

# Top Couplings @ Beyond...

A. Onofre

University of Minho, School of Sciences, Portugal



LHC Physics

Course on Physics at the LHC, 6<sup>th</sup> April, 2021

Cofinanciado por:



# Main Topics in this Talk

- Global Fits of Data
- More on Top couplings:  
Top-Higgs Yukawa Couplings

....a change in analysis strategy  
to improve performance,  
required?

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## Why is it necessary a precise model-independent measurement of the Wtb vertex structure?

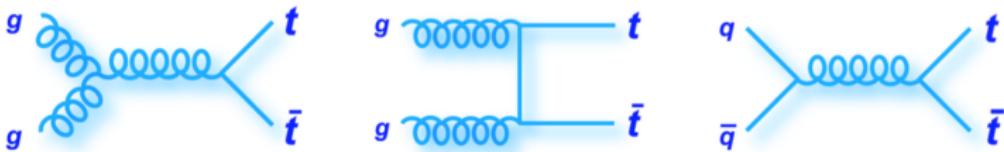
- It may reveal physics beyond the Standard Model
  - $V_{tb}$  could be different from the Standard Model value
  - Anomalous couplings may appear at the vertex
- It may help understand possible other new physics beyond the Standard Model
  - top quarks decay almost exclusively to  $t \rightarrow W^+ b$
  - understanding the structure of the Wtb vertex helps revealing possible non-standard  $t\bar{t}$  production at LHC,  $Zt\bar{t}/\gamma t\bar{t}$  couplings at ILC, etc.
  - important for  $B$  and  $K$  physics (indirect limits on anomalous couplings, see later)

The  $Wtb$  vertex must be determined by a global fit to several observables:

- Several, theoretically equivalent, observables studied for  $t\bar{t}$  production at LHC (not all explored yet @ LHC)
- Single top cross section useful (sensitive to  $V_{tb}$  and anomalous couplings)
- Indirect limits from  $b \rightarrow s\gamma$  available (not used)
- The most general CP-conserving vertex for top quarks on-shell is used
- All couplings are allowed to vary freely in TopFit to find the allowed regions for a given CL

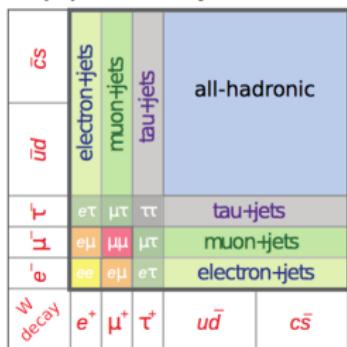
# Global Fits of Data

- Production at the LHC:

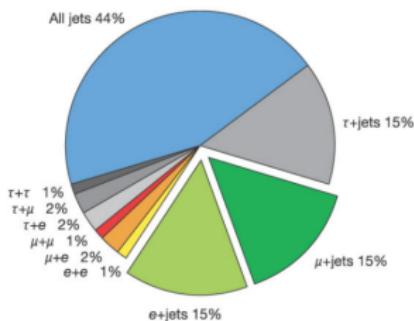


$\sigma(t\bar{t})=177.3 \pm 9.9^{+4.6}_{-6.0} \text{ pb}$  @ 7 TeV,  $\sigma(t\bar{t})=252.9 \pm 11.7^{+6.4}_{-8.6} \text{ pb}$  @ 8 TeV,  $\sigma(t\bar{t})=832^{+40}_{-46} \text{ pb}$  @ 13 TeV  
 NNLO+NNLL,  $m_t = 172.5 \text{ GeV}$  PLB **710** 612 (2012), PRL **109** 132001(2012),  
 JHEP **1212** 054(2012), JHEP **1301** 080(2013), PRL **110** 252004 (2013).

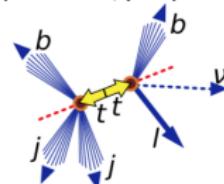
Top pair decay channels



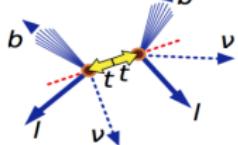
Top pair branching fractions



$\Rightarrow$  Lepton+jets ( $\sim 30\%$ ):  
 $(\ell = e^\pm, \mu^\pm)$



$\Rightarrow$  Dilepton ( $\sim 5\%$ ):  
 $(\ell = e^\pm, \mu^\pm)$



# The $Wtb$ vertex structure

## Effective $Wtb$ vertex from dim-6 operators

$$\begin{aligned}\mathcal{L} = & -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- \\ & -\frac{g}{\sqrt{2}} \bar{b} \frac{i \sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{h.c.}\end{aligned}$$

$V_L \equiv V_{tb} \sim 1$  (within SM)

$V_R, g_R, g_L \Rightarrow$  anomalous couplings

[EPJC50 (2007) 519, NPB804 (2008) 160, NPB812 (2009) 181]

## How to probe anomalous couplings in the $Wtb$ vertex?

- indirect limits from  $B$ -physics
- measurements of single top quark production: cross-section and angular distributions
- measurements of  $t\bar{t}$  production: angular distributions of top quark decays

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# B-physics constraints to $Wtb$ vertex

IFT-2/2008

## Anomalous $Wtb$ coupling effects in the weak radiative $B$ -meson decay

Bohdan Grzadkowski and Mikolaj Misiak

Institute of Theoretical Physics, University of Warsaw, PL-00-681 Warsaw, Poland and  
Theoretical Physics Division, CERN, CH-1211 Geneva 23, Switzerland

(Dated: February 7, 2008)

We study the effect of anomalous  $Wtb$  couplings on the  $\bar{B} \rightarrow X_s \gamma$  branching ratio. The considered couplings are introduced as parts of gauge-invariant dimension-six operators that are built out of the Standard Model fields only. One-loop contributions from the charged-current vertices are assumed to be of the same order as the tree-level flavour-changing neutral current ones. Bounds on the corresponding Wilson coefficients are derived.

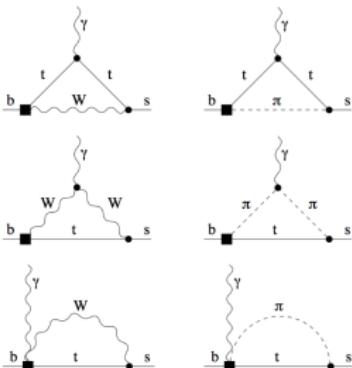


FIG. 1: Diagrams with non-SM  $b \rightarrow t$  vertices that contribute to  $f_7^{g_{L,R}}(x)$ . The pseudogoldstone boson is denoted by  $\pi$ .

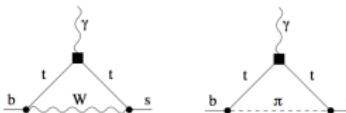


FIG. 2: Diagrams with non-SM  $t\bar{t}\gamma$  vertices that contribute to  $f_7^{g_R}(x)$ .

't Hooft gauge. The relevant Feynman diagrams with non-SM  $b \rightarrow t$  vertices are shown in Fig. 1. In addition, analogous six diagrams with non-SM  $t \rightarrow s$  vertices and two diagrams with non-SM  $t\bar{t}\gamma$  vertices (Fig. 2) occur in the case of  $f_8^{g_R}(x)$ . In the case of  $f_7^{g_{L,R}}(x)$ , there are also diagrams where the intermediate  $t$ -quark gets replaced by  $u$  or  $c$ . The functions  $f_8^{g_{L,R}}(x)$  have been found by replacing the external photon by the gluon in the diagrams like the ones in the first row of Fig. 1.

Our final results for  $f_i^{g_{L,R}}(x)$  read:

# $B$ -physics constraints to $Wtb$ vertex

$$BR(\bar{B} \rightarrow X_s \gamma) = (3.55 \pm 0.24 {}^{+0.09}_{-0.10} \pm 0.03) \times 10^{-4}$$

[hep-ex/0603003]

$$\begin{aligned} BR(B \rightarrow X_s \gamma) \times 10^4 &= (3.15 \pm 0.23) - 4.14 (V_L - V_{tb}) + 411 V_R \\ &- 53.9 g_L - 2.12 g_R - 8.03 C_7^{(p)}(\mu_0) \\ &+ \mathcal{O}\left[\left(V_L - V_{tb}, V_R, g_L, g_R, C_7^{(p)}\right)^2\right] \end{aligned}$$

$$\mathcal{O}\left[(V_L - V_{tb}, V_R, \dots)^2\right] \simeq 1.32(V_L - V_{tb})^2 - 262(V_L - V_{tb})V_R + 12970V_R^2 + \dots$$

	$V_L - V_{tb}$	$V_R$	$g_L$	$g_R$	$C_7^{(p)}(\mu_0)$
upper bound	0.04	0.0024	0.003	0.08	0.02
lower bound	-0.24	-0.0004	-0.018	-0.46	-0.12

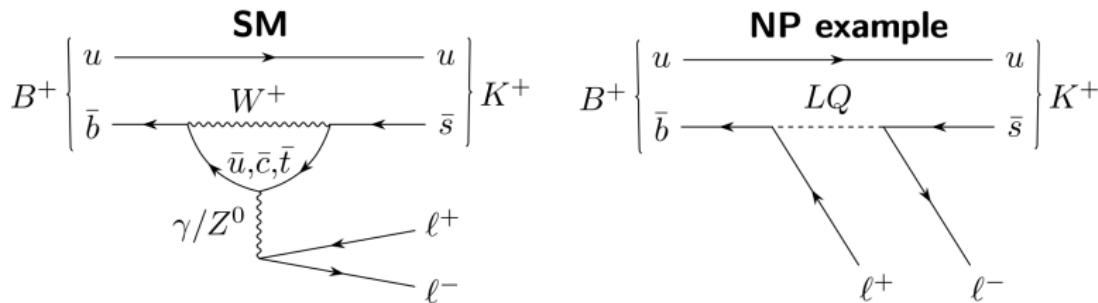
[EPJC57 (2008) 183]

## *B* Mesons Rare Decays

## $B^+ \rightarrow K^+ \ell^+ \ell^-$ and related decays

LHCb  
PHCP

- ▶ Occur through  $b \rightarrow sl^+\ell^-$  transition but in contrast to  $B_s^0 \rightarrow \ell^+\ell^-$ , contain a hadron in the final state.  
e.g  $B^+ \rightarrow K^+\ell^+\ell^-$ ,  $B^0 \rightarrow K^{*0}\ell^+\ell^-$ ,  $B_s \rightarrow \phi\mu^+\mu^-$ ,  $\Lambda_b \rightarrow \Lambda^*\ell^+\ell^-$ ...



- ▶ Offer multitude of observables complementary to  $B_s^0 \rightarrow \ell^+ \ell^-$  measurements.

# B Mesons Rare Decays

## Measurement Strategy

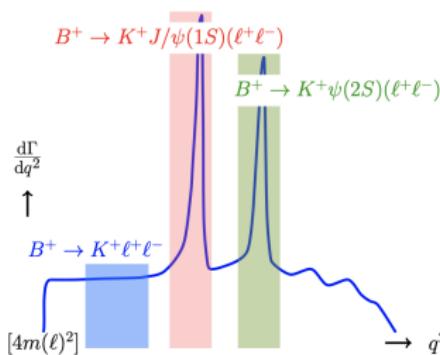


$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-))} / \frac{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(e^+ e^-))} = \frac{N_{\mu^+ \mu^-}^{\text{rare}} \varepsilon_{\mu^+ \mu^-}^{J/\psi}}{N_{\mu^+ \mu^-}^{J/\psi} \varepsilon_{\mu^+ \mu^-}^{\text{rare}}} \times \frac{N_{e^+ e^-}^{J/\psi} \varepsilon_{e^+ e^-}^{\text{rare}}}{N_{e^+ e^-}^{\text{rare}} \varepsilon_{e^+ e^-}^{J/\psi}}$$

→  $R_K$  is measured as a **double ratio** to cancel out most systematics

- Rare and  $J/\psi$  modes share identical selections apart from cut on  $q^2$
- Yields determined from a fit to the invariant mass of the final state particles
- Efficiencies computed using simulation that is calibrated with control channels in data

( $q^2 \equiv$  dilepton invariant mass squared)



[K.A.Petridis, CERN talk, March 23, 2021]

# $B$ Mesons Rare Decays

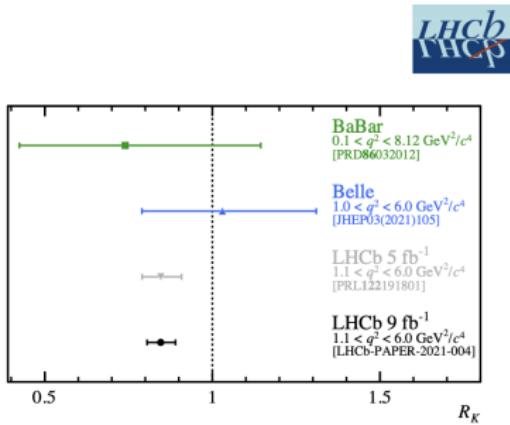
$R_K$  with full Run1 and Run2 dataset

[LHCb-PAPER-2021-004] Submitted to Nature Physics

$$R_K = 0.846^{+0.042}_{-0.039} \text{ (stat)}^{+0.013}_{-0.012} \text{ (syst)}$$

- $p$ -value under SM hypothesis: 0.0010  
→ Evidence of LFU violation at  $3.1\sigma$

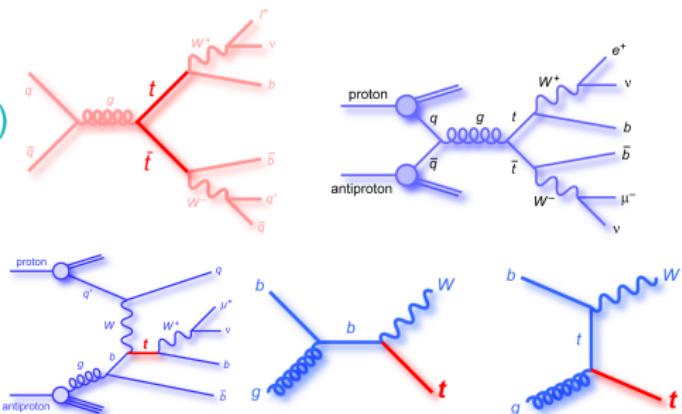
[K.A.Petridis, CERN talk, March 23, 2021]



Main objective: extend the studies already performed at the LHC on top quark Anomalous Couplings/EFT in  $t \rightarrow Wb$  decays to HL-LHC/HE-LHC

Several processes under study to probe the  $Wtb$  vertex<sup>1</sup>:

- Top quark pair production ( $t\bar{t}$ )
  - (i) semileptonic channel
  - (ii) dileptonic decays
- single top quark physics
  - (i)  $t$ -channel (single lepton)
  - (ii)  $Wt$ -channel (dileptonic decay)
- EFT/anomalous couplings studied associated to the  $Wtb$  vertex

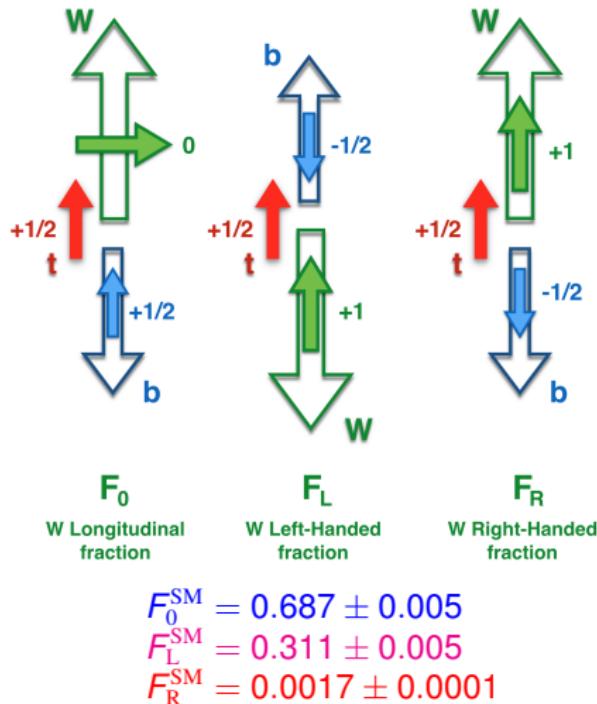


<sup>1</sup> JHEP1206(2012)088, EPJC77(2017)264, JHEP04(2017)124, JHEP04(2016)023, JHEP12(2017)017, PLB717(2012)330, PRD90(2014)112006, PLB716(2012)142, PLB756(2016)228, EPJC77(2017)531, JHEP01(2016)064, JHEP04(2017)086, JHEP01(2018)63, EPJC78(2018)186

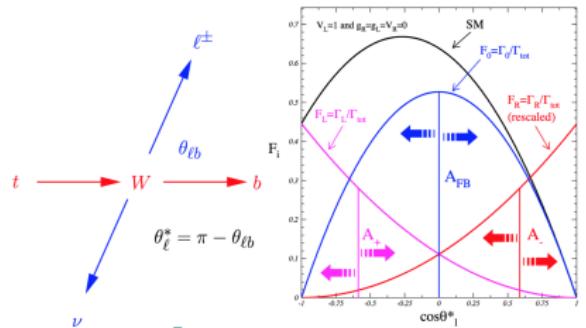
# Top quark pair production

# Top quark pair production ( $t\bar{t}$ )

☞ Observable(s): angular distribution(s)  $\cos \theta_\ell^*$  [ $F_0, F_L, F_R$ ]

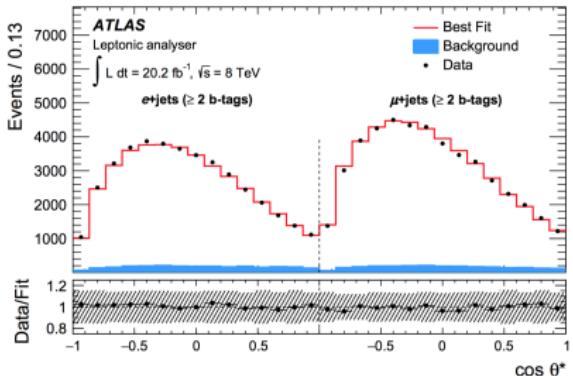


@ NNLO QCD calculation, PRD81(2010)111503  
 $(F_0 + F_L + F_R = 1)$



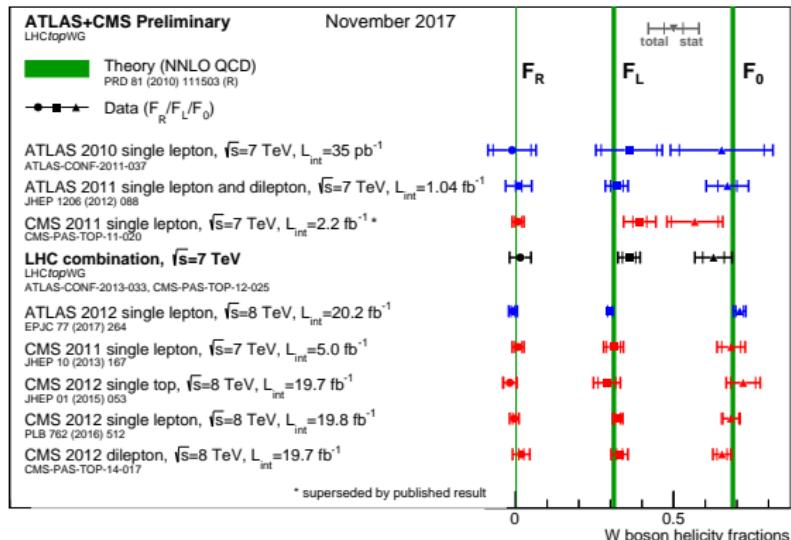
$$\frac{1}{N} \frac{dN}{d \cos \theta_\ell^*} = \frac{3}{2} \left[ F_0 \left( \frac{\sin \theta_\ell^*}{\sqrt{2}} \right)^2 + F_L \left( \frac{1 - \cos \theta_\ell^*}{2} \right)^2 + F_R \left( \frac{1 + \cos \theta_\ell^*}{2} \right)^2 \right]$$

EPJC77(2017)264



# Top quark pair production ( $t\bar{t}$ )

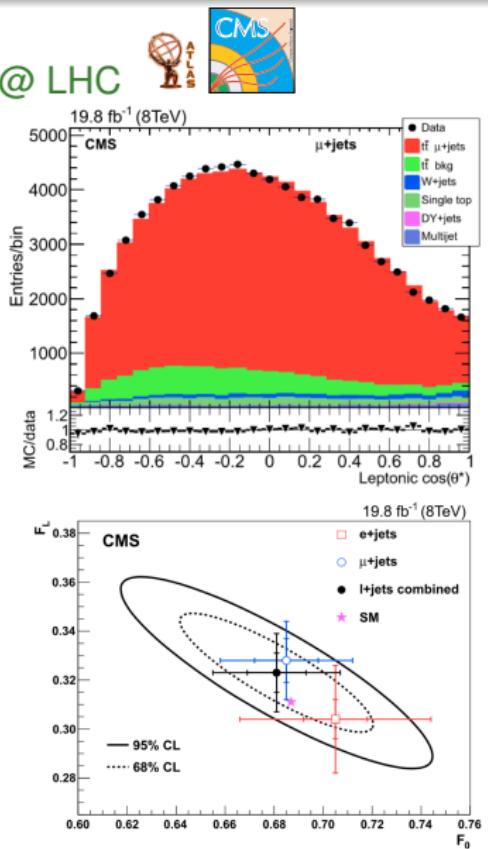
## Summary of $W$ -boson helicity meas. @ LHC



$$\Delta F_0/F_0 \sim 2.7\% \quad (3.7 \times \text{theo. unc.})$$

$$\Delta F_L/F_L \sim 5\% \quad (3.1 \times \text{theo. unc.})$$

$$F_R = -0.008 \pm 0.014$$



# Top quark pair production ( $t\bar{t}$ )

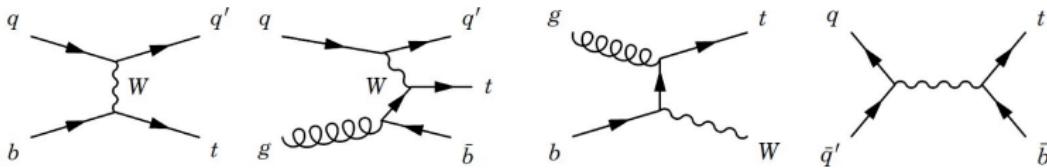
● [arXiv:hep-ph/0605190v2 18 Mar 2007]

the modulus of the  $W$  boson three-momentum in the top quark rest frame. The total top width is

$$\begin{aligned}\Gamma = & \frac{g^2 |\vec{q}|}{32\pi} \frac{m_t^2}{M_W^2} \left\{ \left[ |V_L|^2 + |V_R|^2 \right] \left( 1 + x_W^2 - 2x_b^2 - 2x_W^4 + x_W^2 x_b^2 + x_b^4 \right) \right. \\ & - 12x_W^2 x_b \operatorname{Re} V_L V_R^* + 2 \left[ |g_L|^2 + |g_R|^2 \right] \left( 1 - \frac{x_W^2}{2} - 2x_b^2 - \frac{x_W^4}{2} - \frac{x_W^2 x_b^2}{2} + x_b^4 \right) \\ & - 12x_W^2 x_b \operatorname{Re} g_L g_R^* - 6x_W \operatorname{Re} [V_L g_R^* + V_R g_L^*] \left( 1 - x_W^2 - x_b^2 \right) \\ & \left. + 6x_W x_b \operatorname{Re} [V_L g_L^* + V_R g_R^*] \left( 1 + x_W^2 - x_b^2 \right) \right\}. \quad (4)\end{aligned}$$

# Single top quark production

# Single top quark production

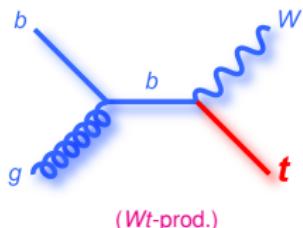
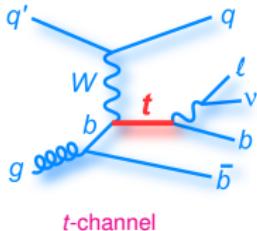


$$\sigma = \sigma_{\text{SM}} (V_L^2 + \kappa^{V_R} V_R^2 + \kappa^{V_L V_R} V_L V_R + \kappa^{g_L} g_L^2 + \kappa^{g_R} g_R^2 + \kappa^{g_L g_R} g_L g_R + \dots)$$

- the  $\kappa$  factors determine the dependence on anomalous couplings
- the  $\kappa$  factors are, in general, different for  $t$  and  $\bar{t}$  production
- the measurement of the single top production cross-section allows to obtain a measurement of  $V_L$  ( $\equiv V_{tb}$ ) and bounds on anomalous couplings

# Single top quark production

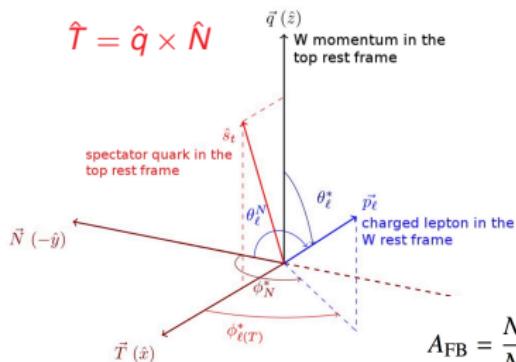
- Processes currently under study:



☞ Observables: 2D angular distributions in *t*-channel production as a function of 6 spin observables  $\langle S_{1,2,3} \rangle$ ,  $\langle T_0 \rangle$ ,  $\langle A_{1,2} \rangle$  [PRD 93 (2016) 011301]

$$\hat{N} = \hat{s}_t \times \hat{q}$$

$$\hat{T} = \hat{q} \times \hat{N}$$



1) Double-differential distribution:

$$\frac{1}{\Gamma} \frac{d\Gamma}{d(\cos \theta_\ell^*) d\phi_\ell^*} = \frac{3}{8\pi} \left\{ \frac{2}{3} + \frac{1}{\sqrt{6}} \langle T_0 \rangle (3 \cos^2 \theta_\ell^* - 1) + \langle S_3 \rangle \cos \theta_\ell^* \right. \\ \left. + \langle S_1 \rangle \cos \phi_\ell^* \sin \theta_\ell^* + \langle S_2 \rangle \sin \phi_\ell^* \sin \theta_\ell^* \right. \\ \left. - \langle A_1 \rangle \cos \phi_\ell^* \sin 2\theta_\ell^* - \langle A_2 \rangle \sin \phi_\ell^* \sin 2\theta_\ell^* \right\}.$$

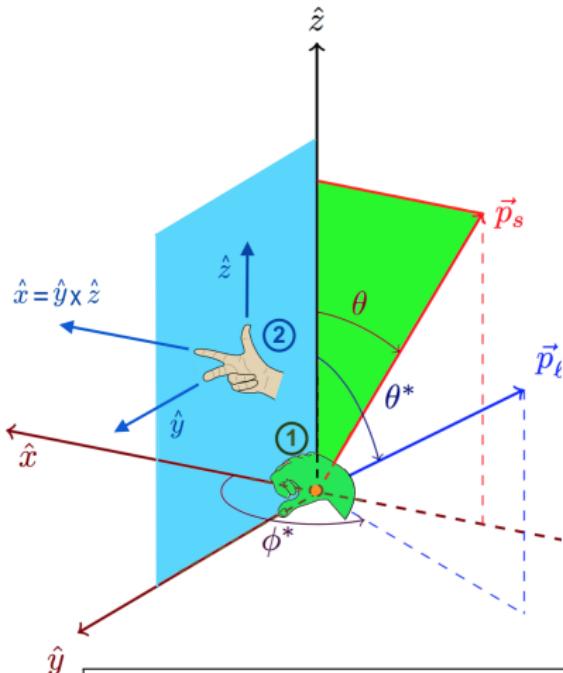
2)  $A_{FB}$  and  $A_{EC}$  Asymmetries:

$$A_{FB} = \frac{N(\cos \theta > 0) - N(\cos \theta < 0)}{N(\cos \theta > 0) + N(\cos \theta < 0)}$$

$$A_{EC} = \frac{N(|\cos \theta| > \frac{1}{2}) - N(|\cos \theta| < \frac{1}{2})}{N(|\cos \theta| > \frac{1}{2}) + N(|\cos \theta| < \frac{1}{2})}$$

# Single top quark production

- Triple-differential (3D) decay rates of polarised top quarks
  - define specific coordinate system (in  $t$  centre-of-mass):



1) System Definition (in  $t$ -system):

$$\hat{z} = \hat{p}_W^* = \vec{p}_W^*/|\vec{p}_W^*|, \quad \vec{p}_s^* = \text{spectator quark mom.}$$
$$\hat{y} = \hat{p}_s^* \times \hat{p}_W^*, \quad \hat{x} = \hat{y} \times \hat{p}_W^*$$

2) Triple-differential distribution:

$$\begin{aligned} \varrho(\theta, \theta^*, \phi^*; P) = \frac{1}{N} \frac{d^3 N}{d(\cos \theta) d\Omega^*} &= \frac{1}{8\pi} \left( \frac{3}{4} |A_{1,\frac{1}{2}}|^2 (1 + P \cos \theta)(1 + \cos \theta^*)^2 \right. \\ &+ \frac{3}{4} |A_{-1,-\frac{1}{2}}|^2 (1 - P \cos \theta)(1 - \cos \theta^*)^2 \\ &+ \frac{3}{2} \left( |A_{0,\frac{1}{2}}|^2 (1 - P \cos \theta) + |A_{0,-\frac{1}{2}}|^2 (1 + P \cos \theta) \right) \sin^2 \theta^* \\ &- \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 + \cos \theta^*) \operatorname{Re} \left[ e^{i\phi^*} A_{1,\frac{1}{2}} A_{0,\frac{1}{2}}^* \right] \\ &- \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 - \cos \theta^*) \operatorname{Re} \left[ e^{-i\phi^*} A_{-1,-\frac{1}{2}} A_{0,-\frac{1}{2}}^* \right] \Big) \\ &= \sum_{k=0}^1 \sum_{l=0}^2 \sum_{m=-k}^k a_{k,l,m} M_{k,l}^m(\theta, \theta^*, \phi^*), \end{aligned}$$

$$A_{\lambda_W, \lambda_b} = \text{helicity amplitudes} \quad M_{k,l}^m(\theta, \theta^*, \phi^*) = \sqrt{2\pi} Y_k^m(\theta, 0) Y_l^m(\theta^*, \phi^*)$$

Results Interpreted in Terms of Anomalous Couplings ( $V_R, g_L, g_R$ )

next slide

# EFT/anomalous Couplings

# Anomalous couplings/EFT parameters in global fits

## General Wtb vertex

Eur.Phys.J. C50 (2007) 519-533

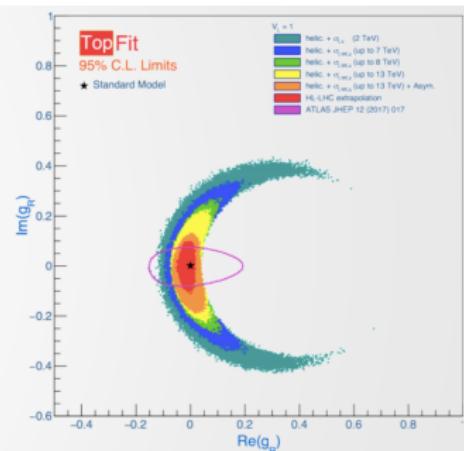
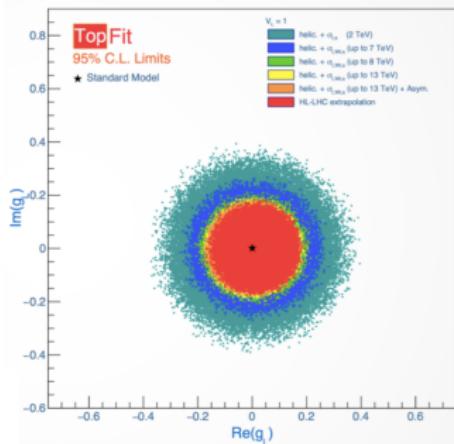
$$\mathcal{L} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i \sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^-$$

vector ( $V_R$ ) and tensor like couplings ( $g_L, g_R$ ) zero @ tree level in SM

☞ EFT parameters: anomalous couplings described by effective operators

$\mathcal{O}_{uW}, \mathcal{O}_{dW}, \mathcal{O}_{\phi q}^{(3)}$  and  $\mathcal{O}_{\phi ud}$  i.e., constraints on anomalous couplings equivalent to constraints on EFT parameters (a more integrating framework) [arXiv:1802.07237]

PRD 97 (2018) 1, 013007 (TopFit), arXiv:1811.02492



Fits  
Using:



$\sigma, W_{hel},$   
 $A_{FB}$  @  
7,8,13 TeV

## [Improvements from Theory]

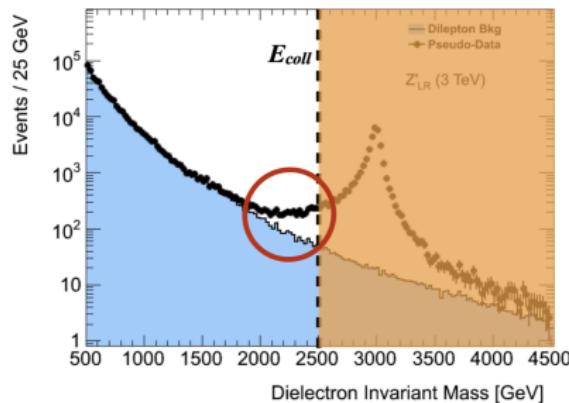
☞ Effective Field Theory approach (EFT):

$$\mathcal{L}_{EFT} = \mathcal{L}_{SM} + \sum_i c_i \frac{\mathcal{O}_i}{\Lambda^2} + \dots \quad (*)$$

EFT

SM  
Precision measurements

BSM  
Explicit Models



# Constraints from Global Fits

## [Improvements from Theory]

### ☞ Effective Field Theory approach (EFT):

- Dimension 6 Operators:

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi}$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi) (\bar{l}_\nu e_\tau \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi) (\bar{q}_\mu u_\tau \tilde{\varphi})$
$Q_W$	$e^{IJK} W_{I\nu}^{J\mu} W_{\mu}^{K\rho} W_{\rho}^{I\nu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^*$ $(\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi) (\bar{q}_\mu d_\tau \varphi)$
$Q_{\tilde{W}}$	$e^{IJK} \tilde{W}_{I\nu}^{J\mu} W_{\mu}^{K\rho} W_{\rho}^{I\nu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_\nu \sigma^{\mu\nu} e_\tau)^T \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{l}_\nu \gamma^\mu l_\tau)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_\nu \sigma^{\mu\nu} e_\tau) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{l}_\nu \tau^I \gamma^\mu l_\tau)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{eG}$	$(\bar{q}_\mu \sigma^{\mu\nu} A_{\nu\tau}) \varphi G_{\mu\nu}^I$	$Q_{\varphi e}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{e}_\tau \gamma^\mu e_\tau)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_\mu \sigma^{\mu\nu} u_\tau) \varphi W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{q}_\tau \gamma^\mu q_\tau)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_\mu \sigma^{\mu\nu} u_\tau) \bar{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu^I \varphi) (\bar{q}_\tau \tau^I \gamma^\mu q_\tau)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_\mu \sigma^{\mu\nu} T^A d_\tau) \varphi G_{\mu\nu}^A$	$Q_{\varphi d}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{d}_\tau \gamma^\mu u_\tau)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_\mu \sigma^{\mu\nu} d_\tau)^T \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overset{\leftrightarrow}{D}_\mu \varphi) (\bar{d}_\tau \gamma^\mu d_\tau)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_\mu \sigma^{\mu\nu} d_\tau) \varphi B_{\mu\nu}$	$Q_{\varphi d}$	$i(\bar{q}_\mu \partial_\nu \varphi) (\bar{d}_\tau \gamma^\mu d_\tau)$

$(LL)(LL)$		$(RR)(RR)$		$(LL)(RR)$	
$Q_{ll}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{l}_\nu \gamma^\mu l_\tau)$	$Q_{ee}$	$(\bar{e}_\mu \gamma_\mu e_\tau) (\bar{e}_\nu \gamma^\mu e_\tau)$	$Q_{le}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{e}_\nu \gamma^\mu e_\tau)$
$Q_{\varphi l}^{(1)}$	$(\bar{q}_\mu \gamma_\mu q_\tau) (\bar{q}_\tau \gamma^\mu q_\tau)$	$Q_{uu}$	$(\bar{u}_\mu \gamma_\mu u_\tau) (\bar{u}_\nu \gamma^\mu u_\tau)$	$Q_{lu}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{u}_\nu \gamma^\mu u_\tau)$
$Q_{\varphi l}^{(3)}$	$(\bar{q}_\mu \gamma_\mu \tau^I q_\tau) (\bar{q}_\tau \gamma^\mu \tau^I q_\tau)$	$Q_{dd}$	$(\bar{d}_\mu \gamma_\mu d_\tau) (\bar{d}_\nu \gamma^\mu d_\tau)$	$Q_{ld}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{d}_\nu \gamma^\mu d_\tau)$
$Q_{lq}^{(1)}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{q}_\nu \gamma^\mu q_\tau)$	$Q_{eu}$	$(\bar{e}_\mu \gamma_\mu e_\tau) (\bar{u}_\nu \gamma^\mu u_\tau)$	$Q_{qe}$	$(\bar{q}_\mu \gamma_\mu q_\tau) (\bar{e}_\nu \gamma^\mu e_\tau)$
$Q_{lq}^{(3)}$	$(\bar{l}_\mu \gamma_\mu l_\tau) (\bar{q}_\nu \gamma^\mu \tau^I q_\tau)$	$Q_{ed}$	$(\bar{e}_\mu \gamma_\mu e_\tau) (\bar{d}_\nu \gamma^\mu d_\tau)$	$Q_{qd}$	$(\bar{q}_\mu \gamma_\mu q_\tau) (\bar{d}_\nu \gamma^\mu d_\tau)$
$(LR)(RL)$ and $(LR)(LR)$		B-violating			
$Q_{lqqg}$	$(\bar{l}_\mu^I e_\tau) (\bar{d}_\nu^I q_\tau^I)$	$Q_{dqg}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \left[ (d_p^\alpha)^T C u_r^k \right] \left[ (q_s^\beta)^T C l_r^k \right]$		
$Q_{\varphi qg}^{(1)}$	$(\bar{q}_\mu^I u_\nu) c_{jk} (q_\tau^I d_\tau)$	$Q_{qgg}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \left[ (q_\mu^\alpha)^T C q_\nu^k \right] \left[ (u_\tau^\beta)^T C e_\tau \right]$		
$Q_{\varphi qg}^{(8)}$	$(\bar{q}_\mu^I T^A u_\nu) c_{jk} (q_\tau^I d_\tau^A)$	$Q_{qgg}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} \left[ (q_\mu^\alpha)^T C q_\nu^k \right] \left[ (q_\tau^m)^T C l_\tau^k \right]$		
$Q_{lqqg}^{(1)}$	$(\bar{l}_\mu^I e_\tau) c_{jk} (q_\tau^I u_\tau)$	$Q_{qgg}^{(2)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I e_\tau)_{jk} (\tau^I e_\tau)_{mn} \left[ (q_\mu^\alpha)^T C q_\nu^k \right] \left[ (q_\tau^m)^T C d_\tau^k \right]$		
$Q_{lqqg}^{(3)}$	$(\bar{L}_\mu^I \sigma_{\mu\nu} e_\tau) c_{jk} (q_\tau^I \sigma^{\mu\nu} u_\tau)$	$Q_{dus}$	$\varepsilon^{\alpha\beta\gamma} \left[ (d_p^\alpha)^T C u_r^k \right] \left[ (u_\tau^\beta)^T C e_\tau \right]$		

- Buchmuller, Wyler Nucl.Phys. **B268** (1986) 621-653,  
Grzadkowski et al arxiv:1008.4884

## [Improvements from Theory]

## ☞ Effective Field Theory approach (EFT):

- Example of top quark operators:

$$O_{\varphi Q}^{(3)} = i \frac{1}{2} y_t^2 \left( \varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi \right) (\bar{Q} \gamma^\mu \tau^I Q)$$

$$O_{\varphi Q}^{(1)} = i \frac{1}{2} y_t^2 \left( \varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{Q} \gamma^\mu Q)$$

$$O_{\varphi t} = i \frac{1}{2} y_t^2 \left( \varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{t} \gamma^\mu t)$$

$$O_{tW} = y_t g_w (\bar{Q} \sigma^{\mu\nu} \tau^I t) \tilde{\varphi} W_{\mu\nu}^I$$

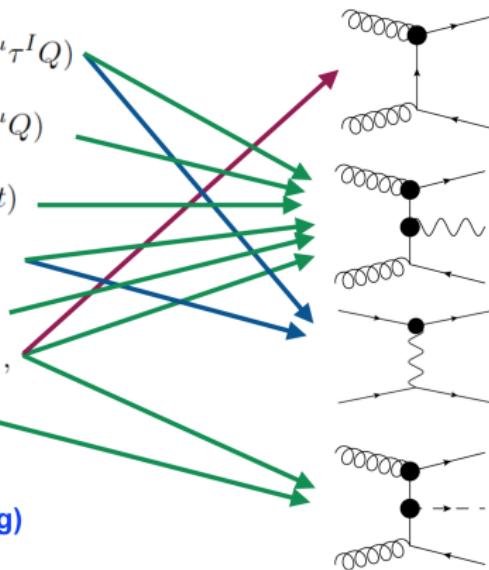
$$O_{tB} = y_t g_Y (\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu}$$

$$O_{tG} = y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\varphi} G_{\mu\nu}^A,$$

$$O_{t\phi} = y_t^3 (\phi^\dagger \phi) (\bar{Q} t) \tilde{\phi}$$

+ Four-Fermion Operators

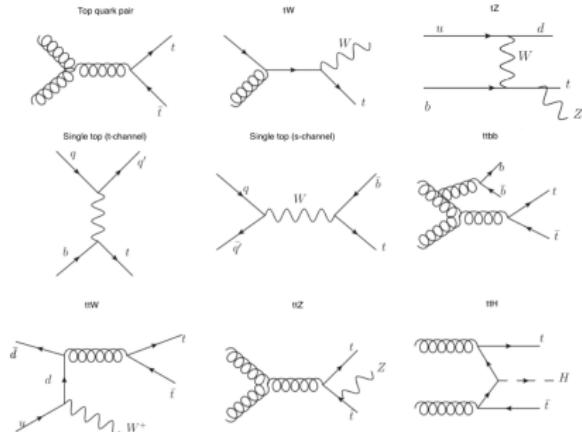
+ non-top operators (mixing)



# Constraints from Global Fits

## [Improvements from Theory]

### Towards a Global SMEFT Fit:



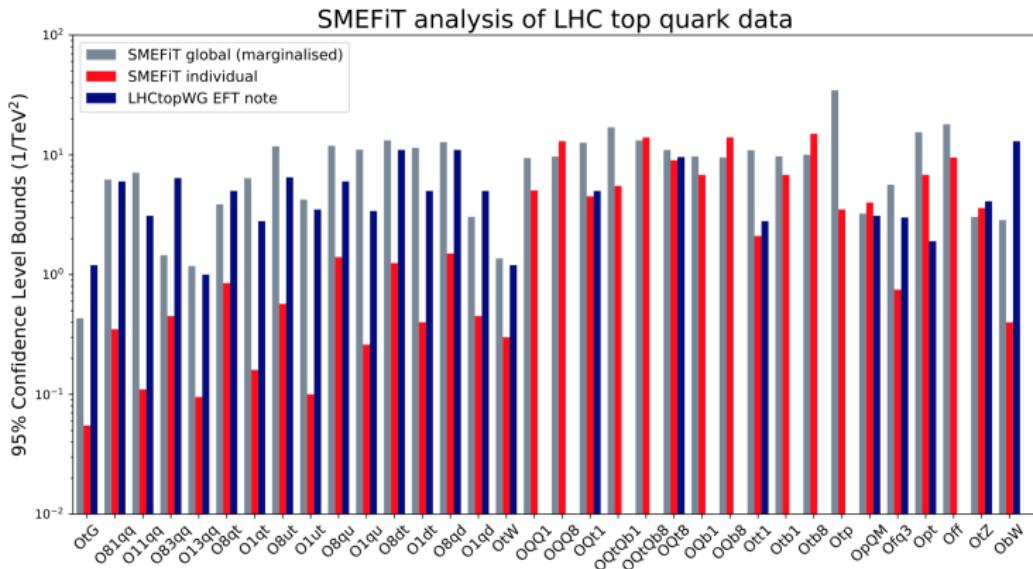
Notation	Sensitivity at $\mathcal{O}(\Lambda^{-2})$ ( $\mathcal{O}(\Lambda^{-4})$ )							
	$t\bar{t}$	single-top	$tW$	$tZ$	$t\bar{t}W$	$t\bar{t}Z$	$t\bar{t}H$	$t\bar{t}t\bar{t}$
0QQ1							✓	✓
0QQ8							✓	✓
0Qt1							✓	✓
0Qt8							✓	✓
0Qb1							✓	✓
0Qb8							✓	✓
0tt1							✓	
0tb1								✓
0tb8								✓
0QtQb1							(✓)	
0QtQb8							(✓)	
081qq	✓				✓	✓	✓	✓
011qq	[✓]				[✓] [✓]	[✓]	✓	✓
083qq	✓	[✓]		[✓]	✓	✓	✓	✓
013qq	[✓]	✓		[✓]	[✓]	[✓]	✓	✓
08qt	✓				✓	✓	✓	✓
01qt	[✓]				[✓] [✓]	[✓]	✓	✓
08bt	✓					✓	✓	✓
01ut	[✓]					[✓] [✓]	✓	✓
08qu	✓					✓	✓	✓
01qu	[✓]					[✓] [✓]	✓	✓
08dt	✓					✓	✓	✓
01dt	[✓]					[✓] [✓]	✓	✓
08qd	✓					✓	✓	✓
01qd	[✓]					[✓] [✓]	✓	✓
0tG	✓			✓		✓	✓	✓
0tW		✓	✓	✓				
0bW	(✓)	(✓)	(✓)	(✓)				
0tZ				✓				
0ff	(✓)	(✓)	(✓)					
0fq3	✓		✓	✓				
0pQM					✓			
Opt					✓	✓		
Otp							✓	

- Maltoni et al., arXiv:1901.05965

- 34 d.o.f.,  $\geq 100$  observables

## [Improvements from Theory]

## 👉 Towards a Global SMEFT Fit: Results

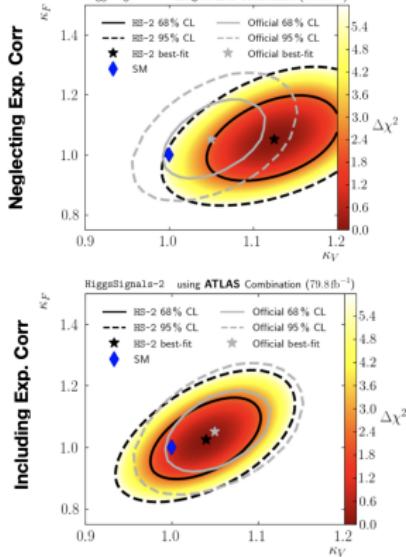


- Maltoni et al., arXiv:1901.05965 [LHCTopWG EFT note, arXiv:1802.07237]

## Simplified Likelihoods

- On the (practical) importance of correlations:
- ✓ Example: Interpreting ATLAS Run 2 Higgs STXS in terms of SM coupling modifiers

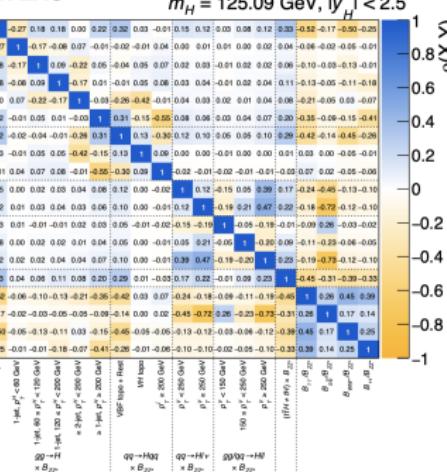
P. Bechtle et al., Eur. Phys. J.C 81 (2021) 2, 145 [arXiv:2012.09197]



ATLAS coll., Phys. Rev. D 101 (2020) 012002 [arXiv:1909.02845]

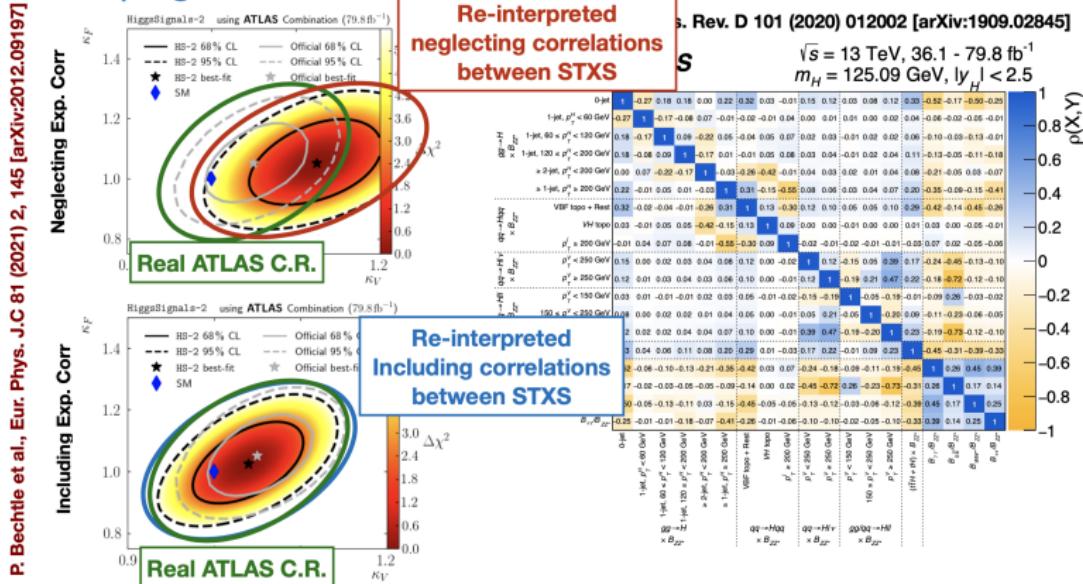
ATLAS

$\sqrt{s} = 13 \text{ TeV}, 36.1 - 79.8 \text{ fb}^{-1}$   
 $m_H = 125.09 \text{ GeV}, |y|, |l| < 2.5$



## Simplified Likelihoods

- On the (practical) importance of correlations:
- ✓ Example: Interpreting ATLAS Run 2 Higgs STXS in terms of SM coupling modifiers



# Main Topics in this Talk

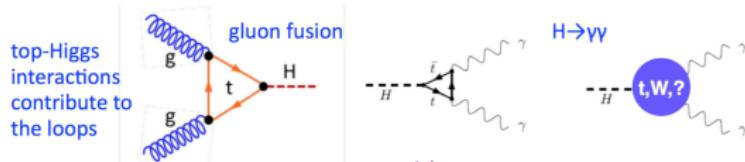
- Global Fits of Data
- More on Top couplings:  
Top-Higgs Yukawa Couplings

....a change in analysis strategy  
to improve performance,  
required?

# Top-Higgs Yukawa Couplings

☞ all about top quark-Higgs Couplings!

- the top quark has the biggest coupling to the Higgs SM boson ( $Y_t \sim 1.$ )
- precision measurements of top quark Yukawa couplings are really important
- .....as well as deviations !!!
- need also to understand the nature of the coupling ( $h = H, A$ )
- indirect constraints are important (involve several contributions)



☞ probing CP-even( $a$ ) -odd( $d$ ) nature of couplings in  $t\bar{t}H$ ,

$$L_{h\bar{t}\bar{t}} \sim [k_t + i\tilde{k}_t\gamma_5] \sim [k\cos(\alpha) + ik\sin(\alpha)\gamma_5]$$

PRL 76, 24 (1996)

J.F.Gunion, Xiao-Gang He

$$a_1, a_2, b_1, b_2, b_3 \dots b_4 = \frac{p_t^z p_{\bar{t}}^z}{|\vec{p}_t| |\vec{p}_{\bar{t}}|}$$

$$\cos(\Delta\theta^{lh}(\ell^+, \ell^-)) = \frac{(\vec{p}_h \times \vec{p}_{\ell^+}) \cdot (\vec{p}_h \times \vec{p}_{\ell^-})}{|\vec{p}_h \times \vec{p}_{\ell^+}| |\vec{p}_h \times \vec{p}_{\ell^-}|}$$

- need to understand  $t\bar{t}H$  production and decay

arXiv:1611.00049v2, A.Broggio,A.Ferroglia,B.D.Pecjak,L.L.Yang

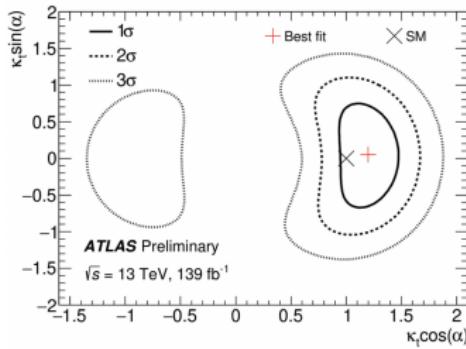
# Constraints from Global Fits

Great first episode - first appearance of constraints on the top CPV angle!

$$pp \rightarrow (h \rightarrow \gamma\gamma)\bar{t}t$$

$$\mathcal{L}_{\bar{t}t h}^{CPV} = -\frac{y_f}{\sqrt{2}} \bar{t}(\kappa_t + i\tilde{\kappa}_t \gamma_5) t h$$

All measurements are consistent with the SM expectations, and the possibility of a pure CP-odd coupling between the Higgs boson and top quark is severely constrained. A pure CP-odd coupling is excluded at  $3.9\sigma$ , and  $|\alpha| > 43^\circ$  is excluded at 95% CL.

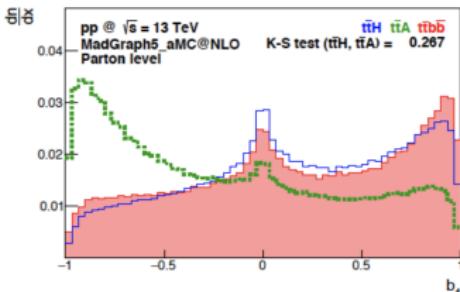


$$\kappa_t = \kappa \cos \alpha$$

$$\tilde{\kappa}_t = \kappa \sin \alpha$$

# Constraints from Global Fits

The spin averaged cross section of  $t\bar{t}$  production has terms proportional to  $a^2+b^2$  and to  $a^2-b^2$ . Terms  $a^2-b^2$  are proportional to the top quark mass. There are many operators that can distinguish  $CP$ -even and  $CP$ -odd parts.



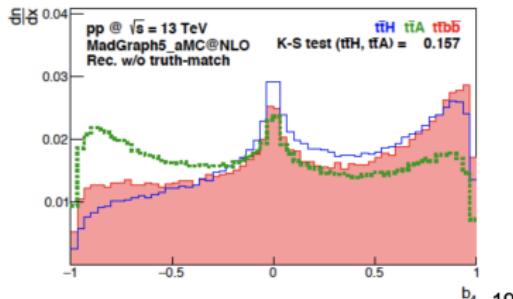
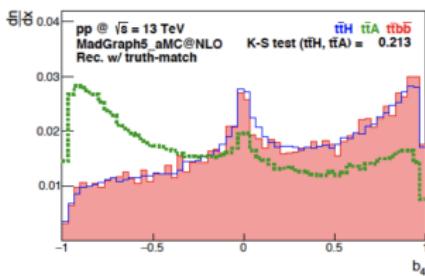
$$b_4 = \frac{p_t^z p_{\bar{t}}^z}{p_t p_{\bar{t}}}$$

Like a good port wine!

GUNION, HE, PRL77 (1996) 5172

BOUDJEMA, GODBOLE, GUADAGNOLI, MOHAN,  
PHYS.REV.D 92 (2015) 1, 015019

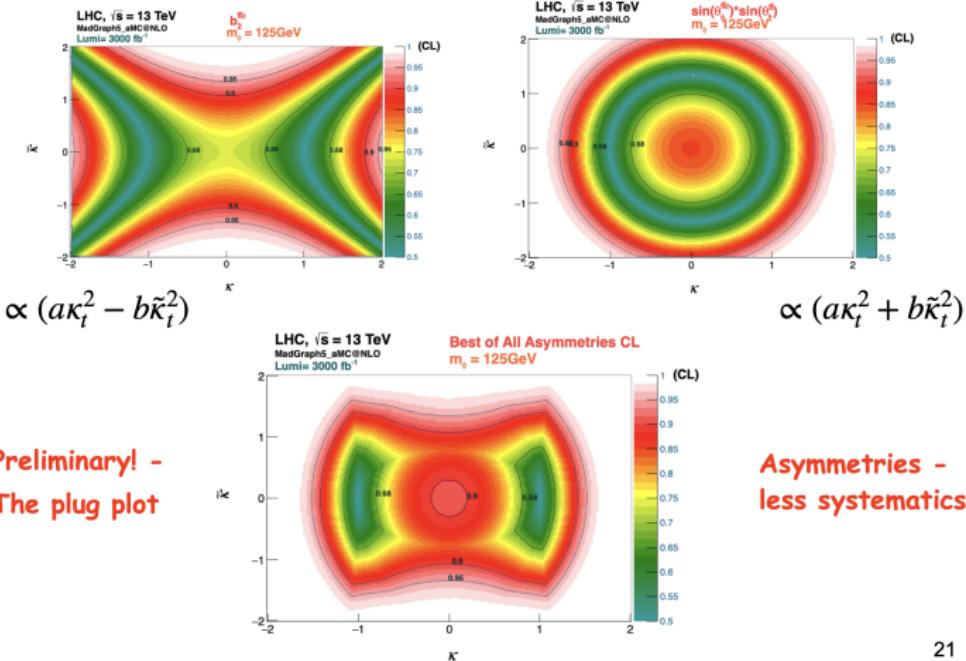
AMOR DOS SANTOS EAL PRD96 (2017) 013004



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# Constraints from Global Fits

We are testing several variables, combining them, to improve the bounds



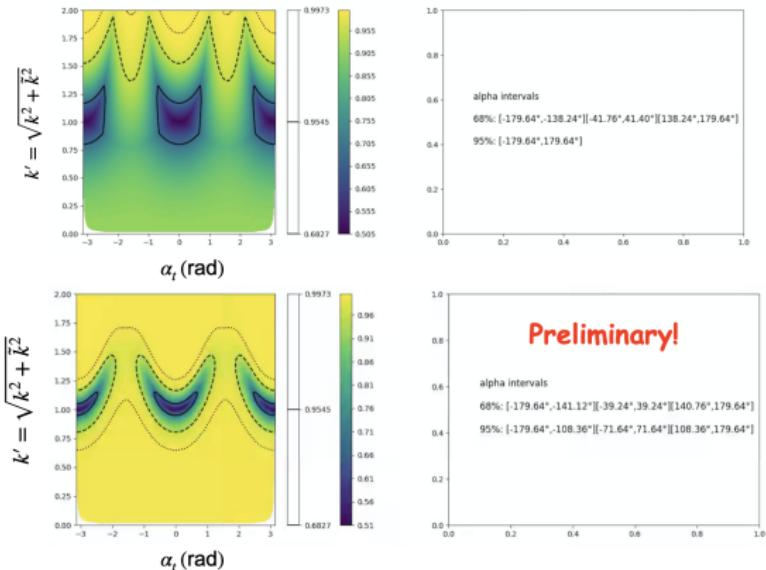
AZEVEDO, CAPUCHA, GOUVEIA, ONOFRE, RS, WORK IN PROGRESS

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Rui Santos @ HPNP Special Edition 2021, Japan

# Constraints from Global Fits

AZEVEDO, CAPUCHA, GOUVEIA, ONOFRE, RS, WORK IN PROGRESS



More shapes?

ELLIS, HWANG, SAKURAI, TAKEUCHI, JHEP 04 (2014) 004

MILEO, KIERS, SZYNKMAN, CRANE, GEGNER, JHEP 07 (2016) 056

$$\sigma_{\bar{t}t\phi} = \kappa^2 \sigma_{\bar{t}t h} + \tilde{\kappa}^2 \sigma_{\bar{t}t A}$$
$$d\sigma(gg \rightarrow t(n_t)\bar{t}(n_t)H) = \kappa_t^2 f_1(p_i \cdot p_j) + \tilde{\kappa}_t^2 f_2(p_i \cdot p_j) + \kappa_t \tilde{\kappa}_t \sum_{l=1}^{15} g_l(p_i \cdot p_j) \epsilon_l$$

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Rui Santos @ HPNP Special Edition 2021, Japan

## Global Fits to Data (up to the HL-LHC):

- 1) global analysis approach
- 2) full kinematical reconstruction
- 3) angular distributions identified in several signal regions
- 4) fit the Standard Model and extract EFT wilson coefficients
- 5) need to go global !!!

## Top-Higgs Yukawa Couplings (contribution to the HL-LHC):

- 1) many new angular observables available
- 2) sensitivity of the semileptonic final state better (factor 5) than dileptonic
- 3) combination allow probing top quark Yukawa coupling in the fermionic sector