

Light hyperon physics at BESIII

Varvara Batozskaya,
on behalf of the BESIII collaboration

Institute of High Energy Physics, Beijing, China
National Centre for Nuclear Research, Warsaw, Poland

32nd Recontres de Blois
Blois, Loire Valley, France
17-22 October 2021



- More than 50 years of the knowledge about CP violation (CPV)
 - Confirmed only in meson decays

- SM CPV is not sufficient to explain observed matter-antimatter asymmetry
- Baryogenesis requires C and CP violation in the processes

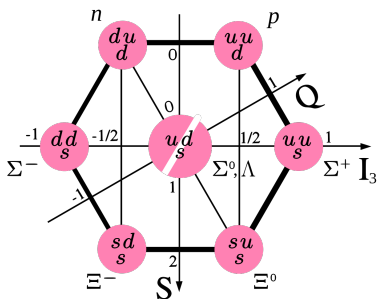
[PismaZh.Eksp.Teor.Fiz.5(1967)32]



- Systematical mapping with different hadronic systems and complementary methods are needed for understanding CPV in flavour sector

Ground-state strange baryons

- Spin- $\frac{1}{2}$ baryon octet
- Weak $\Delta S = 1$ transitions



+ $\Omega^-(sss)$ spin- $\frac{3}{2}$

Hyperon	Mass [GeV/ c^2]	Decay (\mathcal{B})
$\Lambda(uds)$	1.116	$p\pi^-$ (63.9%) $n\pi^0$ (35.8%)
$\Sigma^-(dds)$	1.197	$n\pi^-$ (99.8%)
$\Sigma^+(uus)$	1.189	$p\pi^0$ (51.6%) $n\pi^+$ (48.3%)
$\Xi^0(uss)$	1.315	$\Lambda\pi^0$ (99.5%)
$\Xi^-(dss)$	1.321	$\Lambda\pi^-$ (99.8%)
$\Omega(sss)$	1.672	ΛK^- (67.8%) $\Xi^0\pi^-$ (23.6%) $\Xi^-\pi^0$ (8.6%)

Decay amplitudes in hyperon decays

- P- and S-wave amplitudes:

$$\Lambda \rightarrow p\pi^-, \Xi^- \rightarrow \Lambda\pi^-, \Sigma \rightarrow N\pi$$

$$\mathcal{A} = S + P\vec{\sigma} \cdot \hat{\mathbf{n}}$$

- $|\Delta I| = 1/2$
- Contribution of $|\Delta I| = 3/2$ is $\sim 10\%$

weak CP-odd phases

$$S = |S| \exp(\xi_S) \exp(i\delta_S)$$

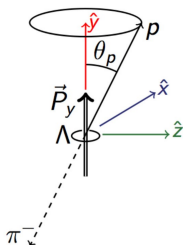
$$P = |P| \exp(\xi_P) \exp(i\delta_P)$$

strong phases

- Two measurable parameters

$$\alpha = \frac{2\text{Re}(S^*P)}{|S|^2 + |P|^2} \quad \beta = \frac{2\text{Im}(S^*P)}{|S|^2 + |P|^2} = \sqrt{1 - \alpha^2} \sin \phi$$

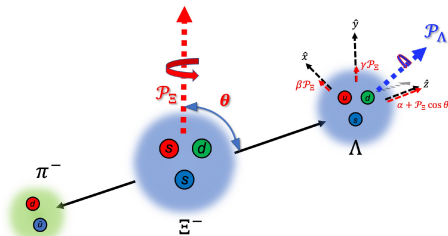
- **Polarisation** of hyperons experimentally accessible in weak parity violating decays



- Example:
angular distribution of $\Lambda \rightarrow p\pi^-$

$$I(\cos \theta_p) \propto 1 + \alpha_\Lambda P_\Lambda \cos \theta_p$$

- **Angle ϕ** accessible when daughter baryon polarisation measured
- Example: $\Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^-$



CP tests in hyperon decays

- If CP conserved: $\bar{\alpha} = -\alpha$, $\bar{\beta} = -\beta$, $\bar{\phi} = -\phi$
- Possible CP tests:

weak P-S phase difference

$$A_{CP} = \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}} = -\sin \phi \tan(\xi_P - \xi_S) \frac{\sqrt{1-\alpha^2}}{\alpha}$$

$$\Phi_{CP} = \frac{\phi + \bar{\phi}}{2} = \cos \phi \tan(\xi_P - \xi_S) \frac{\alpha}{\sqrt{1-\alpha^2}}$$

- HyperCP measurement [PRL93(2004)262001]:

$$A_{CP}^{\Lambda} + A_{CP}^{\Xi} = (0.0 \pm 5.1_{\text{stat}} \pm 4.4_{\text{syst}}) \cdot 10^{-4}$$

- SM predictions [PRD67(2003)056001]

$$-3 \cdot 10^{-5} \leq A_{\Lambda} \leq 4 \cdot 10^{-5}$$

$$-2 \cdot 10^{-5} \leq A_{\Xi} \leq 1 \cdot 10^{-5}$$

Decay mode	$\xi_P - \xi_S$ ($\eta\lambda^5 A^2$)
$\Lambda \rightarrow p\pi^-$	0.2 ± 1.6
$\Xi^- \rightarrow \Lambda\pi^-$	-1.4 ± 1.2

CP tests in hyperon decays

- If CP conserved: $\bar{\alpha} = -\alpha$, $\bar{\beta} = -\beta$, $\bar{\phi} = -\phi$
- Possible CP tests:

weak P-S phase difference

$$A_{CP} = \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}} = -\sin \phi \tan(\xi_P - \xi_S) \frac{\sqrt{1 - \alpha^2}}{\alpha}$$

$$\Phi_{CP} = \frac{\phi + \bar{\phi}}{2} = \cos \phi \tan(\xi_P - \xi_S) \frac{\alpha}{\sqrt{1 - \alpha^2}}$$

- HyperCP measurement [PRL93(2004)262001]:

$$A_{CP}^\Lambda + A_{CP}^\Xi = (0.0 \pm 5.1_{\text{stat}} \pm 4.4_{\text{sys}}) \cdot 10^{-4}$$

$$(\xi_P - \xi_S)_{BSM} = \frac{C'_B}{B_G} \left(\frac{\epsilon'}{\epsilon} \right)_{BSM} + \frac{C_B}{\kappa} \epsilon_{BSM}$$

- SM predictions [PRD67(2003)056001]

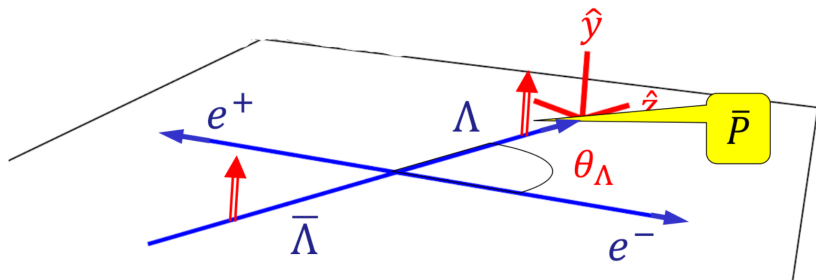
$$\begin{aligned} -3 \cdot 10^{-5} &\leq A_\Lambda \leq 4 \cdot 10^{-5} \\ -2 \cdot 10^{-5} &\leq A_\Xi \leq 1 \cdot 10^{-5} \end{aligned}$$

Decay mode	$\xi_P - \xi_S$ ($\eta\lambda^5 A^2$)
$\Lambda \rightarrow p\pi^-$	0.2 ± 1.6
$\Xi^- \rightarrow \Lambda\pi^-$	-1.4 ± 1.2

- BSM predictions [PRD69(2004)076008]

$$0.5 < B_G < 2 \text{ and } 0.2 < |\kappa| < 1$$

Decay	C_B	C'_B
$\Lambda \rightarrow p\pi^-$	1.1 ± 2.2	0.4 ± 0.8
$\Xi^- \rightarrow \Lambda\pi^-$	-0.5 ± 1.0	0.4 ± 0.7



- Unpolarised e^+e^- beams \implies transverse polarisation (if $\Delta\Phi \neq 0$):

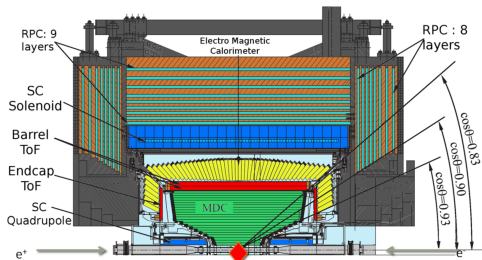
$$P_y(\cos\theta_\Lambda) = \frac{\sqrt{1-\alpha_\psi^2} \cos\theta_\Lambda \sin\theta_\Lambda}{1+\alpha_\psi \cos^2\theta_\Lambda} \sin(\Delta\Phi)$$

- Angular distribution:

$$\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_\psi \cos^2\theta_\Lambda \text{ with } \alpha_\psi \in [-1, 1]$$

- Beijing Electron-Positron Collider (BEPCII)
 - e^+e^- collider with $2.0 \text{ GeV} < E_{\text{CMS}} < 4.95 \text{ GeV}$
 - $\mathcal{L}_{\text{peak}} = 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
 - Data taking since 2009

- Beijing Spectrometer (BESIII)
 - Optimized for flavour physics
 - Covers 93% of the 4π solid angle
 - 1.0 T super-conducting solenoid
 - Momentum resolution:
 $\sigma(p)/p = 0.5\%$ at $1 \text{ GeV}/c$
 - Time resolution:
 68 (65) ps in the barrel (end cap)



Decay	$\mathcal{B}(\cdot 10^{-4})$	$\epsilon(\%)$	N_{Obs}	Reference
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$19.43 \pm 0.03 \pm 0.33$	42.37 ± 0.14	$441 \cdot 10^3$	[PRD95(2017)052003]
$J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$	$11.64 \pm 0.04 \pm 0.23$	17.83 ± 0.06	$111 \cdot 10^3$	[PRD95(2017)052003]
$J/\psi \rightarrow \Xi^- \bar{\Xi}^+$	$10.40 \pm 0.06 \pm 0.74$	18.40 ± 0.04	$43 \cdot 10^3$	[PRD93(2016)072003]
$\psi(2S) \rightarrow \Lambda \bar{\Lambda}$	$3.97 \pm 0.02 \pm 0.12$	42.83 ± 0.34	$31 \cdot 10^3$	[PRD95(2017)052003]
$\psi(2S) \rightarrow \Sigma^0 \bar{\Sigma}^0$	$2.44 \pm 0.03 \pm 0.11$	14.79 ± 0.12	$6.6 \cdot 10^3$	[PRD95(2017)052003]
$\psi(2S) \rightarrow \Xi^- \bar{\Xi}^+$	$2.78 \pm 0.05 \pm 0.14$	18.04 ± 0.04	$5.3 \cdot 10^3$	[PRD93(2016)072003]

Formalism $e^+e^- \rightarrow J/\psi(\psi(2S)) \rightarrow B_1\bar{B}_1, B_1 \rightarrow B_2 M + \text{c.c.}$

- Two spin- $\frac{1}{2}$ particle state:

$$\rho_{1/2, \overline{1/2}} = \frac{1}{4} \sum_{\mu\bar{\nu}} C_{\mu\bar{\nu}} \sigma_{\mu}^{B_1} \otimes \sigma_{\bar{\nu}}^{\bar{B}_1}$$

$$C_{\mu\bar{\nu}} = \begin{pmatrix} 1 + \alpha_{\psi} \cos^2 \theta & 0 & \beta_{\psi} \sin \theta \cos \theta & 0 \\ 0 & \sin^2 \theta & 0 & \gamma_{\psi} \sin \theta \cos \theta \\ -\beta_{\psi} \sin \theta \cos \theta & 0 & \alpha_{\psi} \sin^2 \theta & 0 \\ 0 & -\gamma_{\psi} \sin \theta \cos \theta & 0 & -\alpha_{\psi} - \cos^2 \theta \end{pmatrix}$$

Transverse polarisation
Spin correlations

where $\beta_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \sin(\Delta\Phi)$ $\gamma_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \cos(\Delta\Phi)$

- Decay can be presented via decay matrices:

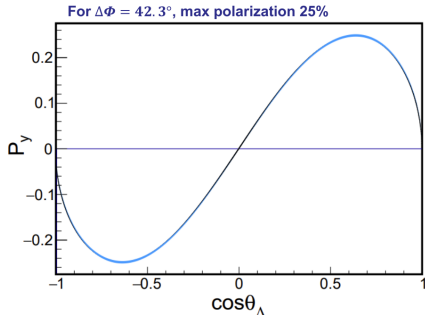
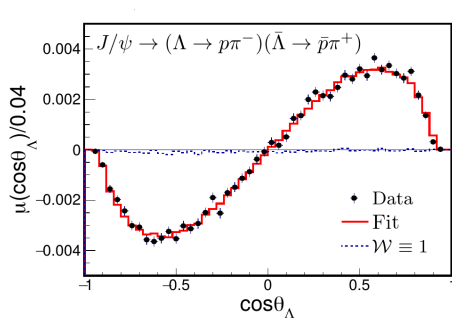
$$\sigma_{\mu}^{B_1} \rightarrow \sum_{\mu'=0}^3 a_{\mu\mu'}^{B_1} \sigma_{\mu'}^{B_2}$$

- Full angular distribution:

$$\mathcal{W}(\xi, \omega) = \text{Tr} \rho_{B_2 \bar{B}_2} = \sum_{\mu, \bar{\nu}=0}^3 C_{\mu\bar{\nu}} a_{\mu 0}^{B_1} a_{\bar{\nu} 0}^{\bar{B}_1}$$

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}, \Lambda \rightarrow p\pi^- + \text{c.c.} \quad (1)$$

- Data sample of $1.31 \cdot 10^9$ J/ψ events
- Exclusive analysis: $N_{\text{sig}} = 421 \cdot 10^3$ with $N_{\text{bkg}} = 399$



Parameters	This work	Previous results
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 [BESIII]
$\Delta\Phi$ (rad)	$0.740 \pm 0.010 \pm 0.008$	—
α_Λ	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 [PDG]
$\bar{\alpha}_\Lambda$	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 [PDG]

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}, \Lambda \rightarrow p\pi^- + \text{c.c.} \quad (2)$$

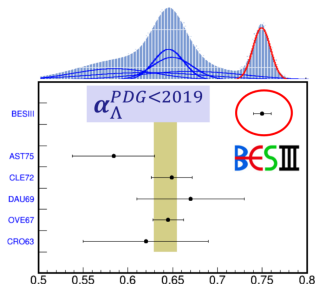
[Nature Phys.15(2019)631]

$$A_{CP}^{\Lambda} = \frac{\alpha_{\Lambda} + \bar{\alpha}_{\Lambda}}{\alpha_{\Lambda} - \bar{\alpha}_{\Lambda}} = -0.006 \pm 0.012_{\text{stat}} \pm 0.007_{\text{syst}}$$

- PS185: $A_{CP}^{\Lambda} = 0.013 \pm 0.021_{\text{tot}}$ [PRC54(1996)1877]

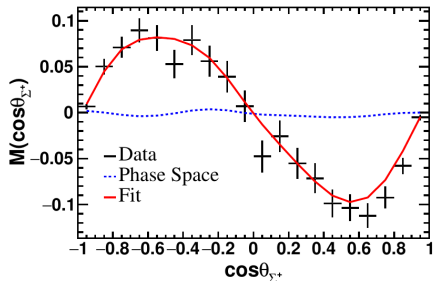
$$\langle \alpha_{\Lambda} \rangle = \frac{\alpha_{\Lambda} - \bar{\alpha}_{\Lambda}}{2} = 0.754 \pm 0.003_{\text{stat}} \pm 0.002_{\text{syst}}$$

- CLAS: $\alpha_{\Lambda} = 0.721 \pm 0.006_{\text{stat}} \pm 0.005_{\text{syst}}$ [PRL123(2019)182301]



$e^+e^- \rightarrow J/\psi, \psi' \rightarrow \Sigma^+\bar{\Sigma}^-, \Sigma^+ \rightarrow p\pi^0 + c.c.$

Plots acceptance uncorrected



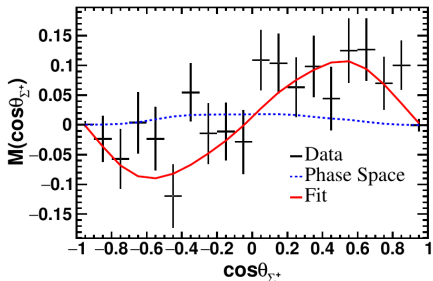
- Data sample of $1.31 \cdot 10^9$ J/ψ events
- $87 \cdot 10^3$ events with 5% bkg

$$\alpha_{J/\psi} = -0.507 \pm 0.006_{\text{stat}} \pm 0.002_{\text{syst}}$$

$$\Delta\Phi(J/\psi) = (-15.4 \pm 0.7_{\text{stat}} \pm 0.3_{\text{syst}})^\circ$$

$$\langle\alpha_\Sigma\rangle = -0.994 \pm 0.004_{\text{stat}} \pm 0.002_{\text{syst}}$$

$$A_{CP}^\Sigma = -0.004 \pm 0.037_{\text{stat}} \pm 0.010_{\text{syst}}$$



- Data sample of $0.5 \cdot 10^9$ ψ' events
- $5 \cdot 10^3$ events with 1% bkg

$$\alpha_{\psi'} = 0.676 \pm 0.030_{\text{stat}} \pm 0.006_{\text{syst}}$$

$$\Delta\Phi(\psi') = (21.5 \pm 0.4_{\text{stat}} \pm 0.5_{\text{syst}})^\circ$$

- SM predictions [PRD67(2003)056001]

$$A_{CP}^{\Sigma^+} \sim 3.6 \cdot 10^{-6}$$

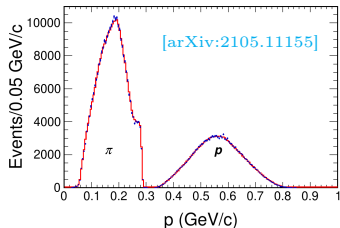
- Decays $B_1 \rightarrow B_2(\rightarrow B_3 + M_2) + M_1$
 - $\Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- + \text{c.c.}$
- Formalism exploits **polarisation**, **entanglement** and **sequential decays**

$$\mathcal{W}(\xi, \omega) = \sum_{\mu, \bar{\nu}=0}^3 \boxed{C_{\mu\bar{\nu}}} \sum_{\mu', \bar{\nu}'=0}^3 \boxed{a_{\mu\mu'}^{B_1} a_{\bar{\nu}\bar{\nu}'}^{\bar{B}_1} a_{\mu'0}^{B_2} a_{\bar{\nu}'0}^{\bar{B}_2}}$$

- 9-dimensional phase space given by 9 helicity angles
- 8 free parameters determined by unbinned MLL method

$$\omega = (\alpha_\psi, \Delta\Phi, \alpha_\Xi, \bar{\alpha}_\Xi, \phi_\Xi, \bar{\phi}_\Xi, \alpha_\Lambda, \bar{\alpha}_\Lambda)$$

not measured before



- $e^+e^- \rightarrow J/\psi \rightarrow \Xi^- \bar{\Xi}^+$,
 $\Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- + \text{c.c.}$
- Data sample of $1.3 \cdot 10^9 J/\psi$ events
- $73.2 \cdot 10^3$ events with $N_{\text{bkg}} = 199$

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^-\bar{\Xi}^+, \Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- + \text{c.c.} \quad (1)$$

- First measurement of the polarisation
- First direct determination of all $\Xi^-\bar{\Xi}^+$ decay parameters
- Independent measurement of Λ decay parameters
 - Excellent agreement with previous BESIII results

Parameter	This work	Previous result	
α_ψ	$0.586 \pm 0.012 \pm 0.010$	$0.58 \pm 0.04 \pm 0.08$	[1]
$\Delta\Phi$	$1.213 \pm 0.046 \pm 0.016 \text{ rad}$	–	
α_Ξ	$-0.376 \pm 0.007 \pm 0.003$	-0.401 ± 0.010	[2]
ϕ_Ξ	$0.011 \pm 0.019 \pm 0.009 \text{ rad}$	$-0.037 \pm 0.014 \text{ rad}$	[2]
$\bar{\alpha}_\Xi$	$0.371 \pm 0.007 \pm 0.002$	–	
$\bar{\phi}_\Xi$	$-0.021 \pm 0.019 \pm 0.007 \text{ rad}$	–	
α_Λ	$0.757 \pm 0.011 \pm 0.008$	$0.750 \pm 0.009 \pm 0.004$	[3]
$\bar{\alpha}_\Lambda$	$-0.763 \pm 0.011 \pm 0.007$	$-0.758 \pm 0.010 \pm 0.007$	[3]
$\xi_P - \xi_S$	$(1.2 \pm 3.4 \pm 0.8) \times 10^{-2} \text{ rad}$	–	
$\delta_P - \delta_S$	$(-4.0 \pm 3.3 \pm 1.7) \times 10^{-2} \text{ rad}$	$(10.2 \pm 3.9) \times 10^{-2} \text{ rad}$	[4]
A_{CP}^Ξ	$(6.0 \pm 13.4 \pm 5.6) \times 10^{-3}$	–	
$\Delta\phi_{\text{CP}}^\Xi$	$(-4.8 \pm 13.7 \pm 2.9) \times 10^{-3} \text{ rad}$	–	
A_{CP}^Λ	$(-3.7 \pm 11.7 \pm 9.0) \times 10^{-3}$	$(-6 \pm 12 \pm 7) \times 10^{-3}$	[3]
$\langle\phi_\Xi\rangle$	$0.016 \pm 0.014 \pm 0.007 \text{ rad}$		

¹[PRD93(2016)072003] ²[PTEP2020(2020)083C01] ³[Nature Phys.15(2019)631] ⁴[PRL93(2004)011802]

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^- \bar{\Xi}^+, \Xi^- \rightarrow \Lambda(\rightarrow p\pi^-)\pi^- + \text{c.c.} \quad (2)$$

[arXiv:2105.11155]

- First measurement of **weak phase difference**

- Consistent with SM prediction

$$(\xi_P - \xi_S)_{\text{SM}} = (1.8 \pm 1.5) \cdot 10^{-4} \text{ rad}$$

[PRD67(2003)056001]

- **Three independent CP tests**

Parameter	This work	Previous result	
α_ψ	$0.586 \pm 0.012 \pm 0.010$	$0.58 \pm 0.04 \pm 0.08$	[1]
$\Delta\Phi$	$1.213 \pm 0.046 \pm 0.016 \text{ rad}$	–	
α_Ξ	$-0.376 \pm 0.007 \pm 0.003$	-0.401 ± 0.010	[2]
ϕ_Ξ	$0.011 \pm 0.019 \pm 0.009 \text{ rad}$	$-0.037 \pm 0.014 \text{ rad}$	[2]
$\bar{\alpha}_\Xi$	$0.371 \pm 0.007 \pm 0.002$	–	
$\bar{\phi}_\Xi$	$-0.021 \pm 0.019 \pm 0.007 \text{ rad}$	–	
α_Λ	$0.757 \pm 0.011 \pm 0.008$	$0.750 \pm 0.009 \pm 0.004$	[3]
$\bar{\alpha}_\Lambda$	$-0.763 \pm 0.011 \pm 0.007$	$-0.758 \pm 0.010 \pm 0.007$	[3]
$\xi_P - \xi_S$	$(1.2 \pm 3.4 \pm 0.8) \times 10^{-2} \text{ rad}$	–	
$\delta_P - \delta_S$	$(-4.0 \pm 3.3 \pm 1.7) \times 10^{-2} \text{ rad}$	$(10.2 \pm 3.9) \times 10^{-2} \text{ rad}$	[4]
A_{CP}^Ξ	$(6.0 \pm 13.4 \pm 5.6) \times 10^{-3}$	–	
$\Delta\phi_{\text{CP}}^\Xi$	$(-4.8 \pm 13.7 \pm 2.9) \times 10^{-3} \text{ rad}$	–	
A_{CP}^Λ	$(-3.7 \pm 11.7 \pm 9.0) \times 10^{-3}$	$(-6 \pm 12 \pm 7) \times 10^{-3}$	[3]
$\langle\phi_\Xi\rangle$	$0.016 \pm 0.014 \pm 0.007 \text{ rad}$		

¹[PRD93(2016)072003] ²[PTEP2020(2020)083C01] ³[Nature Phys.15(2019)631] ⁴[PRL93(2004)011802]

- BESIII has performed
 - Measurements of **polarisation** and **spin correlations** in
 - * $J/\psi(\psi') \rightarrow \Lambda\bar{\Lambda}, \rightarrow \Sigma\bar{\Sigma}$
 - * $J/\psi \rightarrow \Xi\bar{\Xi}, \psi(3686) \rightarrow \Omega\bar{\Omega}$
 - Determination of **hyperon and anti-hyperon decay parameters**
 - **CP tests** comparing hyperon and anti-hyperon
 - * Separation of strong and weak decay phases \implies more **sensitive** CP tests
- **Future prospects**
 - Recently collected 10^{10} J/ψ and $3 \cdot 10^9$ ψ' events
 - * **Many interesting results** are expected
 - Good prospects for future **Super Charm-Tau Factories**
[Phys.-Usp.61(2018)405] [IPAC2018Proceedings]
 - * Planning produce more than 10^{12} J/ψ events
 - * Polarized electron beam
 - * Statistical precision will be comparable to the SM predictions

Thank you for your attention!



" I ALWAYS BACK UP EVERYTHING."

Polarisation and spin correlations $e^+e^- \rightarrow J/\psi \rightarrow \Xi^-\bar{\Xi}^+$

[arXiv:2105.11155]

