



# Production of $b$ & $c$ and Quarkonia Physics with CMS

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*on behalf of the  
CMS Collaboration*

FPCP2011  
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# Summary

- LHC and CMS at Glance
- Heavy Flavour Physics  
Main Features and Reasons of Interest
- $J/\psi$  and  $Y$  production
- B Physics Analyses:  
Features and Findings
- Challenges and Prospects for the Future
- Conclusions

# The LHC accelerator

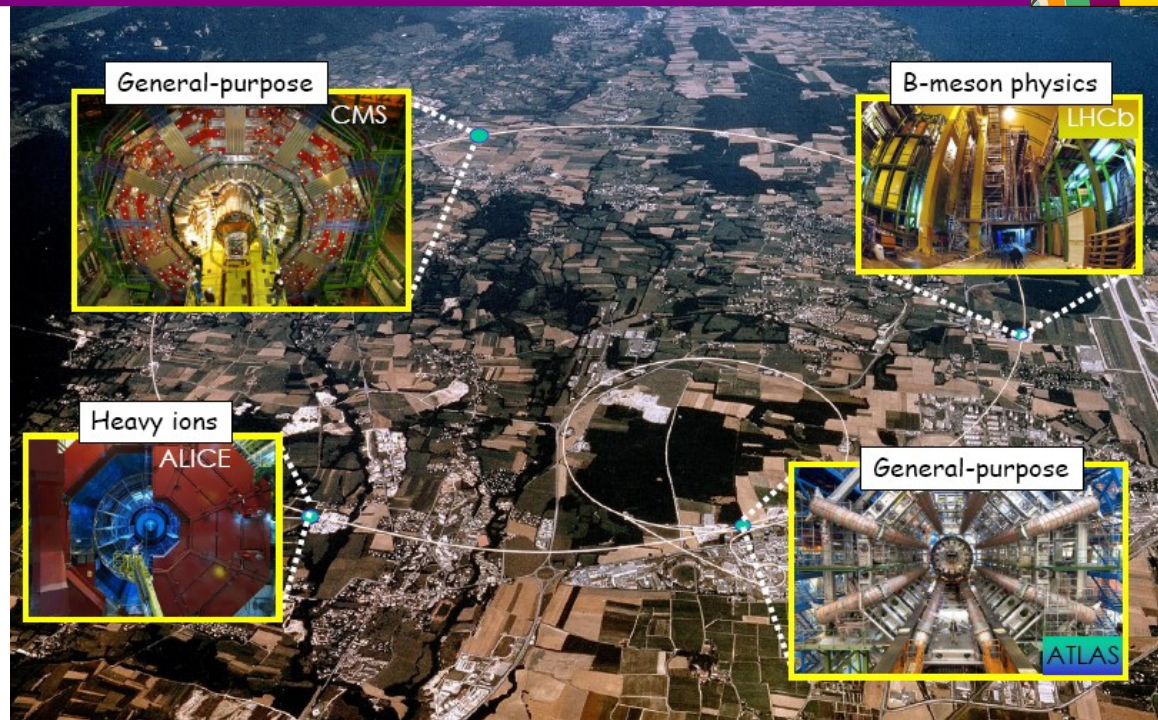


Excellent performances of the machine running smoothly @ 7 TeV since 2010

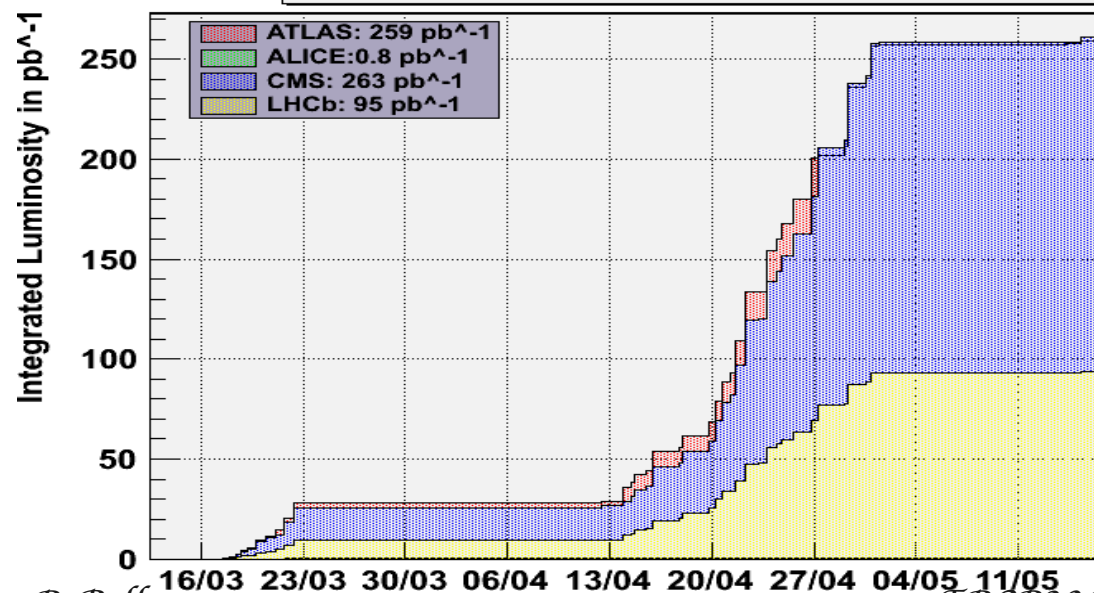
Instantaneous luminosity already reached  $8.4 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$

Current records:

768 proton bunches circulating,  
with  $1.7 \cdot 10^{11}$  protons/bunch;  
time spacing 50 ns



2011 Luminosity Production



47  $\text{pb}^{-1}$  delivered to CMS by the end of the 2010 pp run;

In 2011,  $\sim 250 \text{ pb}^{-1}$  up to mid of May;

Overall CMS data taking efficiency  $> 90\%$ ;

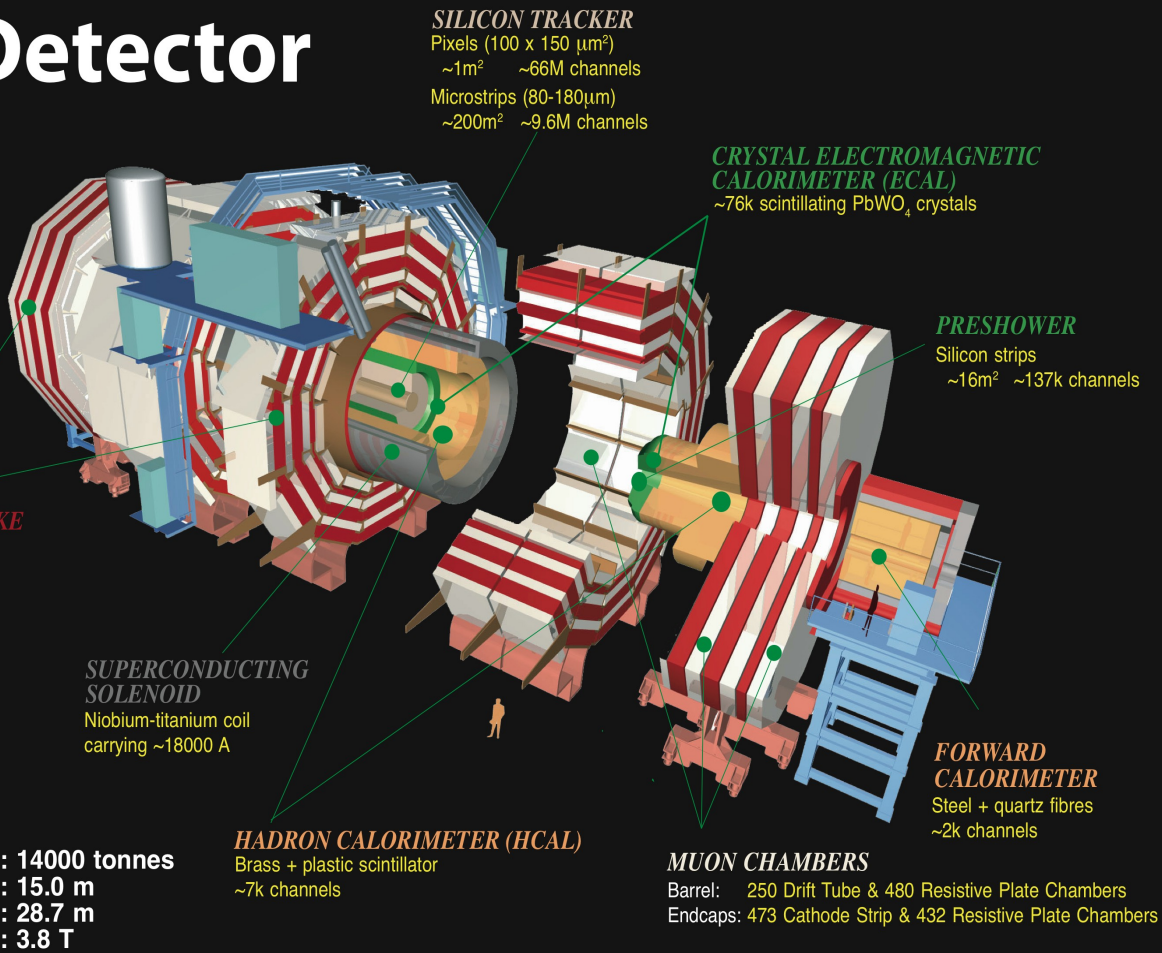


# The CMS Collaboration



3170 Physicist and engineers, 169 institutes from 39 countries

## CMS Detector



- Highly redundant muon system, triggering and recording muons with  $p_T > 1\text{-}3 \text{ GeV}$  and  $|\eta| < 2.4$
- Tracking efficiency  $> 99\%$  for central muons

4 T solenoid + return yoke

Si pixels, strips  
 $\sigma/p_T \approx 1.5 \times 10^{-4} p_T + 0.005$

PbWO<sub>4</sub> crystals  
 $\sigma/E \approx 3\%/\sqrt{E} + 0.003$

Brass+scintillator (7  $\lambda$  + catcher)  
 $\sigma/E \approx 100\%/\sqrt{E} + 0.05 \text{ GeV}$

$\sigma/p_T \approx 1\% @ 50\text{GeV}$  to  $10\% @ 1\text{TeV}$   
(DT/CSC+Tracker)

L1+HLT (L2 + L3)

All silicon inner tracker allowing good resolution on  $p_T$  and impact parameter measurements

B-hadron reconstruction mainly exploits:

- Muon detectors, for muon ID in semi-leptonic decays;
- Silicon Tracker detector, for b-tagging, lifetime measurements and inv. mass reconstruction. 3

# HF Physics: topics and reasons of interest (I)

## Open beauty Production

A testing bed for QCD;  
calculations scale up to a new energy regime

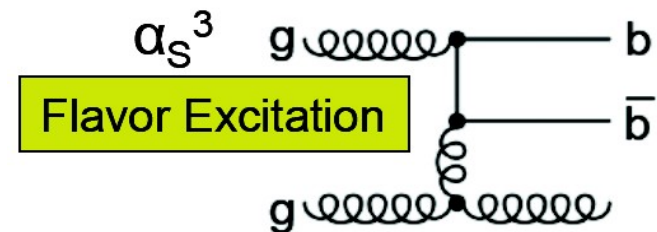
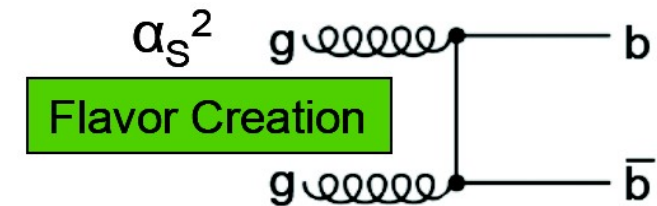
- NLO contributions essential at LHC;
- High energy scale makes perturbation calculations safe;
- Large uncertainties from factorization and renormalization scales.

## b physics

- Very active research field, either experimentally and theoretically;
- Allows testing the CP and Flavour violation;
- Interesting challenge with B-factories in some topics.

## b-jets

- Enclosing most of the radiation emitted by the b-quark → reliable messenger of the original parton, allowing purely perturbative predictions;
- High performance of tracking capabilities required, exploiting full detector potentialities;
- Measurements complementary to b-hadrons;
- Crucial role in many new physics studies.



## Many results from CMS:

- $J/\psi$  and  $Y$  production
- Inclusive b production,  $bb$  angular correlations
- Exclusive  $B^+$ ,  $B^0$ ,  $B_s$  production

# HF Physics: topics and reasons of interest (II)

## Quarkonia Physics

### Strong test for:

- non-relativistic QCD (NRQCD);
- models calculation methods describing the long-distance interaction and the bound state formation.

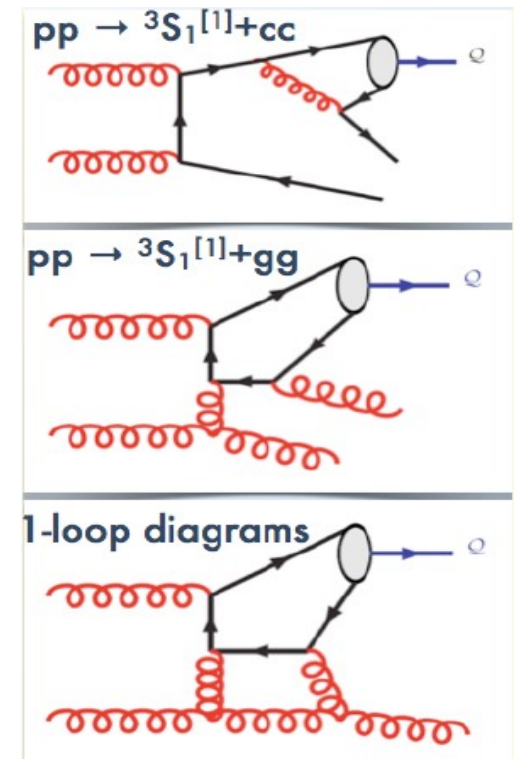
### J/ψ 'troubles'

#### Production mechanisms:

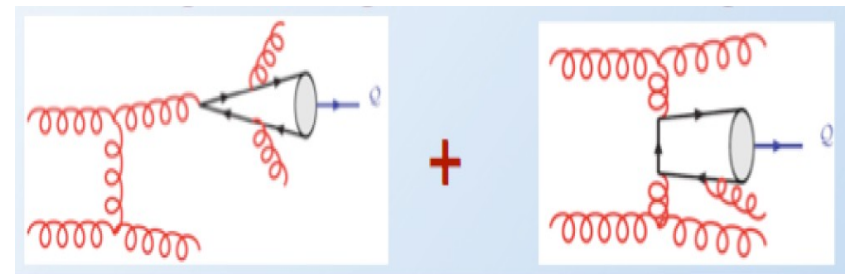
- to be fully understood yet
- role for higher order vs color-octet contributions unclear

### Polarization issues

- Predictions of some models for the J/ψ's polarization at large  $p_T$  not confirmed by HERA/Tevatron data;
  - Apparent inconsistencies among experiments.
- 
- Interesting to analyse the Y polarization behaviour;
  - Possibility to cross-check some measurements with b-jets (e.g. non-prompt J/ψ for bb cross sect.)



*NLO Singlet contributions*



*"NNLO" Singlet contributions*

# J/ψ production

Eur.Phys.J. C71 (2011) 1575

- Reconstructing J/ψ decaying in two muons
- Cross section determined in  $p_T$  and  $y$  intervals
- Muon momentum corrected for scale distortion through a fit on the invariant mass peak shape
- Yields corrected for **acceptance** and **efficiency**:

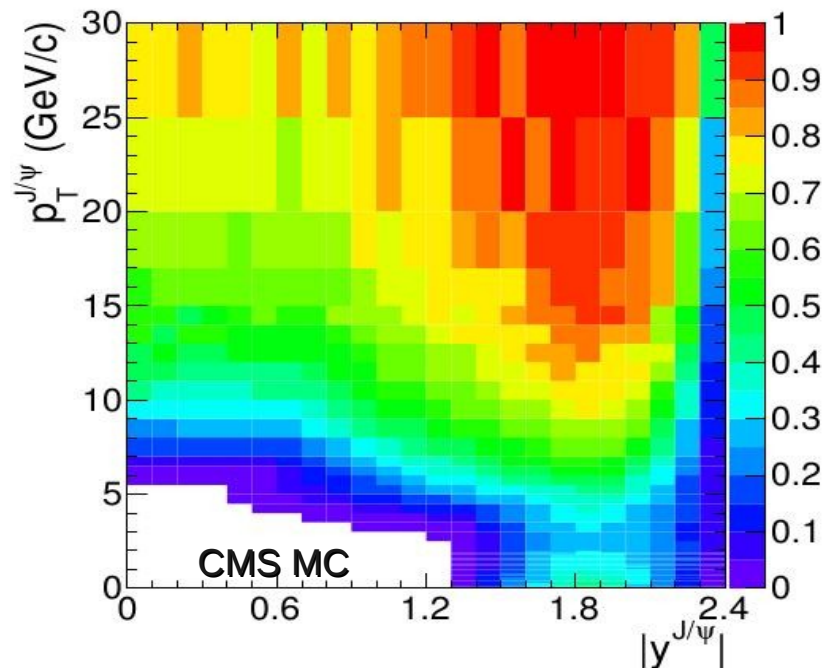
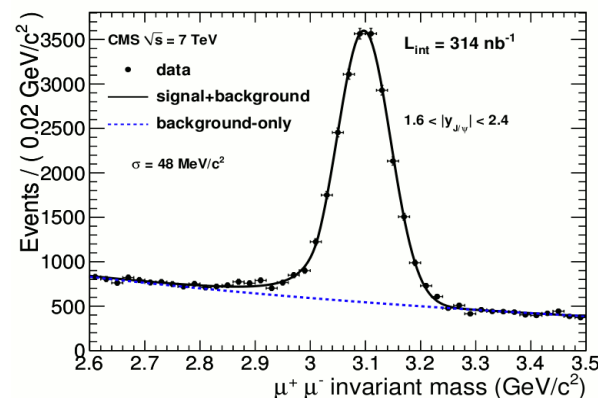
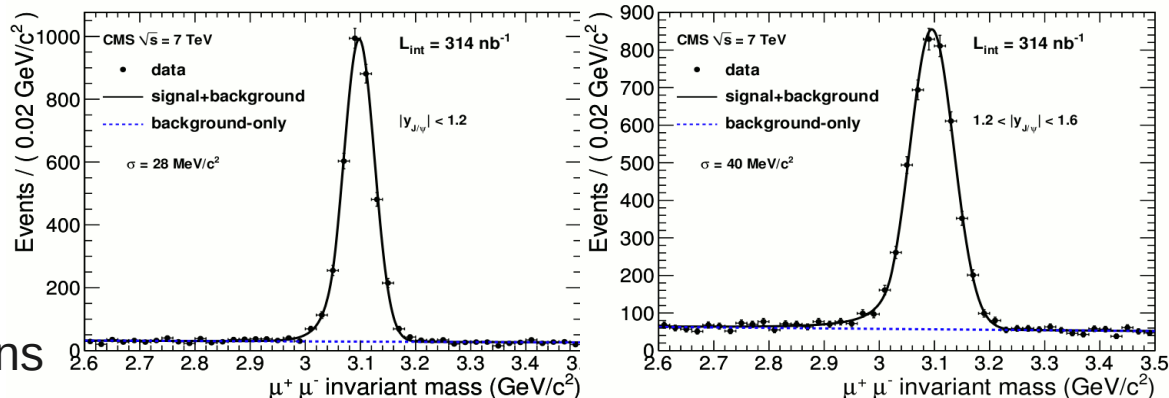
**Acceptance calculated from MC; it depends on the assumed polarization scenario:**

- isotropic (unpolarized);
- extreme values of  $\lambda_\theta (= \pm 1)$  in the helicity frame (along the J/ψ momentum);
- extreme values of  $\lambda_\theta (= \pm 1)$  in the Collins-Soper frame (along the collision axis);

**Efficiency determined from data with the Tag & Probe method**

Main systematic uncertainties:

- kinematical distributions (< 3%)
- b-hadron fraction (< 3.1%)

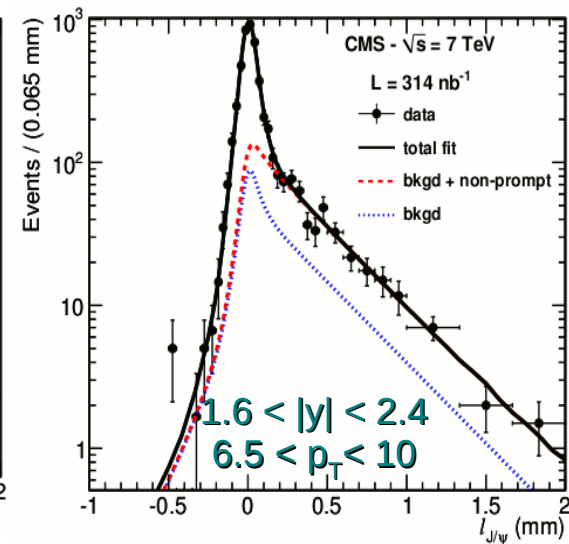
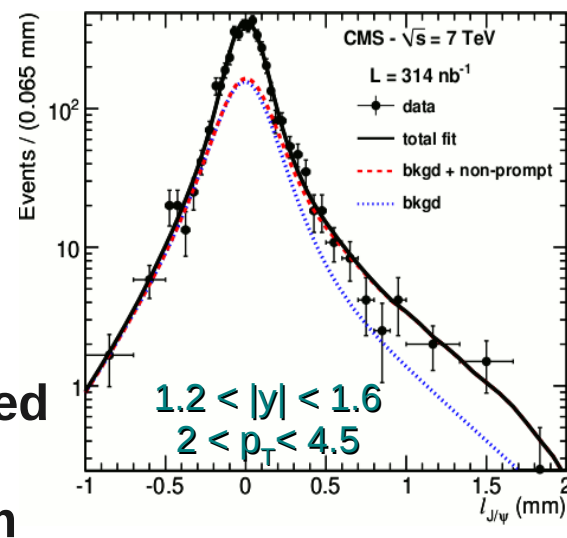




# J/ψ prompt and non-prompt components

Triggered with di-muon ; Total yields ~12000 ev

Fraction of J/ψ from b-hadron estimated by fitting the proper decay length together with di-muon mass spectrum



Prompt:  $\sigma_{pp \rightarrow J/\psi X} \cdot Br(J/\psi \rightarrow \mu^+ \mu^-) = (70.9 \pm 2.1 (stat) \pm 3.0 (sys) \pm 7.8 (lumi)) nb$

(assuming unpolarized production)

Non-prompt:  $\sigma_{pp \rightarrow bX \rightarrow J/\psi X} \cdot Br(J/\psi_{lb} \rightarrow \mu^+ \mu^-) = ((26.0 \pm 1.4 (stat) \pm 1.6 (syst) \pm 2.9 (lumi)) nb$

J/ψ and b-hadron pairs events simulated with PYTHIA; final-state bremsstr. implemented with PHOTOS;  
b-hadrons decaying inclusively into J/ψ simulated with EvtGen package

In good agreement with measurements from ATLAS and LHCb

Different polarizations shift results as much as 20%

## SYSTEMATICS:

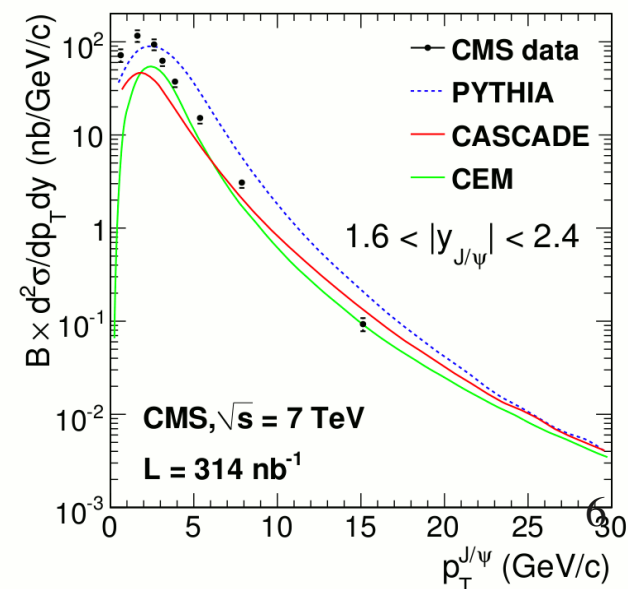
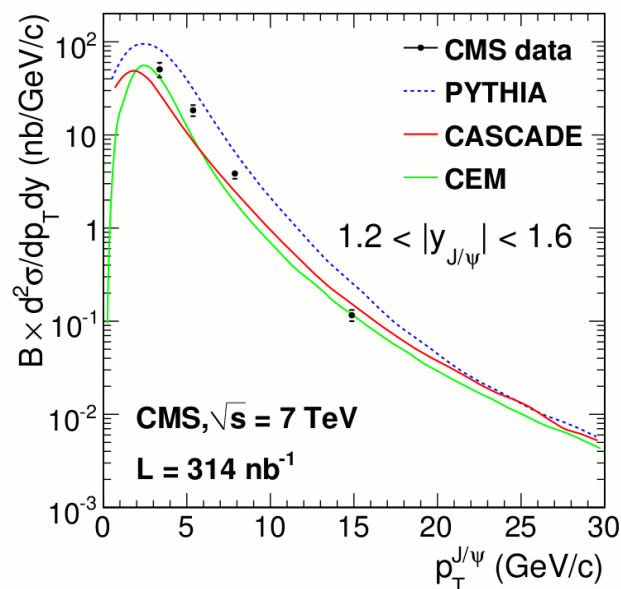
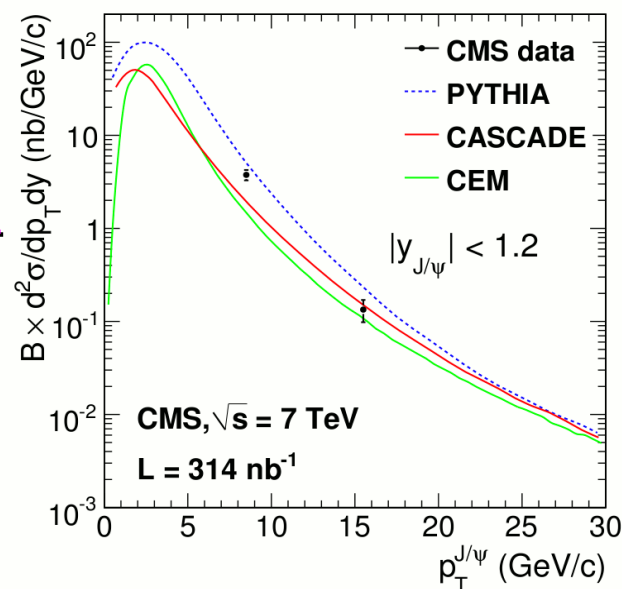
- Primary vertex estimation
- Decay length resolution function
- Background fit
- Residual misalignments in the tracker
- b-hadron lifetime model
- Different prompt and non-prompt efficiencies



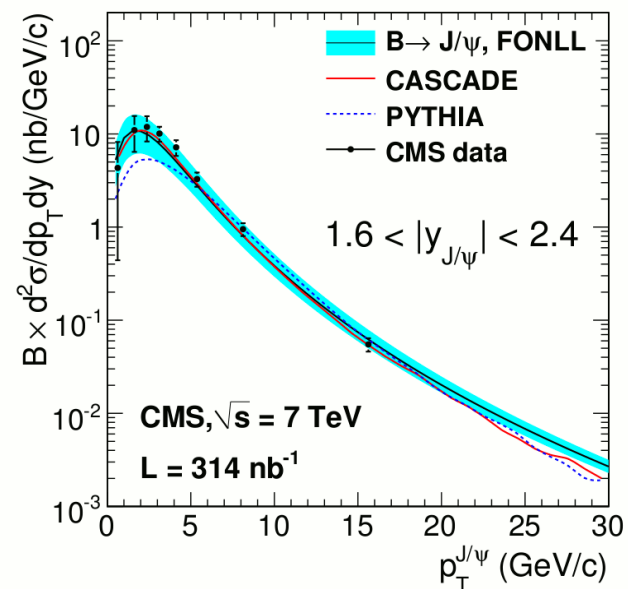
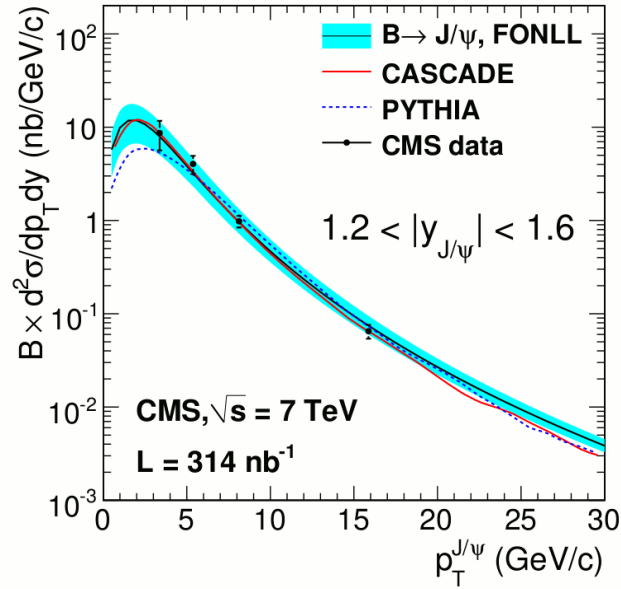
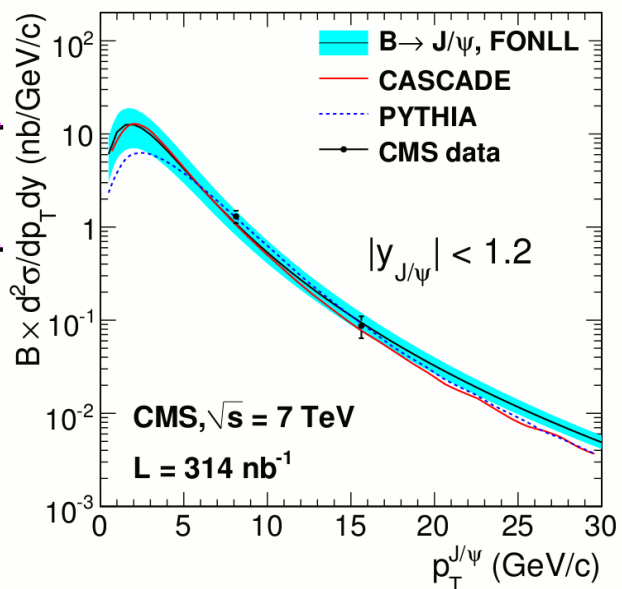
# Comparison with models



Prompt



Non-prompt:



Prompt measurements including a significant contribution from feed-down decays ( ~30% )

# Y production

Submitted to Phys. Rev. D

Y family reconstructed in di-muon final state;  
1,2 and 3S states all evident above background

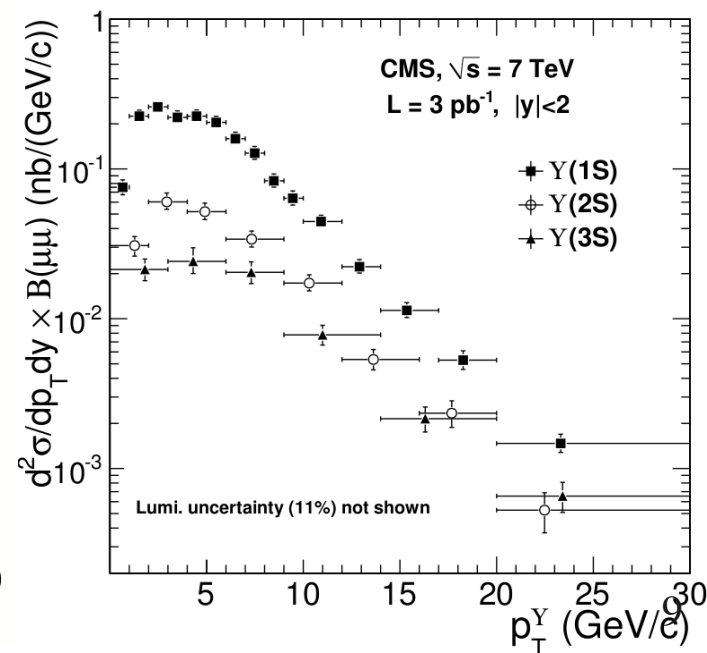
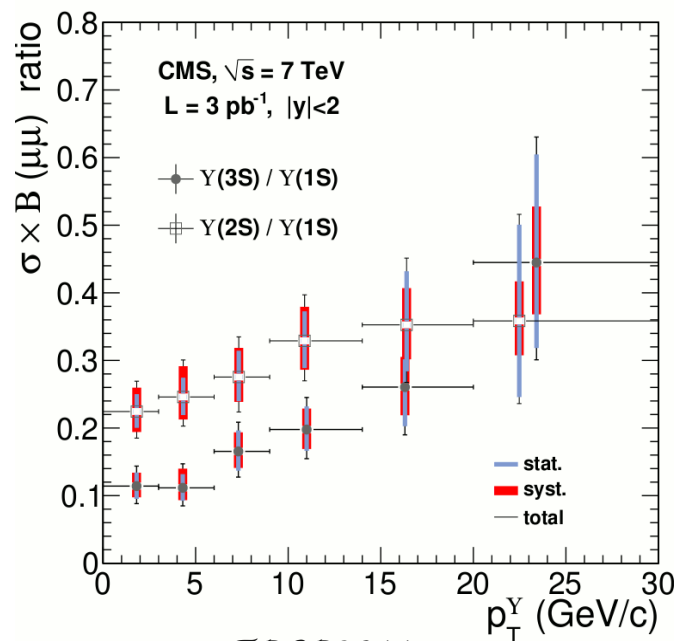
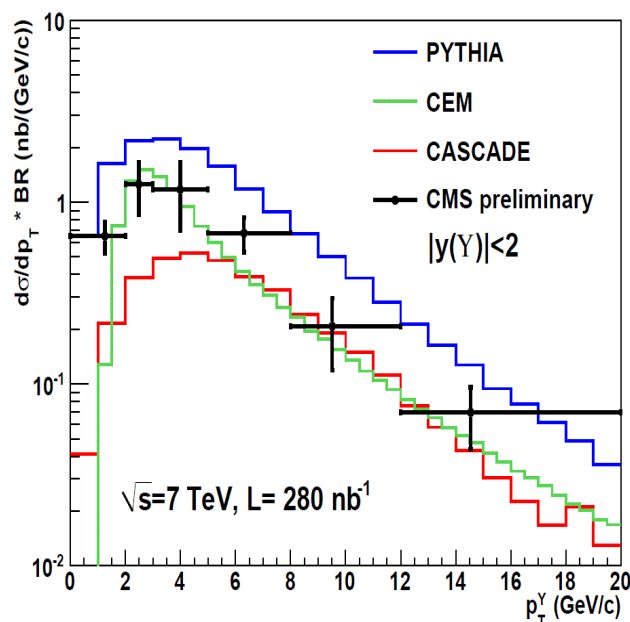
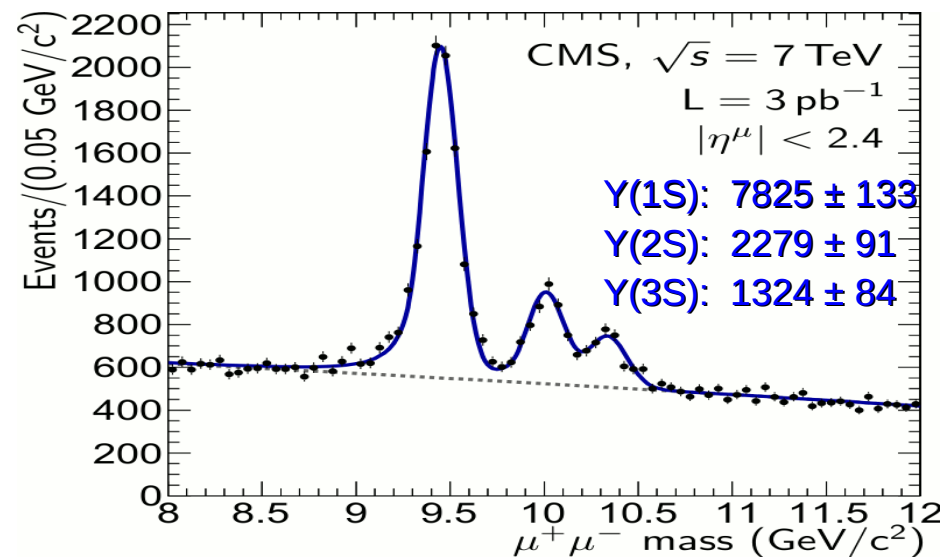
Mass resolution  $\sim 70$  MeV for  $|\eta| < 1.0$   
yields extracted simultaneously with a maximum  
likelihood fits in  $p_T$  and  $y$  intervals

Double differential cross sections vs  $p_T$  and  $y$

$$\begin{aligned}\sigma(pp \rightarrow Y(1S)X) \cdot Br(Y \rightarrow \mu^+\mu^-) &= (7.37^{+0.61}_{-0.42} (\text{syst}) \pm 0.13 (\text{stat}) \pm 0.81 (\text{lumi})) \text{ nb} \\ \sigma(pp \rightarrow Y(2S)X) \cdot Br(Y \rightarrow \mu^+\mu^-) &= (1.90^{+0.20}_{-0.14} (\text{syst}) \pm 0.09 (\text{stat}) \pm 0.24 (\text{lumi})) \text{ nb} \\ \sigma(pp \rightarrow Y(3S)X) \cdot Br(Y \rightarrow \mu^+\mu^-) &= (1.02^{+0.11}_{-0.08} (\text{syst}) \pm 0.07 (\text{stat}) \pm 0.11 (\text{lumi})) \text{ nb}\end{aligned}$$

Good agreement with  
previous Tevatron  
measurements

Fraction of 2S and 3S  
increases with  $p_T$

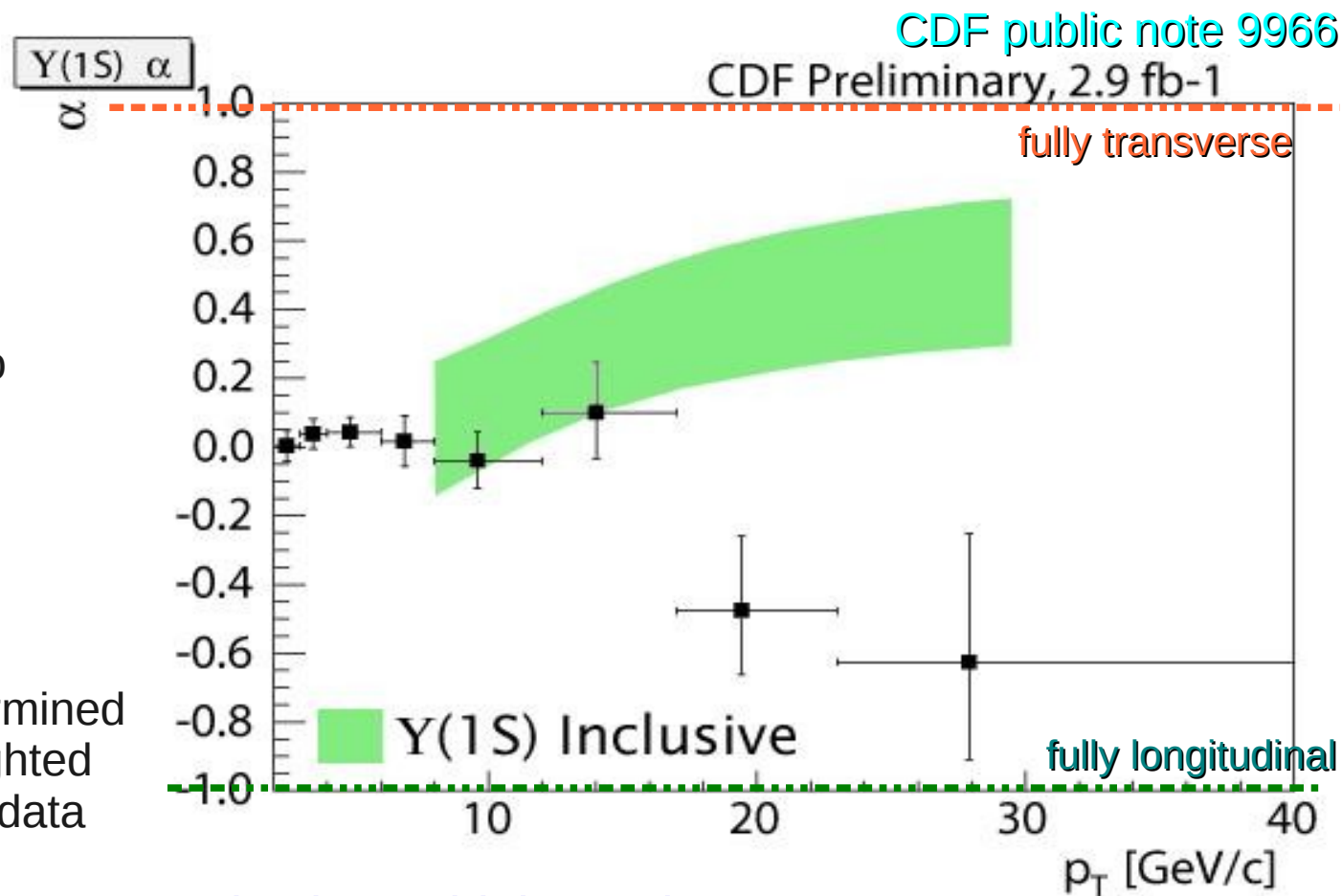


# Latest results on $\Upsilon(1S)$ polarization from CDF

Fully transverse and fully longitudinal MC generated and subjected to detector acceptance and efficiency effects to form templates; MC iteratively re-weighted to match data  $p_T$  distributions.

Events selected using a mass fit, backgrounds from mass side-bands.

Polarization parameter determined matching a polarization-weighted combination of templates to data



NRQCD predicts a transverse polarization at high  $p_T$ , whereas

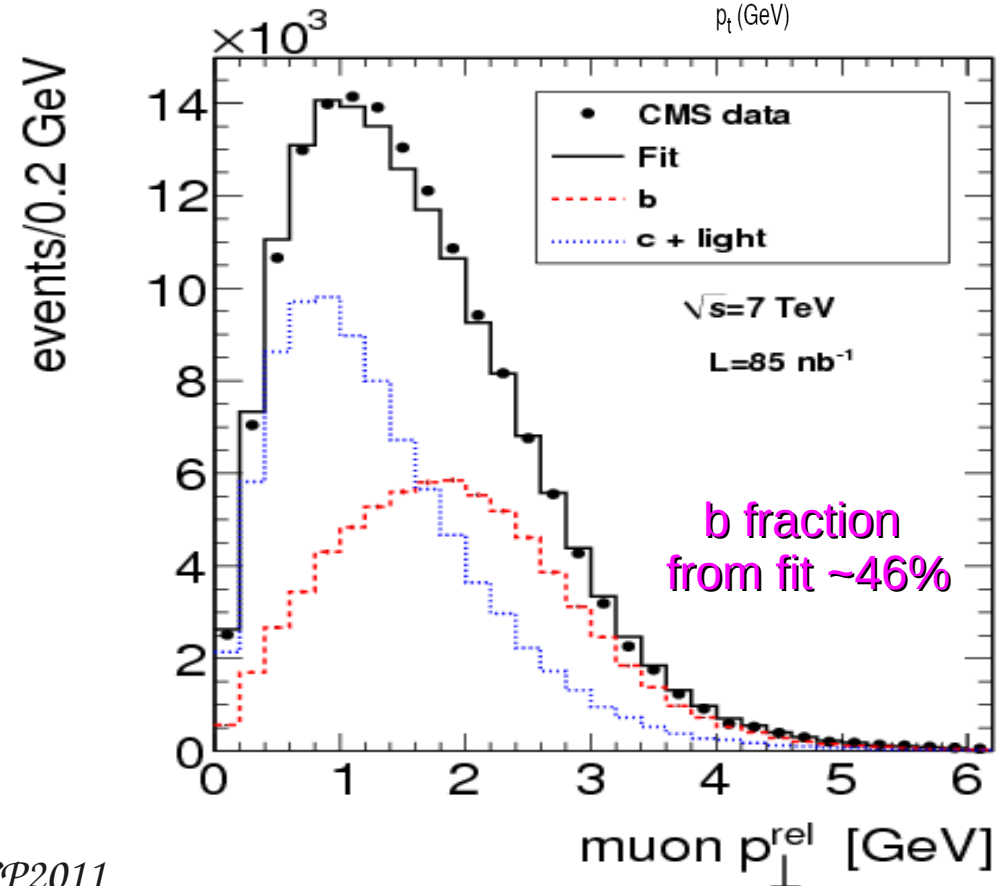
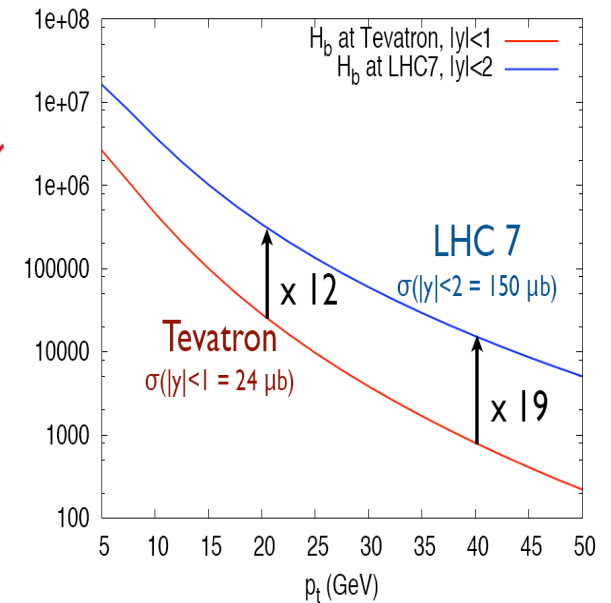
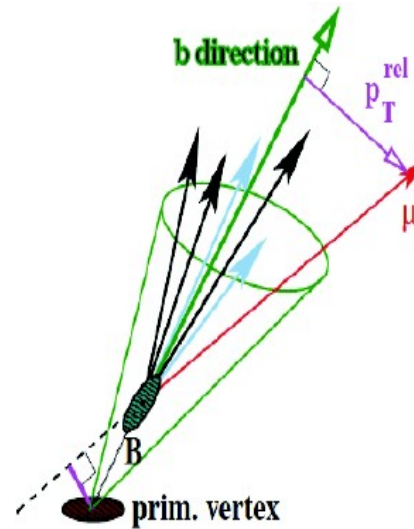
$\Upsilon$  found to be unpolarized at low  $p_T$  before exhibiting marked polarization at high  $p_T$ !

Consistent with CDF Run I [PRL 88, 161802 (02)], disagreement with  $D\bar{D}$  run II [PRL 101, 182004 (08)]

# Inclusive beauty production

JHEP 1103 (2011) 090

- Use semi-leptonic decays to separate b-jets from udscg jets
- Triggering on muon ( $p_T > 3$  GeV) and require  $p_T > 6$  GeV,  $|\eta| < 2.1$  offline
- Jets clustered with anti- $k_T$  ( $R=0.5$ ) from tracks with  $p_T > 300$  MeV
- Muon from b decays discriminated with the distance from jet axis, on average larger than light quarks
- $p_T$ -rel templates from MC (data) for b and c (udsg), with signal validated in b-enriched data
- Background templates combined in fit





# Inclusive beauty cross section



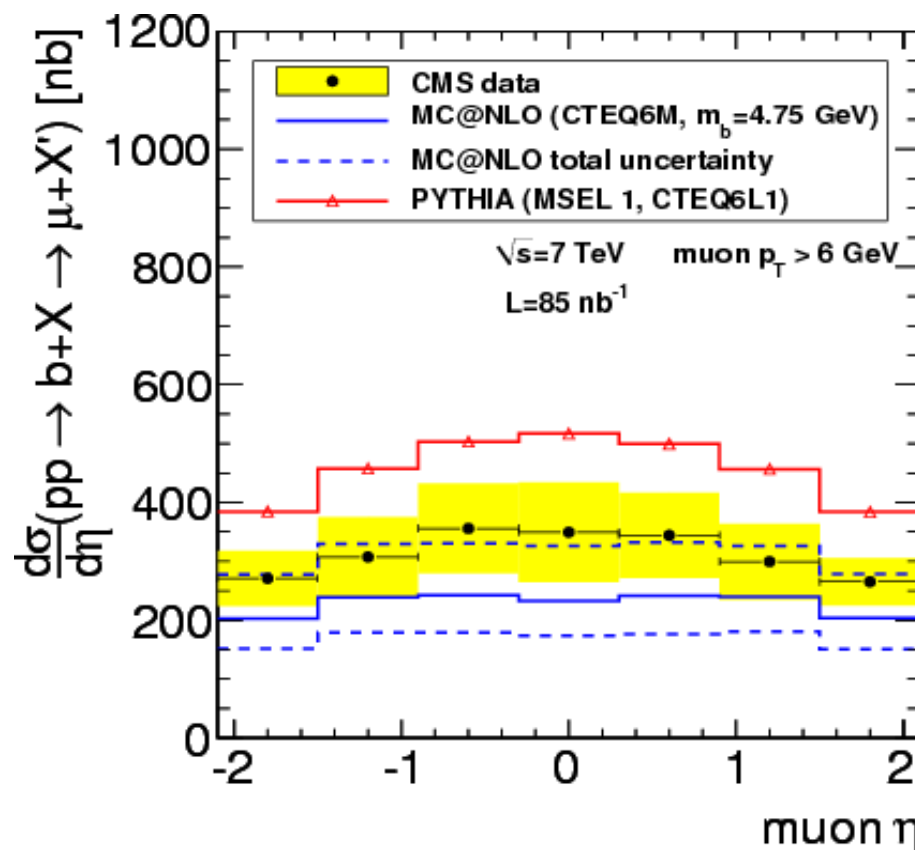
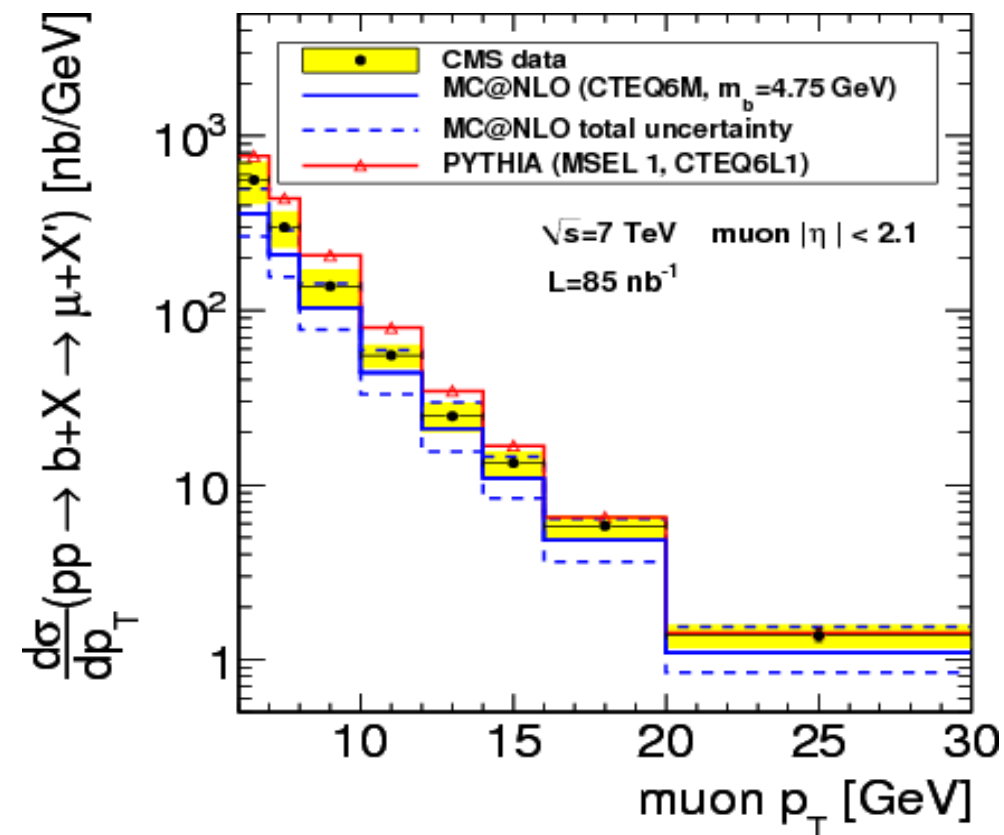
JHEP 1103 (2011) 090

Measured visible cross section: muon  $p_T > 6$  GeV,  $|\eta| < 2.1$ ;

$$\sigma(pp \rightarrow b \bar{b} X \rightarrow \mu X) = (1.32 \pm 0.01(\text{stat.}) \pm 0.30(\text{syst.}) \pm 0.15(\text{lumi.})) \mu\text{b}$$

$$\sigma_{\text{MC@NLO}} = (0.95_{-0.21}^{+0.42}(\text{scale}) \pm 0.09(m_b) \pm 0.05(\text{pdf})) \mu\text{b}; \quad \sigma_{\text{PYTHIA}} = 1.9 \mu\text{b}$$

uncertainty dominated by signal and background  $p_T$  rel shapes

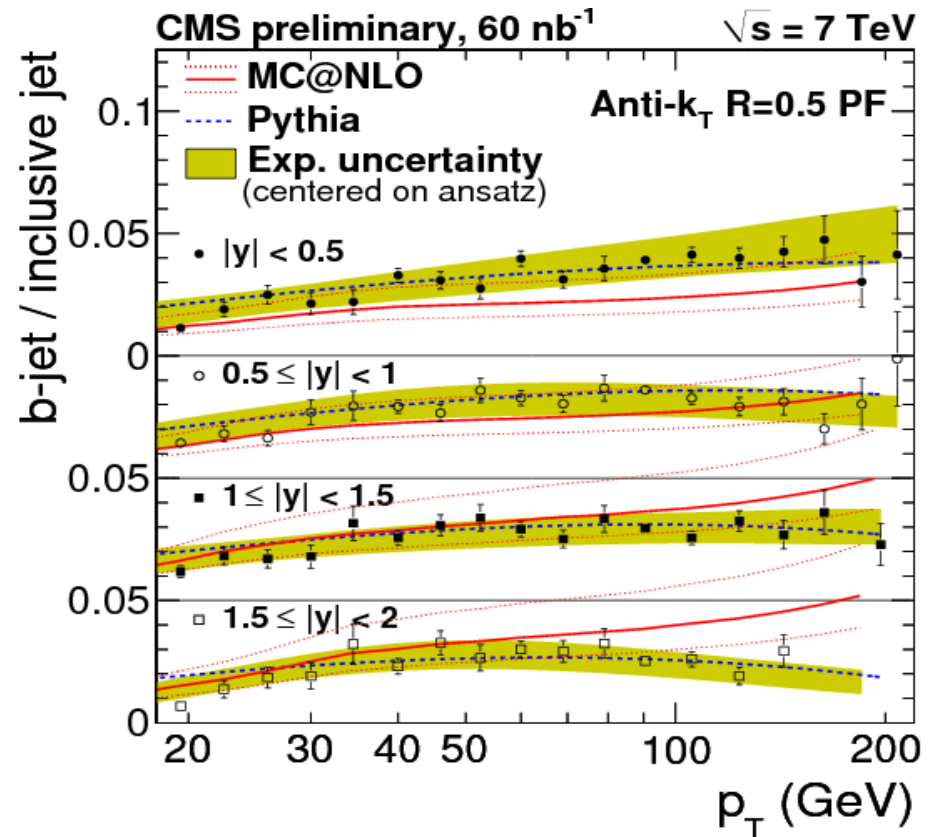
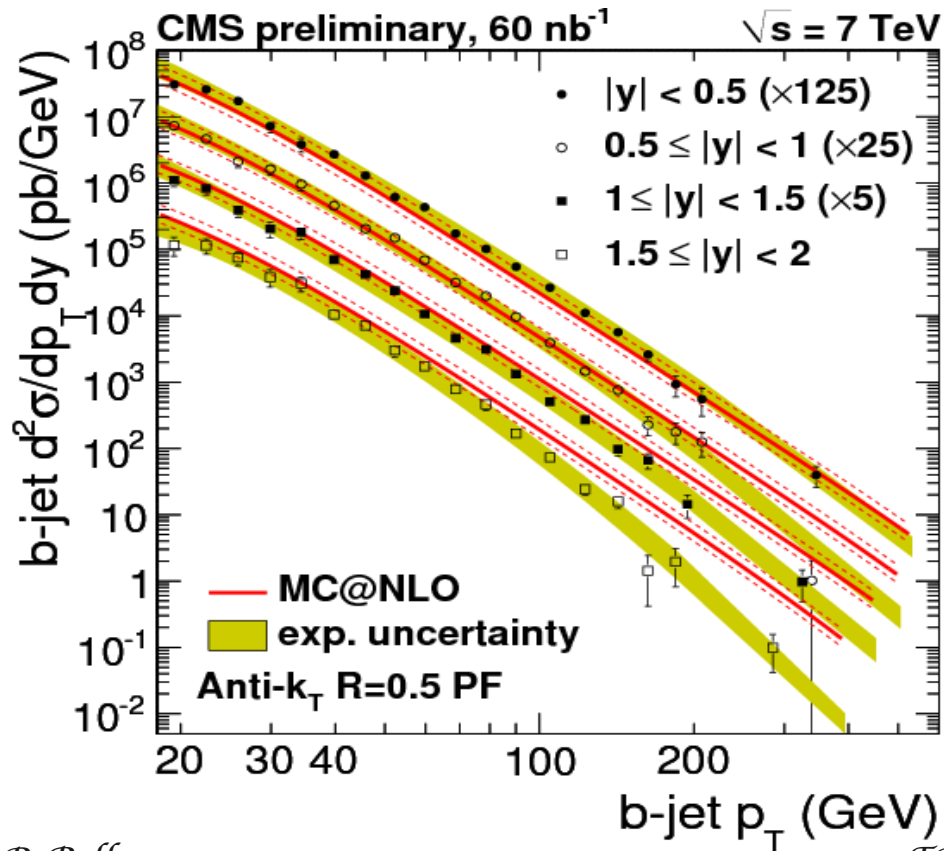


# Inclusive b from jet tagging



## Identification of b jets performed through the Secondary Vertex tagging

- Significantly extends the measurement in  $p_T$ ;  
tagging efficiency 50-60% for jet  $p_T = 100$  GeV, with  $\sim 0.1\%$  contamination
- Jets from anti- $k_T$  algorithm using tracks and calorimeter information
- Displaced vertices selected with  $\geq 3$  tracks to identify b events
- Uncertainties dominated by b-tag efficiency and jet energy scale



# $B\bar{B}$ correlations

JHEP 1103 (2011) 136



Use secondary vertex to study correlations between two B hadrons  
probed for the first time the region at small angular separation:

require exactly two secondary vertices, with  $\geq 3$  tracks, 3D flight length  $\geq 5 \sigma$   
calculate  $\Delta R = \sqrt{(\Delta\phi^2 + \Delta\eta^2)}$  of directions from primary vertex to each secondary

Measured momentum corrected through the 'true' B hadron momentum from MC

Results shown in different ranges for the leading jet  $p_T$

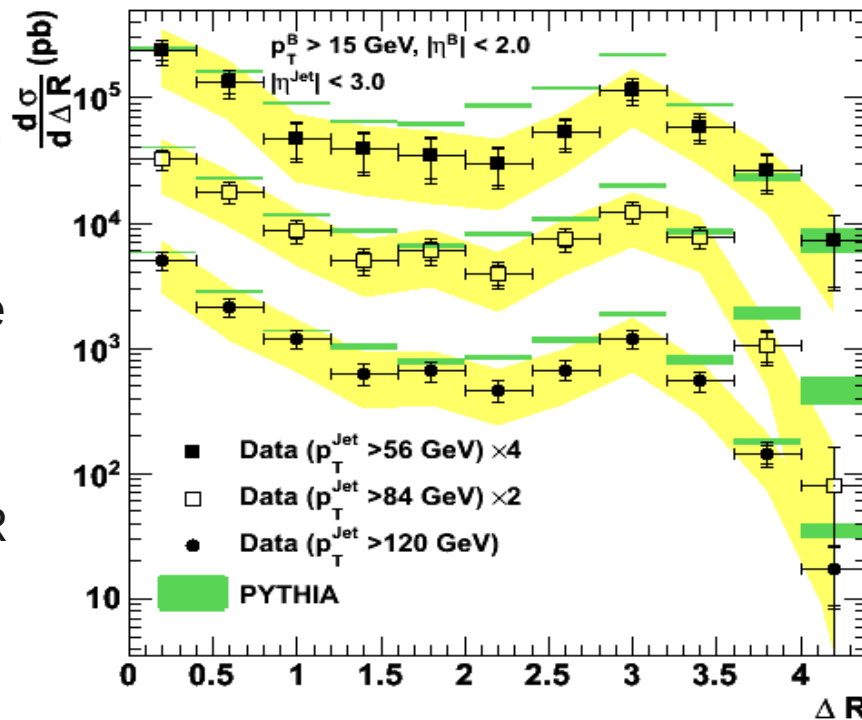
both B's in  $|\eta| < 2.0$ ,  $p_T > 15$  GeV

CMS  $\sqrt{s} = 7$  TeV,  $L = 3.1$  pb $^{-1}$

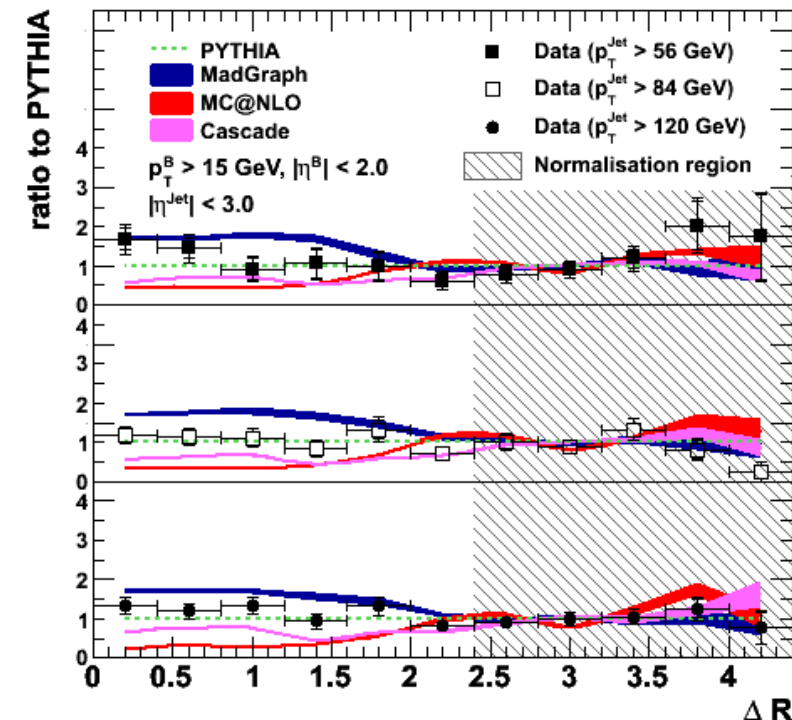
Flavour creation  
expected to  
dominate at high  
 $\Delta R$ ;

gluon splitting  
contributes more  
at low  $\Delta R$ .

Data normalized  
to MC in high  $\Delta R$   
region.



CMS  $\sqrt{s} = 7$  TeV,  $L = 3.1$  pb $^{-1}$



The differential cross section shows that **a sizeable fraction of the  $B\bar{B}$  pairs is produced with small opening angles.**

# Exclusive beauty production



CMS Preliminary,  $\sqrt{s}=7$  TeV

Spring 2011

High  $bb$  cross section at the LHC already allows for measurements with early data

Reconstruct B hadrons in exclusive final states:

$$B^+ \rightarrow J/\psi K^+$$

$$B^0 \rightarrow J/\psi K_s (\rightarrow \pi^+ \pi^-)$$

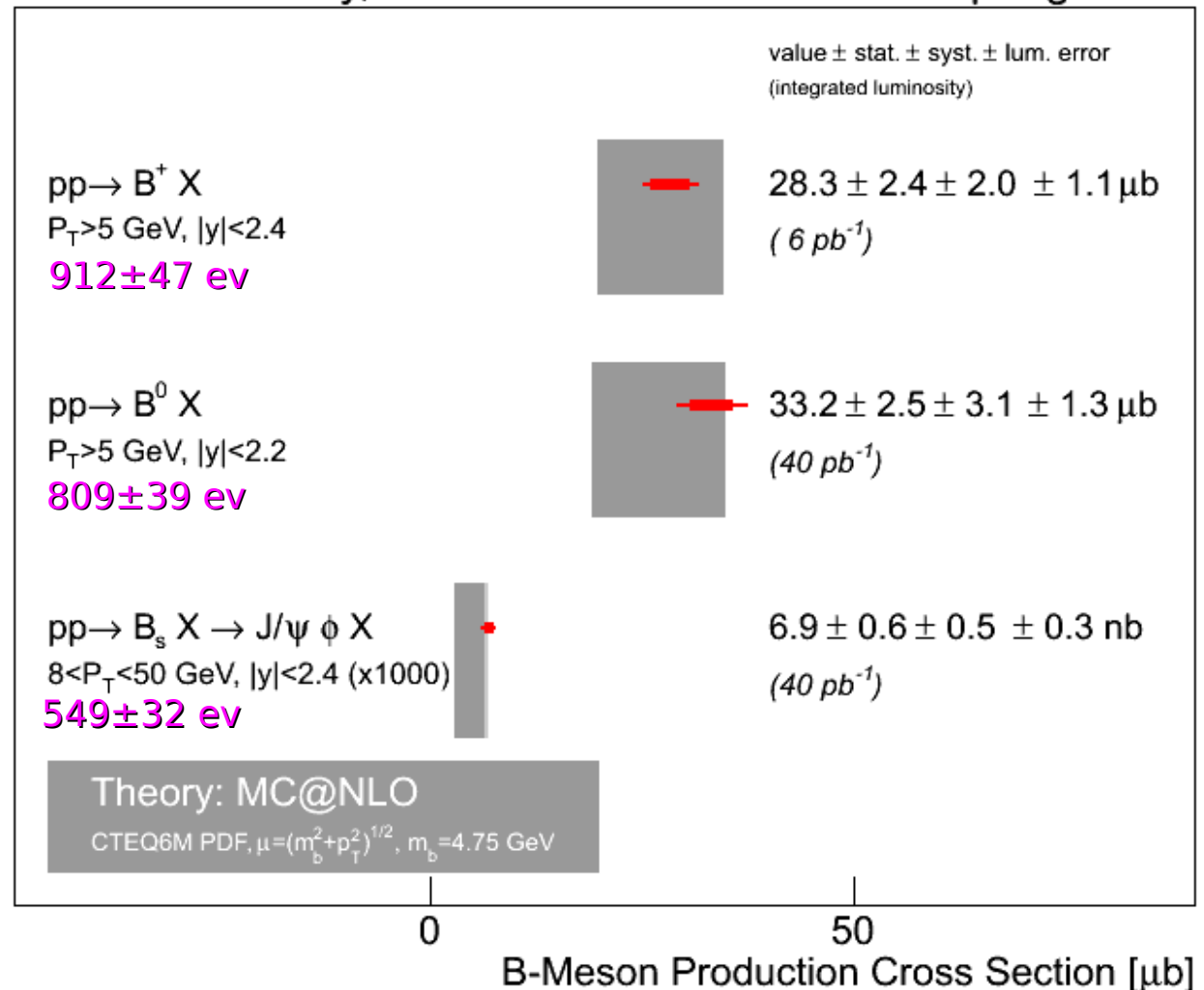
$$B_s \rightarrow J/\psi \Phi (\rightarrow K^+ K^-)$$

Always  $J/\psi \rightarrow \mu^+ \mu^-$

Triggering on di-muon from  $J/\psi$

$B^0$  and  $B_s$  results obtained over the whole 2010 statistics ( $39.6 \text{ pb}^{-1}$ )

Small branching fractions ( $2 - 6 \times 10^{-5}$ , including product branching fractions)



Combined fit to the B meson mass and lifetime to reject the background  
Measurement of cross sections differentially in  $p_T$  and  $\eta$  performed



$$B^+ \rightarrow J/\psi K^+$$

PRL 106, 112001 (2011)

$$p_T(B^+) > 5 \text{ GeV}$$

$$|y(B^+)| < 2.4$$

2D maximum likelihood fit to the  $B^+$  mass and lifetime  
used to separate signal from background

Backgrounds from prompt  $J/\psi$  and  
mis-reconstructed b-hadron

Most fit shapes derived directly from data;

Peaking background and signal  $B$  mass from MC

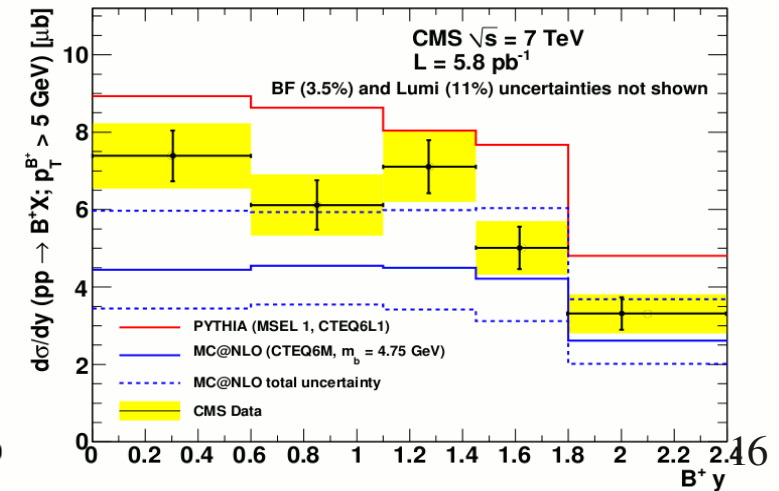
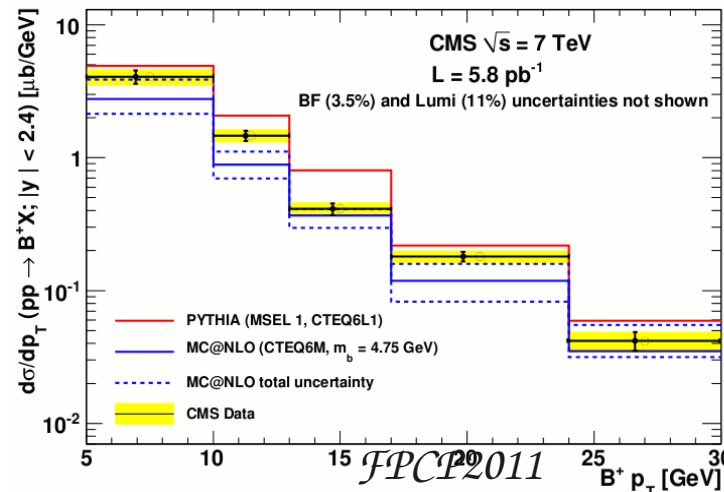
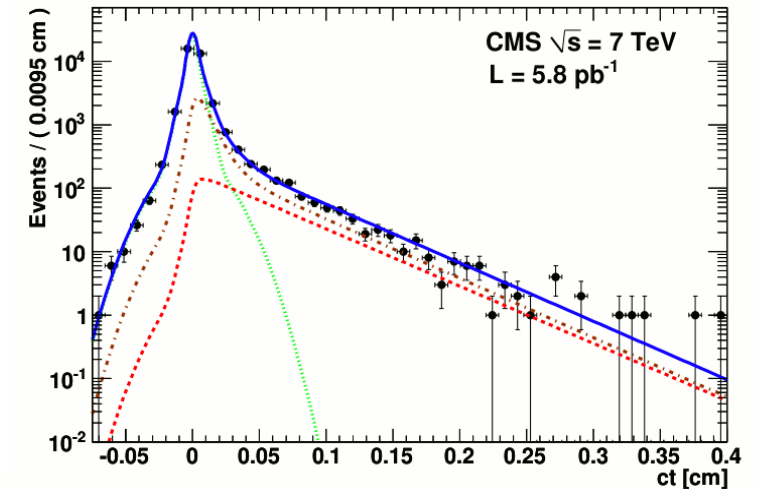
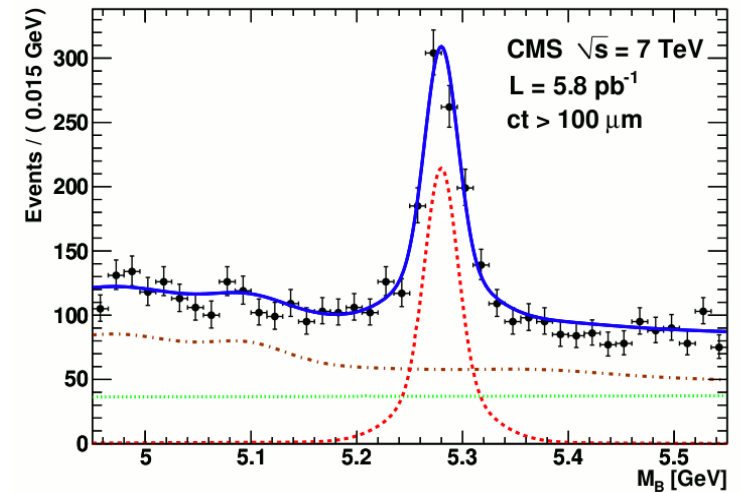
Total yield =  $912 \pm 47$

Efficiency of candidate reconstruction (1.5 - 33%)  
determined from data-driven techniques and MC

$$\sigma(pp \rightarrow B^+ X) = (28.1 \pm 2.4(\text{stat.}) \pm 2.0(\text{syst.}) \pm 3.1(\text{lumi})) \mu\text{b}$$

$$\sigma_{\text{MC@NLO}} = 25.5^{+9.2}_{-5.7} \mu\text{b}; \quad \sigma_{\text{PYTHIA}} = 48.1 \mu\text{b}$$

Fits in bins of  $B^+$ 's  $p_T$   
and  $y$  to measure  $B^+$   
differential cross  
section



$$B^0 \rightarrow J/\psi K_s$$

Submitted to Phys.Rev.Lett.

$$p_T(B^0) > 5 \text{ GeV}$$

$$|y(B^0)| < 2.2$$

$$\sigma(pp \rightarrow B^0 X) = (33.2 \pm 2.5 \text{ (stat.)} \pm 3.5 \text{ (syst.)}) \mu\text{b}$$

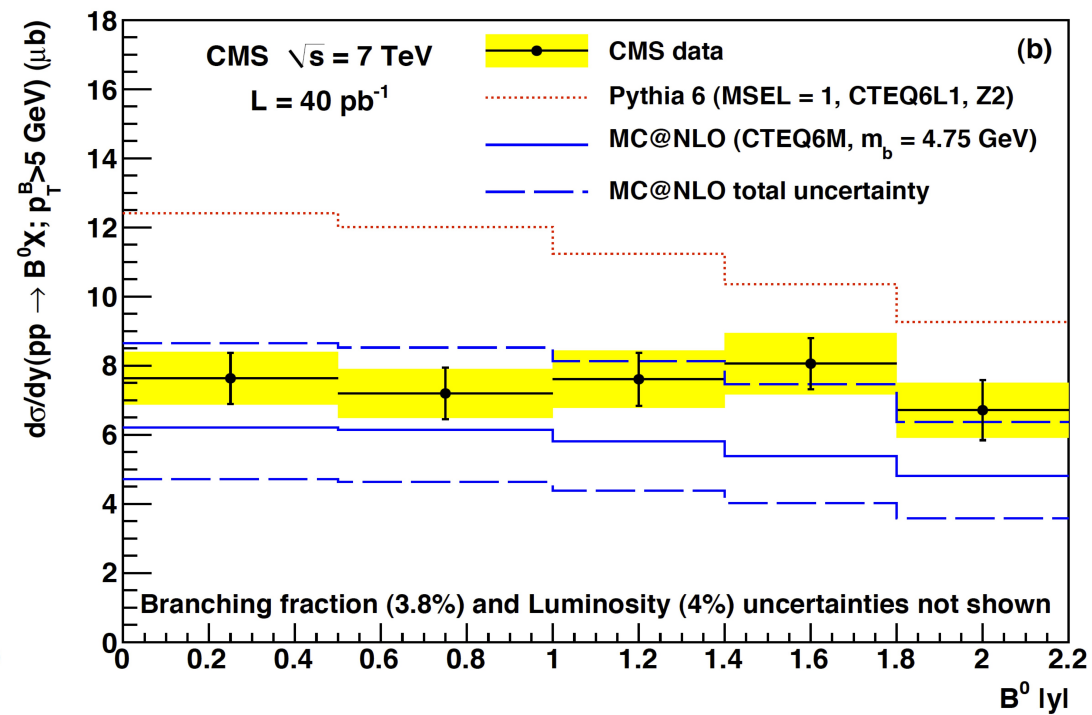
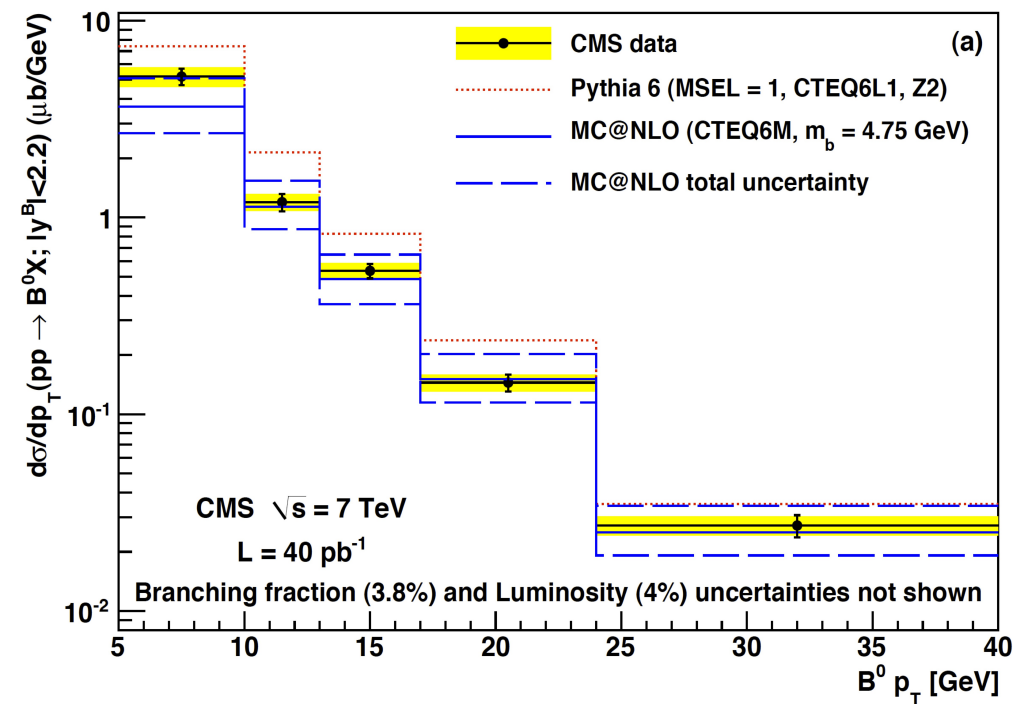
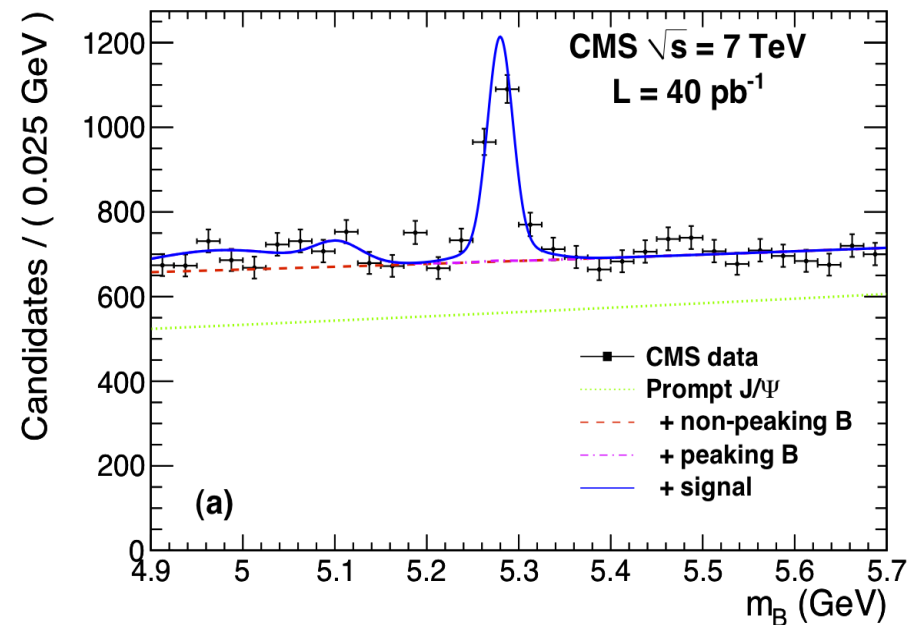
$$\sigma_{\text{MC@NLO}} = 25.2_{-6.2}^{+9.6} \mu\text{b}; \quad \sigma_{\text{PYTHIA}} = 49.1 \mu\text{b}$$

**Resolutions:**

$\sim 20 \text{ GeV}$  for  $M_B$ ,  $\sim 45 \mu\text{m}$  for  $c\tau$ ;

$p_T$  shape in reasonable agreement with the models

Rapidity shape more flat than Pythia and MC@NLO



$$B_s \rightarrow J/\psi \Phi$$

$$p_T(B_s) > 8 \text{ GeV}$$

$$|y(B_s)| < 2.4$$

$$\sigma(pp \rightarrow B_s X) \cdot Br(pp B_s \rightarrow J/\psi) =$$

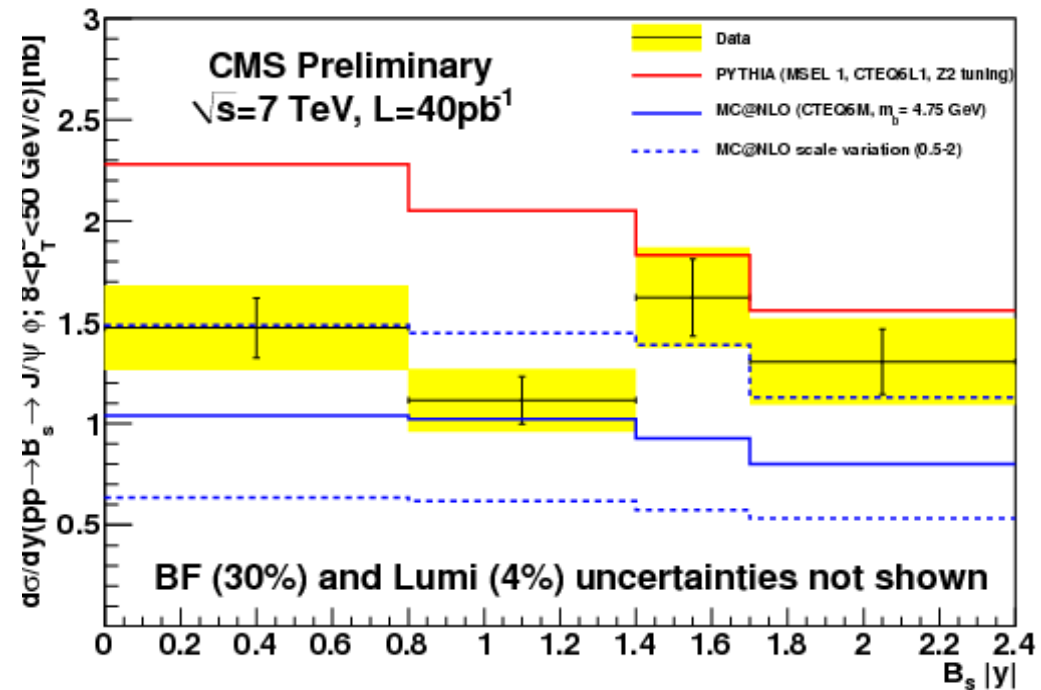
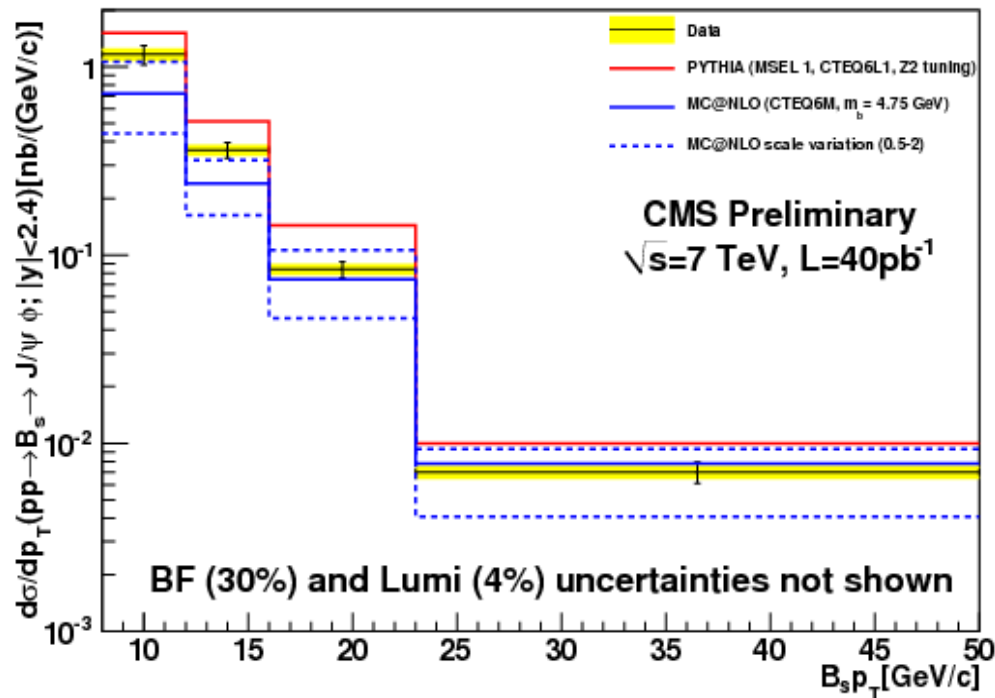
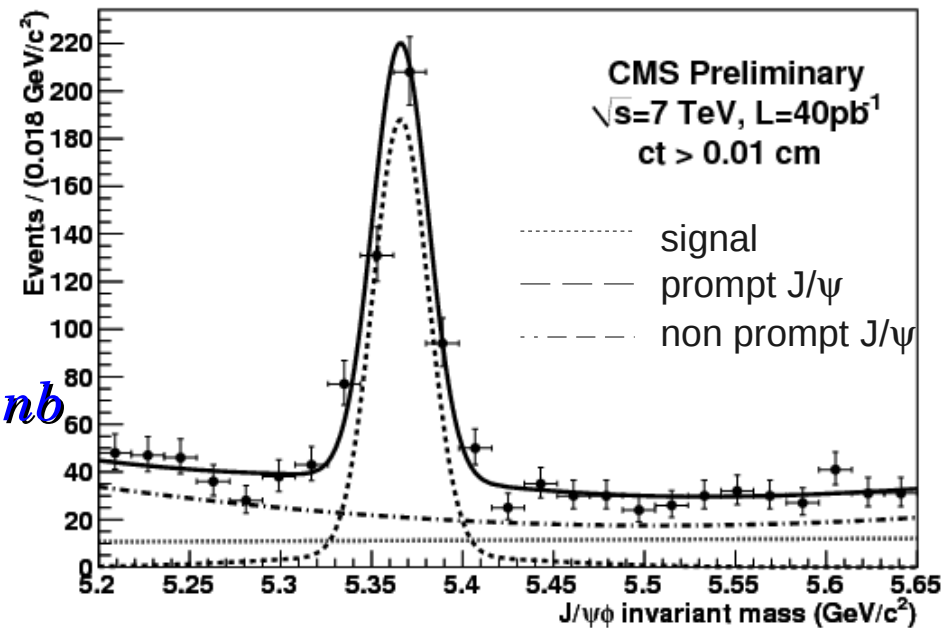
$$= (6.9 \pm 0.6 \text{ (stat)} \pm 0.5 \text{ (syst)} \pm 0.3 \text{ (lumi)}) \text{ nb}$$

$$\sigma_{\text{MC@NLO}} = (4.6^{+1.9}_{-1.7} \pm 1.4) \text{ nb};$$

$$\sigma_{\text{PYTHIA}} = (9.4 \pm 2.8) \text{ nb} \quad [\text{last errors from Br}]$$

$p_T$  shape in drops faster than MC@NLO

Rapidity distribution more flat than both the models



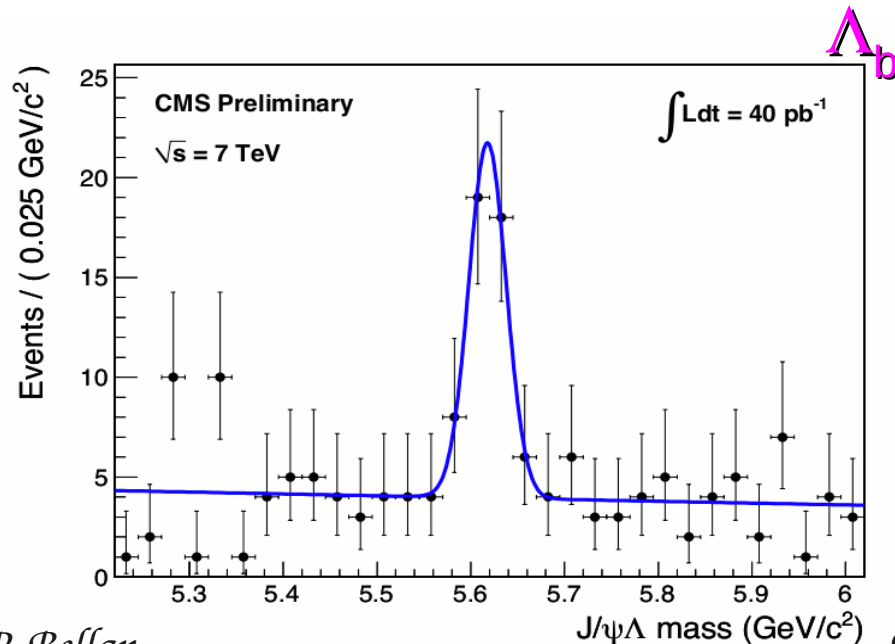
# Observation of other heavy hadrons

$\chi_{c1}$  and  $\chi_{c1}$  seen in CMS in decay to  $J/\psi \gamma$   
 high resolution needed ( $\Delta m = \sim 45 \text{ MeV}$ );  
 CMS resolution very good ( $\sim 11 \text{ MeV}$ );  
 photon conversion rather challenging.

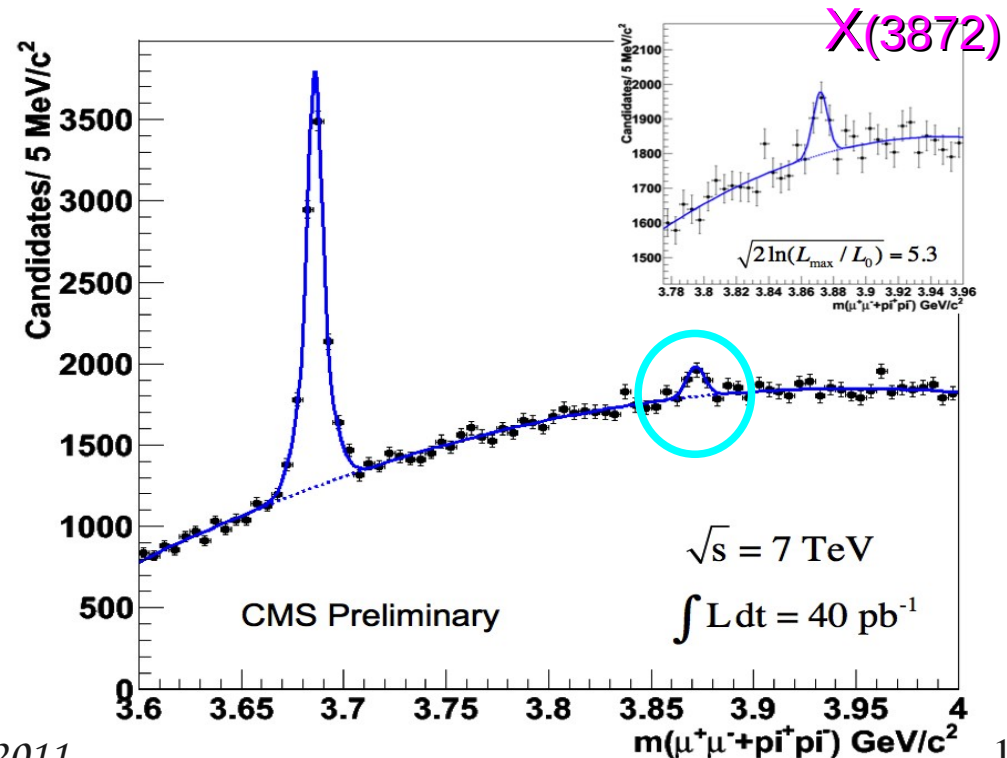
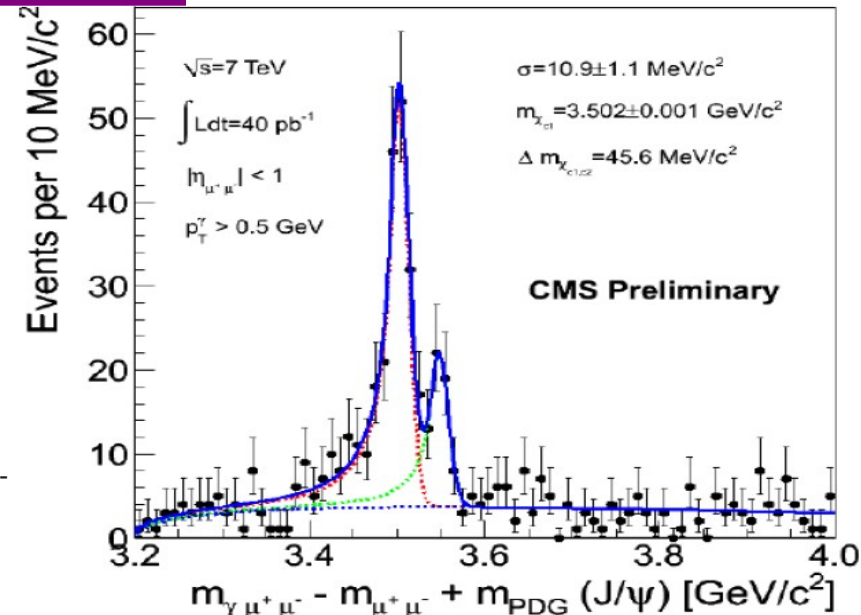
$\Lambda_b$  observed in the decay channel  $J/\psi \Lambda$   
 Yield and lifetime measured with early 2011 data

$X(3872)$  status observed in the decay channel  $J/\psi \pi^+ \pi^-$   
 in  $40 \text{ pb}^{-1}$  with a significance of 5.3  
 Measured ratio of the cross section wrt  $Y(2S)$ :

$$R = 0.087 \pm 0.017(\text{stat}) \pm 0.009(\text{syst})$$



JPCP2011





# Conclusions and outlook



- Very successful B physics results with 2010 data
- More B physics papers from CMS than from other LHC experiments combined
- Heavy flavor production measurements performed with a wide variety of techniques
- Wealth of new data going to be used to refine theoretical models and improve MC simulation
- Many more interesting results to come (among others, efforts put on rare decays as  $B_s \rightarrow \mu\mu$ ,  $K^* \mu\mu$  and CP-violation in  $B_s \rightarrow J/\psi \Phi$ , ...)

Thanks for your attention!

**BACK UP SPLIDES**

# References

Topic	arXiv	Article	Luminosity (pb <sup>-1</sup> )
J/Ψ production	1011.4193	Eur.Phys.J. C71 (2011) 1575	0.314
Υ production	1012.5545	Accepted by PRD	3
B <sup>+</sup> Production	1101.0131	PRL 106:112001,2011	5.8
Inclusive b-hadron production	1101.3512	JHEP 1103 (2011) 090	85
BB(bar) Angular Correlat. with SV	1102.3194	JHEP 1103 (2011) 136	3.1
B <sub>0</sub> <sup>-</sup> Production	1104.2892	Submitted to PRL	40

Diagram illustrating the reconstruction of a secondary vertex from tracks. The diagram shows a primary vertex (green dot) and a secondary vertex (blue oval) with tracks (blue lines) connecting them. A region of tracks is labeled "B candidates" (red text). A region of tracks is labeled "Secondary Vertex with its Tracks" (blue text). A region of tracks is labeled "Tracks from Secondary Vertex" (cyan text). A region of tracks is labeled "Secondary Vertex" (green text). A region of tracks is labeled "jets" (yellow text). The CMS logo is in the top left corner.

CMS Experiment at LHC, CERN  
 Data recorded: Mon Aug 2 08:31:15 2010 CEST  
 Run/Event: 142137 / 12470592  
 Lumi section: 21

MC@NLO do not describe the shape of the  $\Delta R$ , in particular @ small values.

Cascade predictions significantly below the data in all regions, both in the  $\Delta R$  and  $\Delta\phi$  distributions.

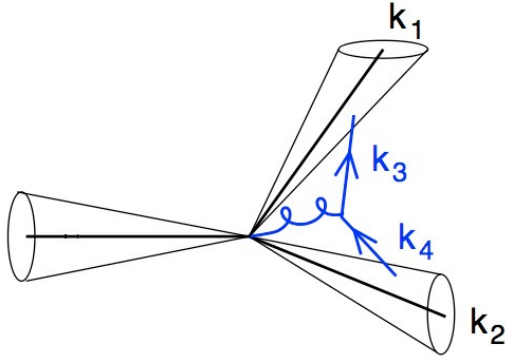




# b-jet cross section measurement

Highly non-trivial measurements

Sizable uncertainties from both th. and exp.



MEMO: standard jet definitions for flavoured jets are infrared-unsafe: soft gluons splitting into a qqbar pair can change the flavour of the jet

## Main ingredients of the measurements

- Number of tagged jets  $N_{\text{tagged}}$
- b-tagging efficiency  $f_b$ : fit from MC, data/MC scale with muon  $p_{T\text{rel}}$
- b-tag purity  $e_b$ : fit from MC, data/MC scale from SV mass templates

### Theoretical Uncertainties (~ in order of importance):

- ➔ **PDF Uncertainty**
- ➔ pQCD (Scale) Uncertainty
- ➔ Non-perturbative Corrections
- ➔ PDF Parameterization
- ➔ Knowledge of  $\alpha_s(M_Z)$
- ➔ ...

### Recall: Jet Algorithms used by CMS:

- ➔ Iterative Cone  $R = 0.5$
- ➔ SIS Cone  $R = 0.5, 0.7$
- ➔  $k_T$   $D = 0.4, 0.6$

### Experimental Uncertainties (~ in order of importance):

- ➔ **Jet Energy Scale (JES)**
- ➔ Noise Treatment
- ➔ Pile-Up Treatment
- ➔ Luminosity
- ➔ Jet Energy Resolution (JER)
- ➔ Trigger Efficiencies
- ➔ Resolution in Rapidity
- ➔ Resolution in Azimuth
- ➔ Non-Collision Background
- ➔ ...

Master formula:

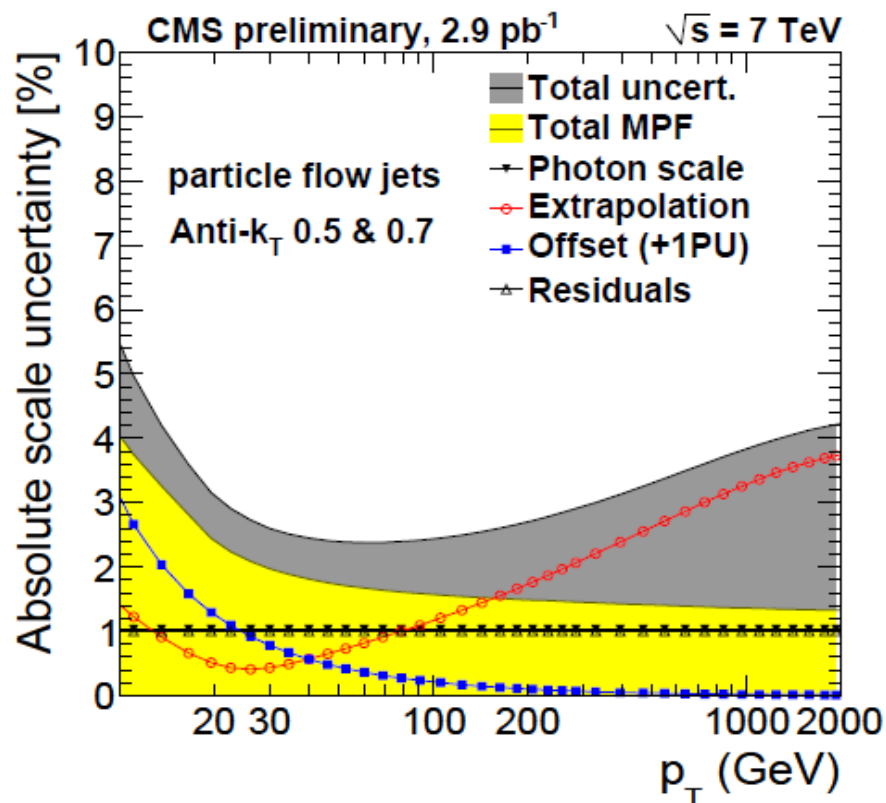
$$\frac{d^2\sigma_{b\text{-jets}}(p_T, y)}{dp_T dy} = \frac{N_{\text{tagged}}(p_T, y) f_b c_{\text{smear}}}{\epsilon_b \Delta p_T \Delta y \mathcal{L} \epsilon_{\text{jet}}}$$

Other corrections:

- Unfolding correction  $C_{\text{smear}}$ : need jet energy resolutions, ansatz fit
- b-jet JEC: same as inclusive jets (Pythia predicts residual difference  $< \sim 1\%$ )

# Jets and b-tagging

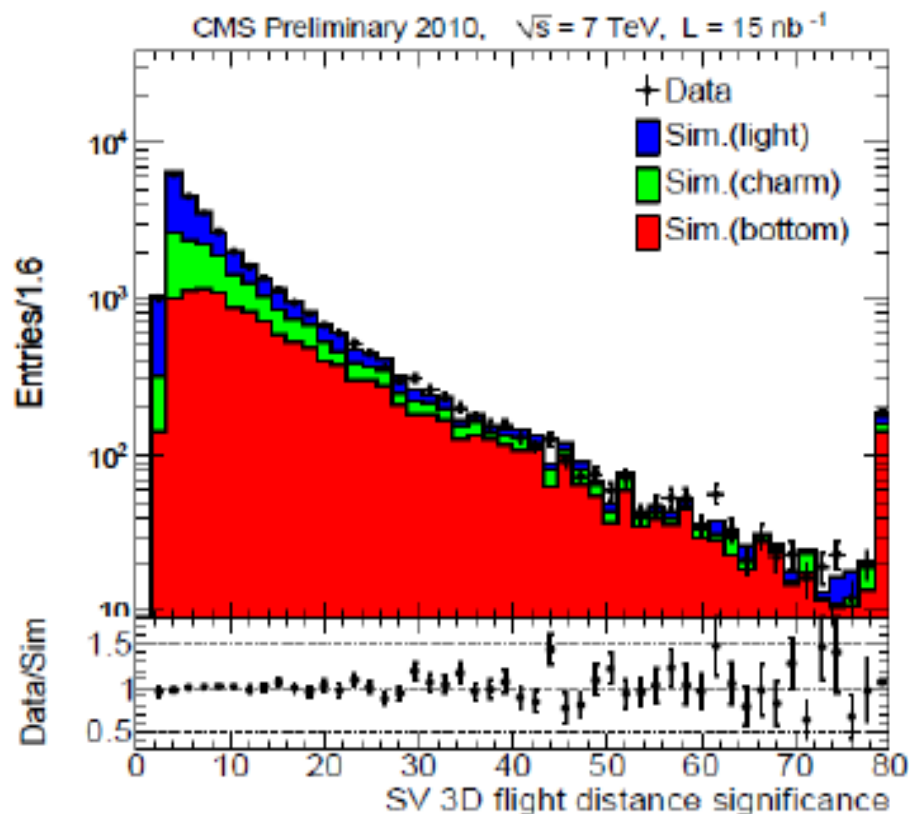
- Most of jet analyses use particle-flow techniques to define the jet and anti-kT algorithm with  $DR < 0.5$
- Typical scale uncertainty for EWK measurements  $< 3\%$ ;
- Typical jet resolution 10-15%



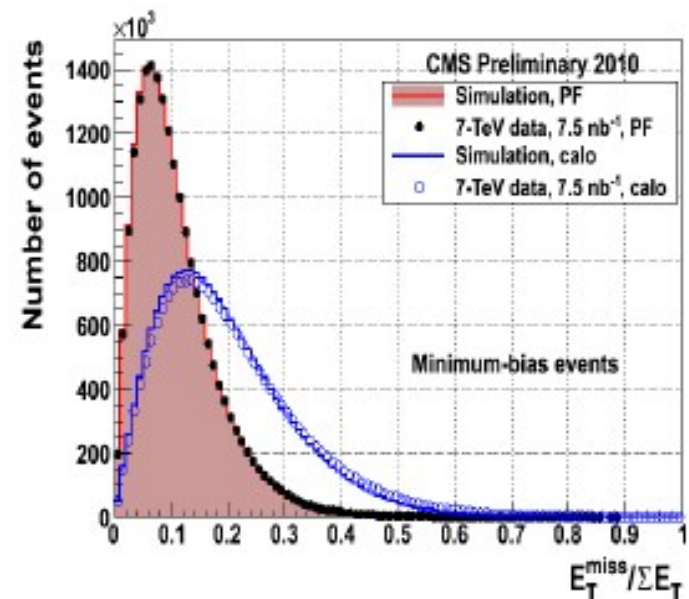
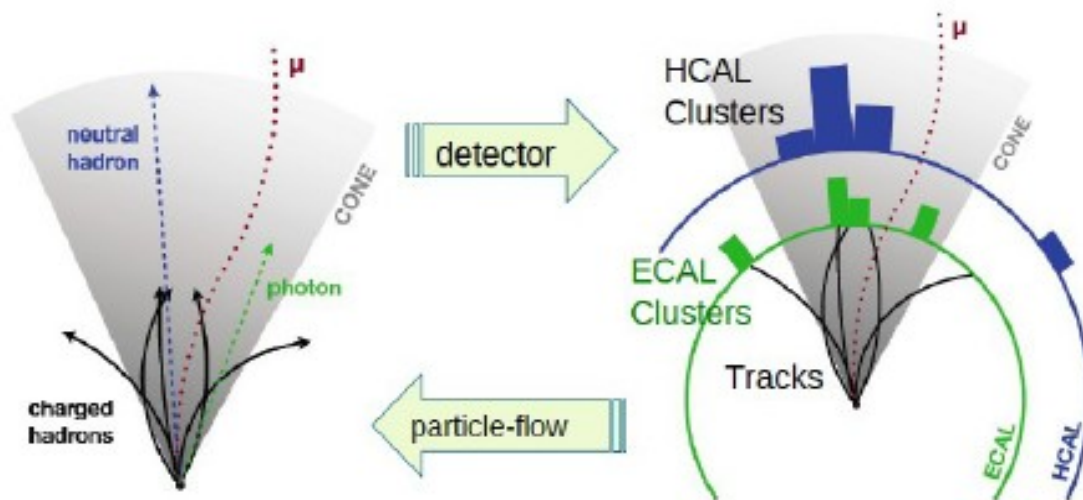
Good tracker performance and alignment  
→ good b-tagging capabilities

Different algorithms:

- \* Track counting (above some impact parameter significance threshold)
- \* Secondary vertex tagging (decay length significance)
- \* Combined



# Particle Flow Technique in CMS

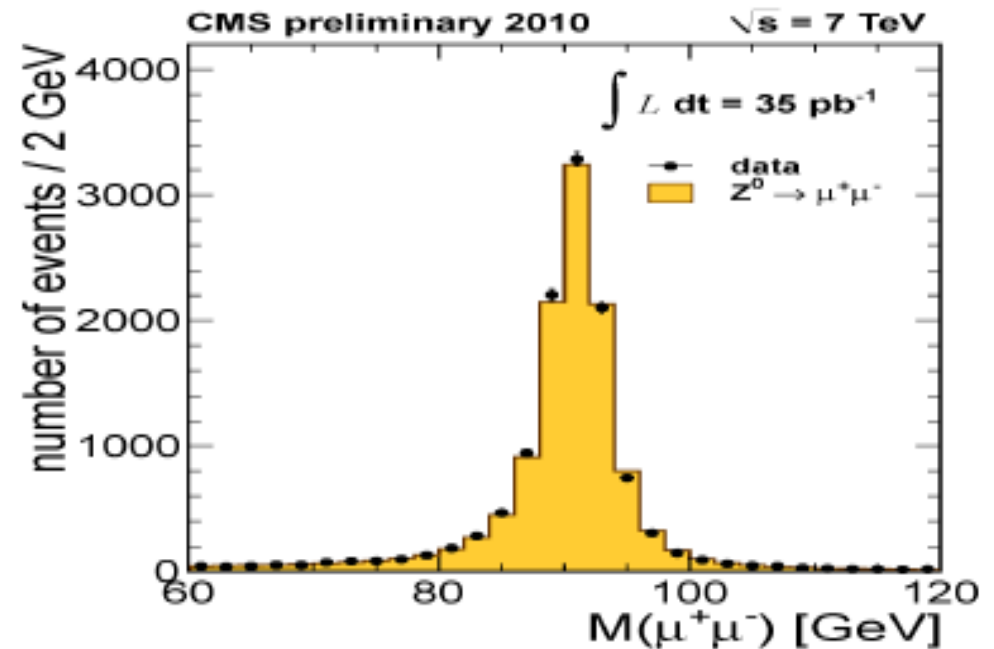
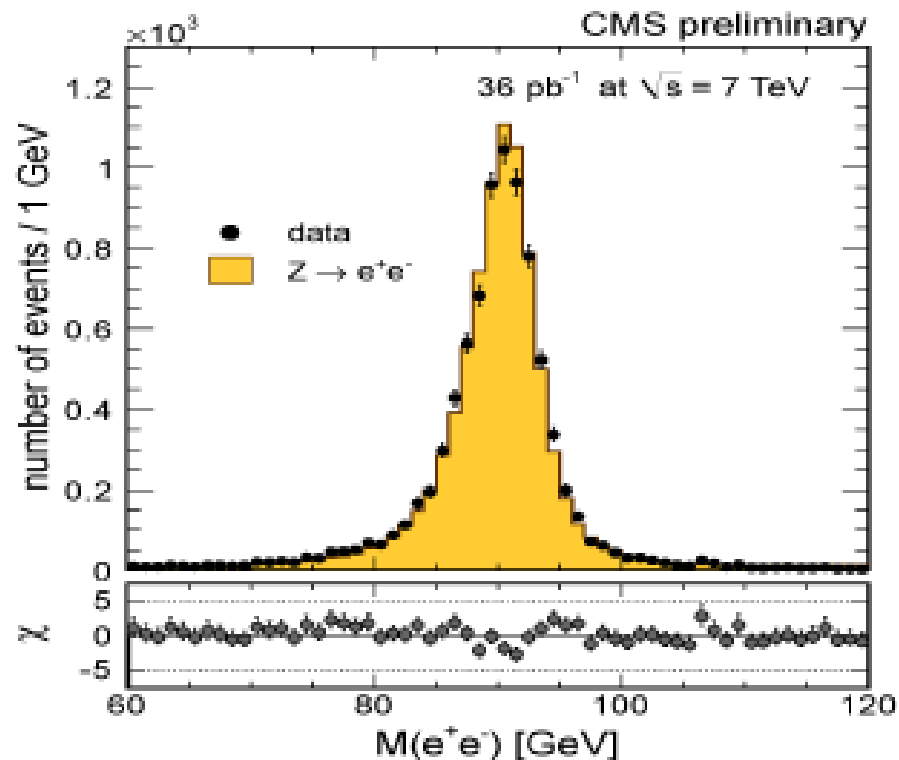


- In CMS, charged particles get well separated due to the huge tracker volume and the high magnetic field (3.8 T)
- CMS has an excellent tracking resolution, able to go down to very low momenta (~few hundred MeV)
- CMS has also an excellent electromagnetic calorimeter with good granularity
- In multijet events, only 10% of energy corresponds to neutral (stable) hadrons

Big improvement in energy resolution and tau identification using particle-flow techniques

# Muons and electrons

- Muon resolution dominated by inner tracking for up to  $p_T \sim 200$  GeV. Typical  $p_T$  resolution 1-2%
- Muon chambers: redundant trigger and coverage, muon identification
- Good identification capabilities: muons reconstructed both in inner tracker and muon spectrometer



- Excellent energy resolution thanks to the precise  $\text{PbWO}_4$  crystal calorimeter.
- Typical  $E_T$  resolution for EWK studies: 1%
- Good charge assignment and track matching, fitting techniques taking into account bremsstrahlung emissions
- Identification based on shower shape variables, tracking matching and HAD/EM. ratio (good agreement with the simulations)

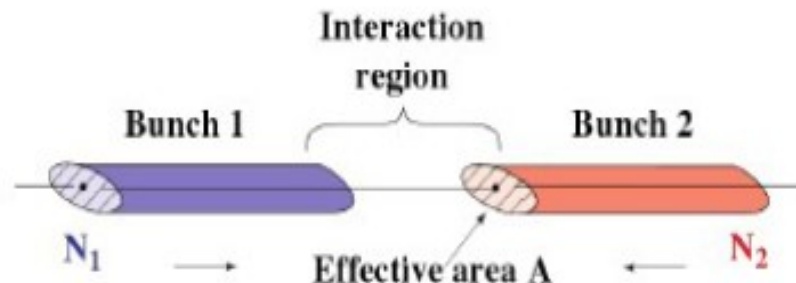
# Luminosity Measurements



$$\mathcal{L} = N_1 N_2 f n_b \int \rho_1(x, y) \rho_2(x, y) dx dy$$

$$\mathcal{L} = \frac{N_1 N_2 f n_b}{A_{\text{eff}}}$$

$$A_{\text{eff}} = 2\pi\sigma_x\sigma_y$$



- Intensities  $N_{1,2}$  measured by LHC beam current transformers
- Shape and size of the interaction region,  $A_{\text{eff}}$ , measured via Van der Meer scans: relative variations or rate as a function of the transverse separation between beams
- Rates measured in CMS using fraction of zero counts of HF and vertexing

Systematic	Error (%)
Effective Area Determination	2.7
Beam Intensity	2.9
Sample Dependence	0.7
<b>Total</b>	<b>4.0</b>

**Uncertainty: 4%**

**Luminosity correction wrt  
initial estimates: -0.7%**



# FONLL (Fixed Order plus Next-to-Leading Logarithms)

( M.Cacciari, M. Greco, S. Frixione, P. Nason) <http://home.cern.ch/cacciari/FONLL>

FONLL is a code for calculating double-differential, single inclusive heavy quark production cross sections in  $p\bar{p}$  and (electro)photoproduction.

it merges the massive NLO calculation with the NLL resummation of terms of collinear origin,  $\alpha \text{Slog}(p_T/m)$ , which become large when  $p_T \gg m$

Two advantages of an FONLL-like framework:

- 1- the perturbative uncertainty does not increase when  $p_T \gg m$
- 2- non-perturbative input describing the quark-to-meson hadronization can be extracted from  $e^+e^-$  data and included in predictions for hadronic collisions in a self-consistent way

## Colour Evaporation Model (CEM)

based on the 'local hadron parton duality approach', Improved by including next to leading order processes. It predicts the  $J/\Psi$  prod Xsec from that of the  $c\bar{c}$  pair.

It assumes that color can be "bleached" (evaporate) by multiple soft gluon interactions, implying a statistical treatment of color

(Because color is the source of hadrons, only the c.o. states yield asymptotically hadronic states)  
CEM does not explain how the formation of the  $J/\Psi$  proceeds. It assumes that the open  $c\bar{c}$  pair transforms with a certain probability into a bound  $c\bar{c}$  pair by soft gluon interactions.

## Cascade

It incorporates off-shell ME for photon-gluon fusion @LO  
with co, based on  $k_T$  fact.

Initial state parton shower generated accordingly to the CCFM equation  
 $j/\psi$  produced in the CSM unintegrated gluon PDFs  
Hadronizat. With Lund string model