Embedding primordial black holes in the early universe: theory and phenomenological applications of cosmological metrics to PBH dark matter binary abundance constraints and evaporation limits on asteroid-mass candidates



Zachary S.C. Picker

Dunking PBHs in Cosmological

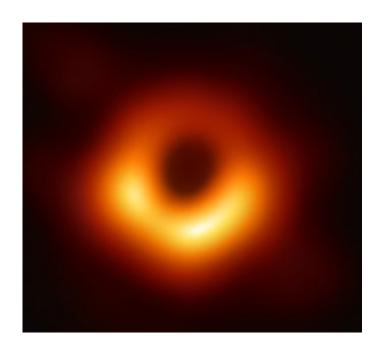
(PRANK GONE WRONG!)

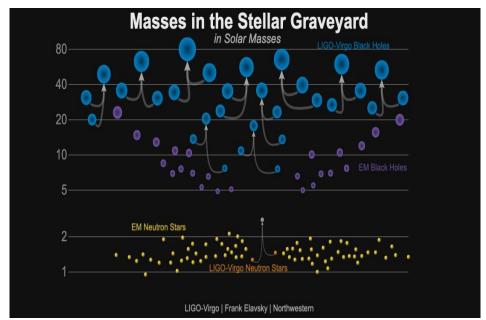
Zachary "S.C." Picker

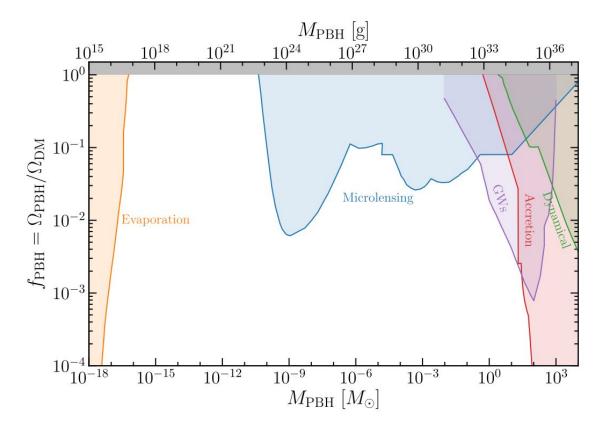


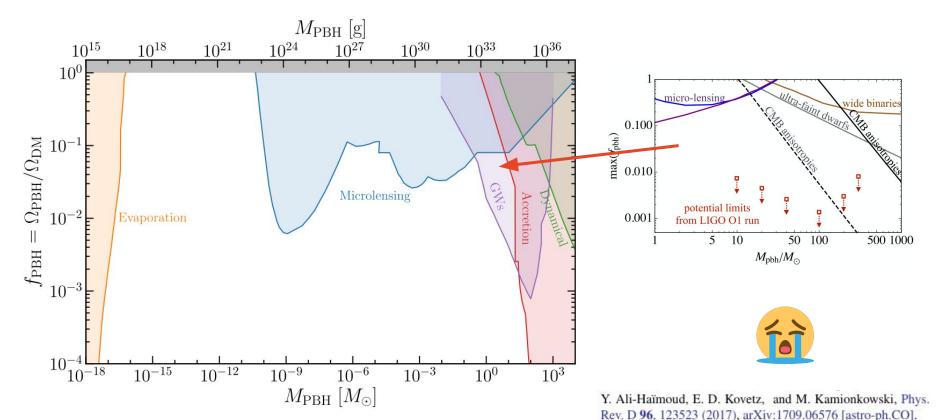




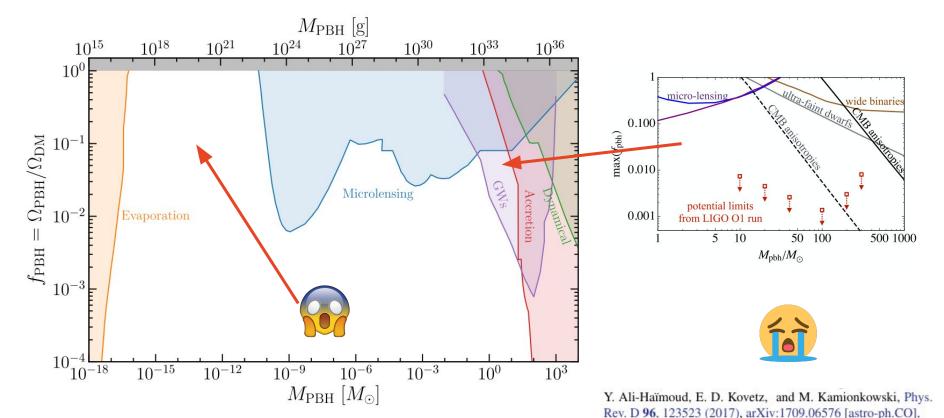


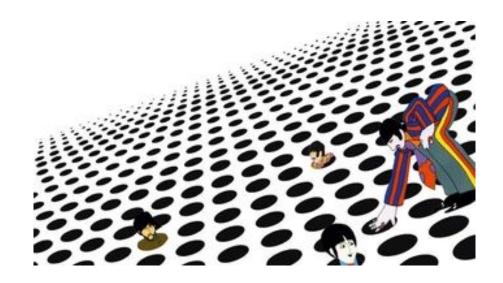


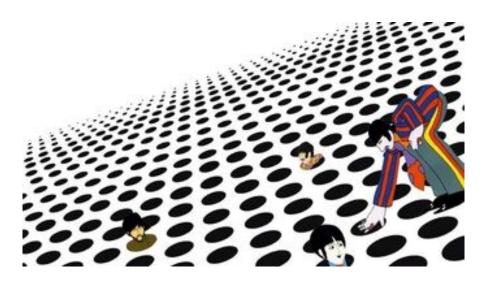


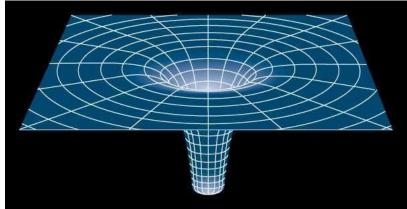


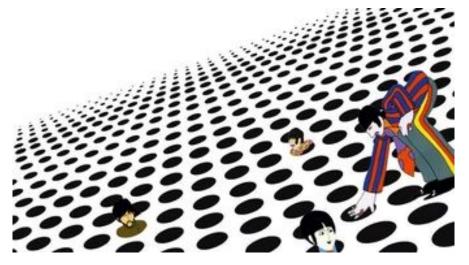
Green & Kavanaugh, 2020

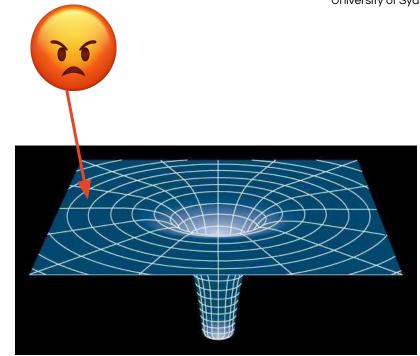












Einstein-Strauss ("Swiss Cheese Vacuole")



Einstein-Strauss ("Swiss Cheese Vacuole")





McVittie metric

Einstein-Strauss ("Swiss Cheese Vacuole")





McVittie metric

Generalized McVittie metrics



Thakurta metric

Attractor solution

Thakurta metric

- Attractor solution
- Simple + elegant:

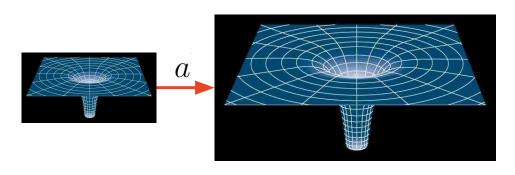
$$\mathrm{d}s^2 = a^2 \mathrm{d}s_{schw.}^2$$

Thakurta metric

- Attractor solution
- Simple + elegant:

$$\mathrm{d}s^2 = a^2 \mathrm{d}s_{schw.}^2$$

Local effective mass/ apparent horizon:





Binary abundance constraints

PREPARED FOR SUBMISSION TO JCAP

CPPC-2020-05

Eliminating the LIGO bounds on primordial black hole dark matter



Céline Bœhm,^a Archil Kobakhidze,^a Ciaran A. J. O'Hare,^a Zachary S. C. Picker,^a Mairi Sakellariadou^b

^aSydney Consortium for Particle Physics and Cosmology, School of Physics, The University of Sydney, NSW 2006, Australia

^bTheoretical Particle Physics and Cosmology Group, Physics Department, King's College London, University of London, Strand, London WC2R 2LS, UK

E-mail: celine.boehm@sydney.edu.au, archil.kobakhidze@sydney.edu.au, ciaran.ohare@sydney.edu.au, zachary.picker@sydney.edu.au, mairi.sakellariadou@kcl.ac.uk

Abstract. Primordial black holes (PBHs) in the mass range (30–100) M_{\odot} are interesting candidates for dark matter but are tightly constrained by the LIGO merger rate. In deriving these constraints, PBHs were treated as constant Schwarzschild masses. A careful analysis of cosmological black holes however leads to a time-dependent effective mass. This implies stricter conditions for binary formation, so that the binaries formed merge well before LIGO's observations. The observed binaries are those coalescing within galactic halos, at a rate consistent with LIGO data. This reopens the possibility of LIGO mass PBH dark matter.



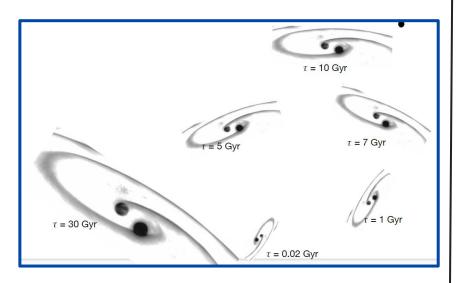




Binary abundance constraints

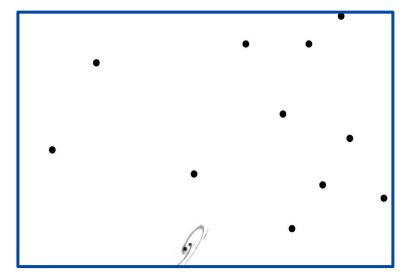
Previously

At matter-radiation equality:

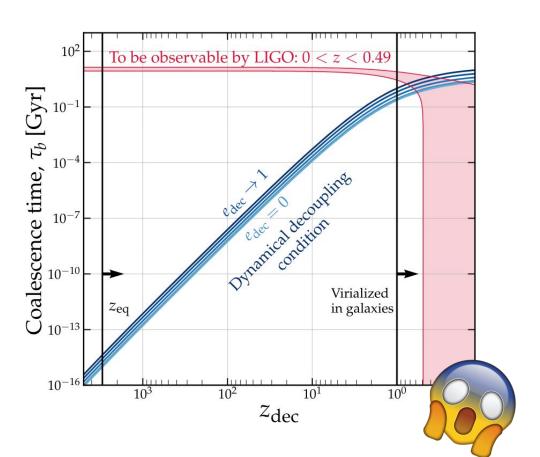


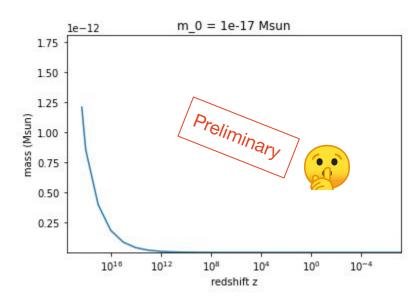
Thakurta PBHs

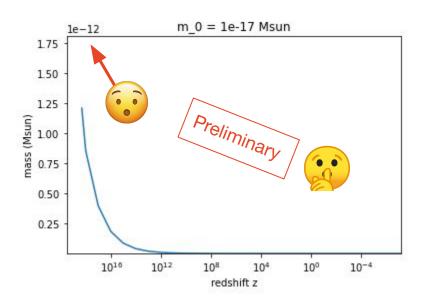
At matter-radiation equality:



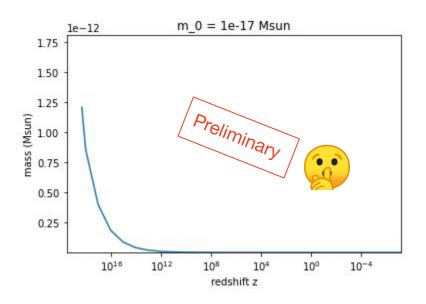
Binary abundance constraints

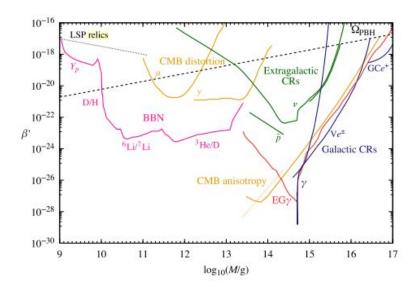






Carr et al, 2010



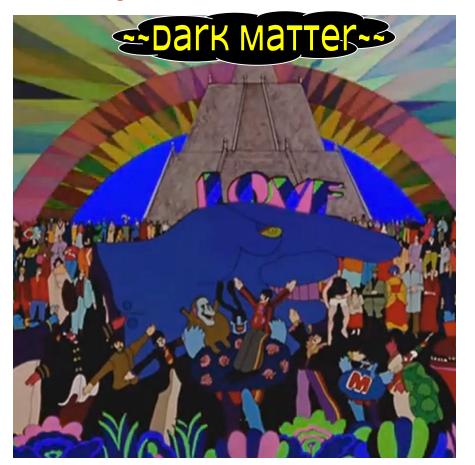


Carr et al, 2010

Morals and takeaways



Morals and takeaways



Actual physics: Thakurta metric

$$\mathrm{d}s^2 = f(R) \left(1 - \frac{H^2 R^2}{f^2(R)} \right) \mathrm{d}t^2 + \frac{2HR}{f(R)} \mathrm{d}t \, \mathrm{d}R - \frac{\mathrm{d}R^2}{f(R)} - R^2 \left(\mathrm{d}\theta^2 + \sin^2\theta \, \mathrm{d}\phi^2 \right)$$
 t -> new Kodama time t

$$ds^{2} = \left(1 - \frac{2m(r,t)}{r}\right) dt^{2} + \frac{dr^{2}}{1 - 2m(r,t)/r} + r^{2} \left\{d\theta^{2} + \sin^{2}\theta d\phi^{2}\right\}$$

Misner-Sharp mass:
$$m(r,t) = ma(t) + \frac{H^2R^3}{2Gf(R)}$$

Actual physics: decoupling conditions

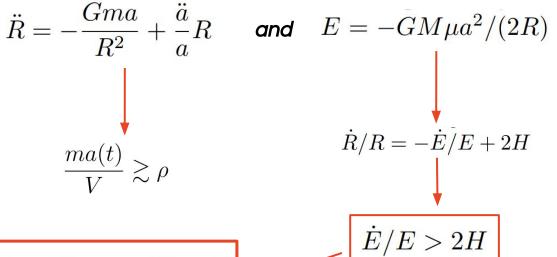
Previous:

$$\ddot{R} = \frac{\ddot{a}}{a}R - \frac{Gm}{R^2}$$

$$\frac{m}{V} \gtrsim \rho$$

$$\ddot{R} = -\frac{Gma}{R^2} + \frac{\ddot{a}}{a}R$$

$$\frac{ma(t)}{V} \gtrsim \rho$$



$$(1+z_{\rm dec})^3 H(z_{\rm dec}) < \frac{1}{\tau_b} \frac{96}{425} \left(1 + \frac{73}{24} e_{\rm dec}^2 + \frac{37}{96} e_{\rm dec}^4 \right)$$

Actual physics: hawking radiation

