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Royal Holloway University of London, Egham, United Kingdom



Long optical undulators with Traveling-Wave Thomson Scattering

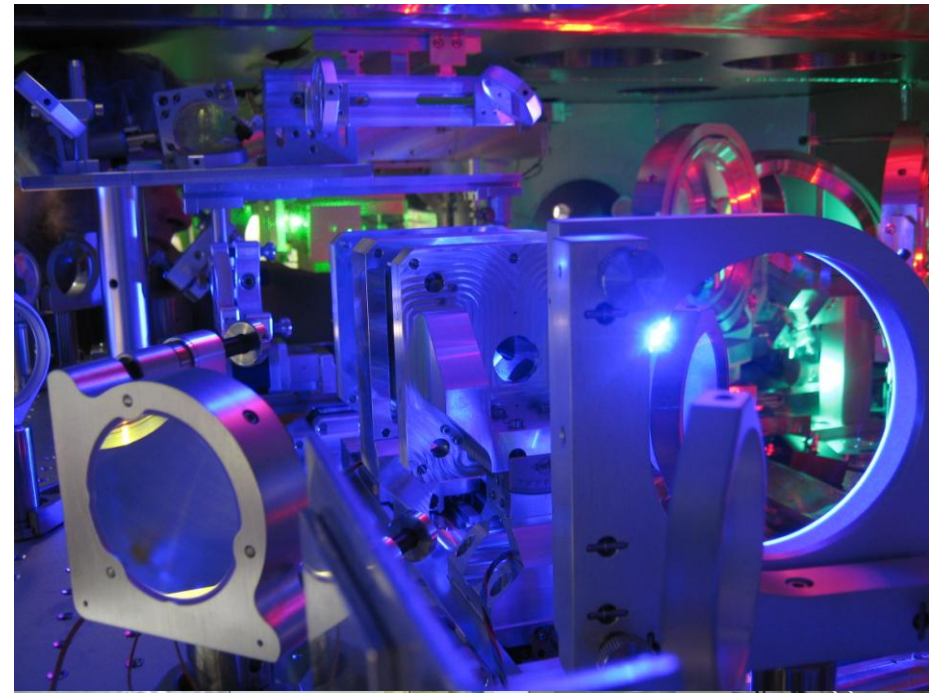
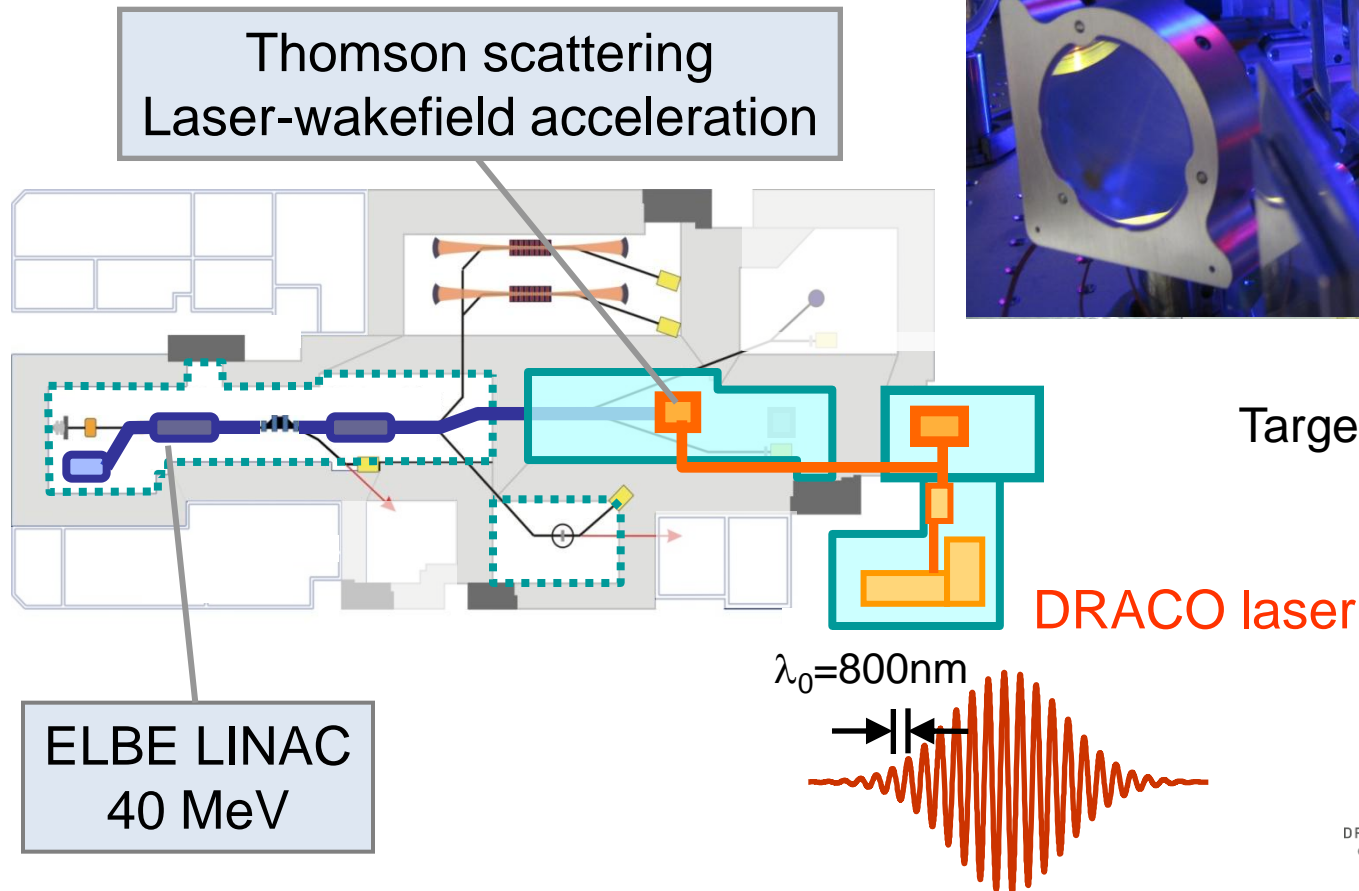
**Towards tunable, high-yield sources
in the hard X-ray range**

A. Debus, K. Steiniger, M. Siebold, A. Jochmann, A. Irman
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HZDR

 **HELMHOLTZ**
ZENTRUM DRESDEN
ROSSENDORF

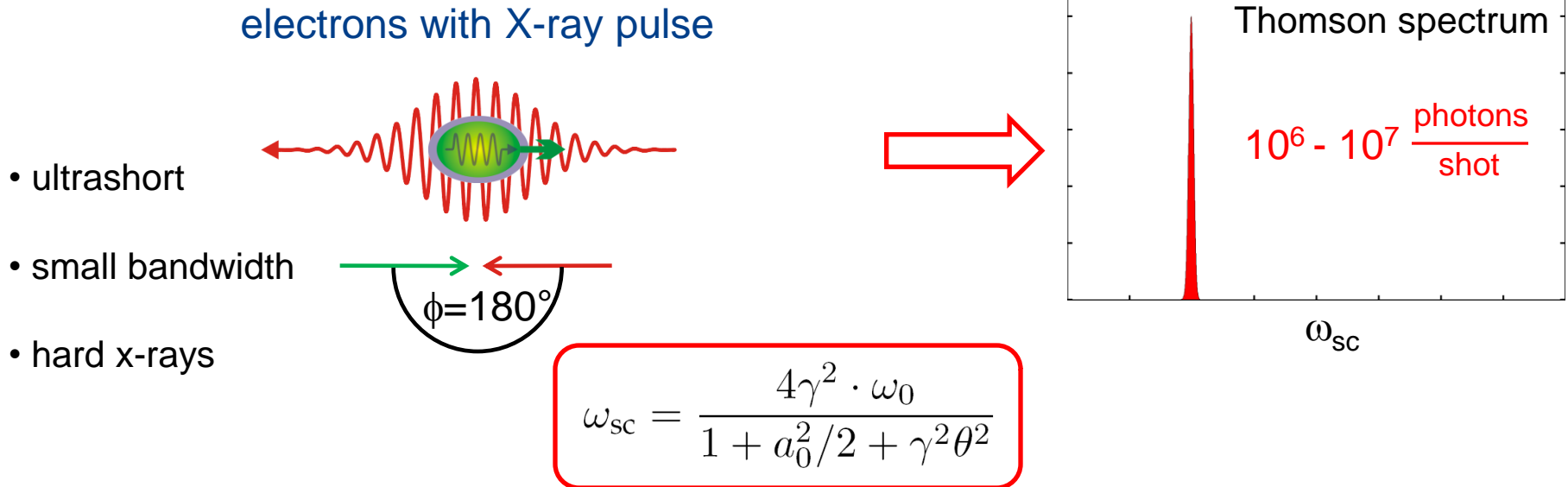
At the ELBE facility
the DRACO laser is used for
head-on Thomson scattering



Target area at ELBE

250 Terawatt
4 J / 25 fs
synchronized to
electron beam

Head-on Thomson Scattering produces ultrashort X-ray pulses



Most of the planned Thomson sources world-wide are aiming for high-repetition lasers combined with optical power enhancement cavities to achieve high-average powers.

Many X-ray photons per shot are desired, but not pursued. Why?

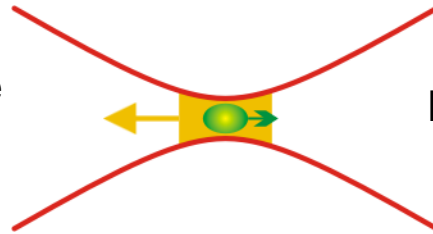
So, what is wrong with ultrashort, high-power lasers for Thomson scattering?

Why is it difficult to scale up the yield?

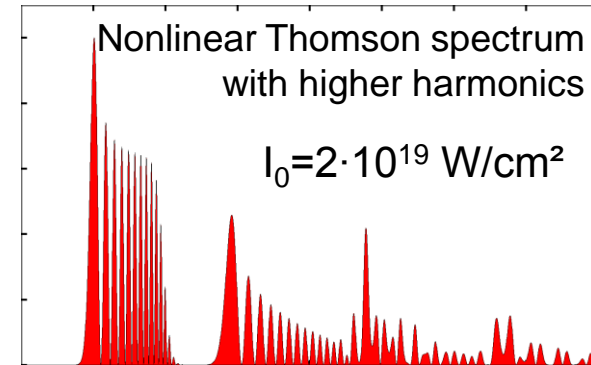
The photon yield can be improved by either increasing the intensity or the interaction duration.

①

Increase the intensity!



Maximum intensity
 $< 2 \cdot 10^{18} \text{ W/cm}^2$



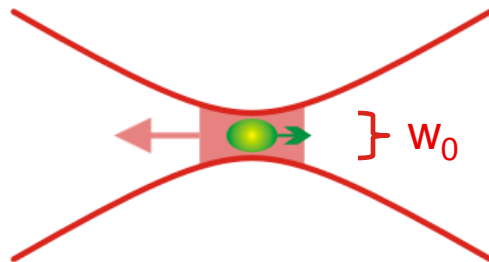
In the nonlinear Thomson regime the scattered laser energy is distributed among many higher harmonics instead only the fundamental.

Today's high-power lasers have intensities up into the 10^{21} W/cm^2 range.

②

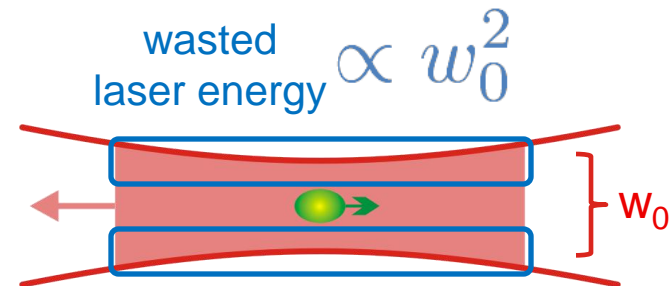
Increase the laser duration!

$$Z_0 = \frac{\pi w_0^2}{\lambda_0}$$

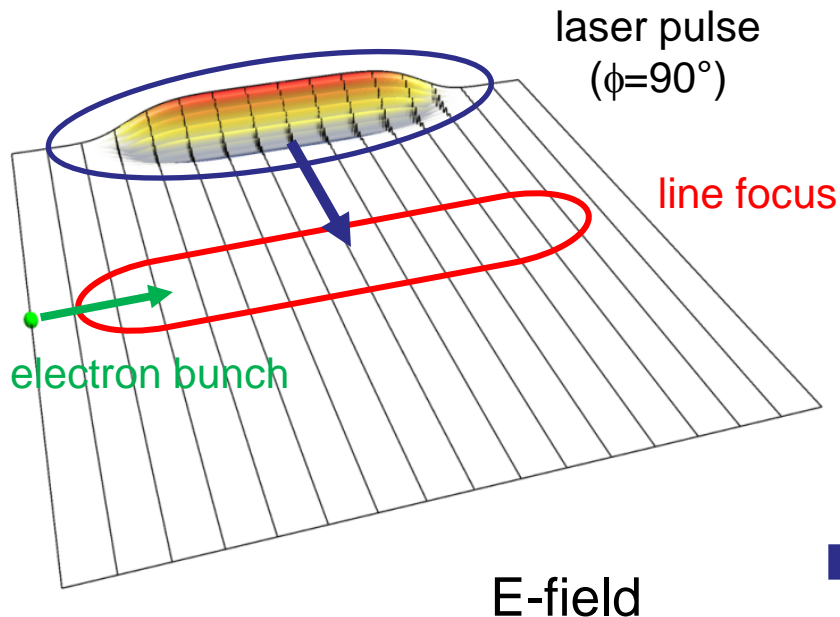


Increase laser waist

to extend Rayleigh length



Idea: In a side-scattering geometry the focus can be extended to a line



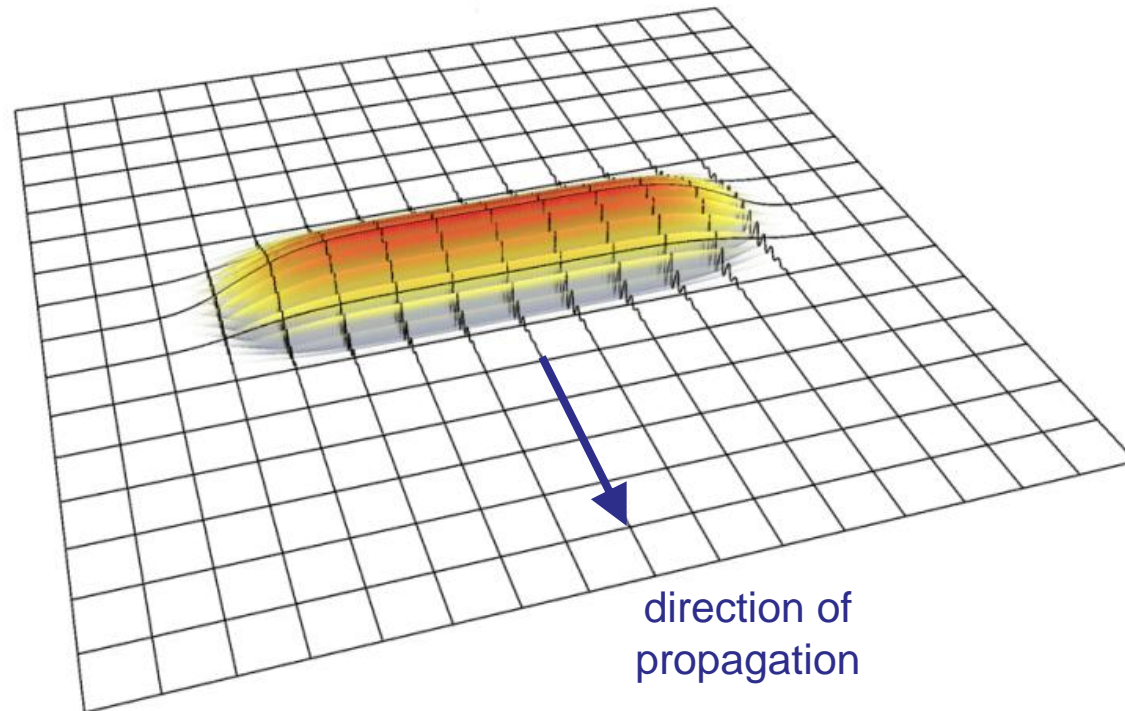
- A cylindrical mirror creates a line focus.
- Electrons propagate along this focal line. The length of that line is determined by the beam width rather than the focal properties.
- Side-scattering red-shifts the frequency of the scattered radiation.

$$\omega_{sc} = 2(1 - \beta_0 \cos \phi) \gamma^2 \cdot \omega_0$$

- Electrons remain in the focal region, but temporal overlap becomes an issue.
- Can we adjust the pulse such that all parts of the laser beam interact with the electron bunch?

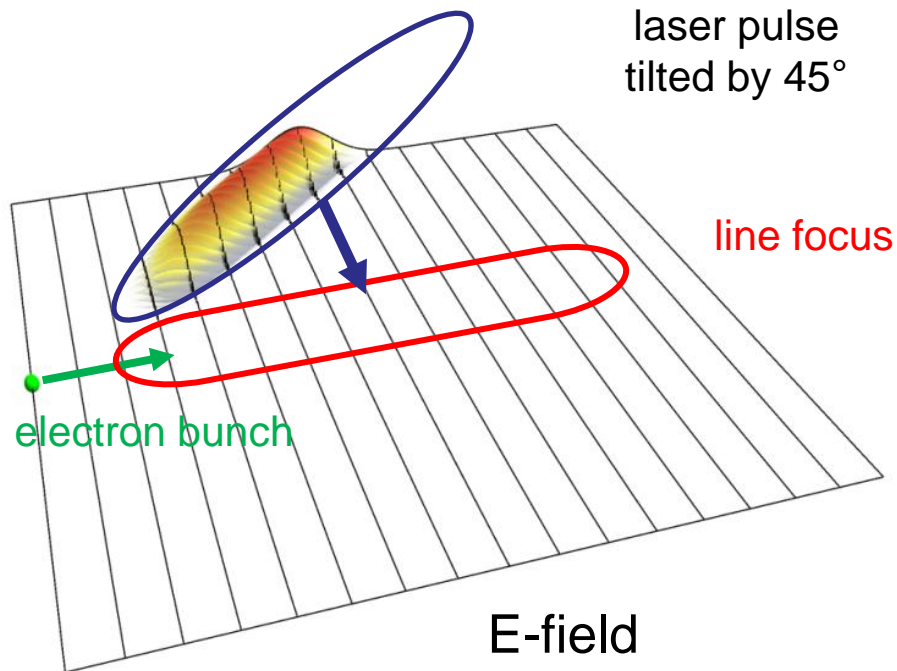
Tilt the laser pulse front to optimize temporal overlap with electrons

No pulse front tilt



- Pulse front tilts do not affect the phase fronts. Instead, the laser envelope is shifted with respect to its carrier frequency.
- At scattering angle ϕ , one needs a pulse front tilt of $\phi/2$.

Travelling-wave Thomson scattering (TWTS) provides continuous overlap with electrons

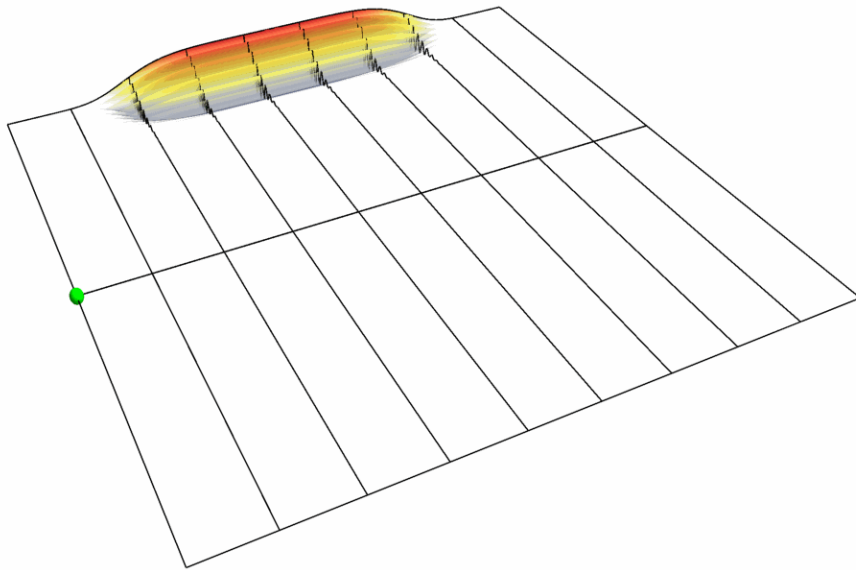


- In an extended overlap laser energy is continuously transferred into the x-ray pulse
- Both electrons and laser travel over distances much longer than the Rayleigh length.

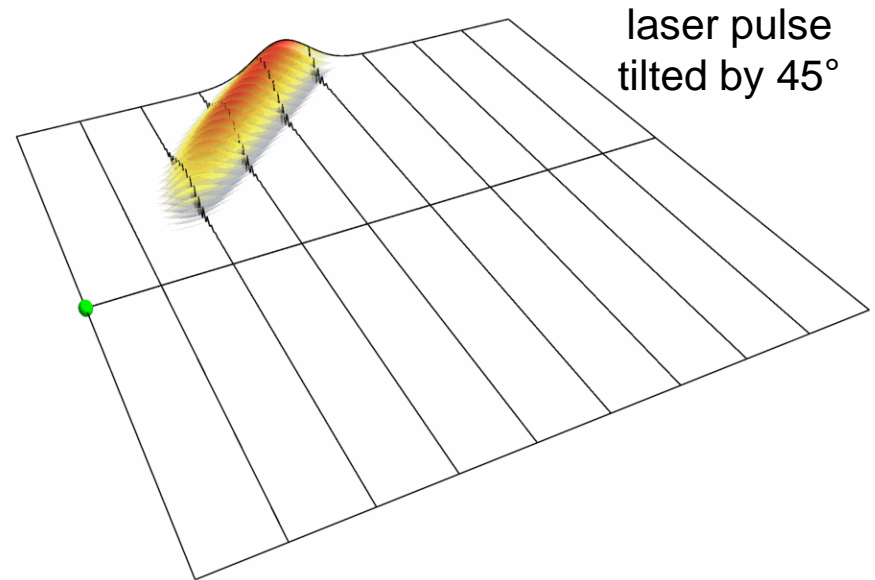
- Electrons oscillate with the carrier frequency $\omega_0 \cdot (1 - \cos\phi)$.
- Effective intensity envelope extends over the entire laser beam width.

Travelling-wave Thomson scattering (TWTS) provides continuous overlap with electrons

Partial overlap with laser



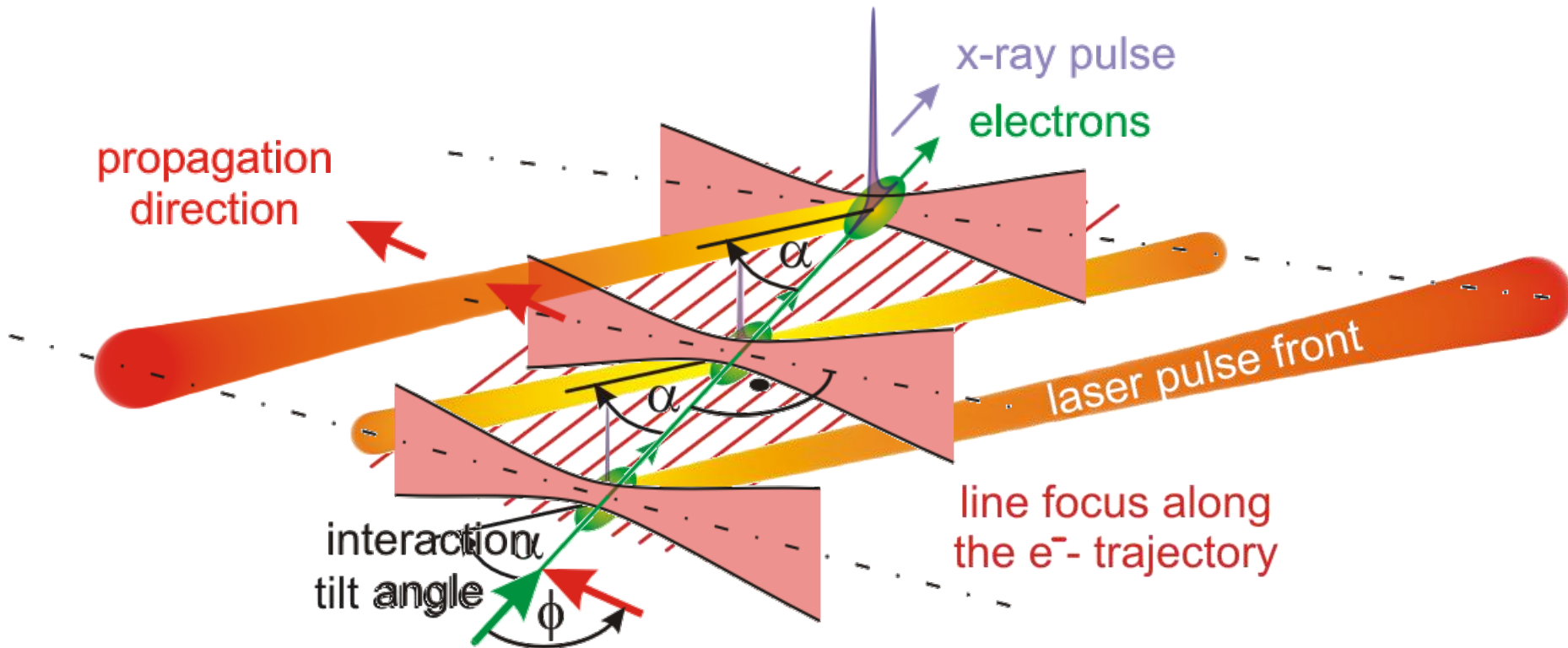
Electrons in a comoving overlap



The „Traveling-wave recipe“

2

Optimize the laser pulse energy and electron bunch length

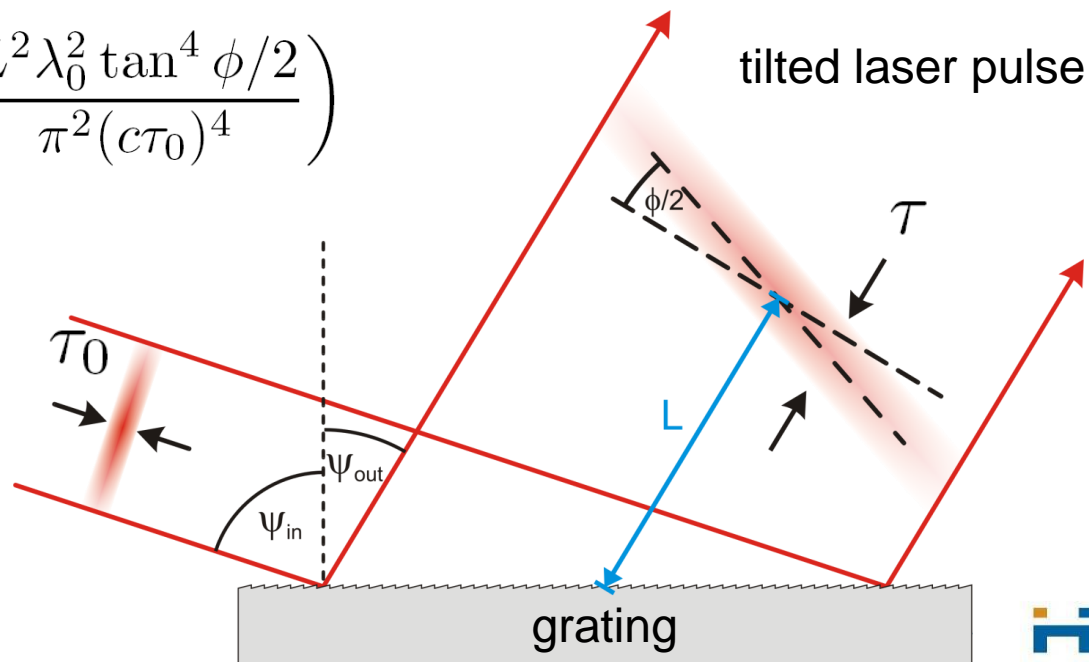


Pulse front tilts are experimentally realized using reflective gratings

pulse front tilts $\phi/2$ are connected to angular dispersion $\tan \phi/2 = \omega_0 \left| \frac{d\theta_{\text{out}}}{d\Omega} \right|_{\Omega=\omega_0}$

group delay dispersion increases pulse duration

$$\tau^2 = \tau_0^2 \left(1 + \frac{L^2 \lambda_0^2 \tan^4 \phi/2}{\pi^2 (c\tau_0)^4} \right)$$



How does a travelling-wave Thomson scattering experiment look like?

Laser provides dispersion precompensation

stretcher / compressor of laser system

$GDD \neq 0$
 $SD \neq 0$

The grating introduces a pulse front tilt

VLS grating

electrons
line focus

x-ray pulse

A varied-line spacing (VLS) adjusts higher-order dispersion

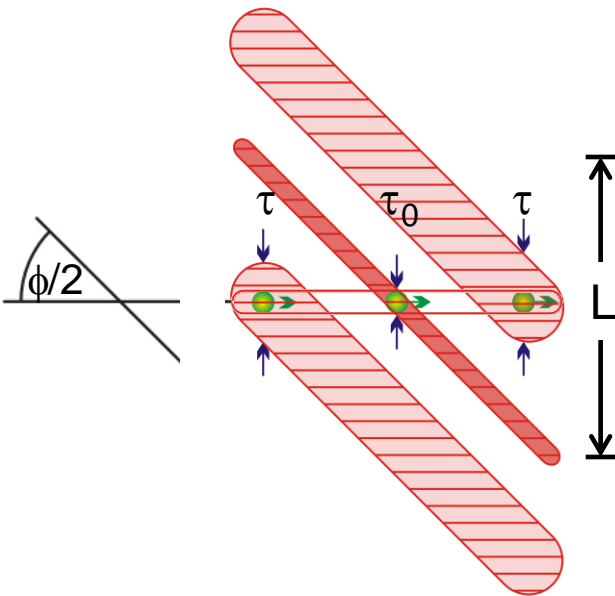
Best laser compression reached at overlap with electrons

cylindrical mirror

The cylindrical mirror focuses perpendicular to the plane of projection and creates a line focus.

Varied line-spacing gratings are essential to compensate for group delay dispersion

Best pulse compression at only one point in time.

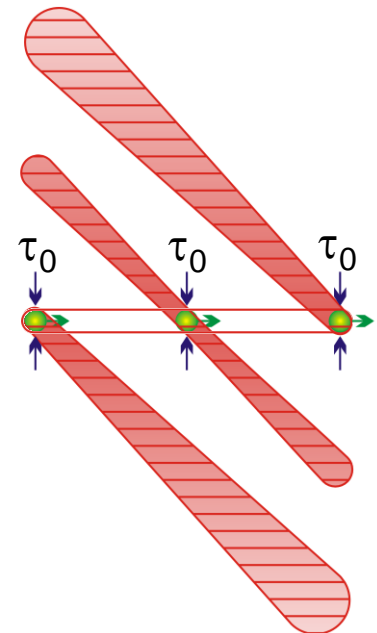


standard gratings

GDD accumulated during interaction becomes relevant for large tilt angles $\phi/2 > 10^\circ$

$$\tau^2 = \tau_0^2 \left(1 + \frac{L^2 \lambda_0^2 \tan^4 \phi/2}{\pi^2 (c\tau_0)^4} \right) > 1$$

Spatially varying dispersion compensation across the beam.



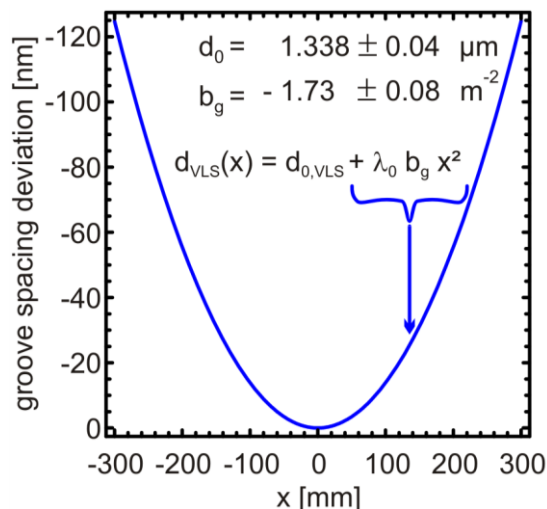
chirped grating (VLS)

How do the Varied-line spacing (VLS) gratings look like?

- Requirements along the line of interaction

- 1.) Group delay dispersion (GDD) vanishes
- 2.) Spatial dispersion (SD) vanishes
- 3.) Pulse front tilt (PFT) does not bend

- Optical setup modeled in a Raytracing framework relative to a central ray using position, angle, frequency and time delay coordinates.



A weak, nonlinear focusing term, combined with spatial dispersion leads to a position dependent angular dispersion.

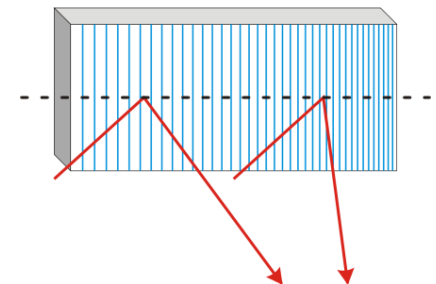
Result:

quadratic line-spacing function introduces linear variation of angular dispersion (AD)

$$d(s) = d_0 + b_g \lambda_0 s^2$$

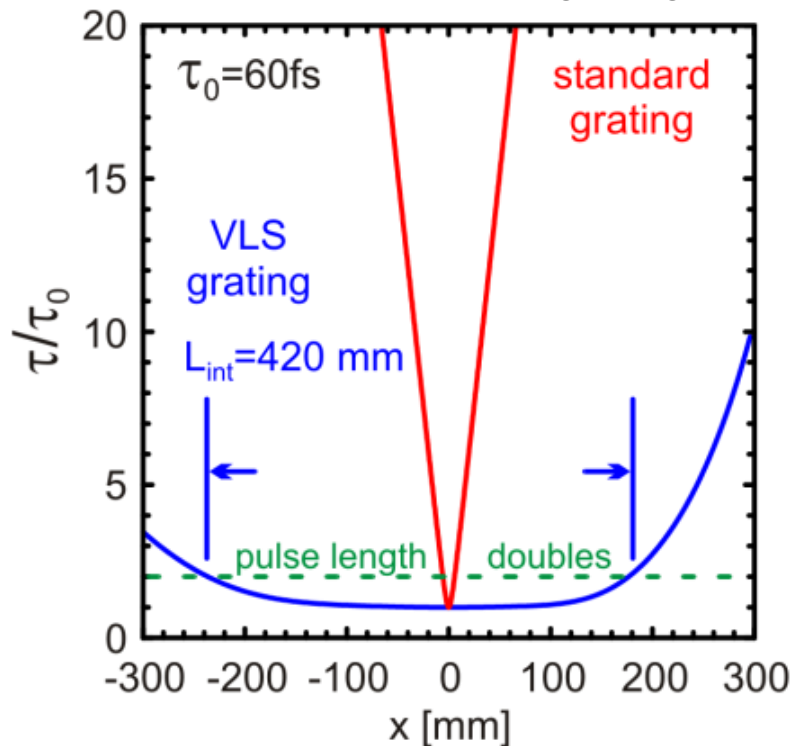
$$b_g = -\frac{\cos \psi_{\text{out}} \cdot (\tan(\pi/2 - \phi) + \tan \phi/2)}{2L_0^2 \tan^2 \phi/2}$$

$$\text{AD}(x) = \text{AD}_0 + \text{SD}_0 C_1 \cdot x$$

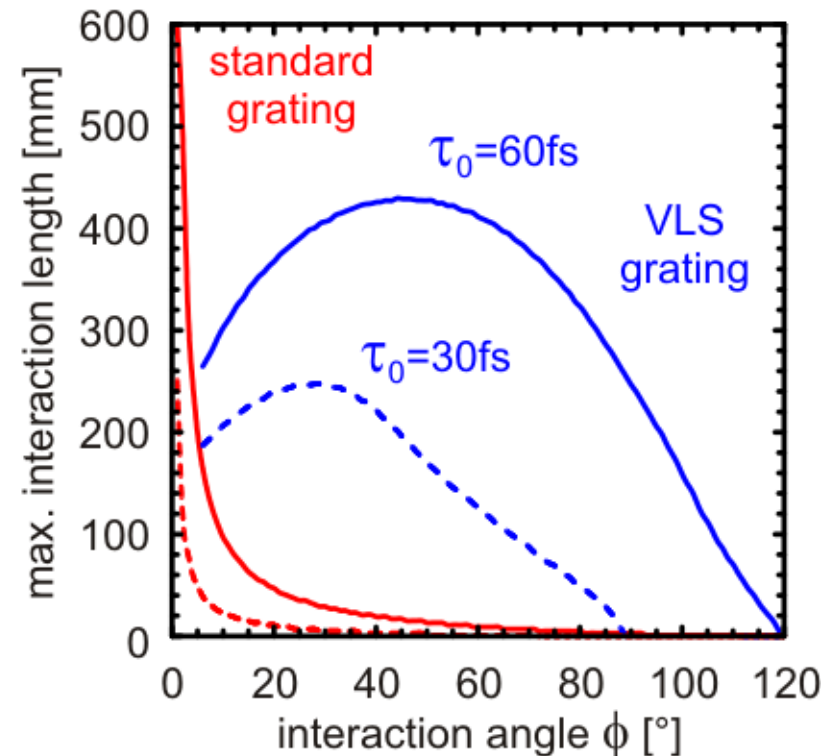


With VLS gratings long interaction lengths become possible

Calculation at $\phi=60^\circ$
standard vs. VLS grating



Maximum interaction lengths



The VLS gratings precompensate
for dispersion during the interaction !

TWTS improves per shot photon yields by orders of magnitudes

	MHz head-on ($\phi=180^\circ$)	kHz head-on ($\phi=180^\circ$)	PW-TWTS ($\phi=120^\circ$)	PW-TWTS (LWFA) ($\phi=120^\circ$)
rep. rate [Hz]	10^6	10^3	1	1
wavelength [μm]	1	0.5	1	1
W_{pulse} [mJ]	0.2	200	200×10^3	200×10^3
avg. laser power [W]	200	200	200	200
I_0 [W/cm^2]	7.9×10^{13}	7.9×10^{16}	5.5×10^{16}	5.7×10^{16}
L_{int} [mm]	0.3	1.5	57.6	200
photon energy [keV]	31	62	23	3500
$N_{\text{phot},5\%}$ per pulse	2.5×10^5	1.2×10^8	4.9×10^{10}	3.4×10^{10}

ELBE electrons

LWFA electrons
are more efficient

Electrons:

ELBE electrons: 40 MeV, 1nC, 2π mm mrad (norm. trans. emittance)

LWFA electrons: 500 MeV, 200 pC,
0.1 π mm mrad (norm. trans. emittance)

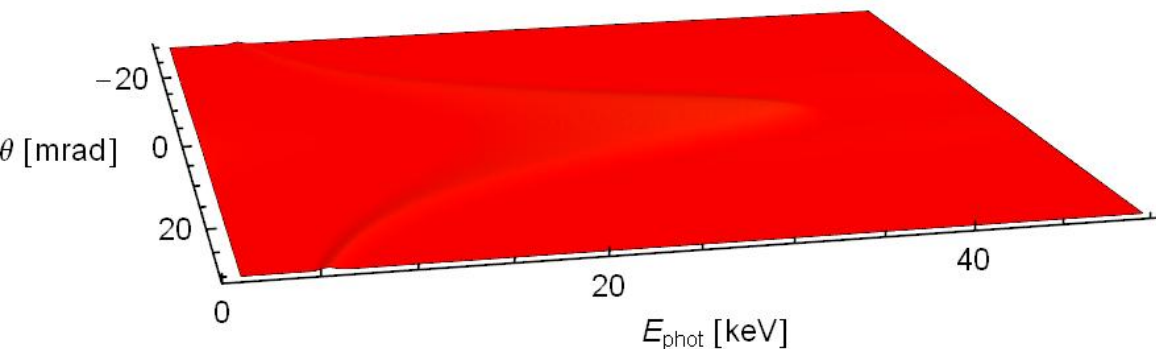
TWTS concentrates photons into the 1st harmonic

- increase interaction length
- local a_0 (intensity) is reduced
- change interaction angle
- adjust laser pulse front

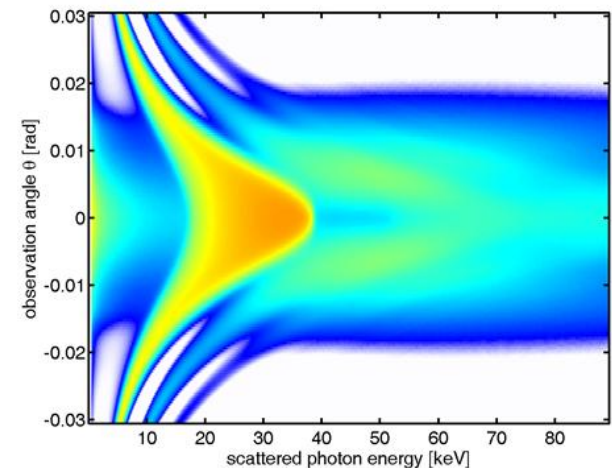
$$\omega_{sc} = \frac{2(1 - \beta_0 \cos \phi) \gamma^2 \cdot \omega_0}{1 + a_0^2/2}$$

interaction angle ϕ : 180.0 °
 interaction length: 0.006 mm
 laser strength a_0 : 1.57

$L_{int} \times 700$



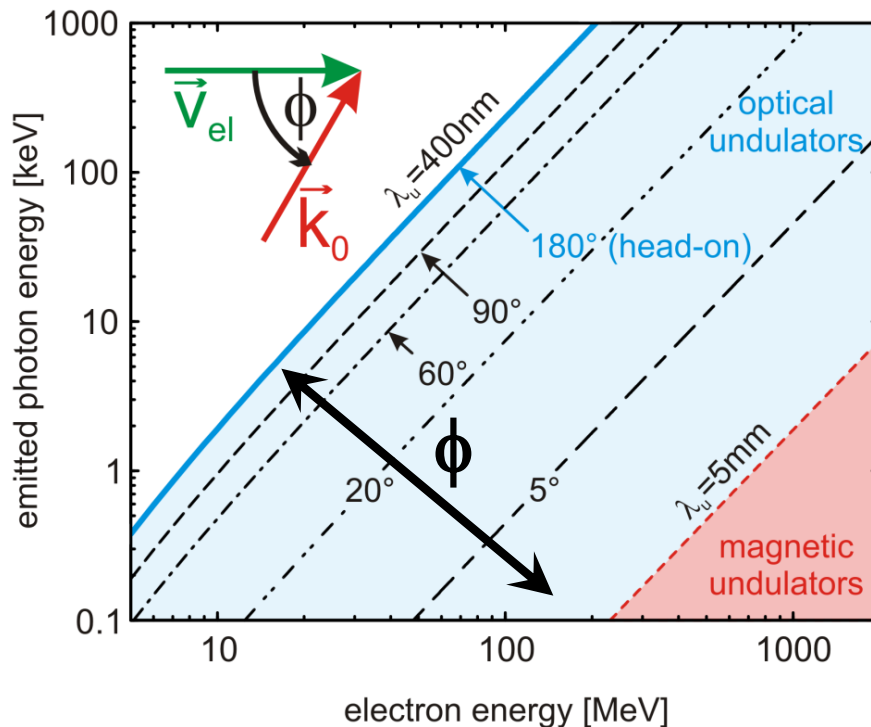
Scattering of DRACO laser at ELBE electrons



Log-scale to
visualize harmonics

Calculations from Liénert-Wiechert solver CLARA and GPT

TWTS provides control over scattered photon energy and bandwidth



photon energy

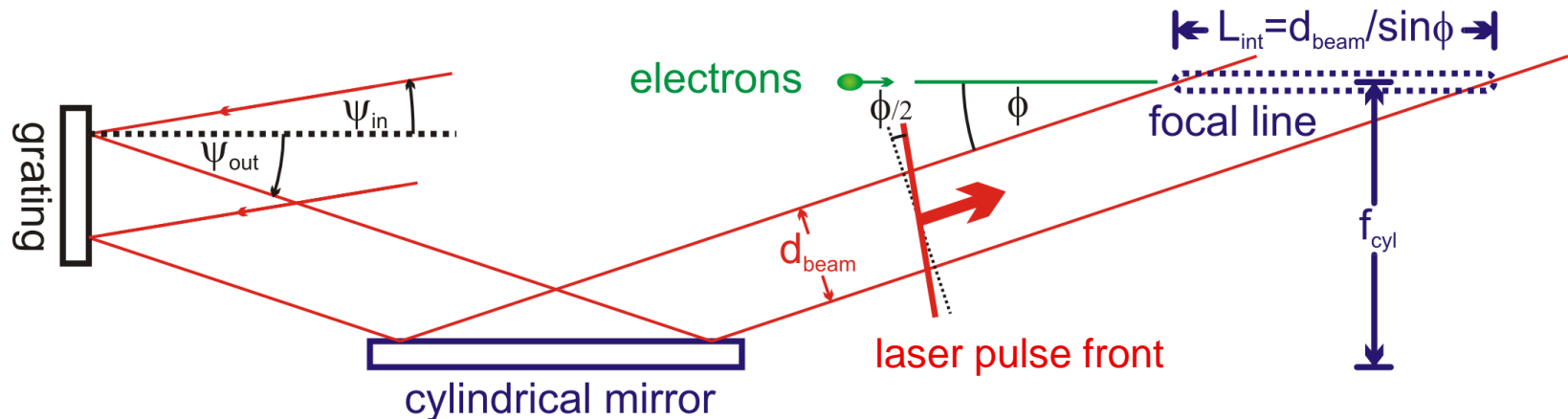
$$\omega_{\text{sc}} = 2\gamma_0^2 \omega_0 \cdot (1 - \beta_0 \cos \phi)$$

photon bandwidth

$$\begin{aligned} \Delta\omega_{\text{sc}}/\omega_{\text{sc}} &\simeq \frac{\lambda_0}{(1 - \beta_0 \cos \phi) L_{\text{int}}} \\ &= \frac{\lambda_0}{d_{\text{laser}} \sin \phi \tan(\phi/2)} \end{aligned}$$

L_{int} ... interaction length

For small interaction angles $\phi < 10^\circ$ angular dispersion becomes negligible, so standard gratings are fine!



$$\lambda_0 = 800 \text{ nm}, d_{\text{beam}} = 10 \text{ cm}, \phi = 7^\circ$$

$$\rightarrow L_{\text{int}} = 82 \text{ cm} \quad \text{and} \quad 3.5^\circ \text{ pulse front tilt}$$

$$\text{Effective undulator period } \lambda_{\text{eff}} = 0.1 \text{ mm}$$

Using existing multi-100 TW lasers it is possible to create such line foci with $a_0 = 0.01 - 0.1$.



Could this lead to a TWTS-FEL?

Could TWTS be an optical free-electron laser?

effective undulator wavelength
& resonant wavelength

$$\lambda_u = \lambda_0 / (1 - \beta_0 \cos \phi)$$

$$\lambda_r = \frac{\lambda_u}{2\gamma^2}$$

FEL parameter

$$\rho = \frac{1}{2\gamma} \left(\frac{I}{I_A} \left(\frac{\lambda_u a_0}{2\sqrt{2}\pi\sigma} \right)^2 \right)^{1/3}$$

gain length

$$L_{\text{gain}} = \frac{\lambda_u}{4\pi\sqrt{3}\rho}$$

Lasers provide short „undulator“ wavelengths, so XUV/X-Ray wavelengths can be achieved at moderate energies.

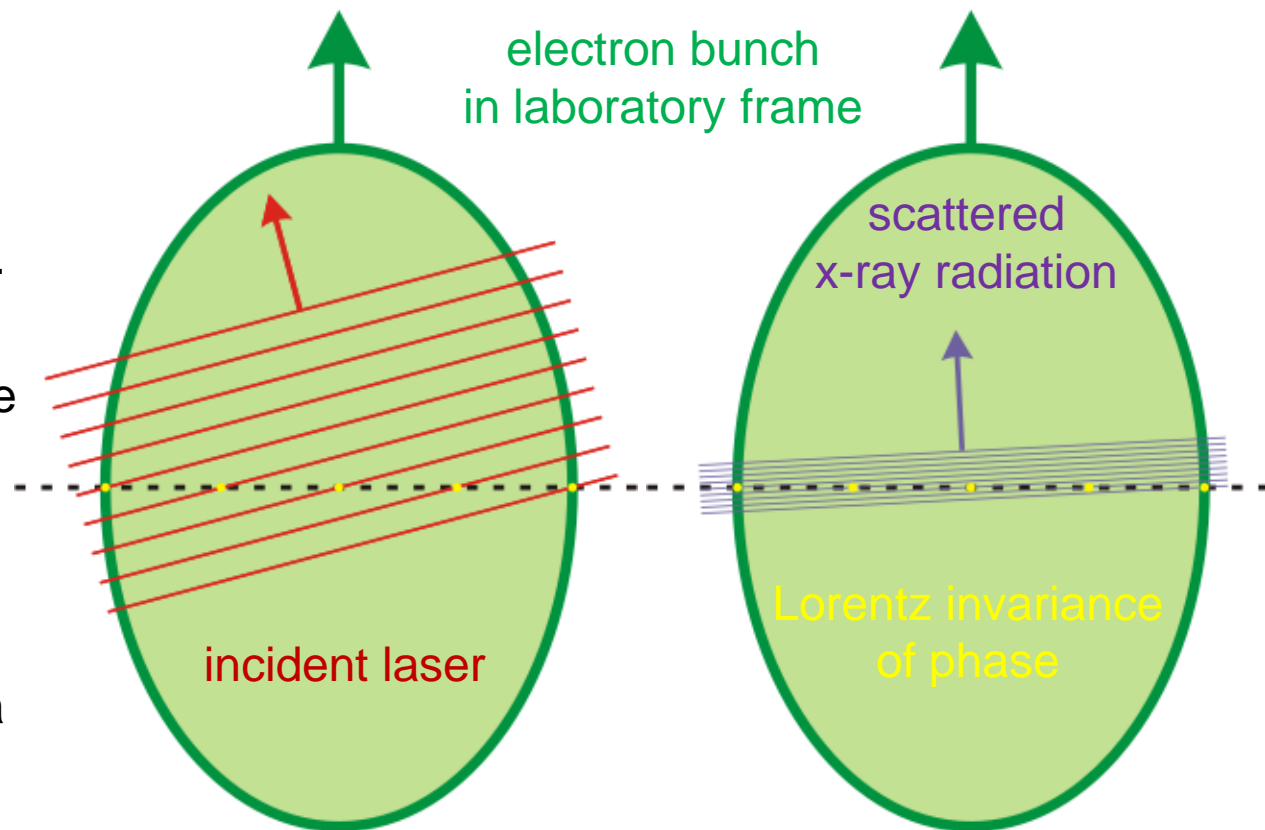
The resulting small γ allows for FEL operation with small undulator wavelengths λ_u and laser strengths a_0 .

λ_u in the sub-mm range and ρ from 10^{-4} to 10^{-3} lead to cm-scale gain lengths.

- Compact FEL - could fit into a laboratory.
- TWTS enables the interaction distances required to enter the FEL regime.
- No issues with field errors or wall wakefields.

What is the effect of side scattering in a TWTS-FEL?

- Each electron emits in propagation direction.
- Plane waves, when electrons emit coherently.
- For TWTS the plane wave propagates at an angle.
- Condition against radiation „leaking“ out of the interaction area



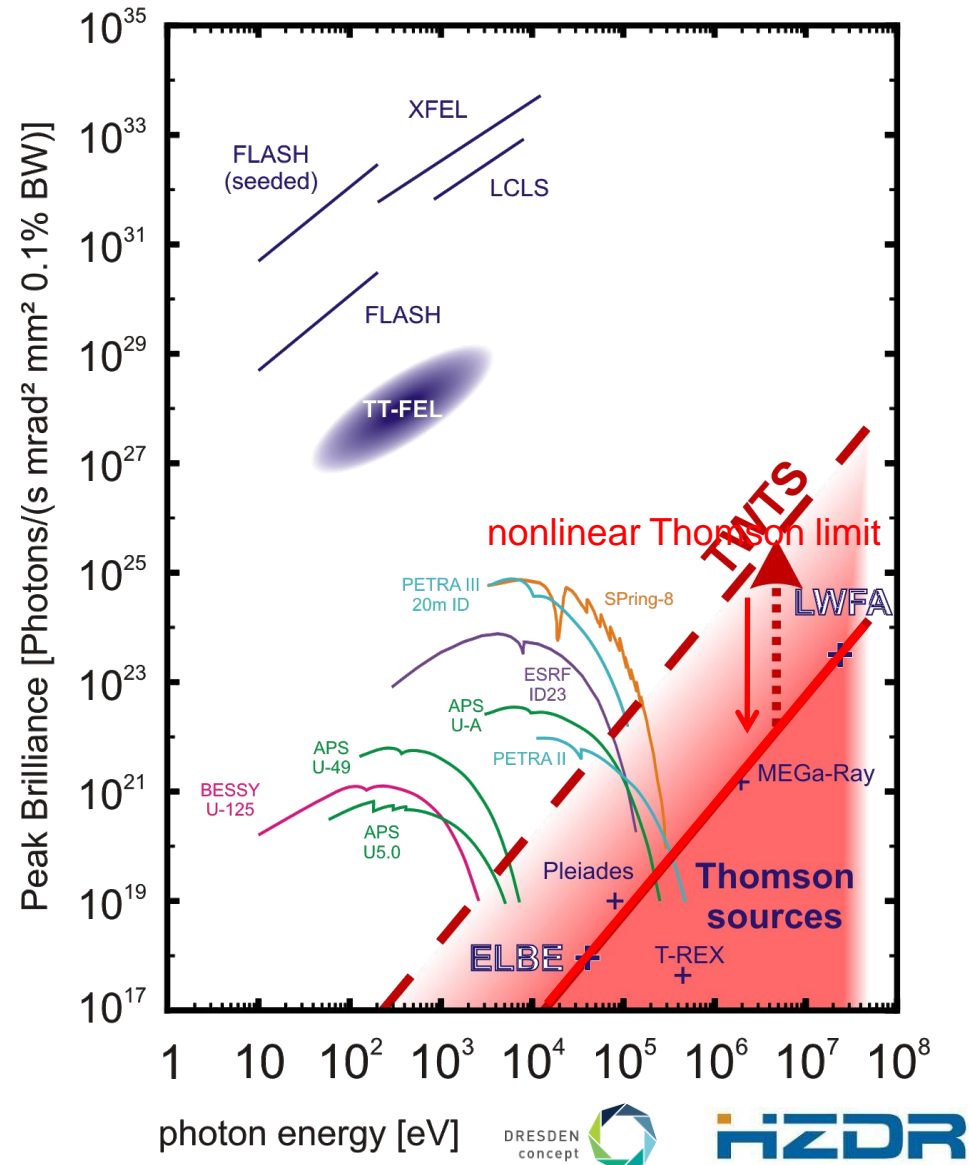
$$\tan \phi_{\text{res}} \cdot L_{\text{gain}} \ll d_{\text{bunch}}$$

$$\leftarrow d_{\text{bunch}} \rightarrow$$

$$\tan \phi_{\text{res}} = \frac{\tan \phi}{2\gamma^2(1 - \beta \cos \phi)}$$

TWTS opens a path towards brilliant X-ray sources

- „Head-on“ Thomson sources are limited in peak brilliance by nonlinear Thomson scattering.
 - TWTS sources can increase peak brilliances in the X-ray range by 2-3 orders of magnitudes.
 - The brilliance limit using TWTS is purely technical.
- It arises from electron divergence, size of optics and available laser power.



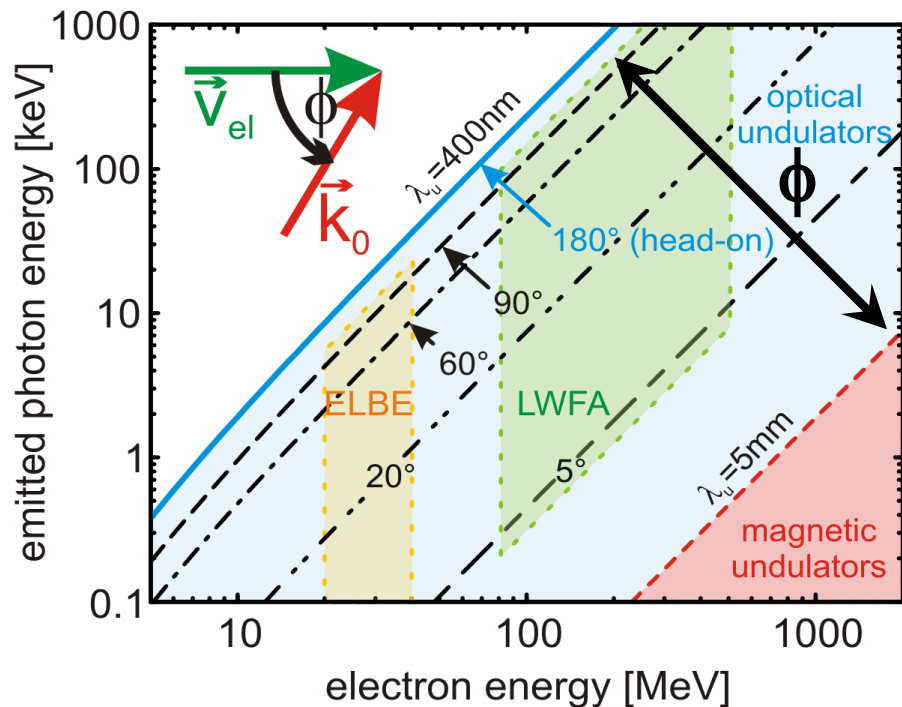
Conclusions

- Travelling-wave Thomson scattering circumvents the Rayleigh limit for both small interaction diameters and long interaction distances.
- Flexibility of interaction angle between laser and electron beams enables adjustments in the effective optical undulator periodicity without negatively impacting beam overlap.
- TWTS surpasses existing Thomson scattering designs by several orders of magnitude and could bring high-yield sources ($\sim 10^{10}$ photons/pulse) to the keV and MeV energy range.
- The scattering setup itself is quite general and is interesting for many other applications.

A.D. Debus, M. Bussmann, M. Siebold, A. Jochmann, U. Schramm, T.E. Cowan, and R. Sauerbrey
"Traveling-wave Thomson scattering and optical undulators for high-yield EUV and X-ray sources"
Applied Physics B **100**, 61-76 (2010)



TWTS provides control over scattered photon energy and bandwidth



photon energy

$$\omega_{\text{sc}} = 2\gamma_0^2 \omega_0 \cdot (1 - \beta_0 \cos \phi)$$

photon bandwidth

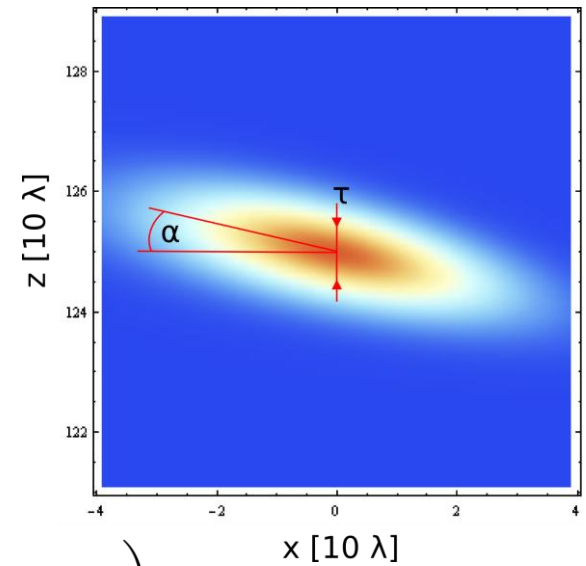
$$\begin{aligned} \Delta\omega_{\text{sc}}/\omega_{\text{sc}} &\simeq \frac{\lambda_0}{(1 - \beta_0 \cos \phi) L_{\text{int}}} \\ &= \frac{\lambda_0}{d_{\text{laser}} \sin \phi \tan(\phi/2)} \end{aligned}$$

L_{int} ... interaction length

The Rayleigh-Sommerfeld diffraction integral yields a wave optical description of the laser pulse behind a VLS grating

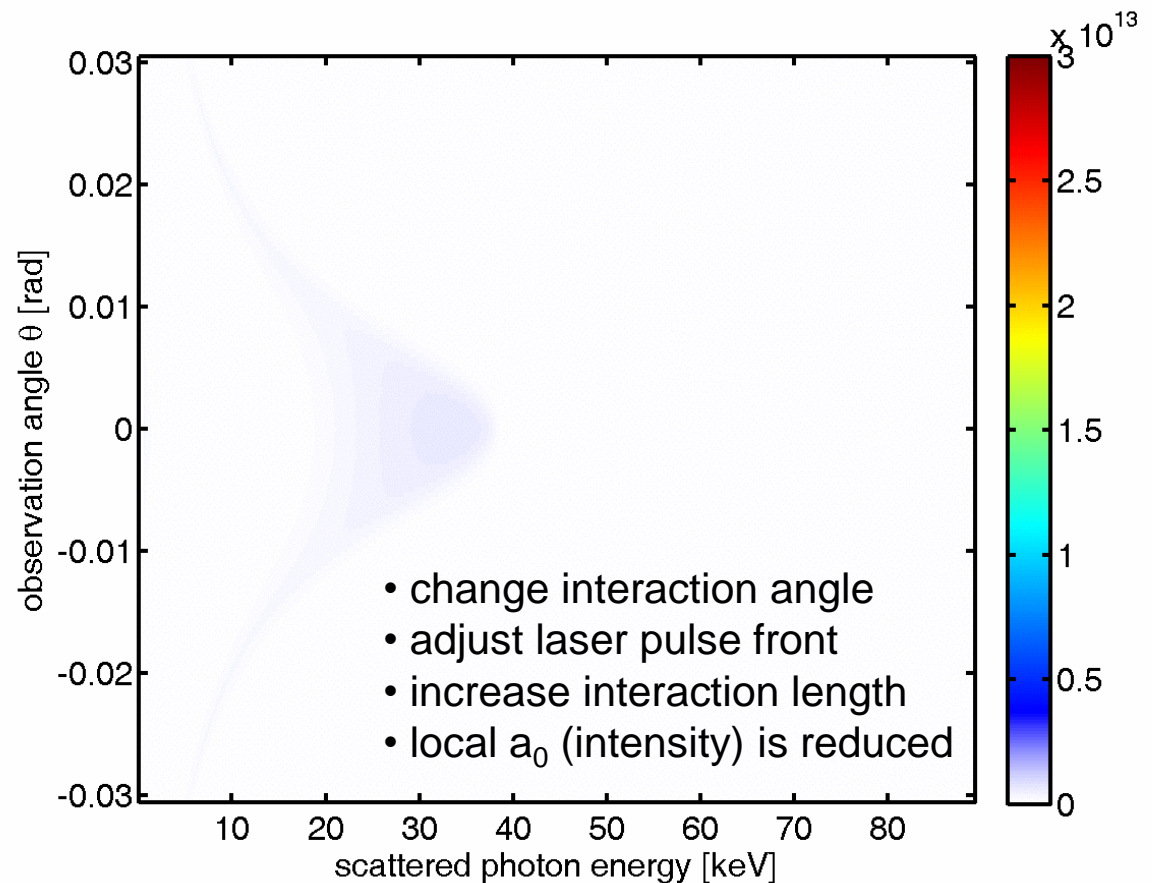
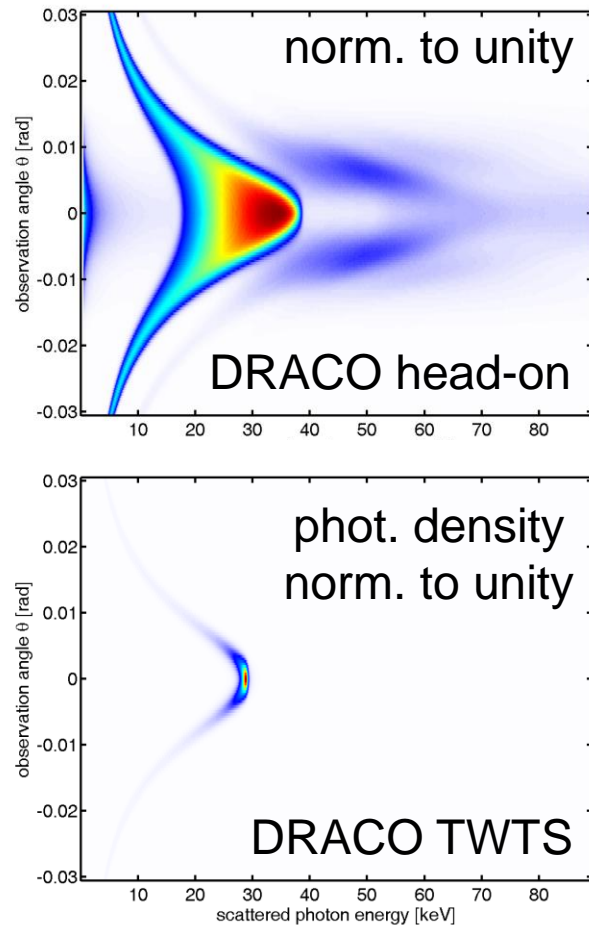
$$\begin{aligned}
 E_{\text{out}}(x, y, z, t)|_{\xi_k > 0} &= \sum_{k=1}^l i \frac{e^{-i\frac{1}{4}\pi}}{\sqrt{2\pi}} \frac{d_0}{\sqrt{c}} \times \\
 &\times \frac{e^{-\frac{(\xi_k \cos \psi_{\text{in}})^2}{w_0'^2}}}{\sqrt{\Omega_0 \tau'^2 + \frac{4SD}{w_0^2} \xi_k \cos \psi_{\text{in}}}} e^{i\frac{\Omega_0^2}{c} AD \xi_k \cos \psi_{\text{in}}} \times \\
 &\times \sqrt{\frac{w_{y,0}}{w_y(z - z_F)}} e^{i\zeta_y(z - z_F)/2} e^{-\frac{y^2}{w_y(z - z_F)^2}} \times \\
 &\times z \cdot e^{-\frac{G_k^2}{\tau'^2}} \frac{e^{-i\left(\Omega_0 \tau'^2 + \frac{4SD}{w_0^2} \xi_k \cos \psi_{\text{in}}\right) \frac{G_k}{\tau'^2}}}{(z^2 + (x - \xi_k)^2)^{3/4}} \left(\Omega_0 \tau'^2 + \frac{4SD}{w_0^2} \xi_k \cos \psi_{\text{in}} - iG_k \right)
 \end{aligned}$$

$$\begin{aligned}
 G_k = G_k(x, z, y, t) &= \frac{1}{c} \left\{ [z^2 + (x - \xi_k)^2]^{1/2} - \xi_k \sin \psi_{\text{in}} + z_0 \right. \\
 &\quad \left. + \frac{y^2}{2R_y(z - z_F)} + \Omega_0 AD \xi_k \cos \psi_{\text{in}} - ct \right\}
 \end{aligned}$$



Traveling-wave Thomson Scattering

TWTS puts all photons into a single harmonic



Laser driven SASE-FEL using ELBE electrons

	FLASH	TWTS	
FEL wavelength [nm]	13.0	13.0	Scalings according to 1D-theory
peak current [kA]	2.5	10.0	
bunch duration [fs]	393	100	
a_0	1.2	0.02	$8.7 \times 10^{14} \text{ W/cm}^2$ in a focal line of 80 cm A free-electron laser made more compact !
electron energy [MeV]	1000	40	
und. period [mm]	27.3	0.16	
gain length [m]	2.55	0.074	
interaction length [m]	27	0.8	
FEL parameter	9.8×10^{-4}	2.0×10^{-4}	
peak power [MW]	2.5×10^3	80	yield: $5.2 \cdot 10^{11}$ photons

TWTS parameters: $\lambda_0=800 \text{ nm}$; $P_{\text{laser}}=84 \text{ TW}$; $d_{\text{beam}}=120\mu\text{m}$ (FWHM) ; $\tau_{\text{laser}}=100\text{fs}$; $\phi=5.69^\circ$

Scaling Laws

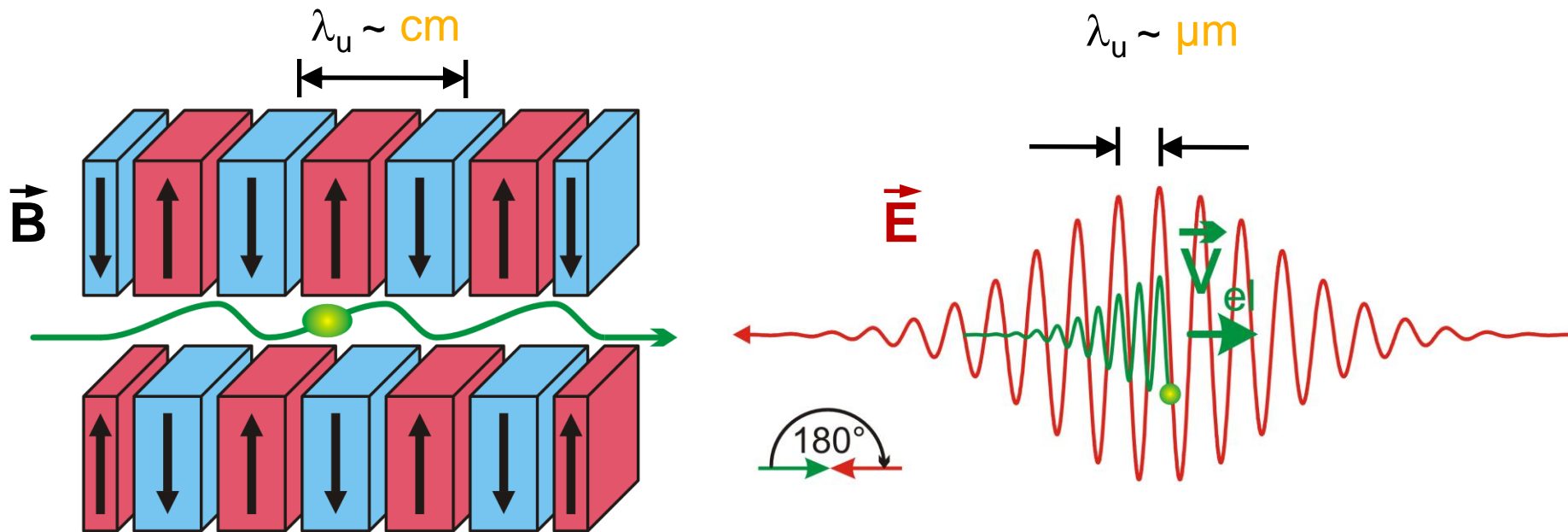
- Interaction angle
- radiated photon energy
- Tilted pulse front
- Interaction length defines minimum attainable bandwidth
- Pulse duration determined by electron bunch

- FEL resonance for sidescattering
- Lasers need to fulfill to intensity conditions

$$\lambda_r = \frac{\lambda_0}{2\gamma^2 \cdot (1 - \beta \cos \phi)} \cdot \left(1 + \frac{1}{\gamma^2 \phi^2}\right)$$

$$\frac{1}{1 + a_0^2/2} (a_0 \cdot \delta a + \delta a^2/2) \ll 2\rho$$

Magnetic undulators and optical undulators are (almost) the same



undulator parameter K

$$K = 0.93 \lambda_u [\text{cm}] B_0 [\text{T}]$$



laser strength parameter a_0

$$a_0 = 0.85 \cdot 10^{-9} \lambda_0 [\mu\text{m}] I_0^{1/2} [\text{W}/\text{cm}^2]$$

$$I_0 \sim 10^{20} \text{ W} / \text{cm}^2$$

How do the Varied-line spacing (VLS) gratings look like?

- Requirements along the line of interaction
 - 1.) Group delay dispersion (GDD) vanishes
 - 2.) Spatial dispersion (SD) vanishes
 - 3.) Pulse front tilt (PFT) does not bend
- Optical setup modeled in a Raytracing framework relative to a central ray using position, angle, frequency and time delay coordinates.
- Standard gratings
 - ➔ Kostenbauder matrix formalism (cite it)
- VLS gratings
 - ➔ nonlinear formalism required
 - ➔ extended Kostenbauder to higher orders using operators instead of matrices
 - ➔ Rather technical and „messy“.

See paper for details.

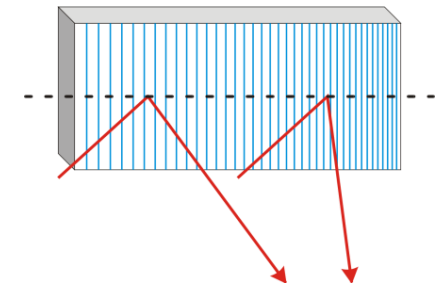
Result:

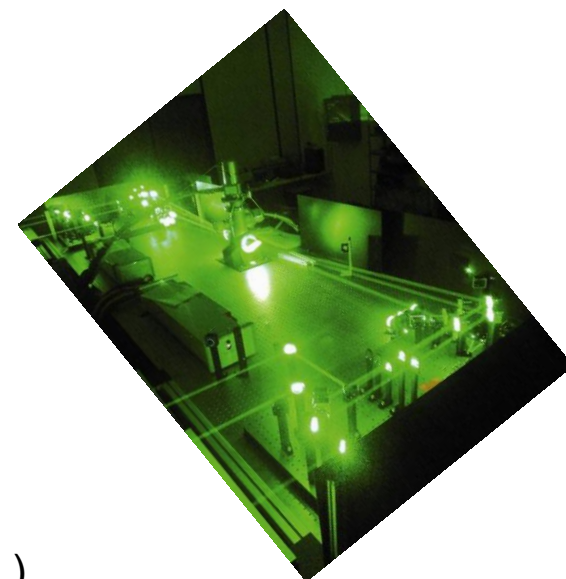
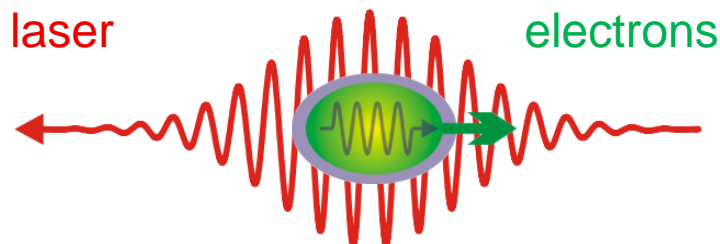
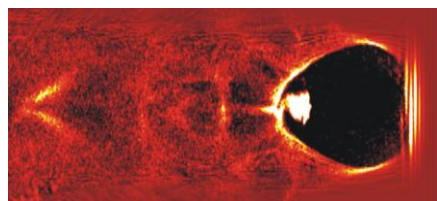
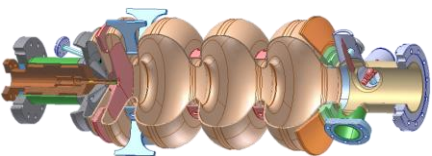
quadratic line-spacing function
introduces linear variation of
angular dispersion (AD)

$$d(s) = d_0 + b_g \lambda_0 s^2$$

$$b_g = -\frac{\cos \psi_{\text{out}} \cdot (\tan(\pi/2 - \phi) + \tan \phi/2)}{2L_0^2 \tan^2 \phi/2}$$

$$\text{AD}(x) = \text{AD}_0 + \text{SD}_0 C_1 \cdot x$$





- Thomson Scattering Facilities (T-REX, NewSUBARU, COBALD, ...)

photon energy	$\sim 10 \text{ keV} - 10 \text{ MeV}$	pulse duration	$\sim 100\text{fs} - 10\text{ps}$
photon yield	$\sim 10^5 - 10^6 \text{ photons / pulse}$	spectral width	$\sim 10^{-2}$

Most Thomson sources worldwide aim for high repetition rates to maximize average photon flux.

Laser-wakefield accelerated electrons are ultrashort $<10 \text{ fs}$ and have small emittances below $\epsilon_{n,\text{rms}}=1.0 \pi \text{ mm mrad}$.

Head-on Thomson Scattering produces ultrashort X-ray pulses

