

# Electric Dipole Moments and Fundamental Symmetries

P. Fierlinger

# Content

**Focus: European efforts & items not covered later today**

## EDM searches

- Atoms / molecules
- Neutron EDM future
- Muon EDM

## Low-energy precision experiments

- Gravity resonance
- Antihydrogen
- nnbar
- Neutron beta decay

# Worldwide EDM activities map

Neutrons: (~ 200 ppl.)

- Beam EDM @ Bern
- LANL nEDM @ LANL
- nEDM @ PSI
- nEDM @ SNS
- PanEDM @ ILL
- PNPI/FTI/ILL @ ILL
- TUCAN @ TRIUMF

Storage rings: (~ 400 ppl.)

- CPEDM/JEDI
- muEDM @ PSI
- g-2 @ FNAL
- g-2 @ JPARC

Atoms: (~ 60 ppl.)

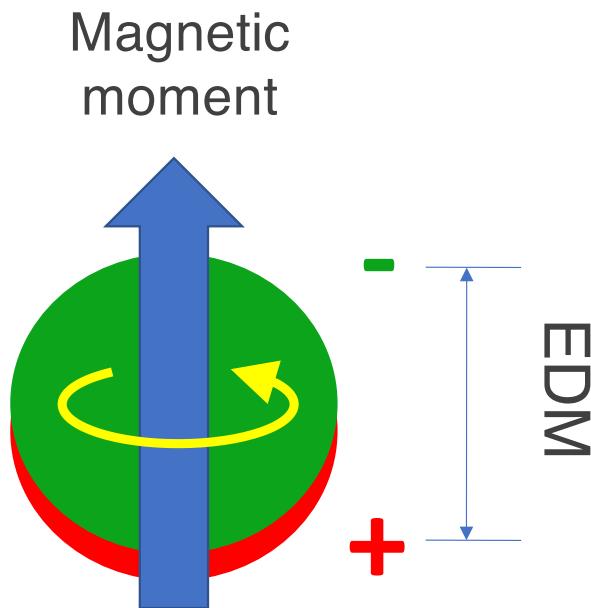
- Cs @ Penn State
- Fr @ Riken
- Hg @ Bonn
- Hg @ Seattle
- Ra @ Argonne
- Xe @ Heidelberg
- Xe @ PTB
- Xe @ Riken



Molecules: (~ 55 ppl.)

- BaF ( $\text{EDM}^3$ ) @ Toronto
- BaF (NLeEDM) @ Groningen/Nikhef
- HfF+ @ JILA
- ThO (ACME) @ Yale
- YBF @ Imperial

# Physics reach of EDM searches

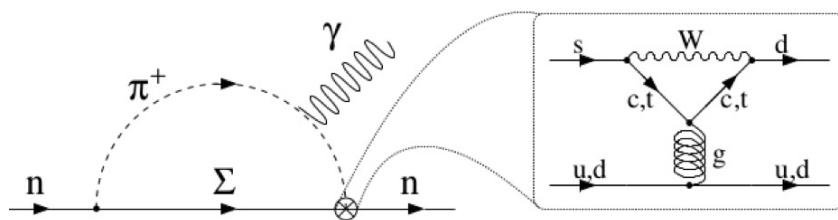


$$H = -\mu \mathbf{B} \cdot \frac{\mathbf{S}}{S} - d \mathbf{E} \cdot \frac{\mathbf{S}}{S}$$

- An EDM violates P, T symmetry  
Purcell and Ramsey, PR78(1950)807
  - CPT: CP violation  $\sim$  T violation
  - Baryon asymmetry
- 
- Among the most precisely measured quantities:  
 $d_{\text{neutron}} < 1.8 \cdot 10^{-26} \text{ ecm}$  ( $10^{-22} \text{ eV}$ )
  - Non-zero meas. = new physics!
  - More general than flavor physics experiments

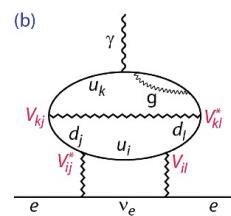
# EDM and the SM

## CP violation from CKM



Neutron EDM  $d_n \approx 10^{-32}$  ecm

$d_{\text{electron}} < 10^{-38}$  ecm...



## Strong Interaction

CP-odd term:

$$L_\theta = \bar{\theta} \frac{\alpha_s}{8\pi} G \tilde{G}$$

$$d_n(\bar{\theta}) \sim \bar{\theta} \frac{e}{m_n} \frac{m_*}{\Lambda_{QCD}} \sim 6 \cdot 10^{-17} \bar{\theta} e \cdot \text{cm}$$

$$\bar{\theta} < 10^{-10}$$

Strong CP problem, Axions

# Physics reach of EDM searches

## Fundamental theory

CKM,  $\theta$ , SUSY, Multi Higgs, LR-symmetry

## Wilson coefficients (13)

$$\mathcal{L}_{CPV}^{\text{eff}} = \sum_{k,d} \alpha_k^{(d)} \left(\frac{1}{\Lambda}\right)^{d-4} \mathcal{O}_k^{(d)}$$

## Low energy parameters

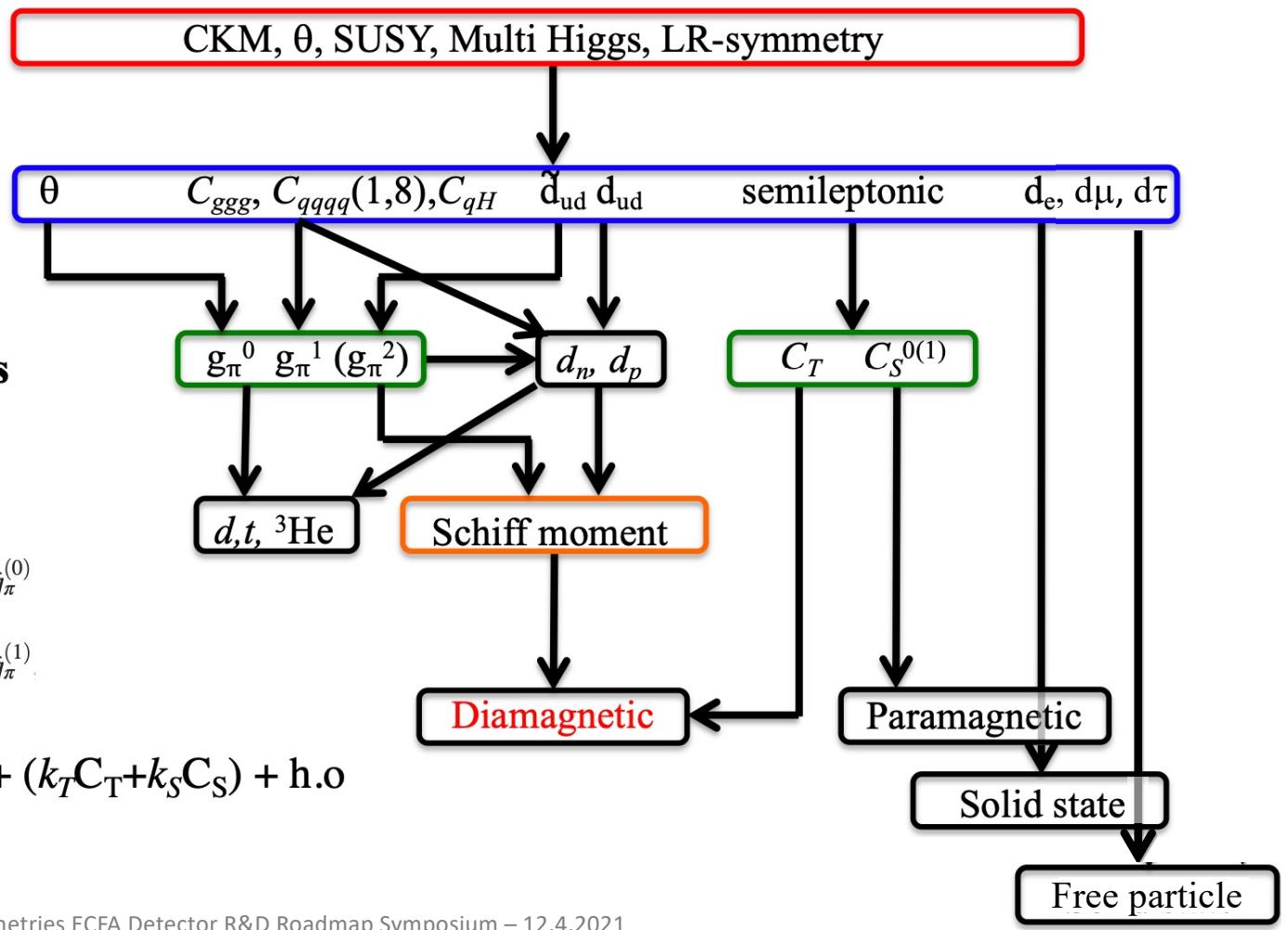
$$\bar{g}_{CP}^0 \approx 0.027 \theta_{QCD}$$

## Nucleus level

$$S = s_N \bar{d}_N^{sr} + \left[ \frac{m_N g_A}{F_\pi} a_0 + s_N \alpha_{n\bar{g}_\pi^{(0)}} \right] \bar{g}_\pi^{(0)} \\ + \left[ \frac{m_N g_A}{F_\pi} a_1 + s_N \alpha_{n\bar{g}_\pi^{(1)}} \right] \bar{g}_\pi^{(1)}$$

## Atom/molecule level

$$d_A = \eta_e d_e + \kappa_S S(\theta_{QCD}, g_\pi) + (k_T C_T + k_S C_S) + \text{h.o}$$



# Experiments are complementary

- Paramagnetic atoms

$$d_{para} = \eta_{de} d_e + k_{C_S} \bar{C}_S$$

- Polar molecules

$$\Delta\omega_{para}^{PT} = \frac{-d_e E_{eff}}{\hbar} + k_{C_S}^{\omega} \bar{C}_S$$

- Diamagnetic atoms

$$d_{dia} = \kappa_S S(\bar{g}_{\pi}^{0,1}) + k_{C_T} C_T + \dots$$

- Nucleons

$$d_{n,p} = d_{n,p}^{lr}(\bar{g}_{\pi}^{0,1}) + d_{n,p}^{sr}(\tilde{d}_{u,d}, d_{u,d})$$

- Fundamental fermions

$$d_e, d_{\mu}, (d_{\tau})$$

...Higher orders (199-Hg!) :

$$d_A = (k_T C_T + k_S C_S) + \eta_e d_e + \kappa_S S + \text{h.o. (MQM)}$$

$$d_i = \sum_i \alpha_{ij} C_j$$



e and  $\mu$  EDM

Nuclear-spin-dependent  
e-N coupling  $C_T$ ,

Nuclear-spin independent  
couplings  $C_S^0$

Intrinsic quark EDMs  
and chromo EDMs

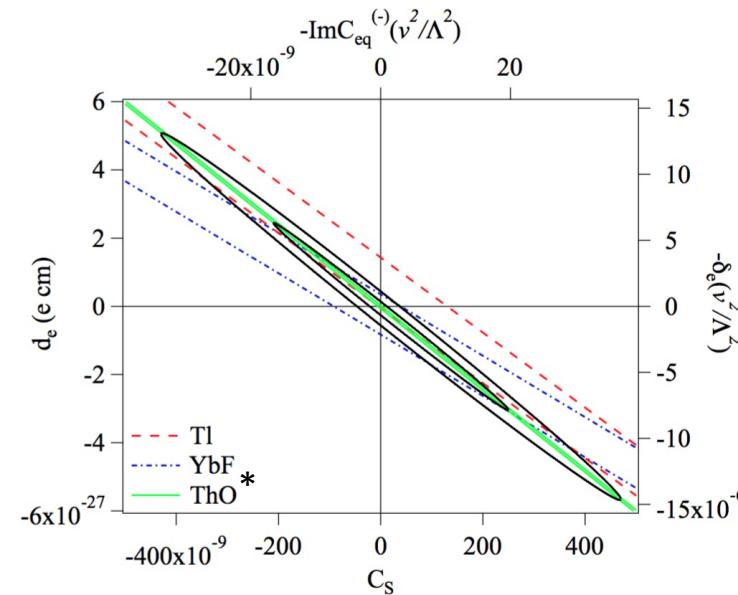
Meson-nucleon couplings  $g_{\pi}^{0,1,(2)}$

# Joint analysis

## Measured limits (note: ‘sole-source’ analysis)

	Result	95% u.l.	ref.
Paramagnetic systems			
Xe <sup>m</sup>	$d_A = (0.7 \pm 1.4) \times 10^{-22}$	$3.1 \times 10^{-22}$ e cm	a
Cs	$d_A = (-1.8 \pm 6.9) \times 10^{-24}$ $d_e = (-1.5 \pm 5.7) \times 10^{-26}$ $C_S = (2.5 \pm 9.8) \times 10^{-6}$ $Q_m = (3 \pm 13) \times 10^{-8}$	$1.4 \times 10^{-23}$ e cm $1.2 \times 10^{-25}$ e cm $2 \times 10^{-5}$ $2.6 \times 10^{-7} \mu_N R_{Cs}$	b
Tl	$d_A = (-4.0 \pm 4.3) \times 10^{-25}$ $d_e = (-6.9 \pm 7.4) \times 10^{-28}$	$1.1 \times 10^{-24}$ e cm $1.9 \times 10^{-27}$ e cm	c
YbF	$d_e = (-2.4 \pm 5.9) \times 10^{-28}$	$1.2 \times 10^{-27}$ e cm	d
ThO	$d_e = (-2.1 \pm 4.5) \times 10^{-29}$ $C_S = (-1.3 \pm 3.0) \times 10^{-9}$	$9.7 \times 10^{-29}$ e cm $6.4 \times 10^{-9}$	e
HfF <sup>+</sup>	$d_e = (0.9 \pm 7.9) \times 10^{-29}$	$1.6 \times 10^{-28}$ e cm	f
Diamagnetic systems			
<sup>199</sup> Hg	$d_A = (2.2 \pm 3.1) \times 10^{-30}$	$7.4 \times 10^{-30}$ e cm	g
<sup>129</sup> Xe	$d_A = (0.7 \pm 3.3) \times 10^{-27}$	$6.6 \times 10^{-27}$ e cm	h
<sup>225</sup> Ra	$d_A = (4 \pm 6) \times 10^{-24}$	$1.4 \times 10^{-23}$ e cm	i
TlF	$d = (-1.7 \pm 2.9) \times 10^{-23}$	$6.5 \times 10^{-23}$ e cm	j
n	$d_n = (-0.21 \pm 1.82) \times 10^{-26}$	$3.6 \times 10^{-26}$ e cm	k
Particle systems			
$\mu$	$d_\mu = (0.0 \pm 0.9) \times 10^{-19}$	$1.8 \times 10^{-19}$ e cm	l
$\tau$	$Re(d_\tau) = (1.15 \pm 1.70) \times 10^{-17}$	$3.9 \times 10^{-17}$ e cm	m
$\Lambda$	$d_\Lambda = (-3.0 \pm 7.4) \times 10^{-17}$	$1.6 \times 10^{-16}$ e cm	n

Illustration: parameters are not independent:  
e.g.  $d_e$  as function of  $C_S$



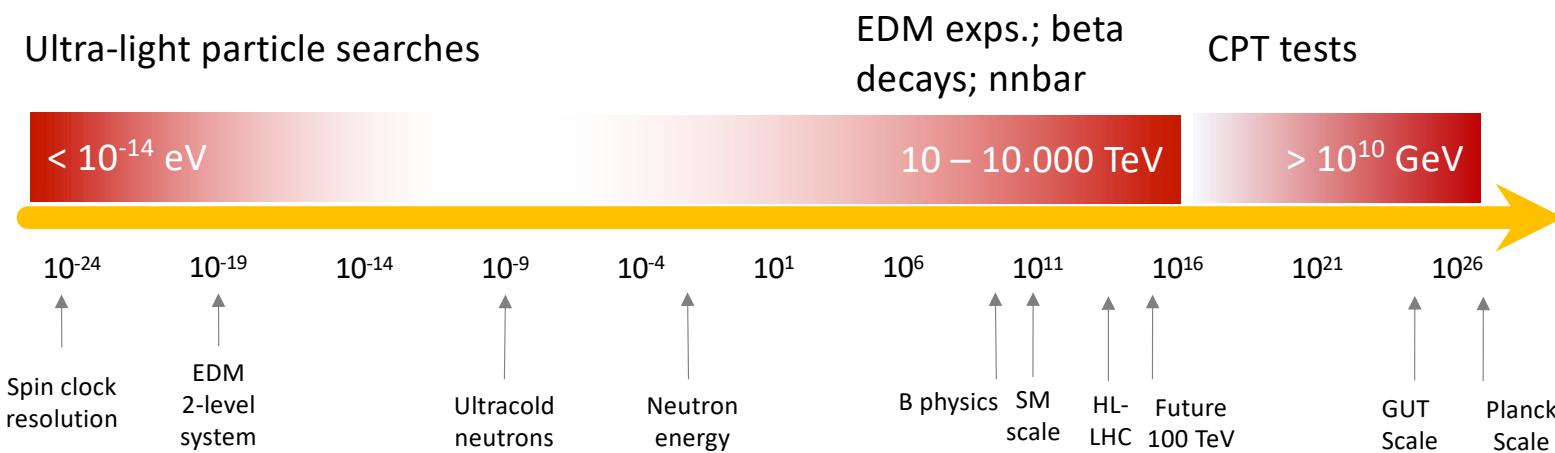
$$d_{\text{para}}^{\text{exp}} = d_e + \frac{\alpha_{C_S}}{\alpha_{d_e}} C_S$$

\*) new data available

# Energy reach of EDMs and symmetry tests

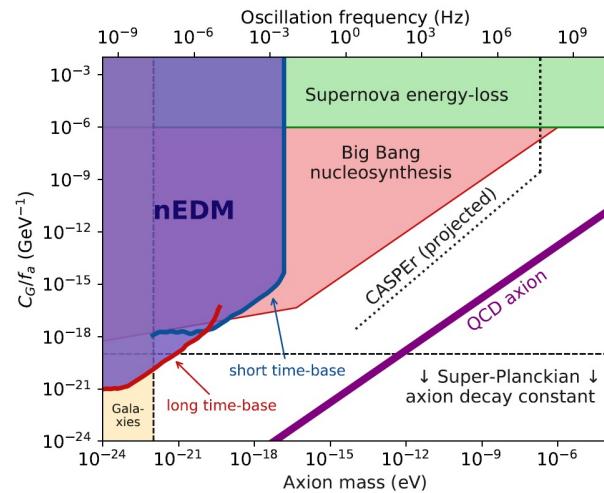
EDMs & (non-accelerator / low-energy) precision experiments:

- probe extremely high energies, beyond future accelerators
- probe otherwise inaccessible parameter space
- open (only) a small window to new physics, but with only few details

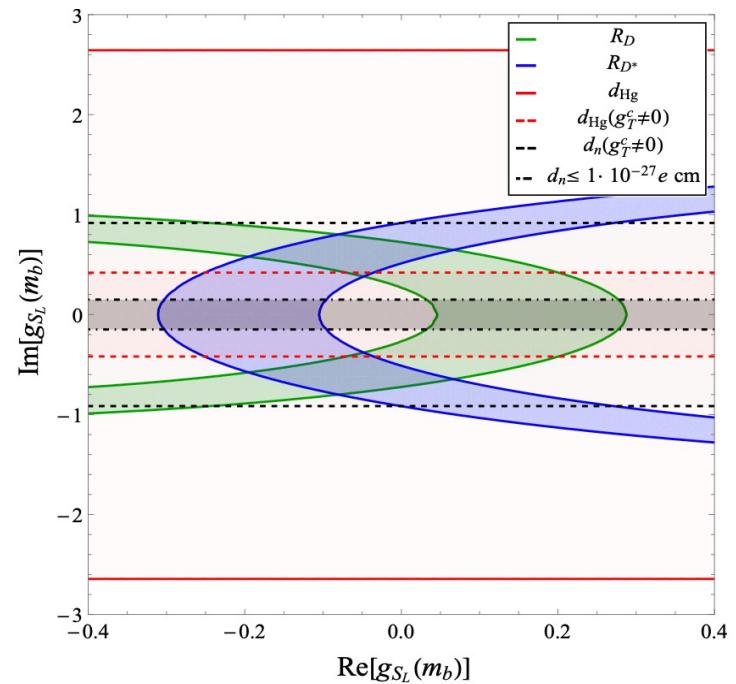


# Energy reach of EDMs and symmetry tests

- EDMs complement HEP experiments
- Effective field theory approach enables combining HEP / B physics and low-energy experiments together.
- Spin offs: e.g. dark matter searches

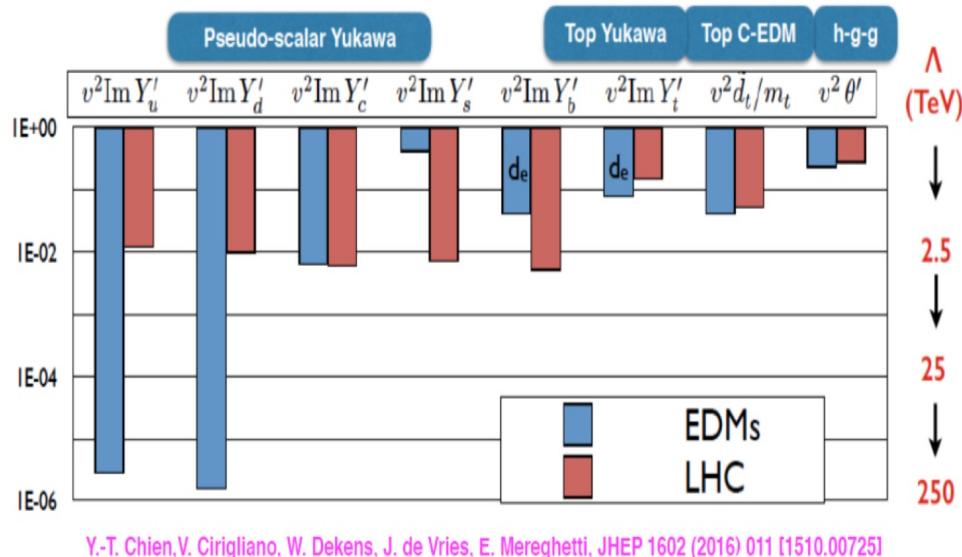


**Illustration:**  
combined NP limits from EDM and B physics



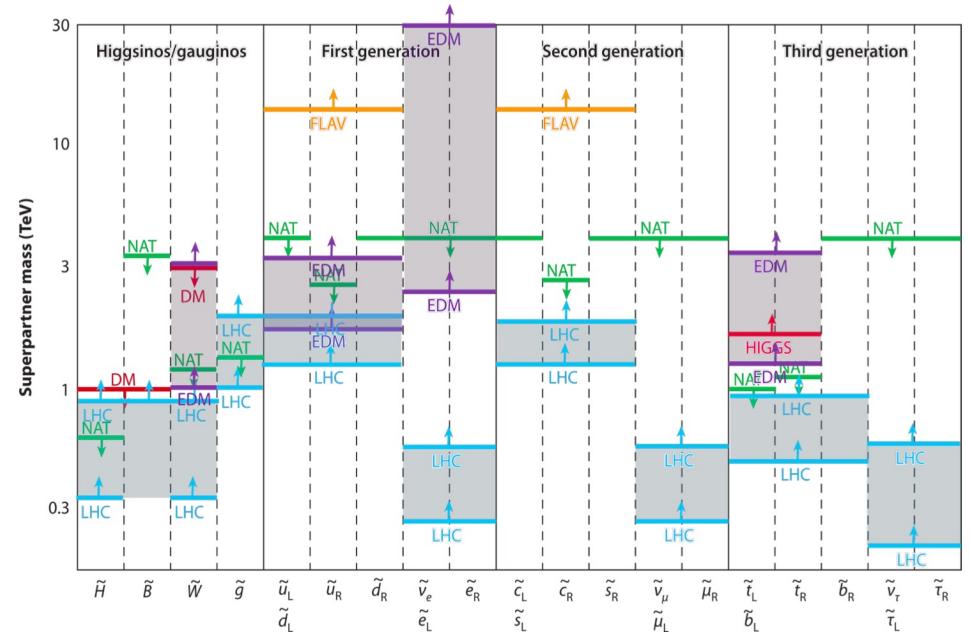
# EDMs are complementary to HEP experiments

**Constraints on different non-standard CPV**  
**Higgs couplings - Higgs production at LHC**  
 vs. EDMs



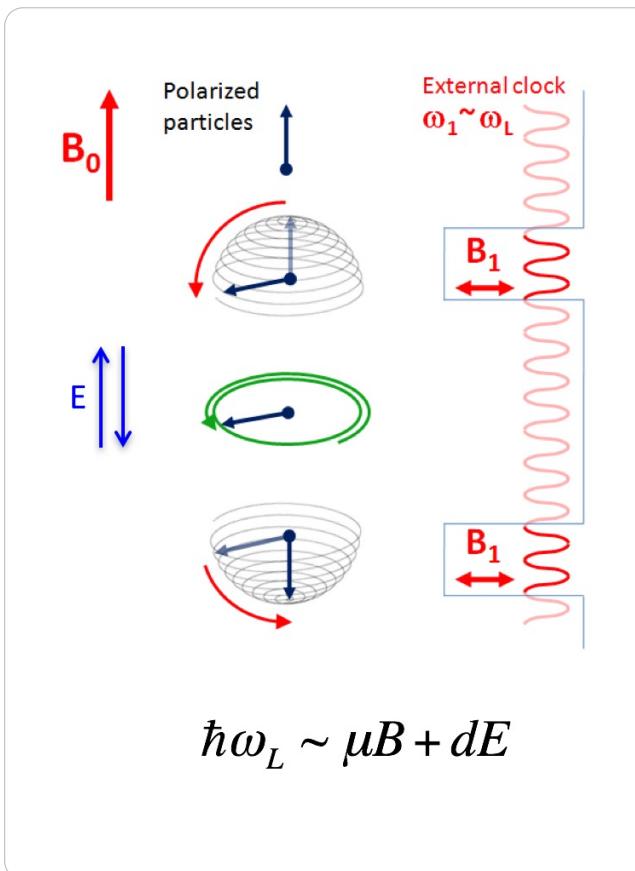
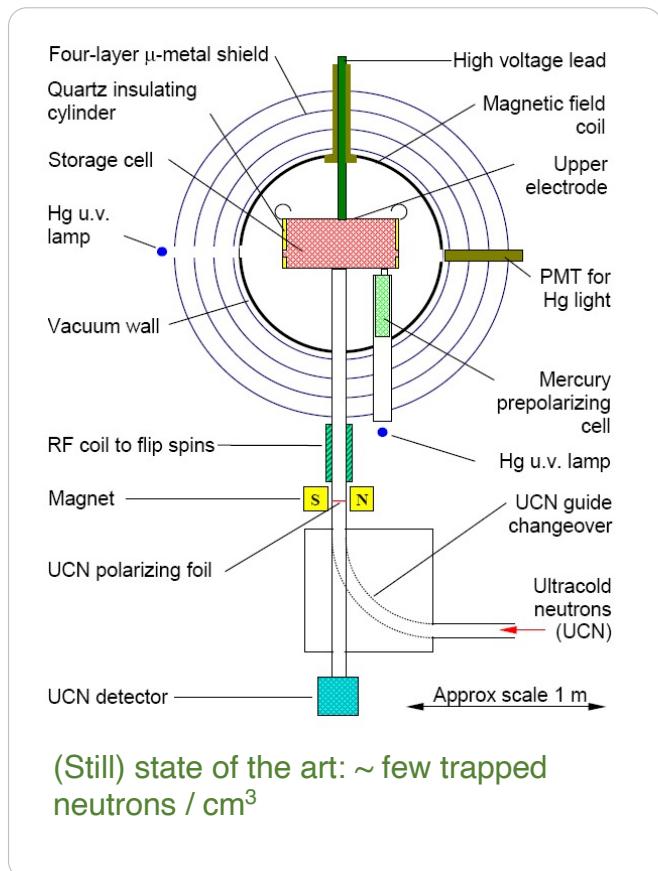
Picture by V. Cirigliano (PPNS2018)

**Constraints on different SUSY type parameters**

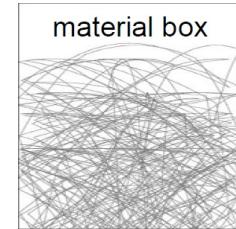


Shading shows progress since 2013 (LHC, ACME,  $^{199}\text{Hg}$ ) –  
 from Ann. Rev. Nuc. Part. Scie 63, 351 (2019) adapted,  
 taken from N. Hutzler

# Basic measurement method



Trapped ultra-cold neutrons with nano-eV kinetic energy



Statistical sensitivity:

$$\sigma_{d_n} = \frac{\hbar}{2\alpha ET \sqrt{N}}$$

Systematics: magnetic fields! ->  
often used: a 'co-habitating magnetometer'

# Neutron EDM

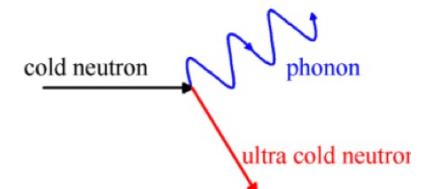
- Approaches with trapped UCN:

	RAL Sussex ILL	PSI nEDM	PSI n2EDM	PanEDM	PanEDM II	(EDM) <sup>n</sup>	LANL	SNS	PNPI	PNPI	TRIUMF
<b>Temperature</b>	RT	RT	RT	RT	RT	0.7K	RT	0.7K	RT	0.7K	RT
<b>Comagnetometer</b>	199-Hg	199-Hg	199-Hg	none	?	none	199-Hg	3-He	none	none	9-Xe, 199-Hg
<b>Source</b>	Turbine	spall + D2	spall + D2	4He	4He	4He (in situ)	spall + D2	4He (in situ)	Turbine	4He	4He
<b># of cells</b>	1	1	2	2	2	>100	1	2	2	>2	2
<b>UCN density goal [ecm]</b>	2	3	5	6	>100	>1000	50	125	4	10000	700
<b>goal [ecm]</b>	3.00E-26	1.80E-26	1.00E-27	5.00E-27	<1e-27	1.00E-29	E-27	2.00E-28	5.00E-26	<1E-27	1.00E-27
<b>Date</b>	2006	2020	2022?	2022	2024+	2022	2022	2022	2015	2022+	2022+
<b>Status</b>	completed	completed	commiss.	commiss.	planned	concept	source ready	install. ongoing	completed	install. ongoing	ongoing
<b>Comment</b>		upgrade of RAL/Sussex/ILL	magnetic shield completed	source startup summer 2021	component design	first test experiments 2021	magnetic shield being installed				first UCN from prototype source 2017

- Beam:

- Crystal EDM (Nagoya)
- Beam EDM -> cold beam at ESS
- (EDM)<sup>n</sup> is also a beam experiment

Most approaches use cooling process to increases phase space density:



$$\tau_{\text{up}}^{-1} \sim \frac{(T[K])^7}{100 \text{ s}}$$

# New systematic issues are expected...

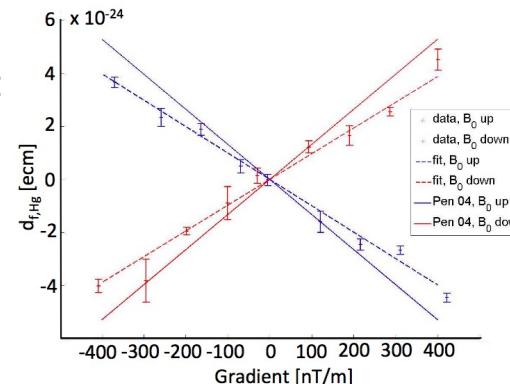
## Geometric phase effect:

$$\Delta\omega = \frac{\omega_{xy}^2}{2(\omega_0 - \omega_r)}$$

$$\omega_{xy}^2 = \left( \frac{\partial B_{0z}}{\partial z} \alpha \right)^2 + \left( \frac{E \times v}{c^2} \right)^2 + 2 \frac{\partial B_{0z}}{\partial z} \alpha \cdot \frac{E \times v}{c^2}$$

B field requirements for  $10^{-28}$  ecm – level accuracy:

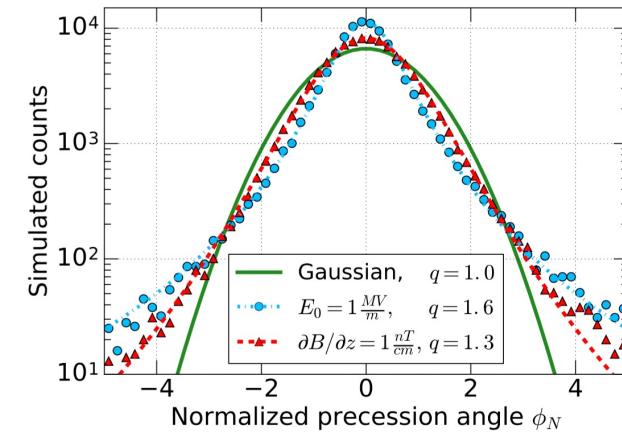
- < 0.3 nT/m gradient
- Max. 1 dipole with 5 pT in 2 cm distance
- < 10 fT drift stability



Pendlebury et al., Phys. Rev. A 70, 032102 (2004) and many more...

## Potentially new class of systematics identified:

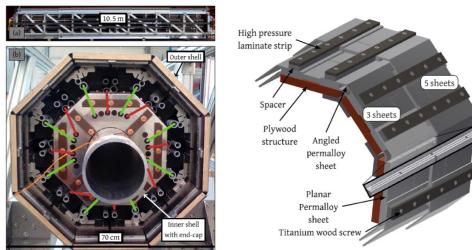
- Non-gaussian spin distributions in traps with gradients or E-fields
- Time-dependent shape of distributions



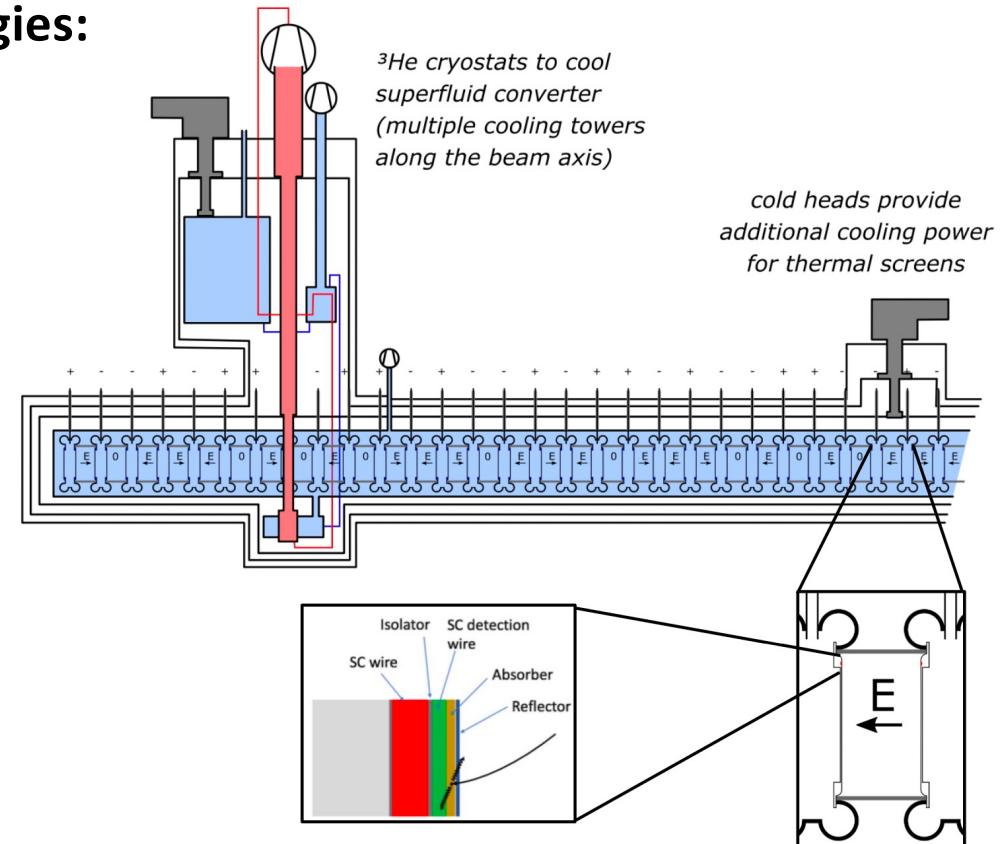
# Future neutron EDM

## Combining (independently) existing technologies:

- UCN production + trapping in superfluid He
- Magnetic shielding
- Avoiding most loss channels: in-situ UCN production + in-situ detection
- Suitable for the best existing beams (ILL)
- Modular design, fits future sites (ESS)
- $1.10^{-29}$  ecm sensitivity in principle possible (factor 1000 compared to now!)



Magnetic Shielding  
(Rev. Sci. Instrum. 91, 035117 (2020))



See S. Degenkolb presentation

# Technology drivers, e.g.:

- Many precise measurements need small magnetic fields & gradients: sample sizes, systematic issues (geometric phase), polarization life-times
- Quantitative numerical modeling
- Factor 1000 improvement in residual gradient in last 20 years

Bx bottom (pT)	38.4	27.0	15.6
7.8	3.8	-0.1	
-22.9	-19.4	-15.9	

By bottom (pT)	27.0	20.4	13.9
-0.1	31.4	-2.3	
-27.2	-22.9	-18.5	

Bz bottom (pT)	15.6	13.9	12.1
-8.0	-6.2	-4.5	
-31.6	-26.4	-21.1	

Bx center (pT)	-1.9	-7.1	-12.4
-6.3	-7.1	-8.0	
-10.6	-7.1	-3.6	

By center (pT)	7.7	0.3	-7.1
2.5	-1.9	-2.3	
-2.8	-0.1	2.5	

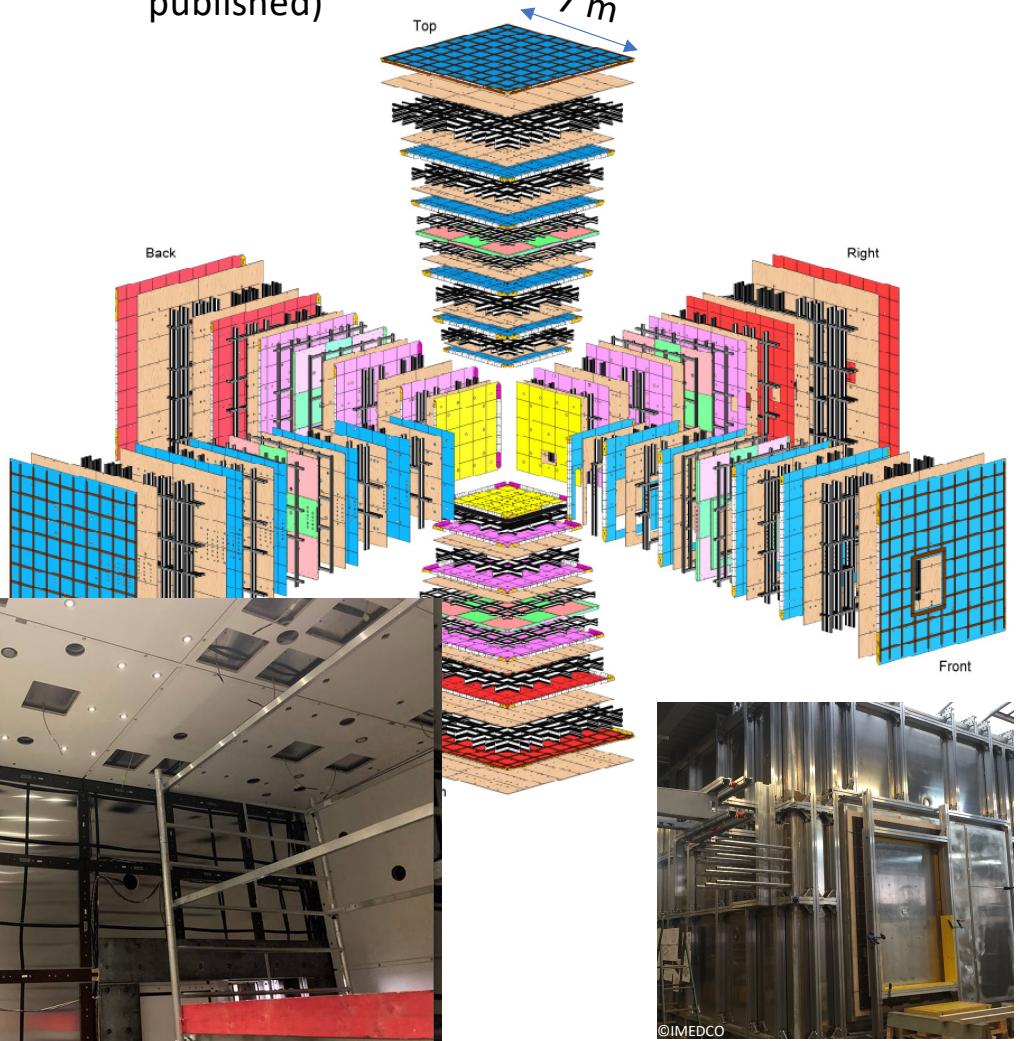
Bz center (pT)	17.4	7.7	-1.9
11.2	7.3	3.4	
5.1	6.9	8.6	

Bx top (pT)	14.9	9.7	4.4
7.9	-1.7	-11.3	
0.9	-13.1	-27.1	

By top (pT)	19.3	12.3	5.3
8.8	-0.8	-8.7	
-1.7	-12.2	-22.7	

Bz top (pT)	23.7	14.9	6.2
9.7	1.8	-6.1	
-4.3	-11.3	-18.3	

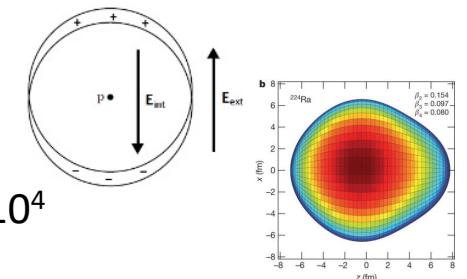
Figure: world's largest shield  
(2020): ~ 100 pT in 30 m<sup>3</sup> (to be published)



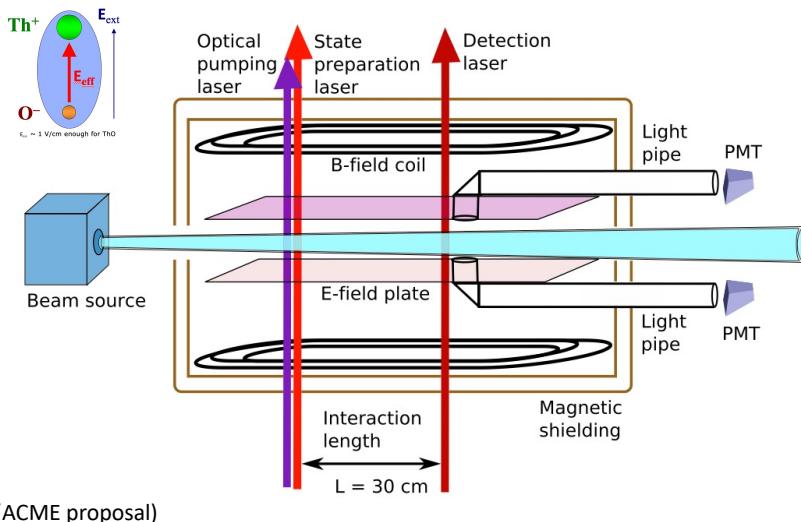
©IMEDCO

# Improving the sensitivity

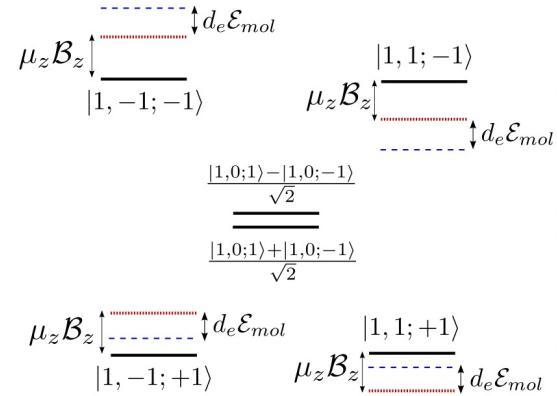
- **Schiff moment:** suppression for  $^{129}\text{Xe}$ ,  $^{199}\text{Hg}$ :  $\sim 10^{-2}$ , enhancement for  $e \sim Z^3$
- Enhancement due to **nuclear deformations** for  $^{220}\text{Rn}$ ,  $^{224}\text{Ra}$  - enhancement  $\sim 10^{2-4}$
- Enhancement due to **large E-fields in molecules**:  $\text{YbF}$ ,  $\text{ThO}$ ,  $\text{HfF}^+$  - enhancement  $\sim > 10^4$



## ACME I - Basic experiment principle:



## ThO substructure of the ‘science state’ $\Delta$ with $J = 1$ :



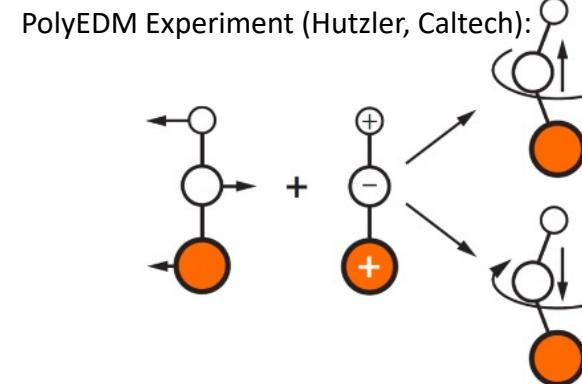
**Figure 3.** Schematic level structure and energy shifts of the  $\text{ThO } H^3\Delta_1(J=1)$  manifold of sublevels, in the presence of the applied external fields  $\mathcal{E} = \mathcal{E}\hat{z}$  and  $\mathcal{B} = \mathcal{B}\hat{z}$  (not to scale). States are labelled by their quantum numbers  $|J, M_J; \mathcal{N}\rangle$ , where  $\mathcal{N} = \text{sgn}(\hat{n} \cdot \mathcal{E})$  describes the orientation of the fully polarized molecules. Note the different signs of the eEDM shift in the  $\mathcal{N} = \pm 1$   $\Omega$ -doublet levels.

- Alignment of E-field, molecular axis and angular momentum optically
- Co-magnetometer
- Small lab E-fields
- Modest B-field problems
- Science state is metastable (in this system)

# Improving the sensitivity

## Improving statistics and systematics:

- Polyatomic molecules like YbOH (many choices!)
- internal co-magnetometer AND suitable structure for laser cooling
- Internal field saturation already at low lab fields
- Spin-off: first MQM measurements



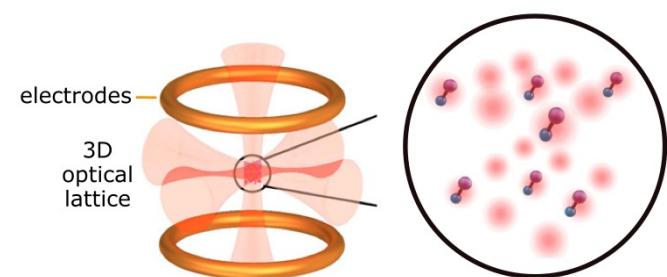
I. Kozyryev and NRH, PRL 119, 133002 (2017)

## Recent advances in preparing high intensity cold molecule beams:

- Possible laser cooling / trapping / fountain e.g. with YbF:
- Line width  $\sim$  dispersion of sample in space  $\sim$  coherence time.
- Numbers from proposal:  $10^6$  trapped YbF molecules;  $\tau = 10$  s; 18 kV/cm ... shot noise limit of  $10^{-32}$  ecm / day.

Note: more physics with molecules etc. see M. Safronova's talk

Illustration of MOT / optical lattice with EDM E-field electrodes (Hinds, Imperial):

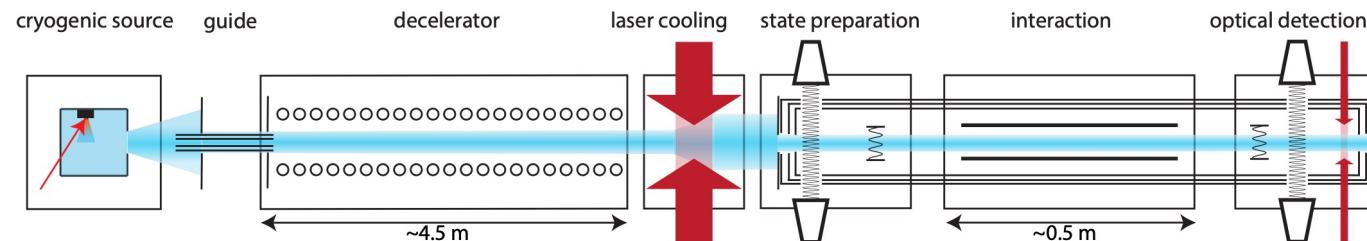


# Molecules: BaF

$5 \cdot 10^{-30}$  ecm level in first generation of experiment:

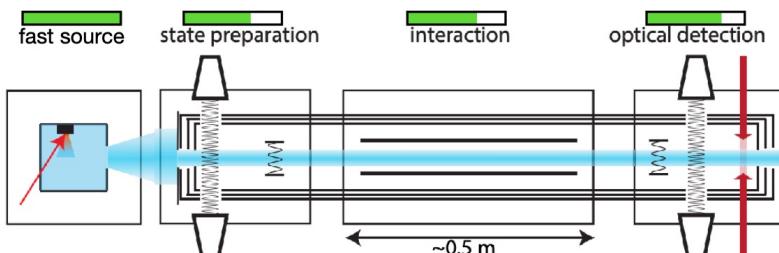
- High intensity slow beam (using all recent advancements)
- Relatively low  $E_{int} \sim 6-8$  GV/cm at saturation
- Efficient laser cooling due to light weight & suitable el. structure / ground state

Planned full experiment:

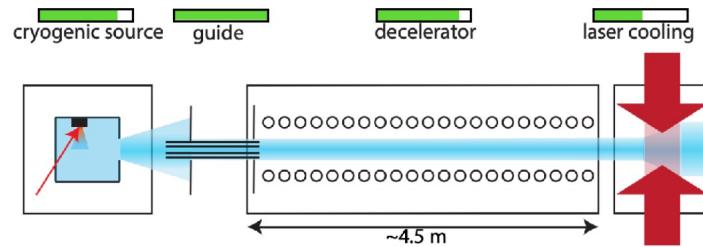


Approach:

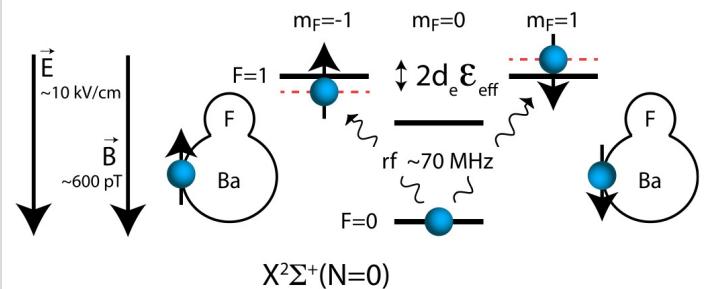
Status: a) Fast beam to demonstrate control of systematics



b) Slow beam for full statistics

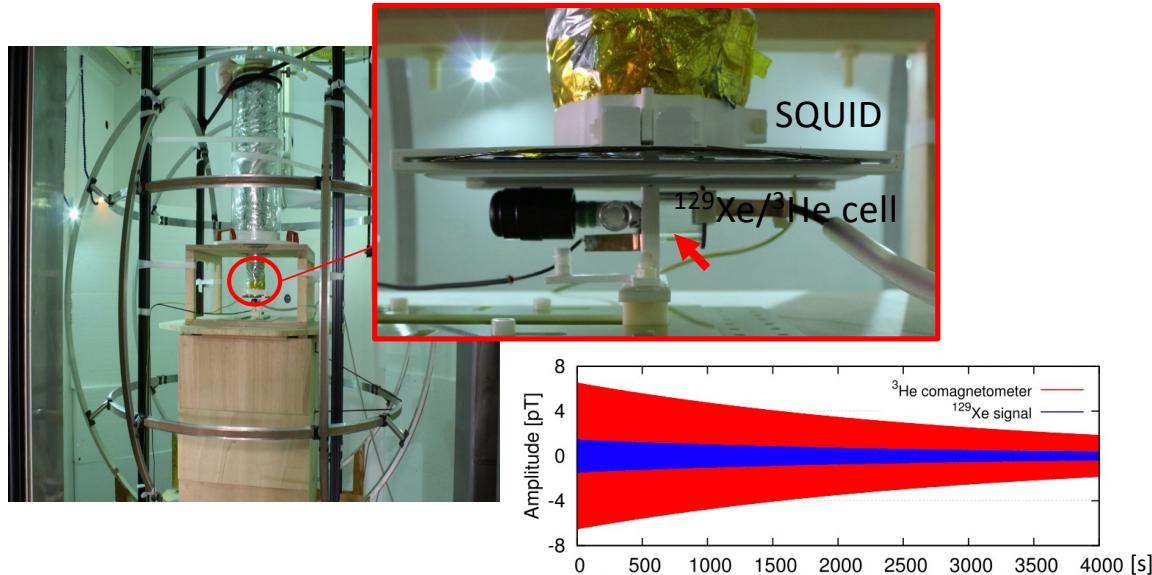


Ground state as science state:



# 129-Xe EDM – Example: HeXe

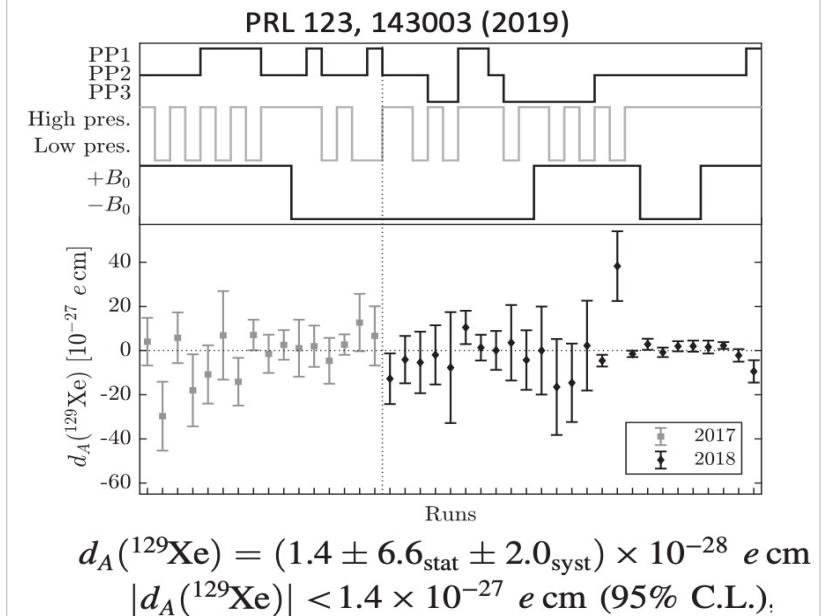
## Experiment scheme:



- Hyperpolarized  $^3\text{He}$  and  $^{129}\text{Xe}$ ,  $B \sim \mu\text{T}$ ,  $E \sim \text{few kV/cm}$
- Spin precession in low field detected with SQUIDs
- Potential:  $10^{-30} \text{ ecm}$
- Important contribution to joint EFT parameter analysis
- Other efforts: MIXed, Liquid Xe, Active Maser, Xe-comag

## EDM data extraction:

$$\sigma_d \approx \frac{1}{2E} \frac{\hbar}{\tau} \frac{1}{S/N} \propto \frac{1}{\tau^{3/2}}$$

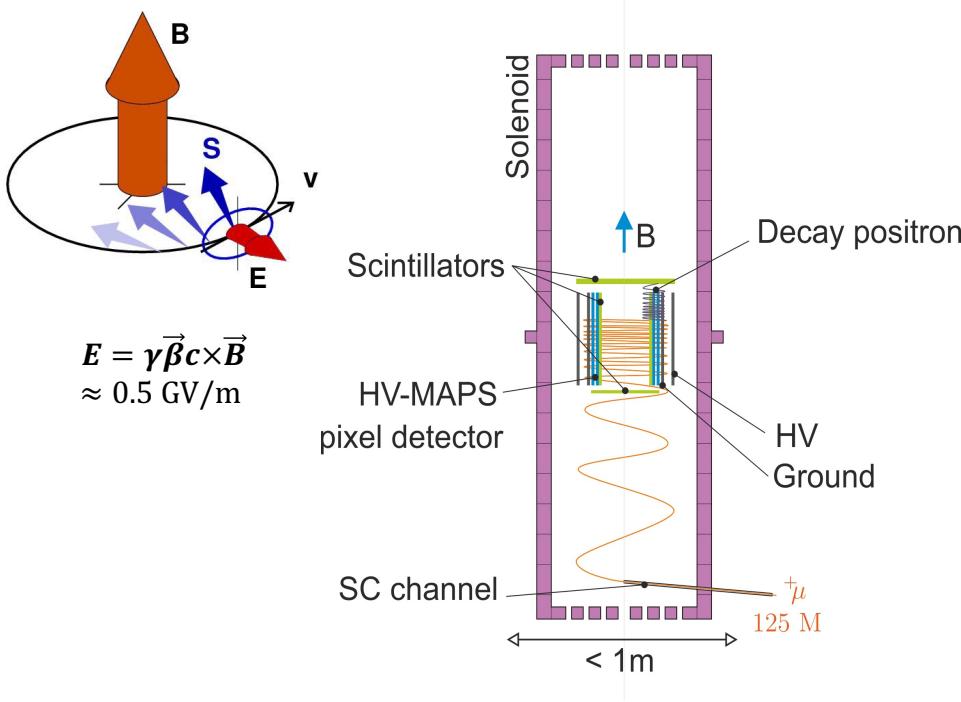


$$d_A(^{129}\text{Xe}) = (1.4 \pm 6.6_{\text{stat}} \pm 2.0_{\text{syst}}) \times 10^{-28} \text{ e cm}$$

$$|d_A(^{129}\text{Xe})| < 1.4 \times 10^{-27} \text{ e cm} \quad (95\% \text{ C.L.})$$

# Muon EDM

**Basic idea: frozen spin method, out-of-plane polarization due to EDM**



- Testing CPV in a second generation lepton, clean of nuclear and atomic background
- Expected sensitivity using existing PSI beamlines:

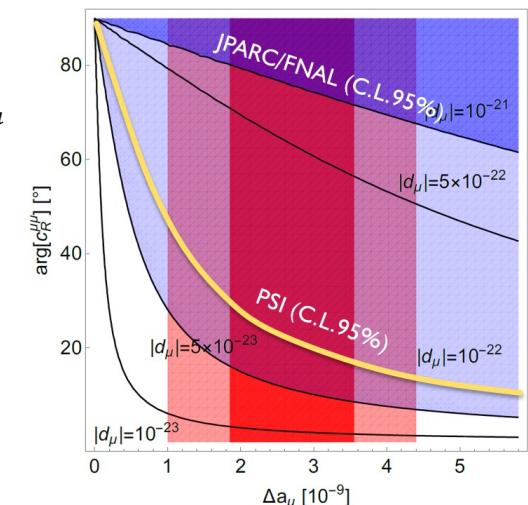
$$d_\mu < 6 \times 10^{-23} \text{ ecm}$$

Further advances in future: HIMB and muCool.

Flavor violating models:  
EFT phase of Wilson parameter  $c_R^{\mu\mu}$   
hardly constrained

A. Crivellin *et al.*,  
PRD 98 (2018) 113002

Other physics motivations: New scalars and fermions, MSSM, Leptoquarks



# Antihydrogen spectroscopy

Standard Model Extension SME:

$$(i\gamma^\mu D_\mu - m_e - [a_\mu^e \gamma^\mu - b_\mu^e \gamma_5 \gamma^\mu] \xrightarrow{\text{CPT & LORENTZ VIOLATION}} - \frac{1}{2} H_{\mu\nu}^e \sigma^{\mu\nu} + i c_{\mu\nu}^e \gamma^\mu D^\nu + i d_{\mu\nu}^e \gamma_5 \gamma^\mu D^\nu) \psi = 0.$$

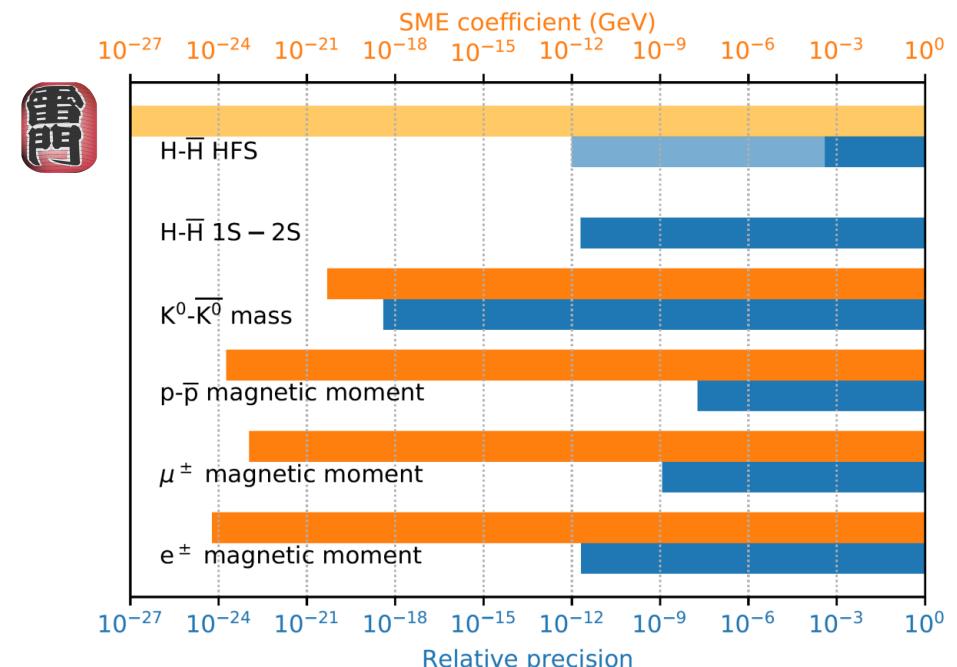
D. Colladay and V.A. Kostelecky, PRD 55, 6760 (1997)

- Minimal SME: CPTV only in hyperfine splitting
- Non-minimal SME: ... also in 1S-2S
- HFS meas. precision: 1S-2S at  $10^{-4}$  level in trapped anti-H (no effect due to mag. field)



Widmann, E. et al. *Hyperfine Interact.* 240:5 (2019)

Bluhm, R., Kostelecký, V., & Russell, N., PRL 82, 2254-2257 (1999).  
Kostelecký, V.A. & Vargas, A.J., PRD, 92, 056002 (2015)

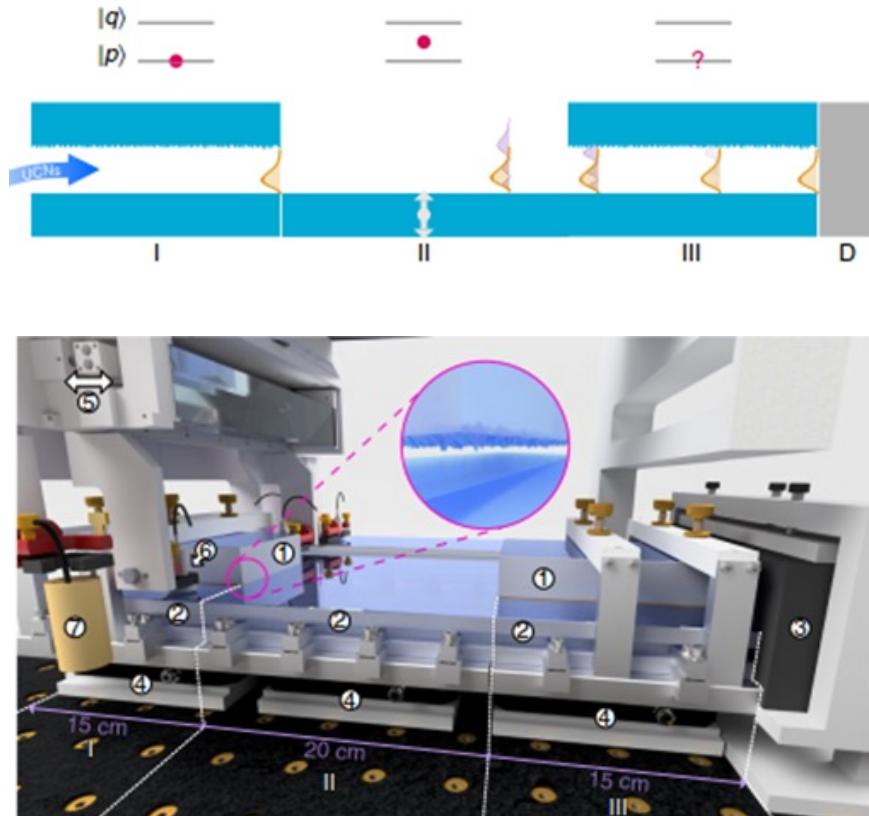


PDG, Kostelecký & Bluhm arXiv:0801.0287

Dark blue: measured for particle and antiparticle  
Light blue: measured for particle only  
Orange: measured SME coefficient  
Yellow: potentially reachable accuracy

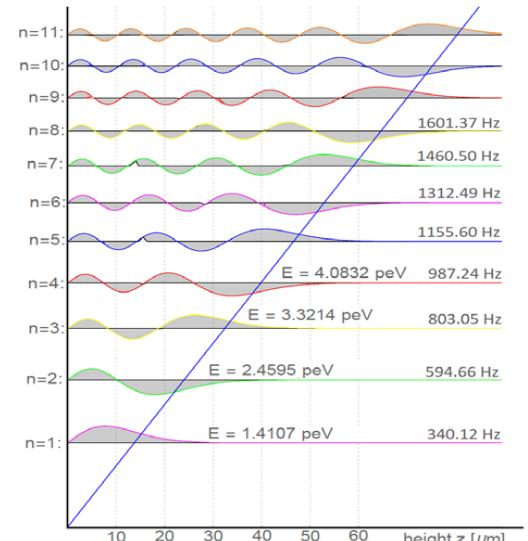
E. Widmann

# Gravity resonance spectroscopy



- Ultra-cold neutrons are put into a superposition of gravitational quantum states; typical scale: micrometers
- Mirror oscillations provide transitions between states: Rabi & Ramsey spectroscopy
- Future: e.g. storage on top of mirror = long 'exposure times'
- CPT, Lorentz invariance  
*Phys. Lett. B 798 134819 (2019)*
- Dark matter
  - Axions
  - Chameleons
  - Symmetrons

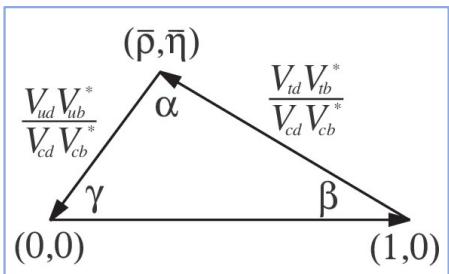
*Nature Physics 14, 1022 (2018)*



# Neutron decay: PERC

- Physics case:

Precision unitarity test of CKM's first row



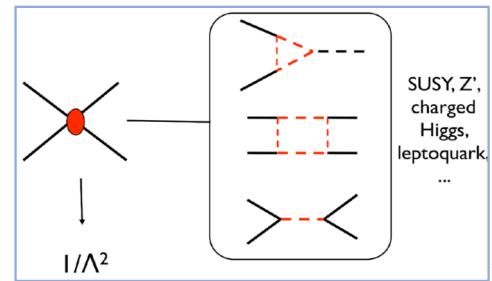
Seng, Gorchtein, Ramsey-Musolf Phys. Rev. Lett. 121 (2018)

$$V_{ud} = \left( \frac{5099.34 \text{ s}}{\tau_n(1 + 3\lambda^2)(1 + \Delta_R)} \right)^{1/2}$$

$$= 0.97301(10)_{\text{RC}}(44)_{\tau_n}(35)_{\lambda}$$

$$= 0.97301(58),$$

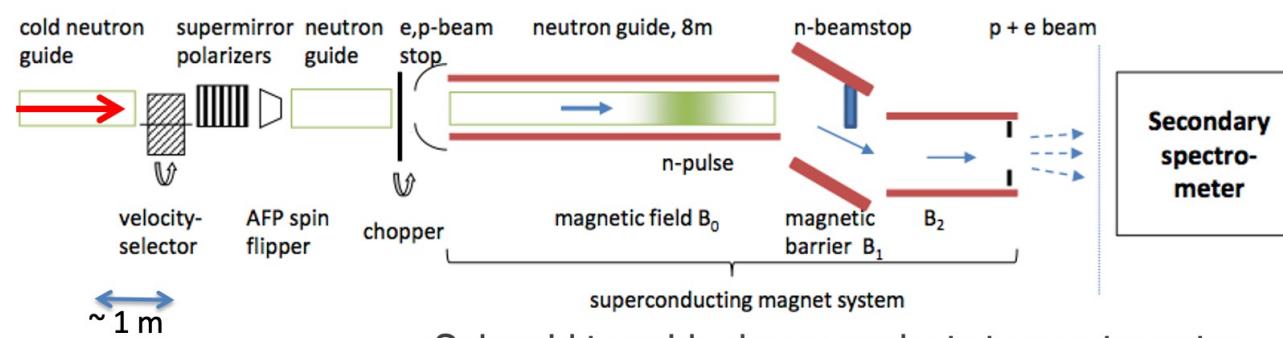
Search for New Physics through EFTs, reach  $\sim 10\text{-}100 \text{ TeV}$



Märkisch et al., Phys. Rev. Lett. 122 (2019)

See e.g.  
M. González-Alonso  
for low-energy EFTs

- PERC instrument at FRM-II (TUM) - future: ESS - improvement  $\times 30$



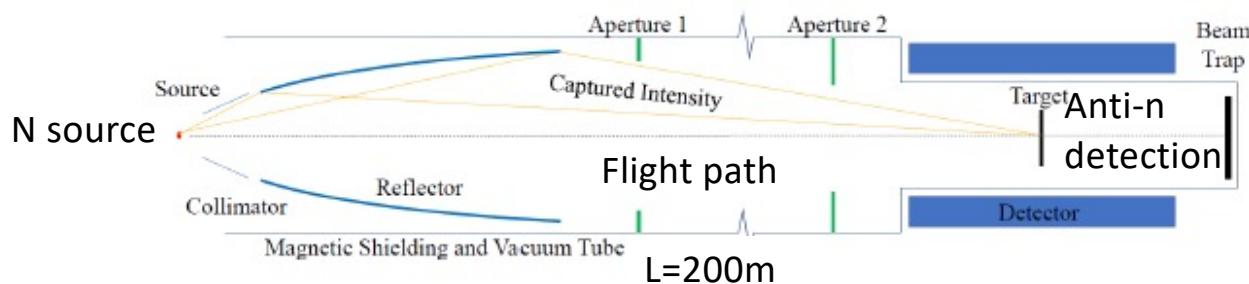
Solenoid to guide decay products to spectrometer



# Neutron-antineutron oscillations

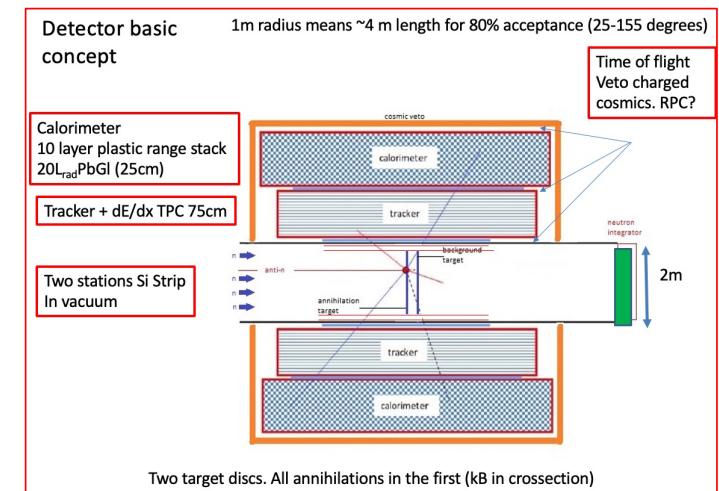
Idea: free neutron converts to antiparticle in flight:  $n \rightarrow \bar{n}$        $\mathcal{H} = \begin{pmatrix} E_n & \varepsilon_{n\bar{n}} \\ \varepsilon_{n\bar{n}} & E_{\bar{n}} \end{pmatrix}$

**Physics case:** Baryogenesis (eg post-sphaleron baryogenesis), RPV-SUSY, LR symmetric models, Extra dimensions ...



- Neutron optics with large angular acceptance
- Magnetic shield around free neutron flight path
- Annihilation target + detector
- Potential: factor 1000 improvement compared to previous generation experiment

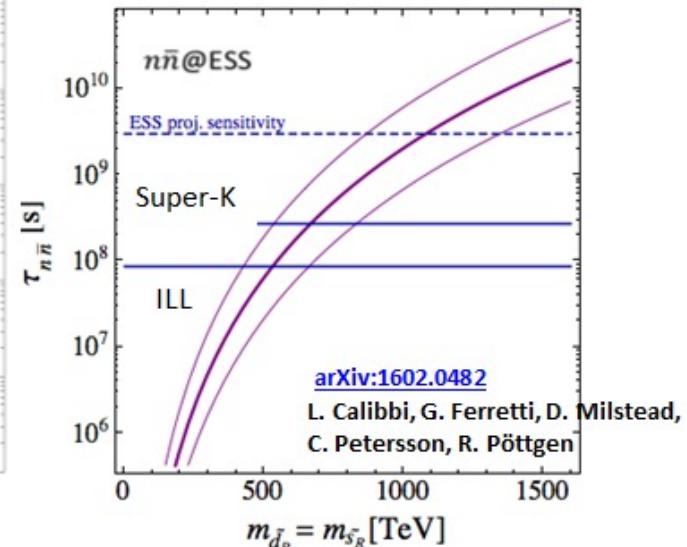
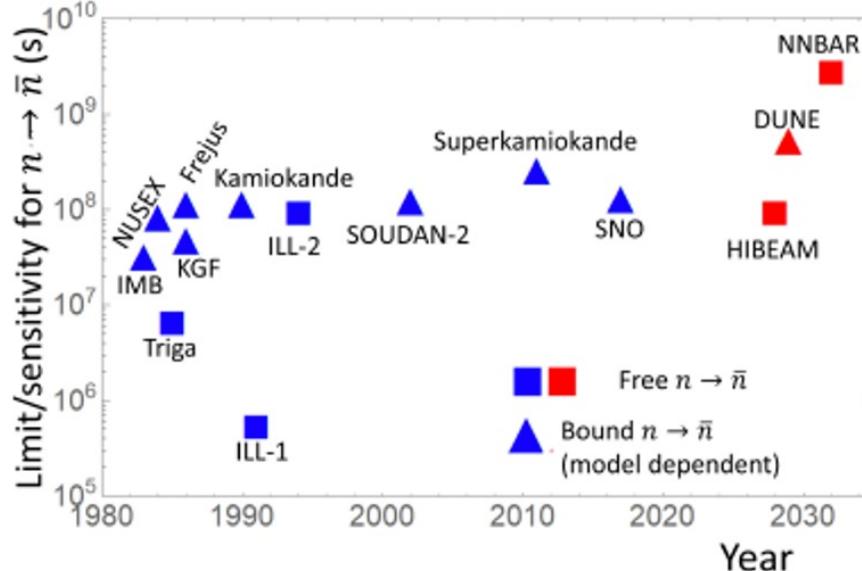
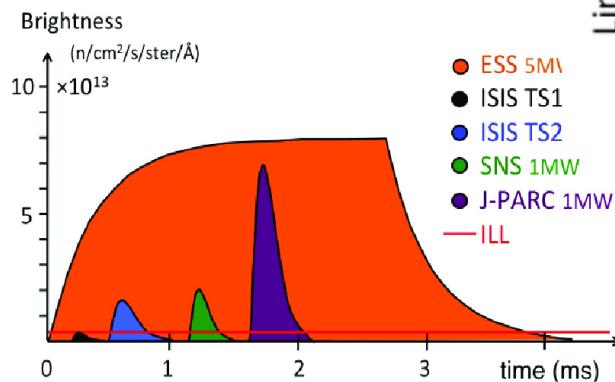
V. Santoro



# Neutron-antineutron oscillations



... European Spallation Source ESS will (in long-term) replace reactor neutron source ILL – pulses instead of continuous flux



- 2 stages: HIBeam (>2025), NNBAR (> 2030)

# Where are we in 20 years?

- EDM experiments are
  - long-term efforts: historically 8 years per order of magnitude (eEDM: now faster!)
  - very difficult, subject to unexpected problems
- It is dangerous to promise and predict EDM results.
  - My naïve guess: surviving/novel efforts reach PeV-scale
- New concepts to improve EDM sensitivities in many areas:
  - nucleon, atom, electron, muon, tau
- Close connection between EDM/low-energy symmetry tests and HEP through EFTs: naively irrelevant cases might become more interesting through this
- Polyatomic molecules, electrostatic storage rings... AMO and nuclear/particle techniques will be closely connected
- New facilities online and available, e.g. for fundamental physics at ESS