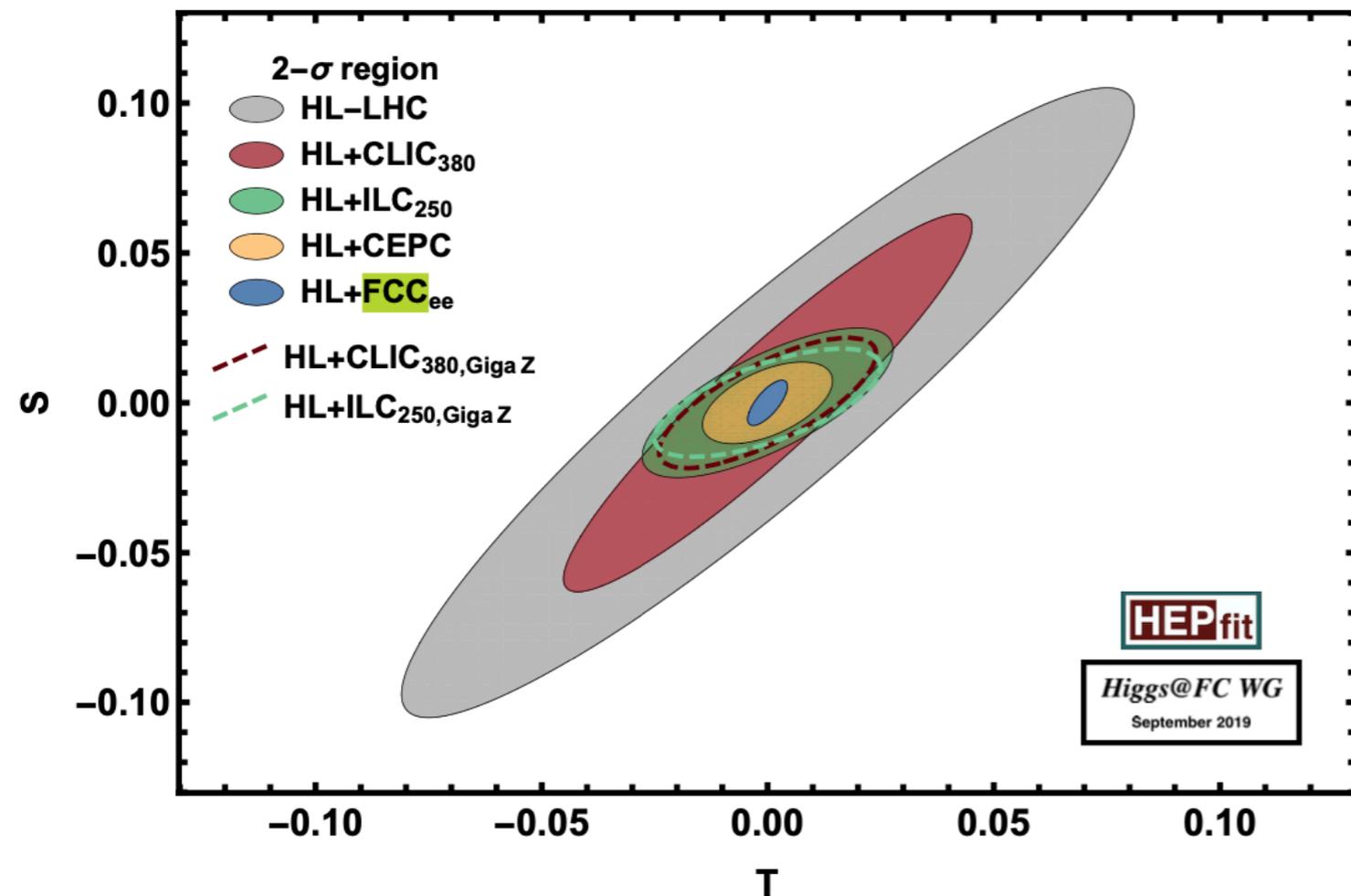
All in a clean environment enabling unprecedented precision

Precision Electroweak Physics at FCC-ee

$$\left. \begin{array}{l} \sin^2 \theta_{\text{eff}}^l (A_{\text{FB}}) \\ m_Z, \Gamma_Z, m_t, \alpha(m_Z) \\ m_W \end{array} \right\} \begin{array}{l} S \text{ parameter:} \\ T \text{ parameter:} \end{array}$$

$$S \left(\frac{\alpha}{4s_W c_W v^2} \right) h^\dagger \sigma^i h W_{\mu\nu}^i B^{\mu\nu}$$

$$-T \left(\frac{2\alpha}{v^2} \right) |h^\dagger D_\mu h|^2$$



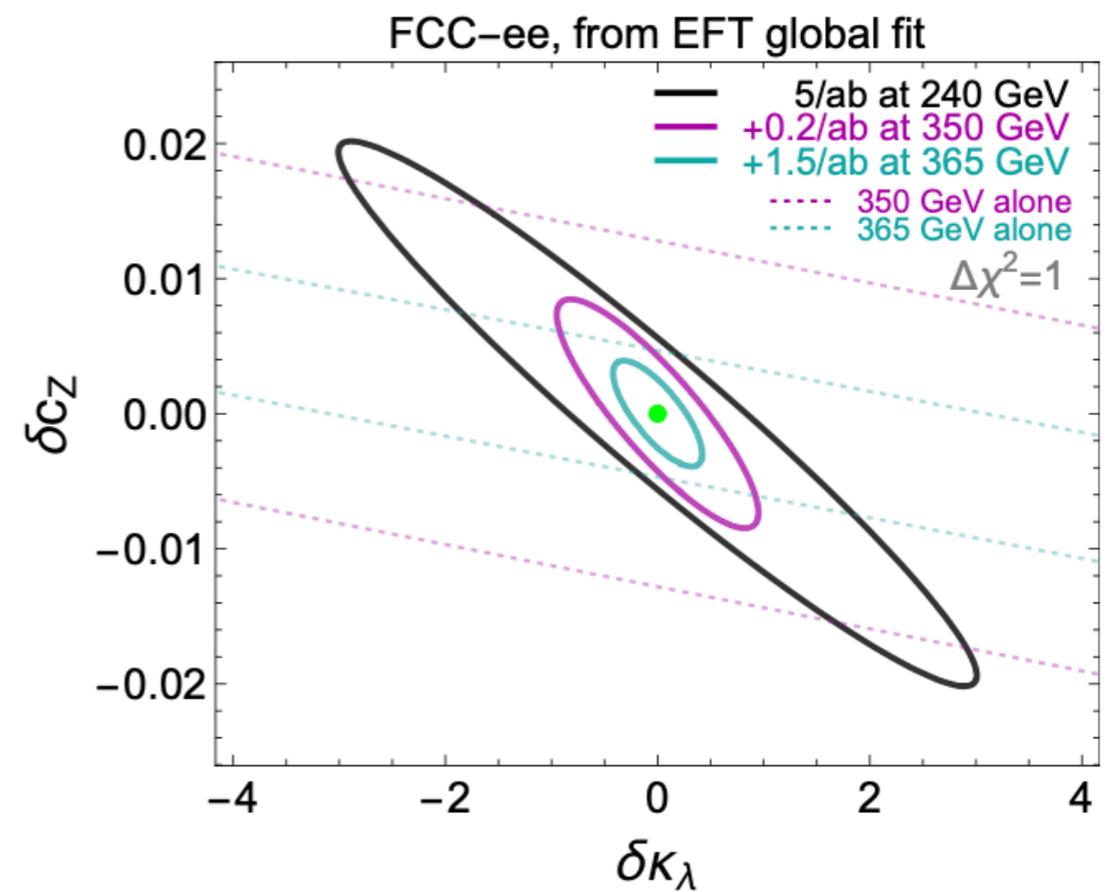
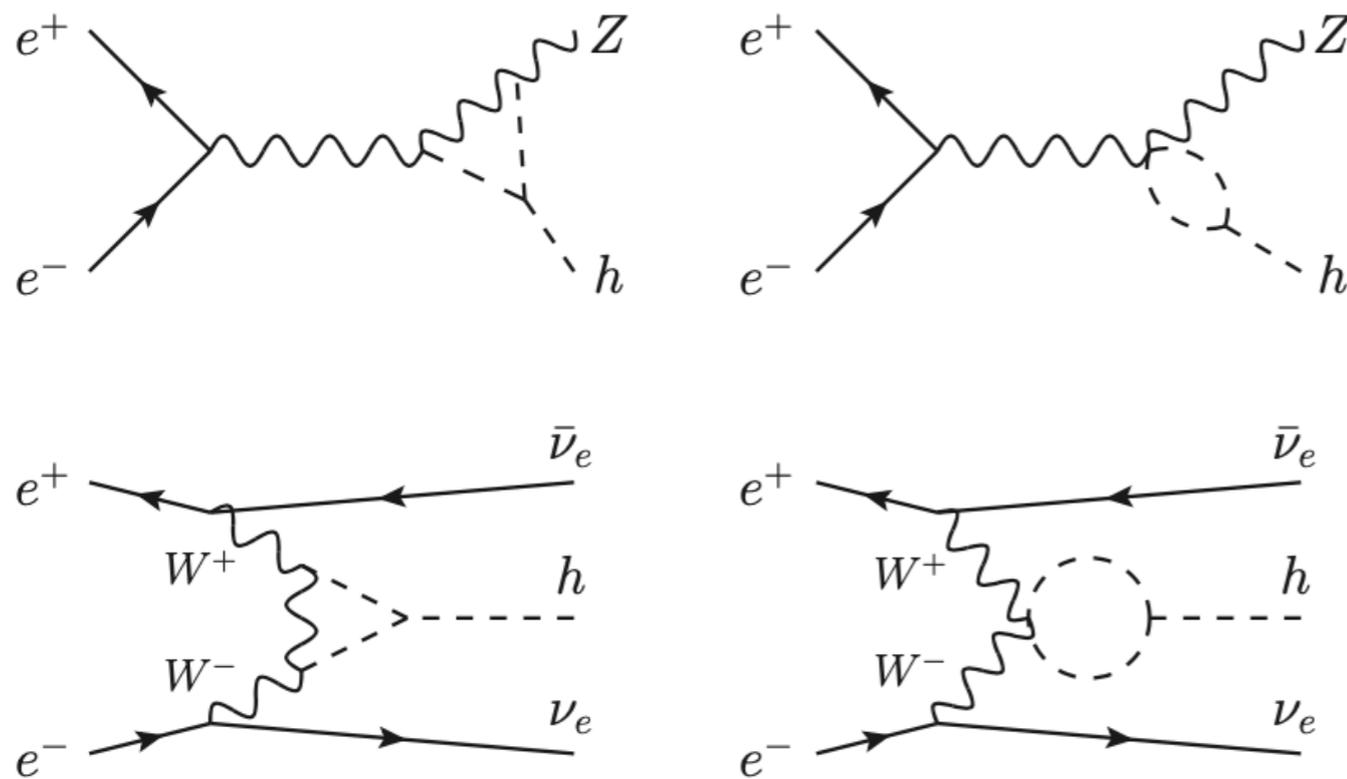
e.g.: stops in loops to ~ 1 TeV
(modulo caveats about blind spots)

Precision Higgs Physics at FCC-ee

Collider	FCC-ee ₂₄₀₊₃₆₅		
Lumi (ab ⁻¹)	5 ₂₄₀	+1.5 ₃₆₅	+ HL-LHC
Years	3	+4	
$\delta\Gamma_{\text{H}}/\Gamma_{\text{H}}$ (%)	2.7	1.3	1.1
$\delta g_{\text{HZZ}}/g_{\text{HZZ}}$ (%)	0.2	0.17	0.16
$\delta g_{\text{HWW}}/g_{\text{HWW}}$ (%)	1.3	0.43	0.40
$\delta g_{\text{Hbb}}/g_{\text{Hbb}}$ (%)	1.3	0.61	0.55
$\delta g_{\text{Hcc}}/g_{\text{Hcc}}$ (%)	1.7	1.21	1.18
$\delta g_{\text{Hgg}}/g_{\text{Hgg}}$ (%)	1.6	1.01	0.83
$\delta g_{\text{H}\tau\tau}/g_{\text{H}\tau\tau}$ (%)	1.4	0.74	0.64
$\delta g_{\text{H}\mu\mu}/g_{\text{H}\mu\mu}$ (%)	10.1	9.0	3.9
$\delta g_{\text{H}\gamma\gamma}/g_{\text{H}\gamma\gamma}$ (%)	4.8	3.9	1.1
$\delta g_{\text{H}tt}/g_{\text{H}tt}$ (%)	–	–	2.4
BR _{EXO} (%)	< 1.2	< 1.0	< 1.0

Higgs Self-Coupling at FCC-ee

FCC-ee can probe the Higgs trilinear coupling through its loop effects (McCullough, arXiv:1312.3322).



Requires fit with multiple center-of-mass energies.

(Di Vita, Durieux, Grojean, Gu, Liu, Panico, Riembau, Vantalon arXiv:1711.03978)

Flavor Physics at FCC-ee

FCC-ee will produce $\sim 5 \times 10^{12}$ Z bosons (vs 10^7 at LEP).

$\sim 10^{12}$ $Z \rightarrow b\bar{b}$ decays.

(Substantially more B mesons than Belle II in the next decade)

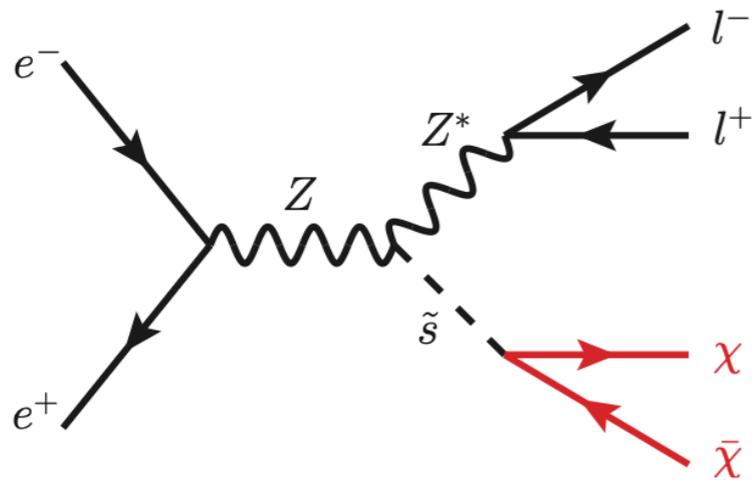
$\sim 10^{11}$ $Z \rightarrow \tau^+\tau^-$ decays.

FCC-ee will serve as a high-intensity flavor factory.

Example: $b \rightarrow s\tau^+\tau^-$ transitions; e.g., kinematic reconstruction of (poorly constrained) $\bar{B}^0 \rightarrow K^{*0}\tau^+\tau^-$ process possible (Kamenik, Monteil, Semkiv, Vale Silva arXiv:1705.11106)

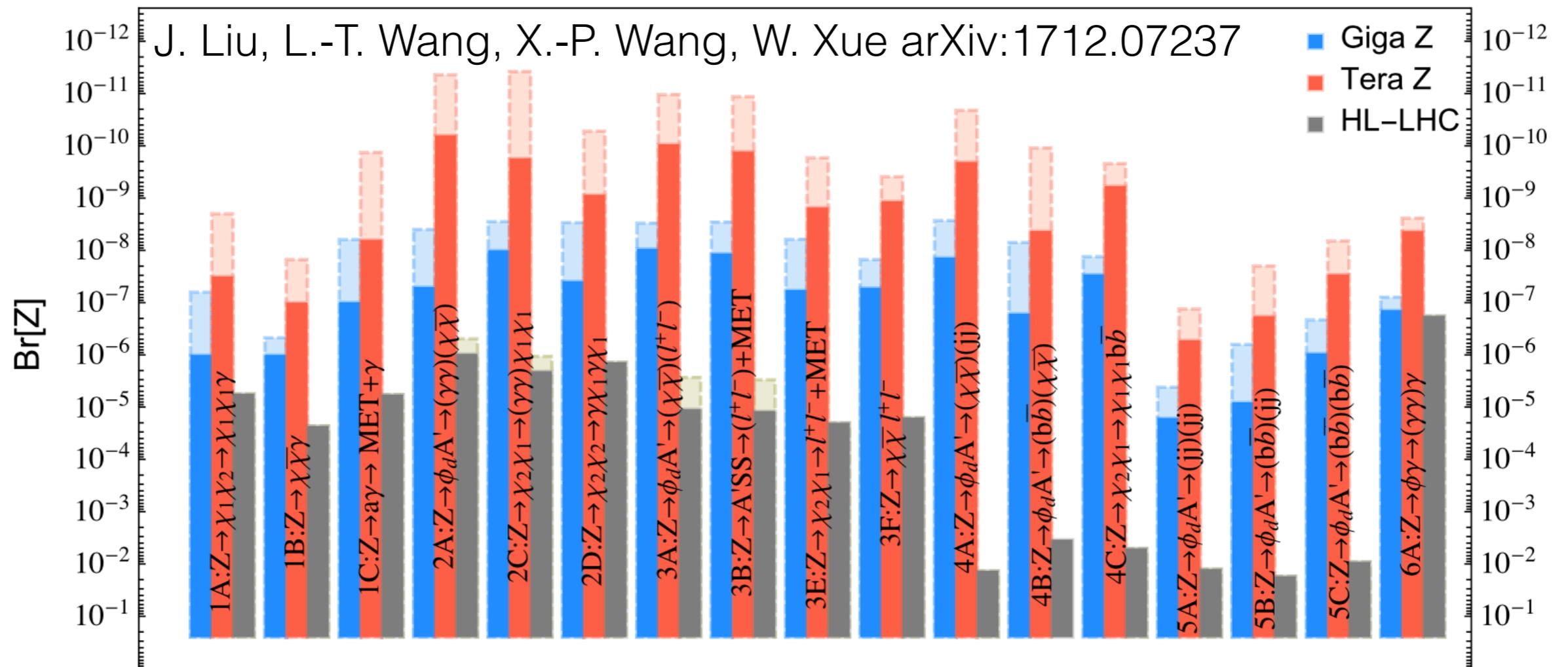
also see: Grossman, Ligeti arXiv:2106.12168

Hidden Sector Physics at FCC-ee: Exotic Z Decays



Full power of Tera-Z luminosity.

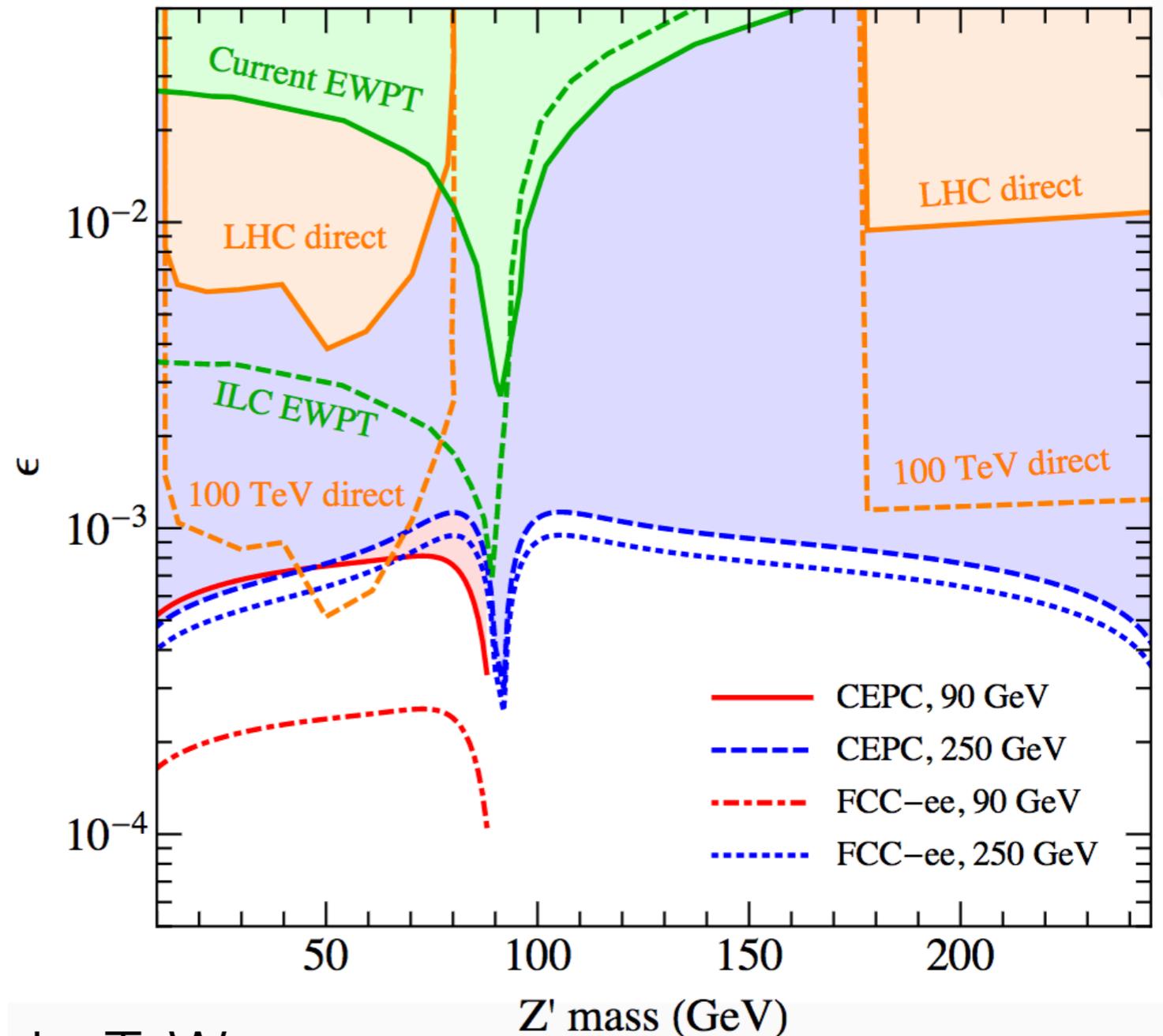
Many scenarios, e.g., dark matter, dark photons or Higgses, axion-like particles.



Hidden Sector Physics at FCC-ee: Heavy Dark Photon in Radiative Return

Make a dark photon in association with an ordinary photon, and do a resonance search:

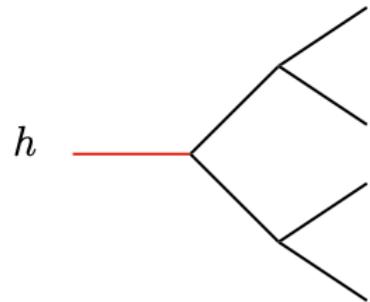
$$e^+e^- \rightarrow \gamma Z_D \rightarrow \gamma \mu^+ \mu^-$$



M. Karliner, M. Low, J.L. Rosner, L.-T. Wang

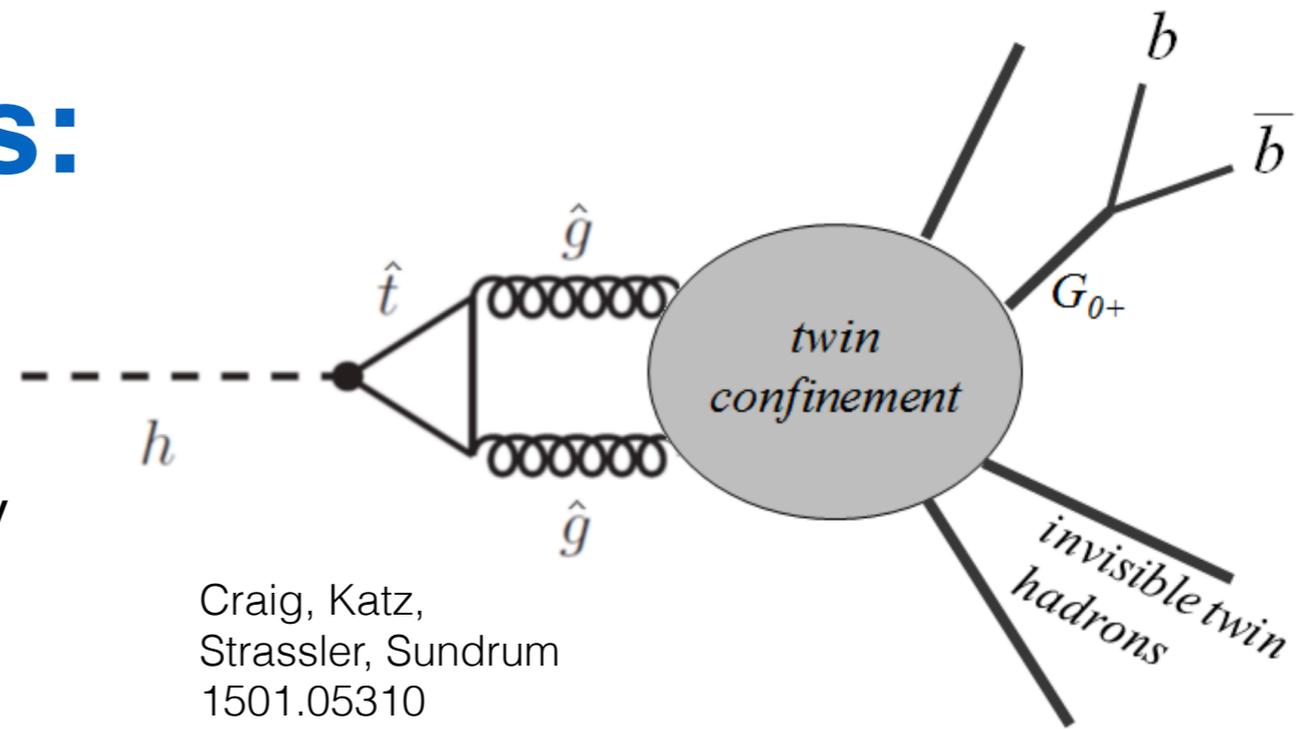
1503.07209

Hidden Sector Physics: Exotic Higgs Decays



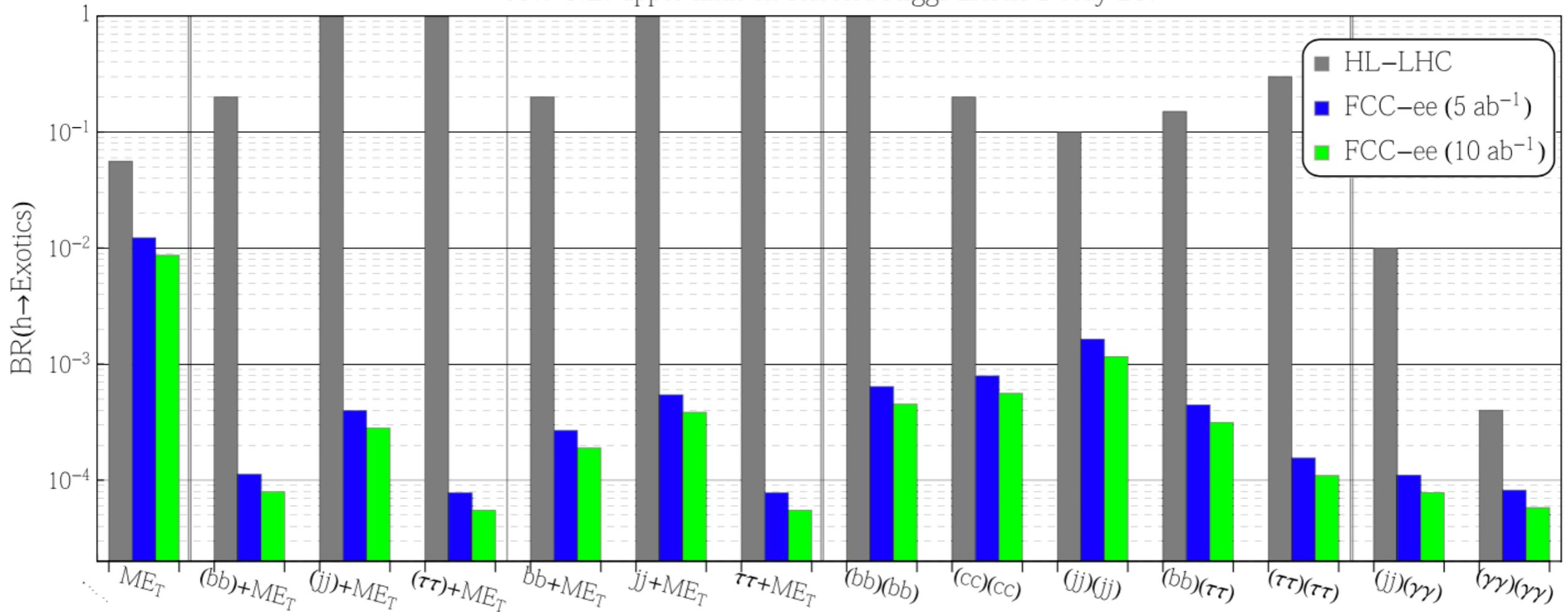
$h \rightarrow 2 \rightarrow 4$

Portal opportunity
or naturalness



Craig, Katz,
Strassler, Sundrum
1501.05310

95% C.L. upper limit on selected Higgs Exotic Decay BR

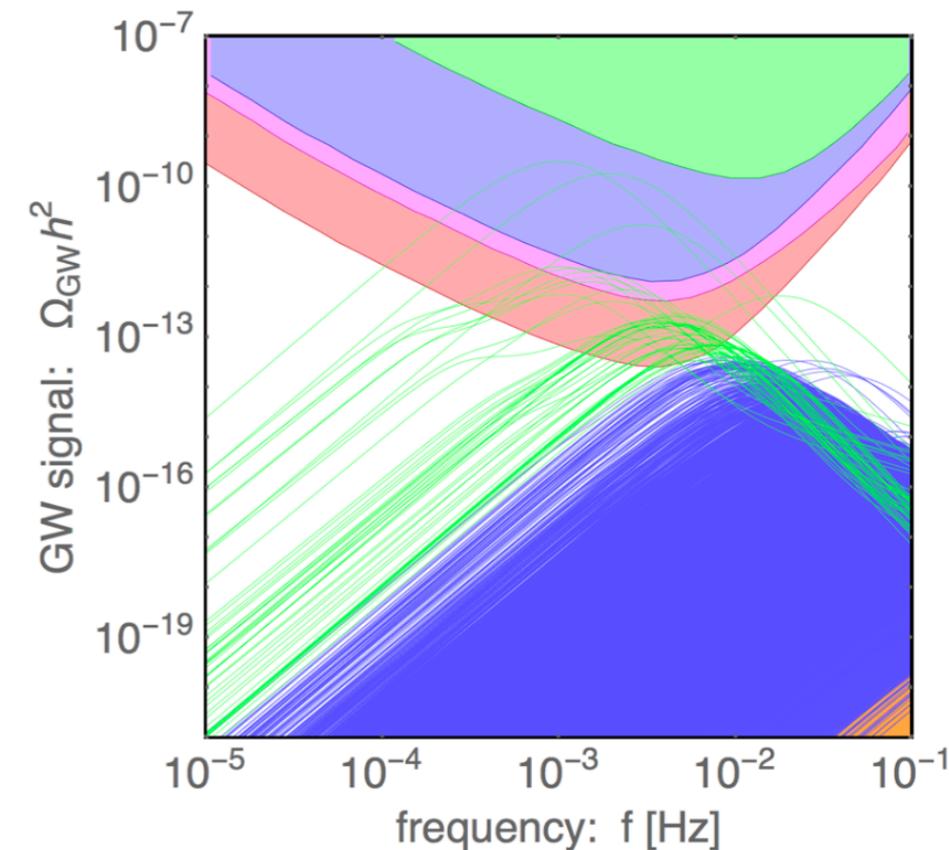
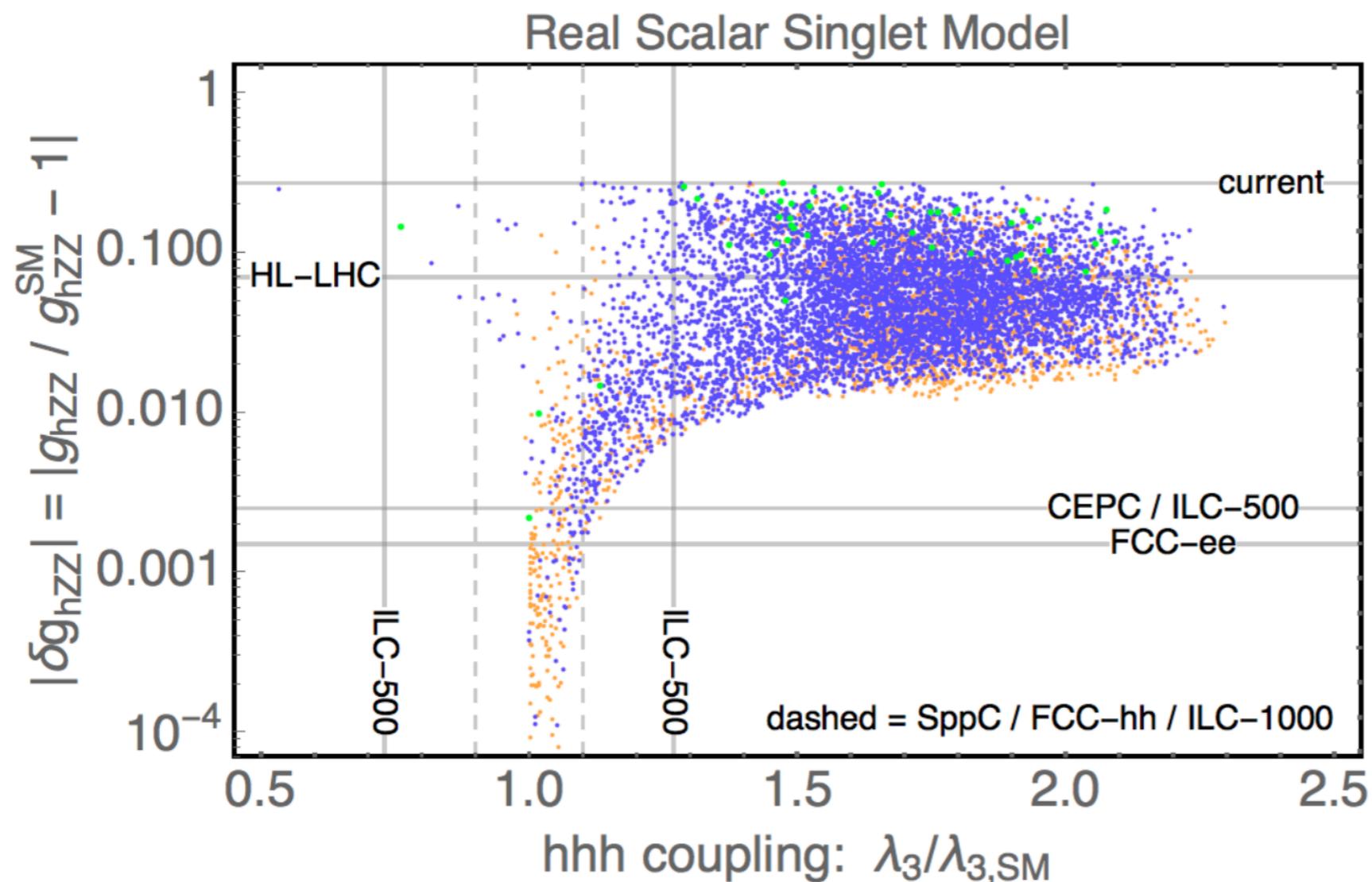


Z. Liu, L.-T. Wang, H. Zhang arXiv:1612.09284

Electroweak Phase Transition

Modify the phase transition with Higgs coupling to a **singlet scalar**.
Dominated by *mixing*.

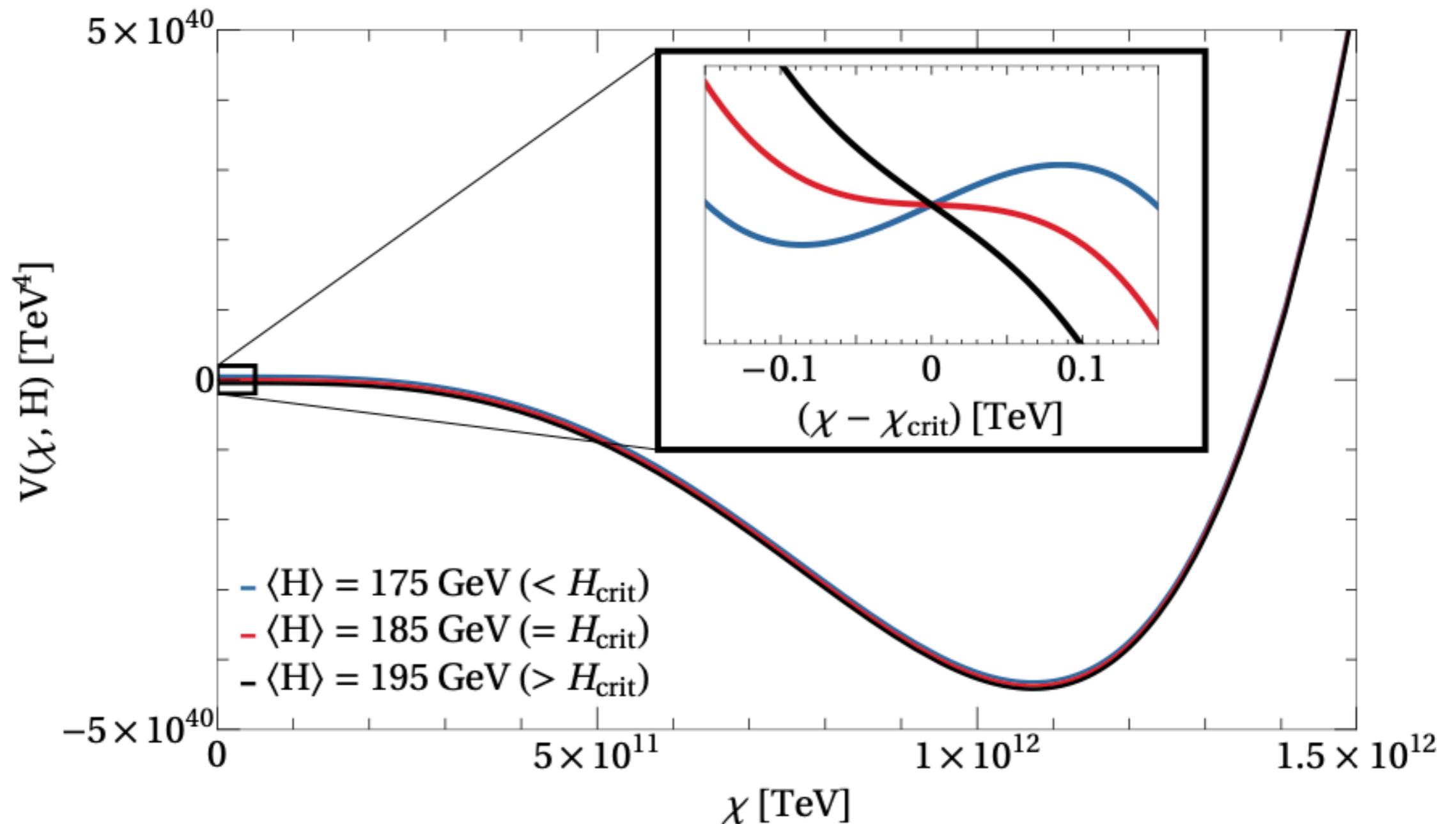
Phase transition can become **first-order**, even **strongly so**, and have **gravitational wave signals!**



**Observability at
LISA!**

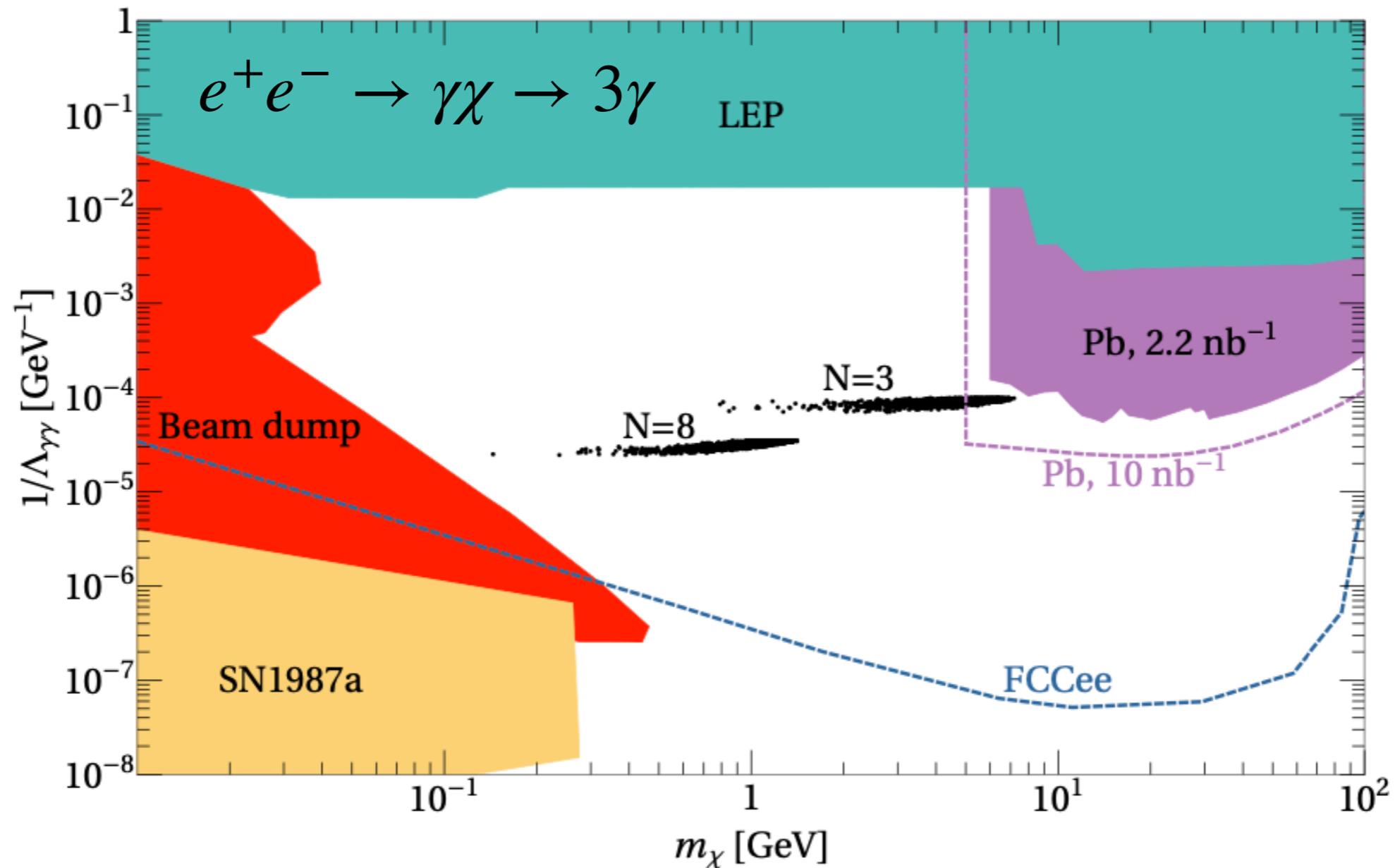
“Crunching Dilaton, Hidden Naturalness”

One example of a new paradigm linking the hierarchy problem to cosmological dynamics



“Crunching Dilaton, Hidden Naturalness”

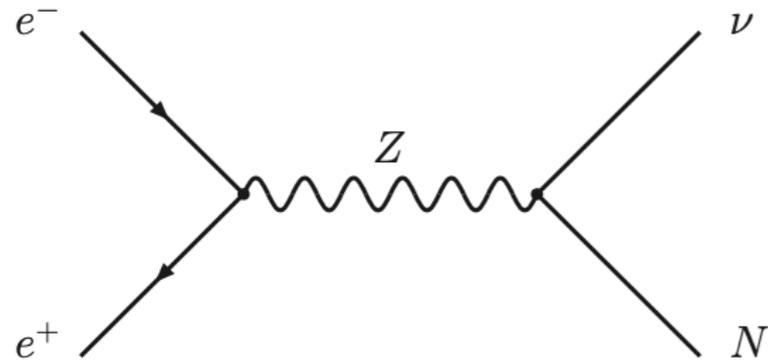
FCC-ee directly probes the dilaton scalar through its couplings to photons



Csáki, D’Agnolo, Geller, Ismail arXiv:2007.14396

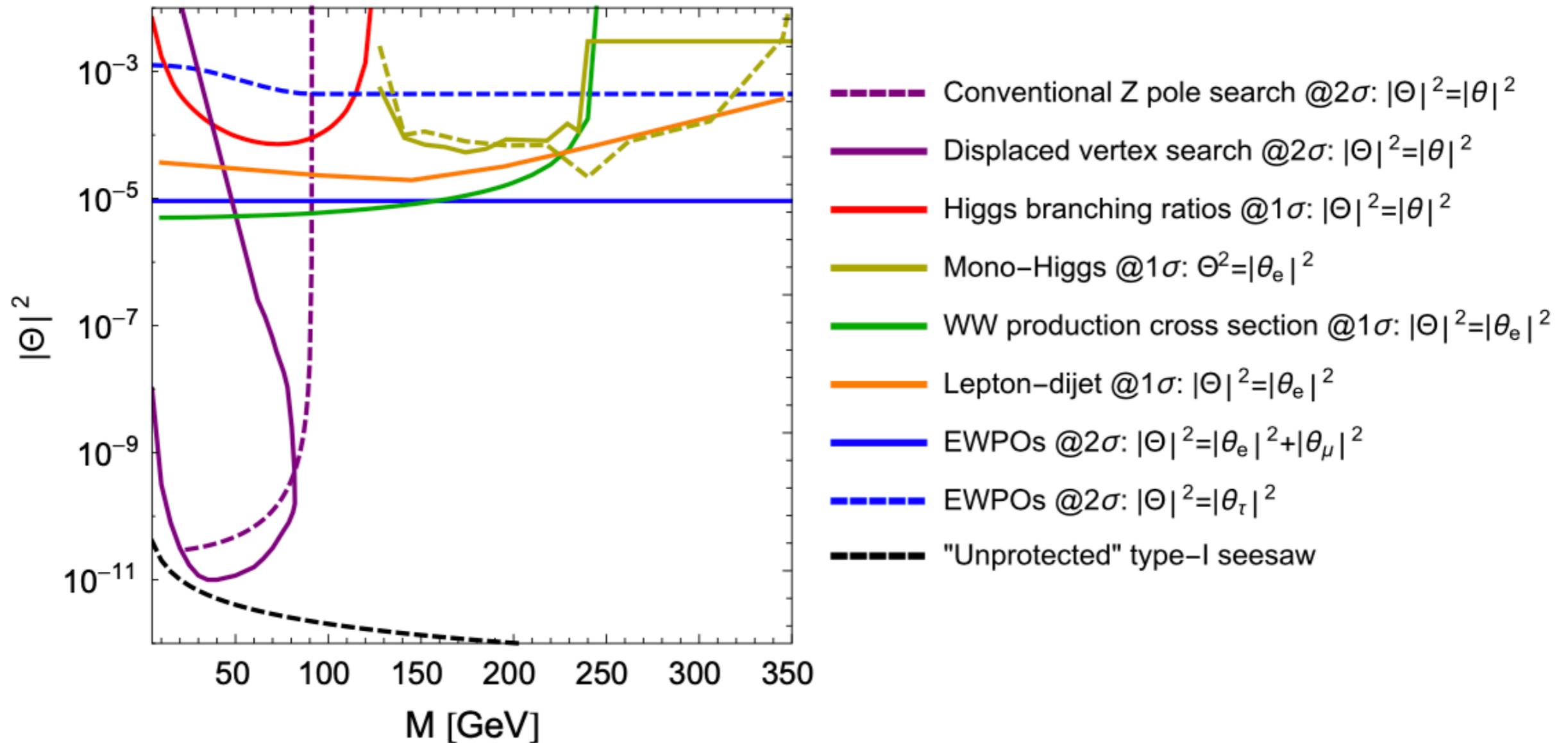
FCC curve based on Bauer, Heiles, Neubert, Thamm ’17/’18

Neutrino Physics at FCC-ee



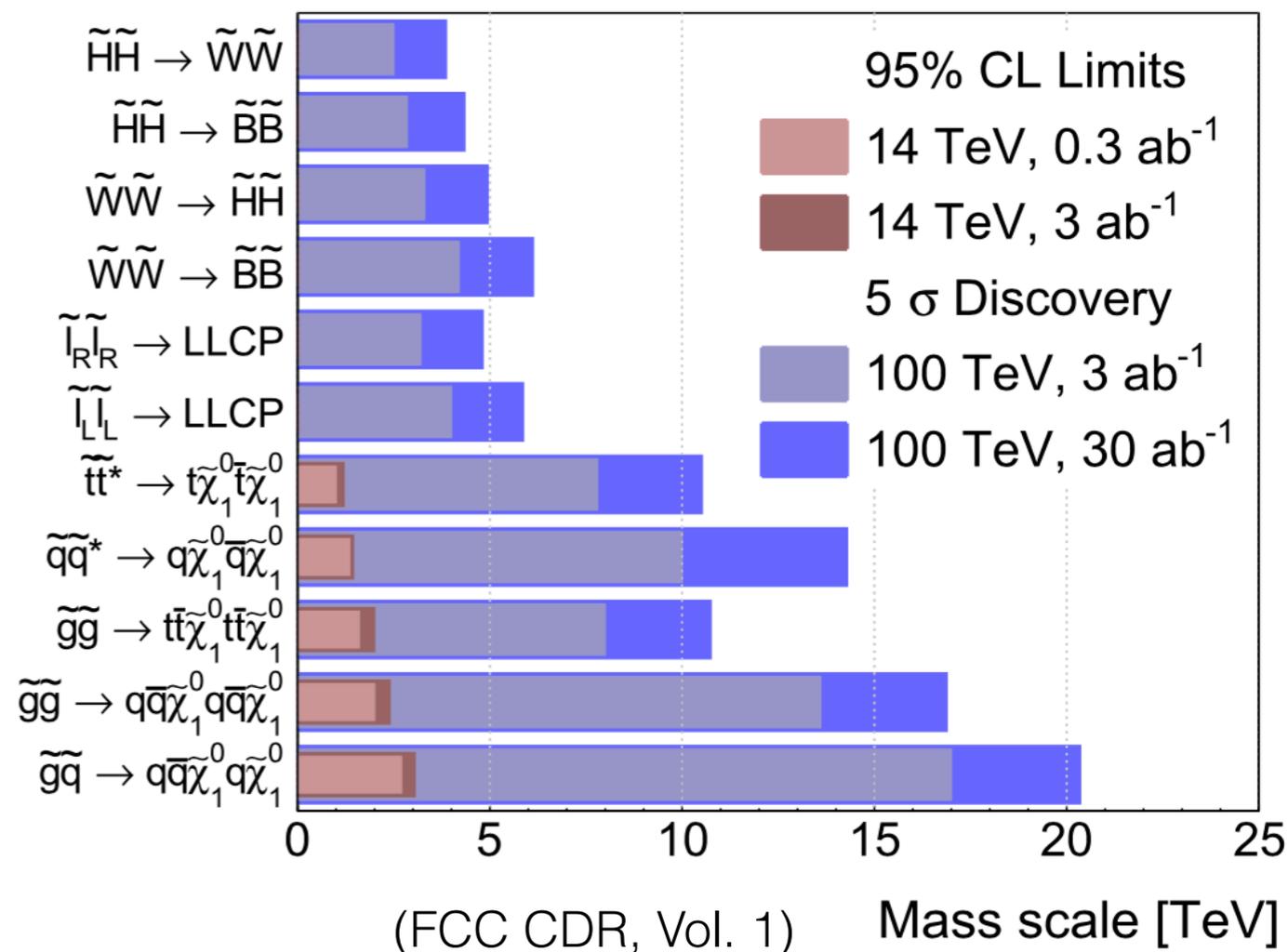
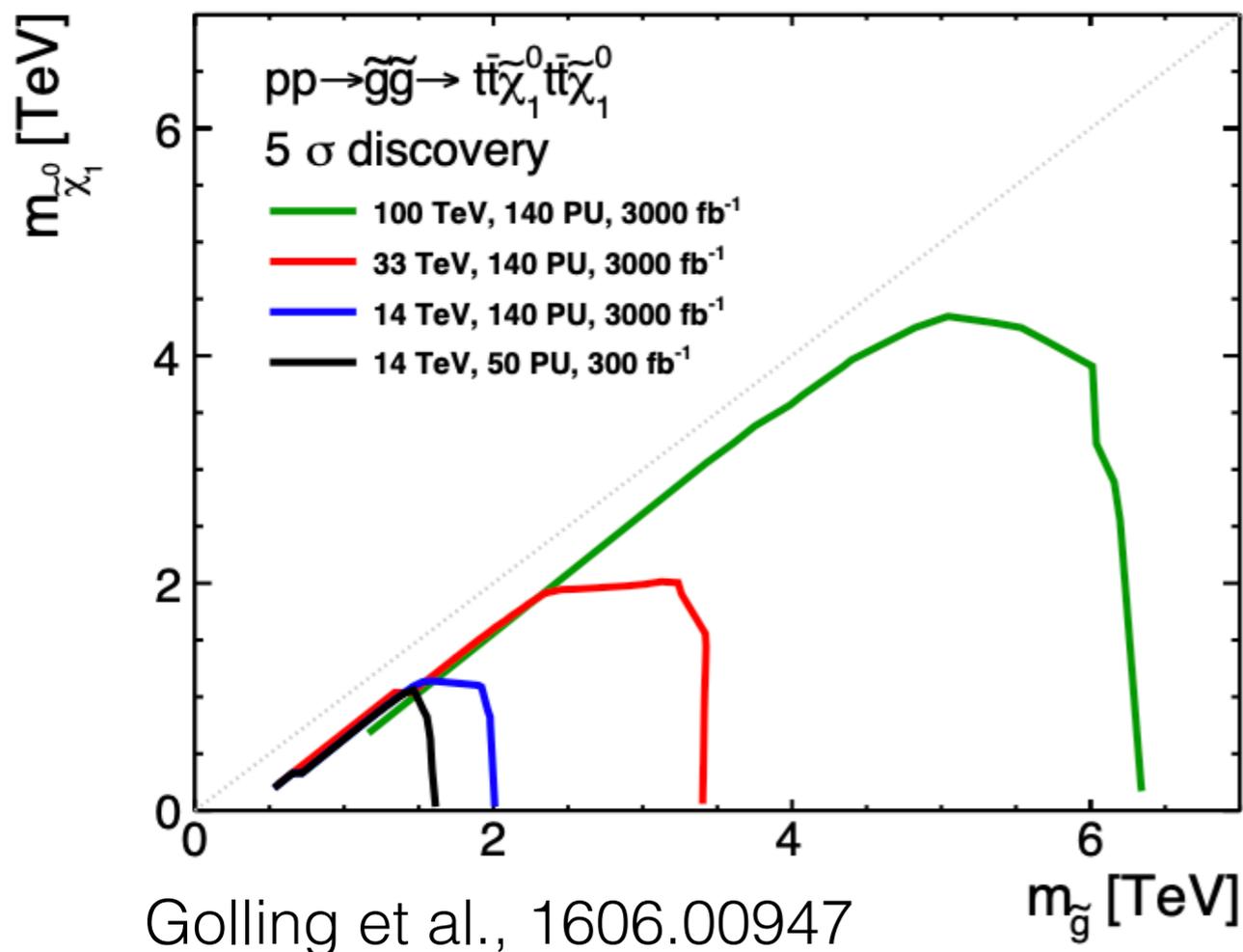
Sterile $N \rightarrow \ell^\pm W^\mp, \nu Z, \nu h$

Nonminimal models allow range of mixing angles
(not correlated with mass as in minimal seesaw)



FCC-hh Physics Case

Direct Mass Reach at 100 TeV FCC-hh



ϵ	High-scale mediation	Low-scale mediation
stop	$5 \times 10^{-5} \left(\frac{10 \text{ TeV}}{m_{\tilde{t}}} \right)^2$	$2 \times 10^{-3} \left(\frac{10 \text{ TeV}}{m_{\tilde{t}}} \right)^2$
gluino	$7 \times 10^{-6} \left(\frac{17 \text{ TeV}}{m_{\tilde{g}}} \right)^2$	$6 \times 10^{-3} \left(\frac{17 \text{ TeV}}{m_{\tilde{g}}} \right)^2$

source: European Strategy briefing book

SU(2) Multiplet Dark Matter

Simple models, but some continue to evade direct and indirect detection experiments.

SU(2)_L multiplets by definition involve **multiple** states, some charged

$$W^* \left(\begin{array}{c} \text{---} \\ M_2 \\ \text{---} \end{array} \right) \begin{array}{l} \tilde{W}^\pm \\ \tilde{W}^0 \end{array} \quad \} \delta m \sim \frac{\alpha}{\pi} m_W \quad (\text{tree-level dim 7})$$

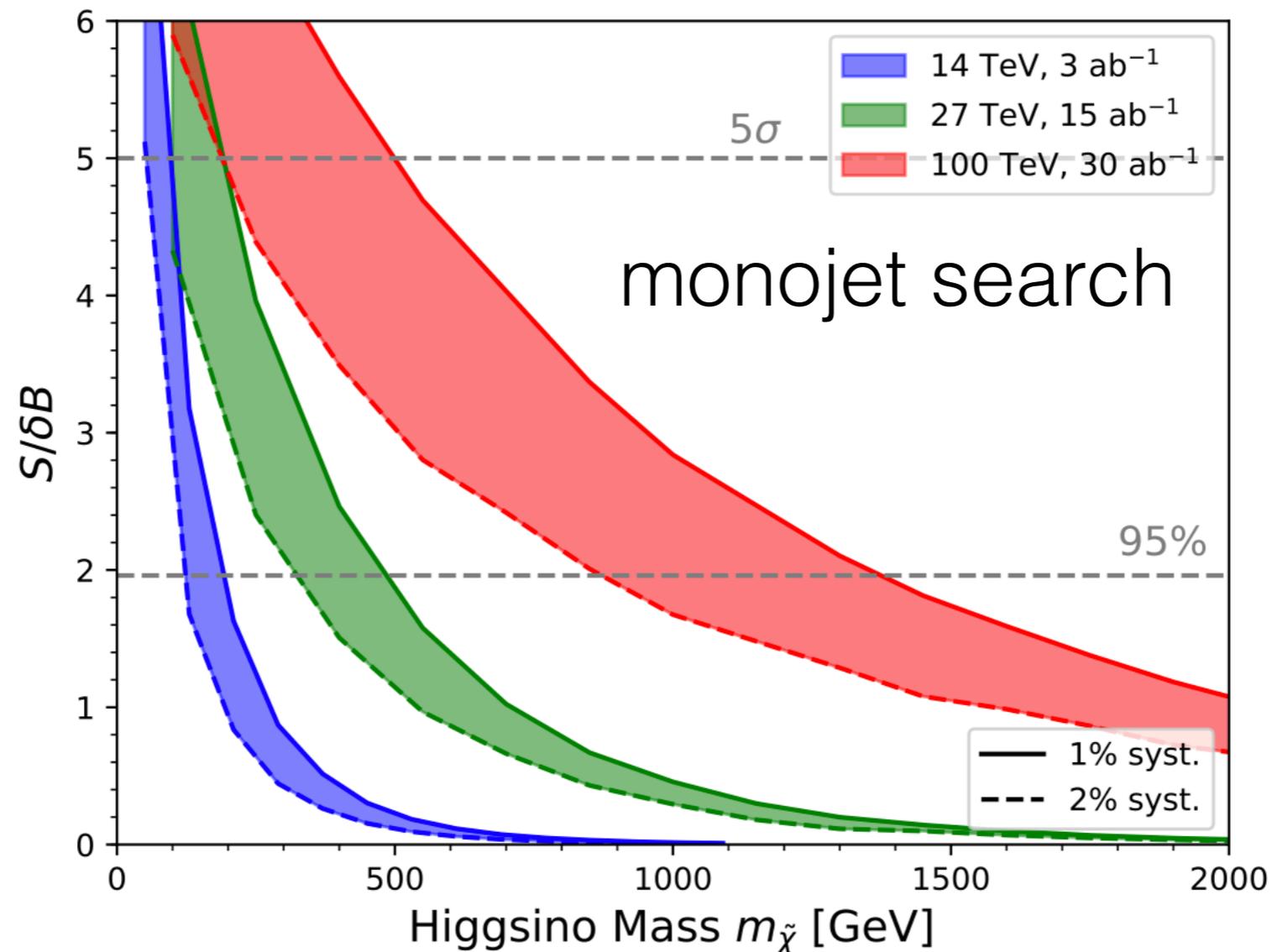
Wino charged \rightarrow neutral: **disappearing track**

$$Z^* \left(\begin{array}{c} W^* \\ W^* \end{array} \right) \left(\begin{array}{c} \text{---} \\ \mu \\ \text{---} \end{array} \right) \begin{array}{l} \tilde{H}_2^0 \\ \tilde{H}^\pm \\ \tilde{H}_1^0 \end{array} \quad \} \delta m \sim \frac{m_Z^2}{M_2}$$

Higgsino (toughest case) charged \rightarrow neutral, neutral \rightarrow neutral: **soft leptons or jets**

SU(2) Multiplet DM at 100 TeV

The thermal relic Higgsino (mass ~ 1 TeV) can be excluded at FCC-hh.

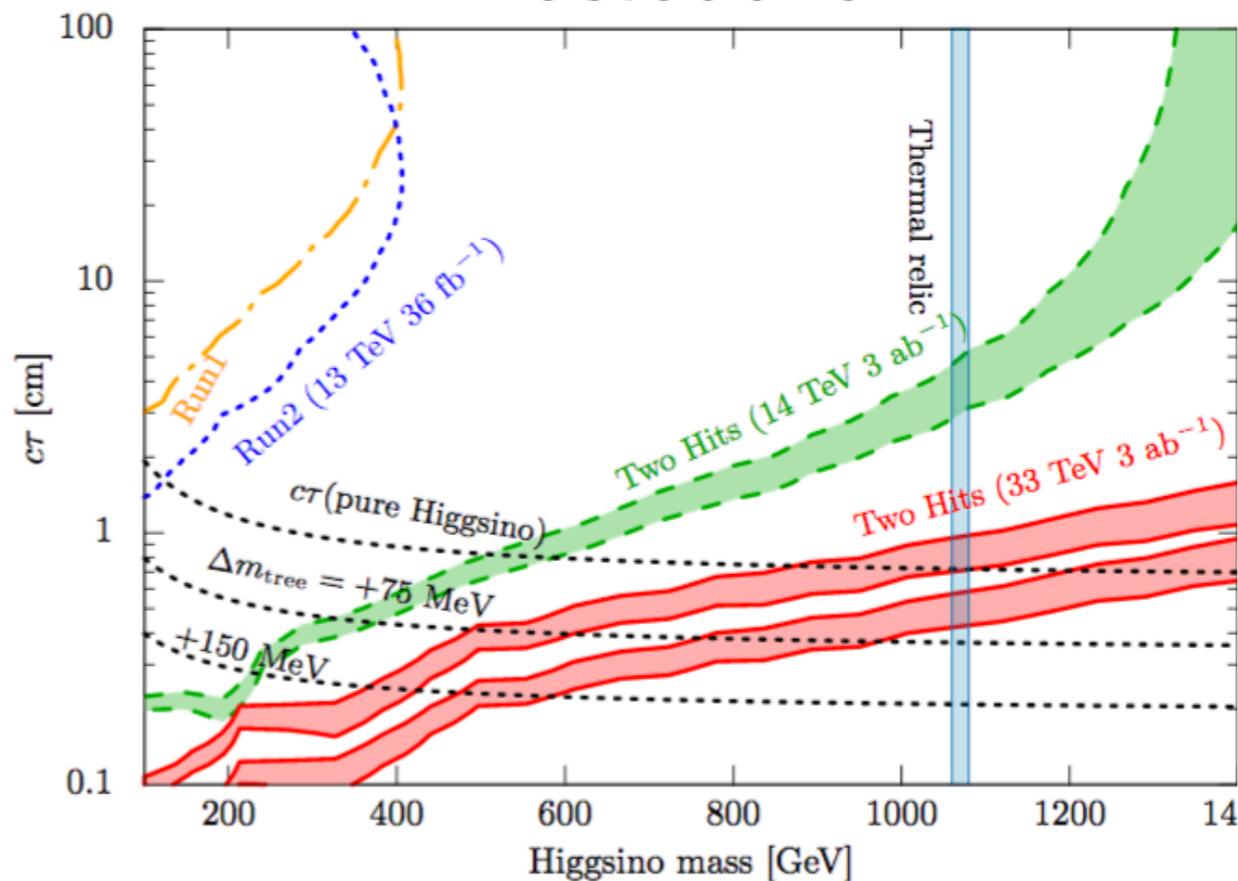


T. Han, S. Mukhopadhyay, and X. Wang, arXiv:1805.00015

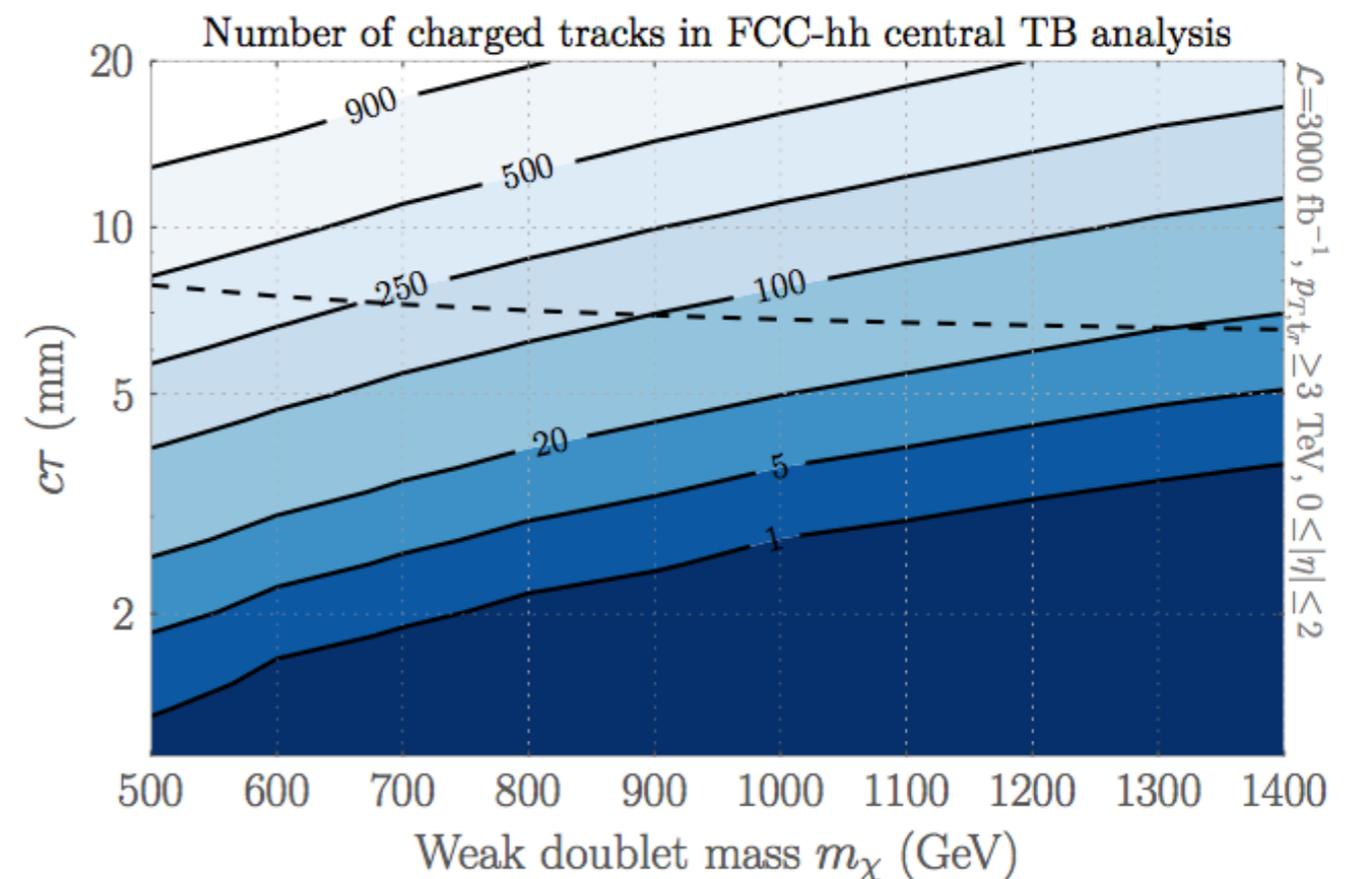
Higgsinos and Disappearing Tracks

The mildly long lifetime of a chargino can provide an additional handle on the very pure higgsino corner of parameter space:

Fukuda, Nagata, Otono, Shirai
1703.09675



Mahbubani, Schwaller, Zurita
1703.05327



Precision Higgs Measurements

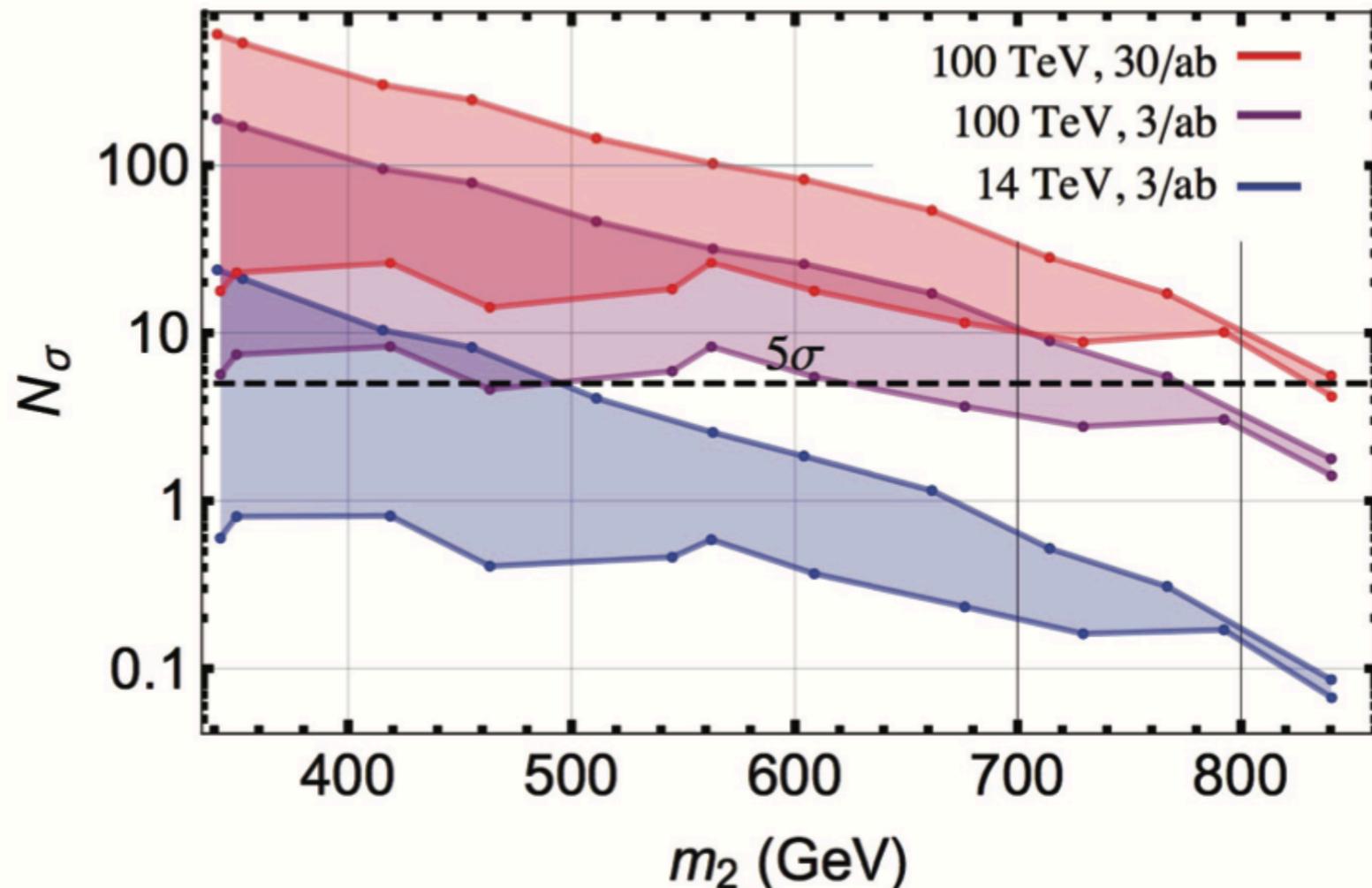
Table 1.2: Target precision for the parameters relative to the measurement of various Higgs decays, ratios thereof, and of the Higgs self-coupling λ . Notice that Lagrangian couplings have a precision that is typically half that of what is shown here, since all rates and branching ratios depend quadratically on the couplings.

Observable	Parameter	Precision (stat)	Precision (stat+syst+lumi)
$\mu = \sigma(H) \times B(H \rightarrow \gamma\gamma)$	$\delta\mu/\mu$	0.1%	1.45%
$\mu = \sigma(H) \times B(H \rightarrow \mu\mu)$	$\delta\mu/\mu$	0.28%	1.22%
$\mu = \sigma(H) \times B(H \rightarrow 4\mu)$	$\delta\mu/\mu$	0.18%	1.85%
$\mu = \sigma(H) \times B(H \rightarrow \gamma\mu\mu)$	$\delta\mu/\mu$	0.55%	1.61%
$\mu = \sigma(HH) \times B(H \rightarrow \gamma\gamma) B(H \rightarrow b\bar{b})$	$\delta\lambda/\lambda$	5%	7.0%
$R = B(H \rightarrow \mu\mu) / B(H \rightarrow 4\mu)$	$\delta R/R$	0.33%	1.3%
$R = B(H \rightarrow \gamma\gamma) / B(H \rightarrow 2e2\mu)$	$\delta R/R$	0.17%	0.8%
$R = B(H \rightarrow \gamma\gamma) / B(H \rightarrow 2\mu)$	$\delta R/R$	0.29%	1.38%
$R = B(H \rightarrow \mu\mu\gamma) / B(H \rightarrow \mu\mu)$	$\delta R/R$	0.58%	1.82%
$R = \sigma(t\bar{t}H) \times B(H \rightarrow b\bar{b}) / \sigma(t\bar{t}Z) \times B(Z \rightarrow b\bar{b})$	$\delta R/R$	1.05%	1.9%
$B(H \rightarrow \text{invisible})$	$B@95\%CL$	1×10^{-4}	2.5×10^{-4}

from: Future Circular Collider Study, Vol. 3 (FCC-hh CDR)

Singlet Scalar with Higgs Mixing

Resonant di-Higgs production: $h_2 \rightarrow 2h_1 \rightarrow 4\tau, b\bar{b}\gamma\gamma$



Parameter space with **strongly first-order phase transition** can be probed

Kotwal, No, Ramsey-Musolf, Winslow 1605.06123

(Also see 4b studies for HL-LHC by Li, Ramsey-Musolf, Willocq, 1906.05289)

Electroweak Phase Transition “Nightmare” Scenario

Singlet scalar with a \mathbb{Z}_2 symmetry $\phi \mapsto -\phi$

$$V(h, \phi) = V_{\text{SM}}(h) + \frac{1}{2}M^2\phi^2 + c_\phi |H|^2 \phi^2$$

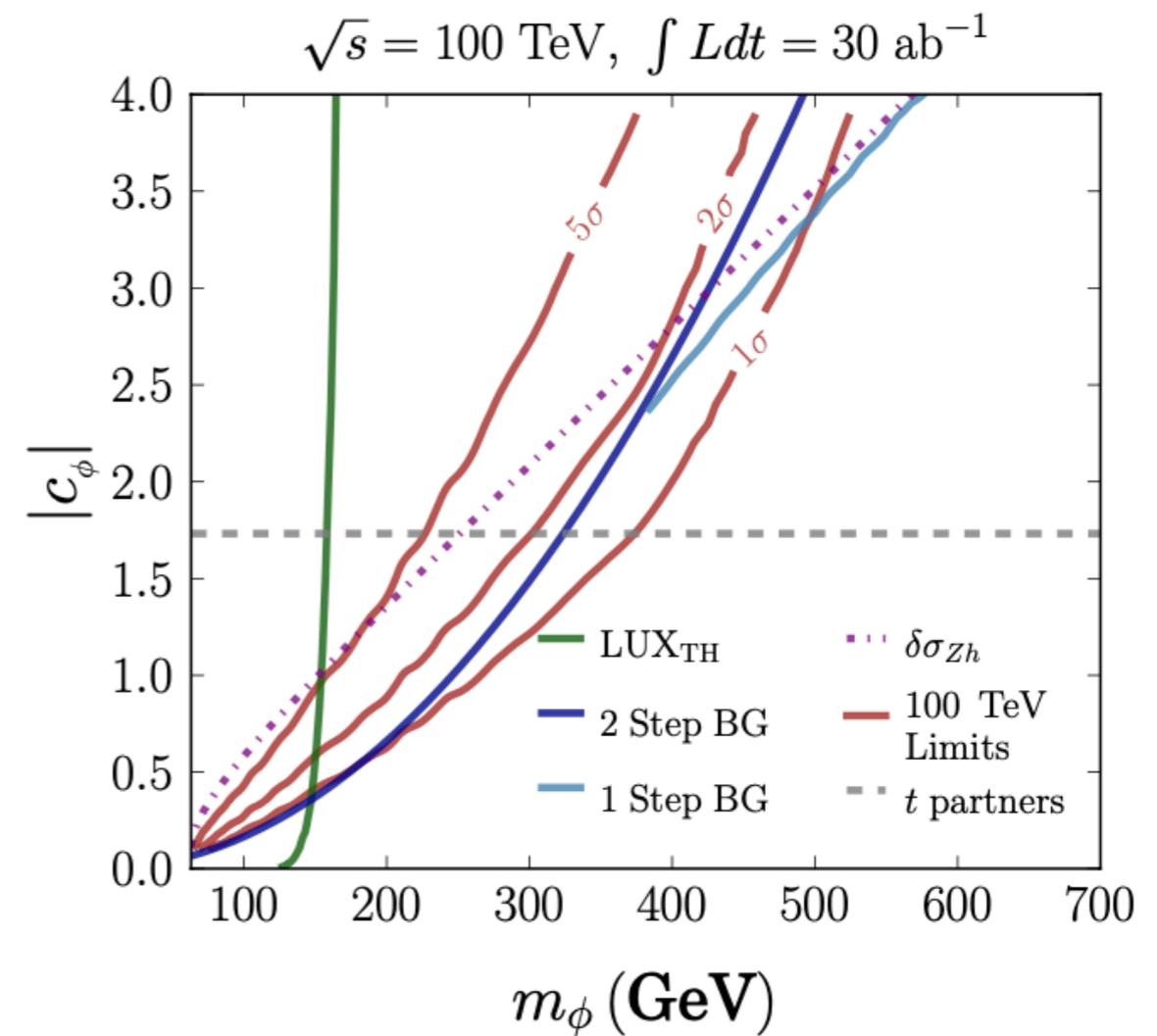
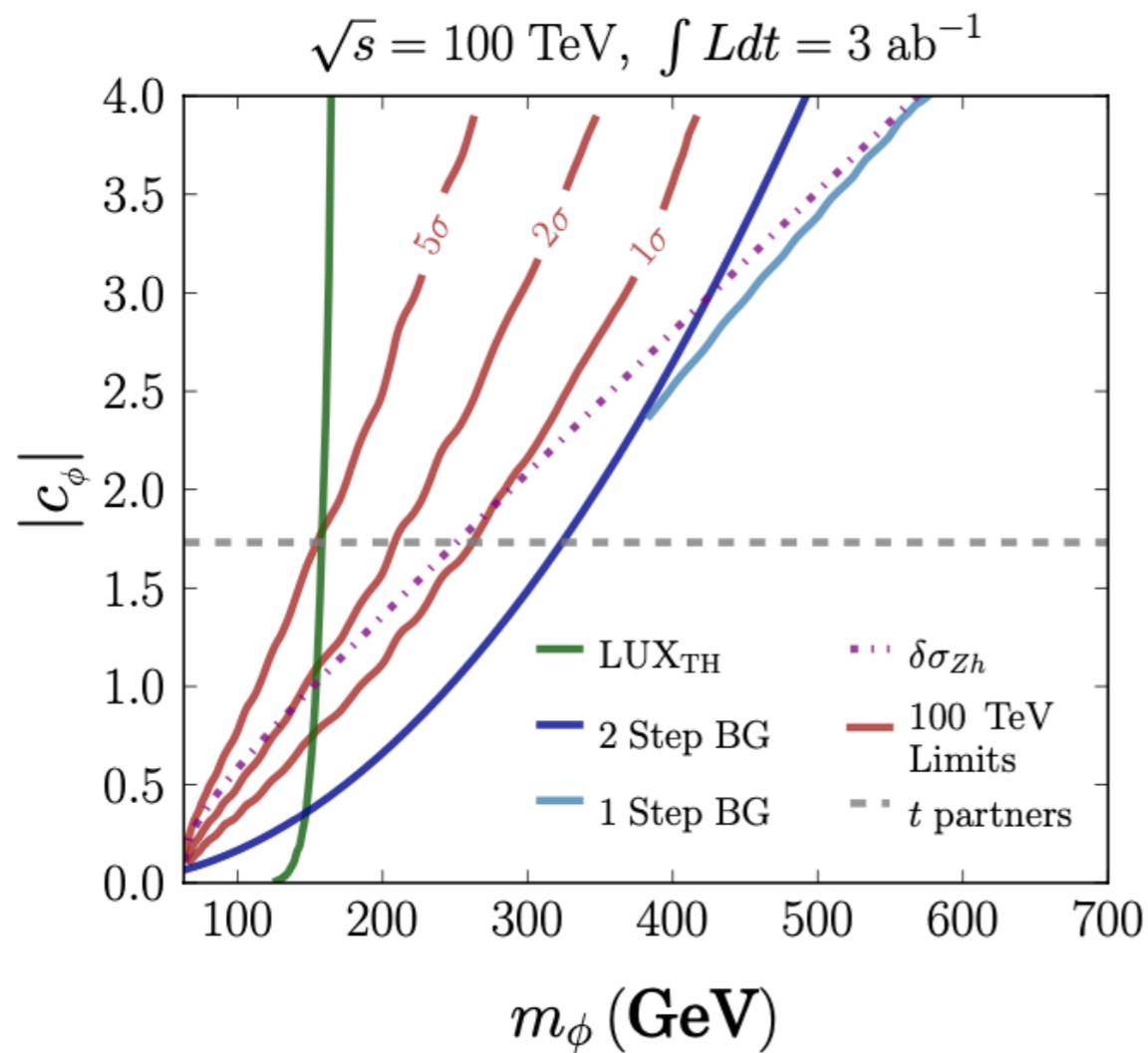
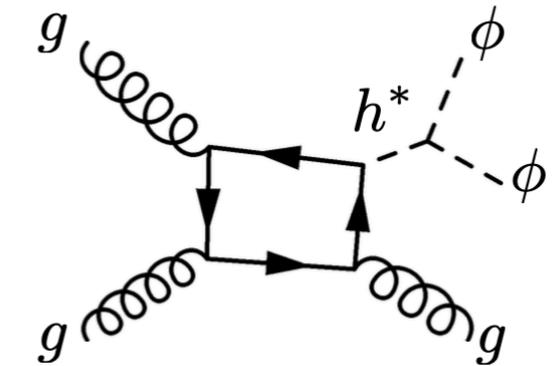
No mixing with the Higgs boson. **Stable, invisible.**

After EWSB: $h\phi^2$ vertex. Light ϕ : invisible width of Higgs.

$m_\phi > \frac{1}{2}m_h$: difficult!

The Higgs Portal Above Threshold

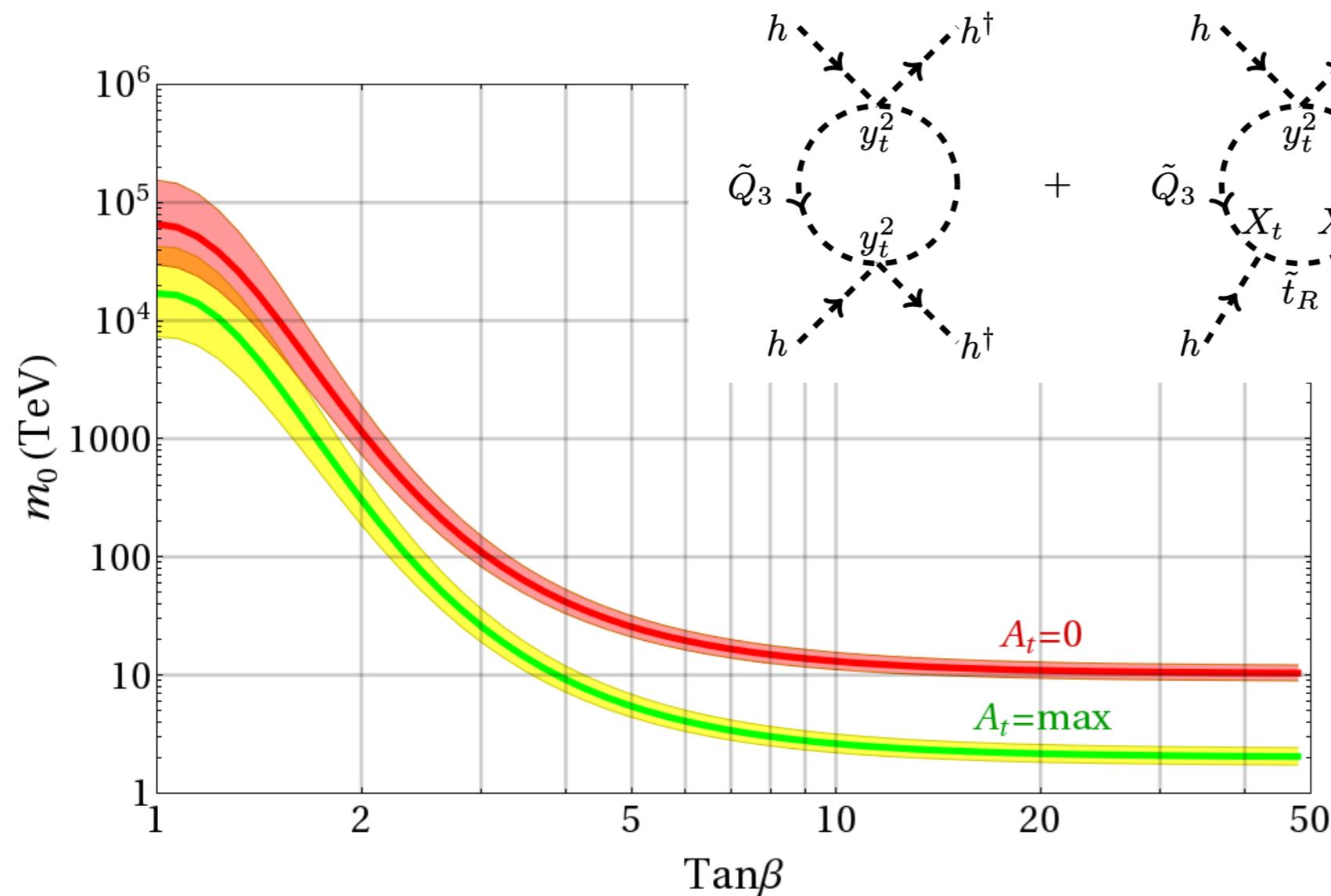
VBF $\phi\phi jj$ (forward jets) and gluon fusion



(Craig, Lou, McCullough, Thalapillil arXiv:1412.0258)

Why is the Higgs Mass 125 GeV?

In the MSSM, largely depends on the **stop mass** and **$\tan\beta$** .



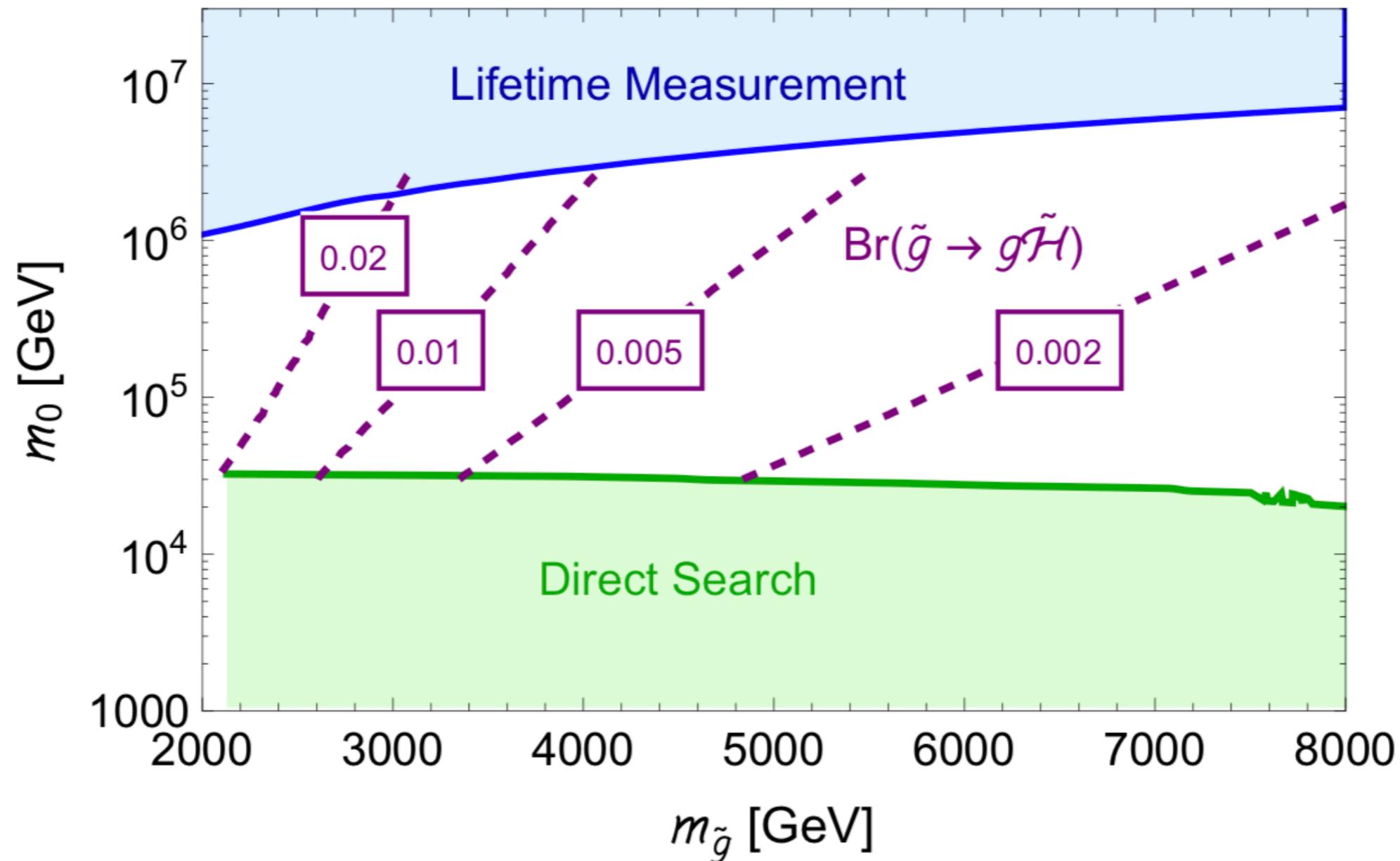
In the simplest models, this points to

$$m_{\tilde{t}} \gtrsim 10 \text{ TeV}$$

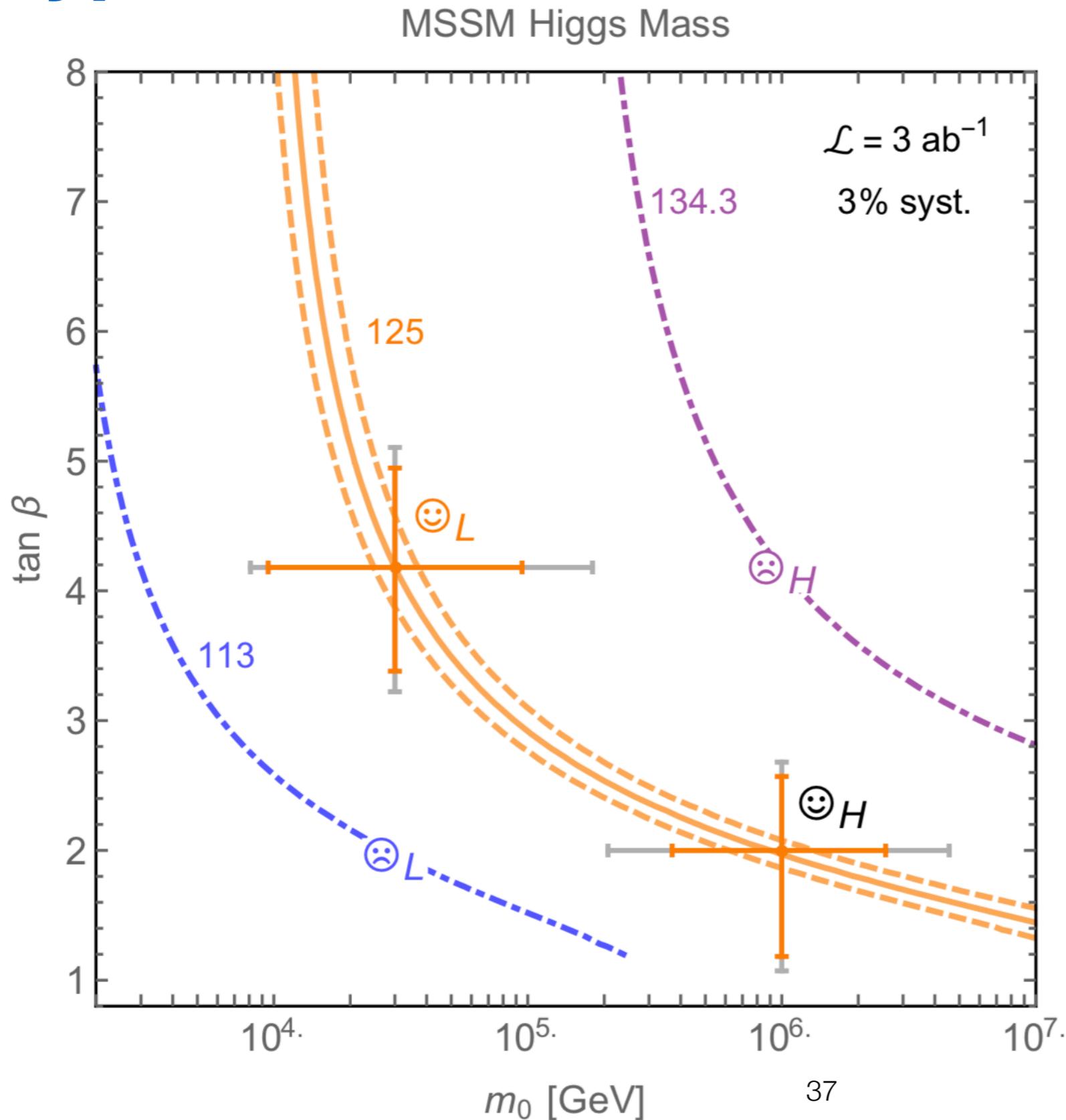
Can we test this?

LHC partial discovery scenario

We may get only *part* of the spectrum. **Example: split SUSY.** Even at a 100 TeV collider, can't make the scalar superpartners. But the 100 TeV collider would be a **gluino factory**.



Testing the MSSM Higgs mass hypothesis



Precision physics @ future hadron collider could answer **big question**: where does the Higgs mass come from?

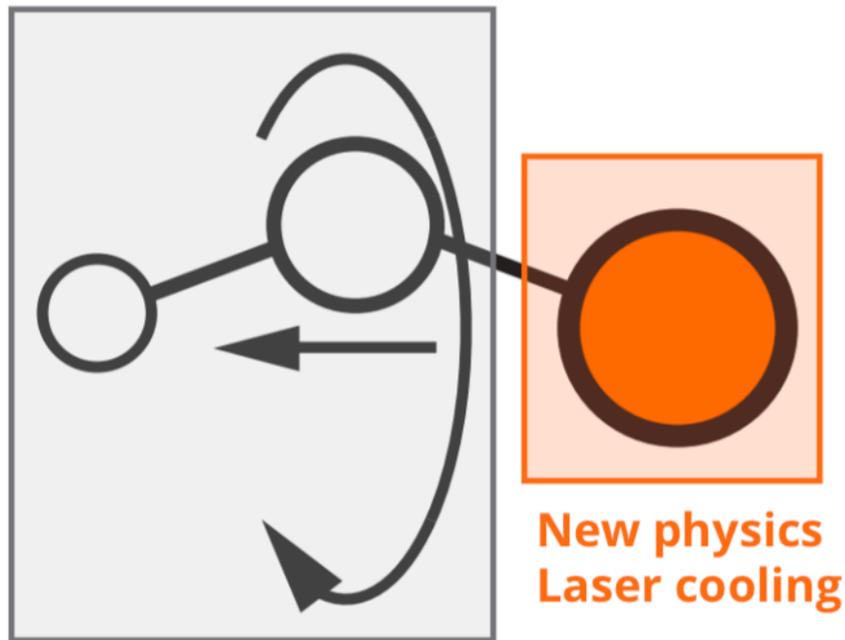
Would open up **new big question**: where does the SUSY breaking scale come from?

FCC in Context

EDM Precision on the Horizon

One of several parallel approaches:

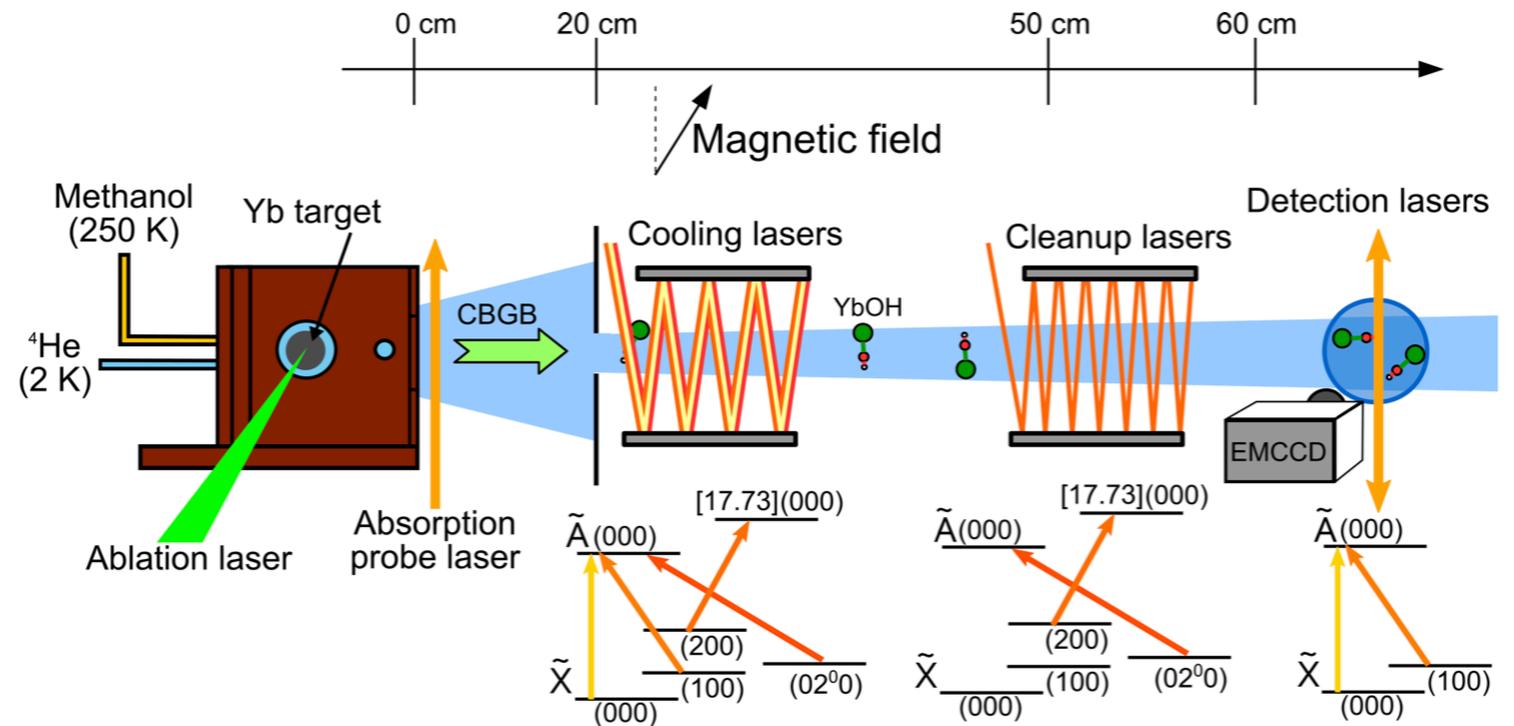
Polyatomic Molecules
(e.g., YbOH)



Polarization
Co-magnetometers

from slide by N.
Hutzler

Hutzler, Kozyryev 1705.11020

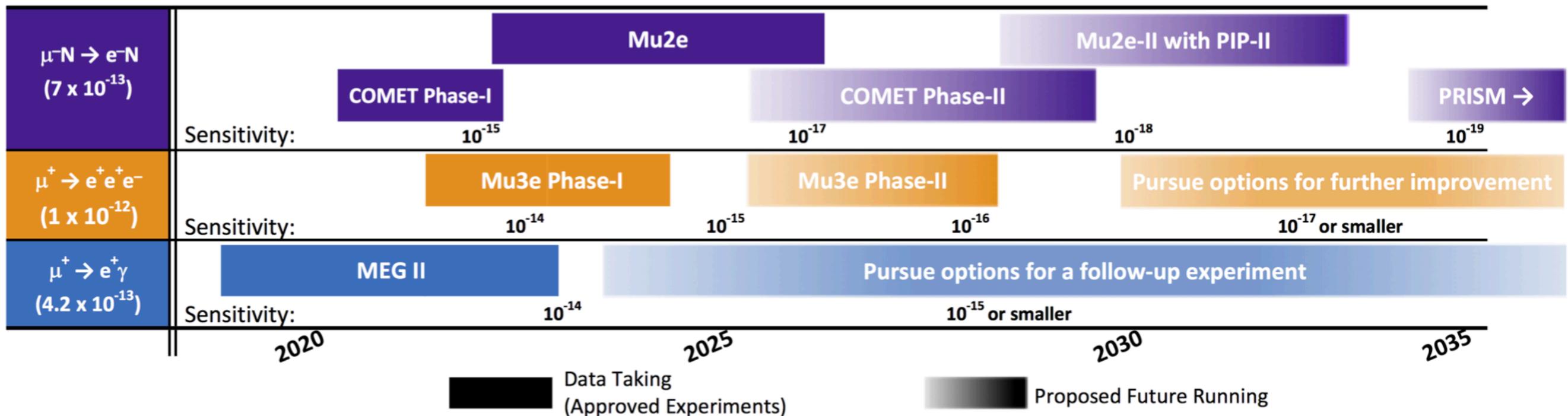


Laser cooling achieved
(Augenbraun et al., 1910.11318)

Electron EDM: $10^{-29} e \text{ cm} \longrightarrow 10^{-32} e \text{ cm} !$

Charged Lepton Flavor Violation

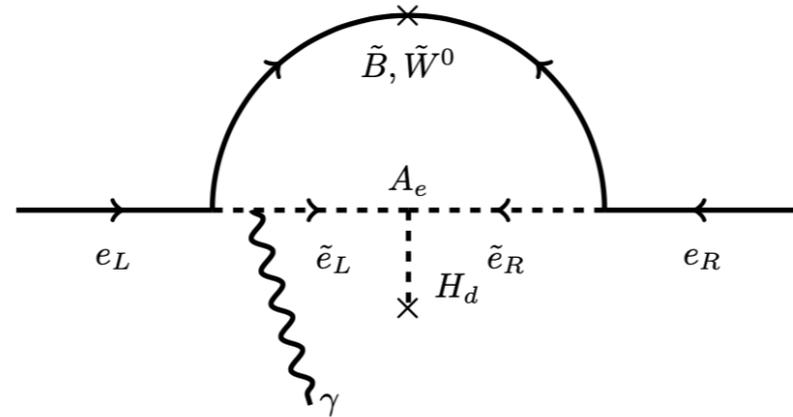
Searches for Charged-Lepton Flavor Violation in Experiments using Intense Muon Beams



Source: Baldini et al., 1812.06540, submission to 2020 European Strategy from COMET, MEG, Mu2e and Mu3e collaborations

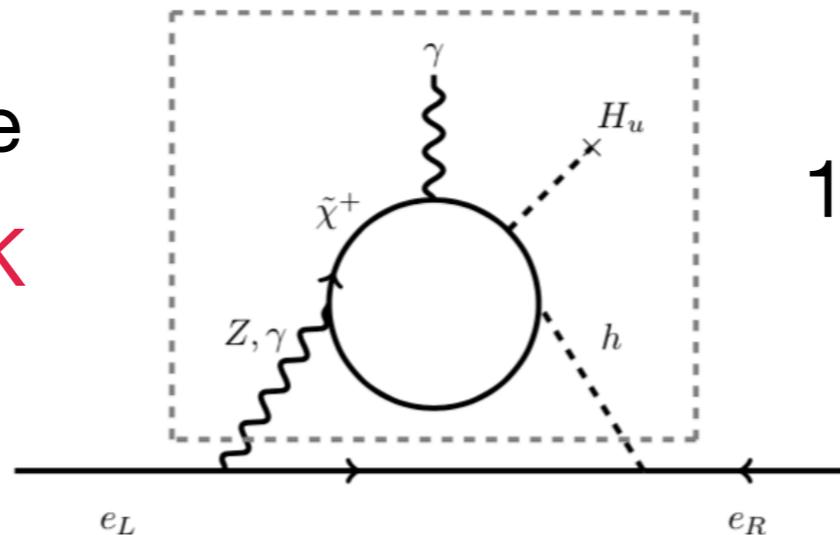
Could CP and Flavor Lead the Way?

EDM, 1-loop
electron-flavored



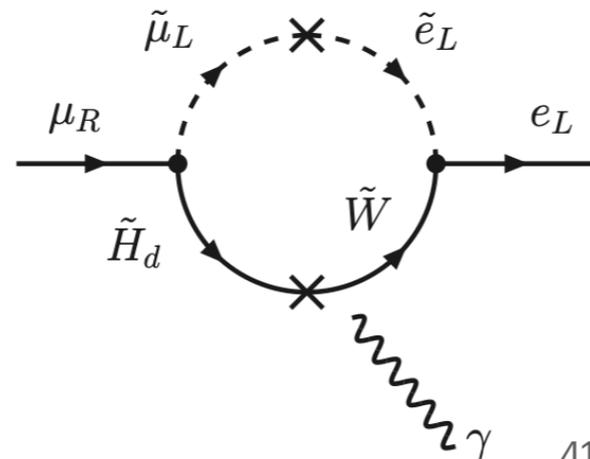
$10^{-32} \text{ e cm} \implies \sim \mathbf{1 \text{ PeV (!)}}$
(if $O(1)$ CP phase)

EDM, 2-loop Barr-Zee
Anything Higgs+EWK



$10^{-32} \text{ e cm} \implies \sim \mathbf{50 \text{ TeV (!)}}$
(if $O(1)$ CP phase)

$\mu \rightarrow e$, 1-loop,
flavor violating



$10^{-19} \text{ on Al} \implies \sim \mathbf{50+ \text{ TeV (!)}}$
(if large flavor violation)

fig. from 1308.3653: Altmannshofer, Harnik, Zupan

The Role of Colliders

If a precision physics experiment (EDMs, CLFV, flavor physics at Belle II, muon $g - 2$, etc) makes a discovery, we will learn ***the coefficient of one higher-dimension operator*** and little else.

Only a collider can **produce** and **systematically characterize** the underlying new physics!

We should support “Physics Beyond Colliders” as a stepping stone—it may provide us our strongest argument for building the next energy-frontier collider!

Conclusions

Colliders offer opportunities to not just discover that the Standard Model is incomplete, but to ***fully uncover the nature of the new physics.***

FCC will define the agenda for particle physics well into the 21st century.

FCC-ee and FCC-hh both have exciting, complementary roles to play in this agenda.

The future of particle physics requires new energy-frontier colliders like FCC!