

A_{FB} at the Tevatron



4th International Workshop on Top Quark Physics

September 25 - 30, 2011

Sant Feliu de Guixols, Spain

A_{FB} at the Tevatron



You are
here

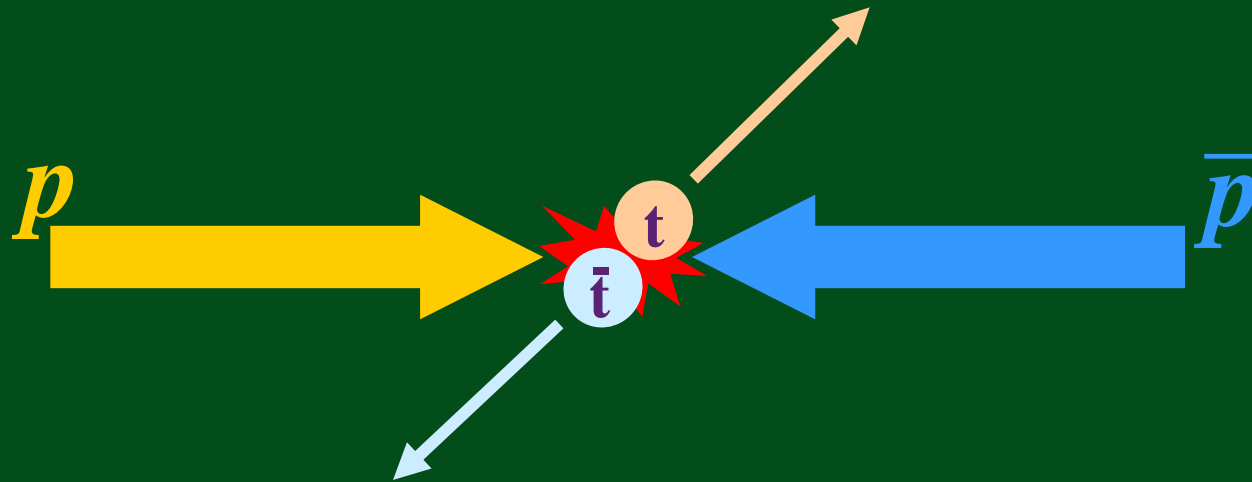
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Forward-Backward?

Is it the top or the antitop that is produced preferentially in the direction of the incoming proton?



Choose an angular variable in some rest frame, and define:

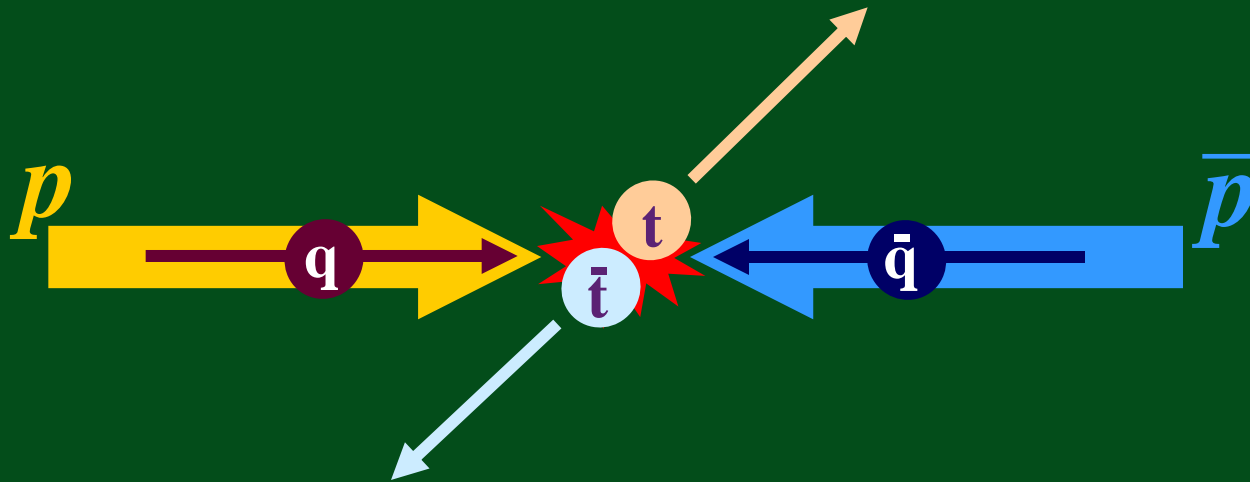
$$A_{FB} = \frac{N_F - N_B}{N_F + N_B}$$

SM motivations

It's not about the incoming protons

It's about the incoming quarks

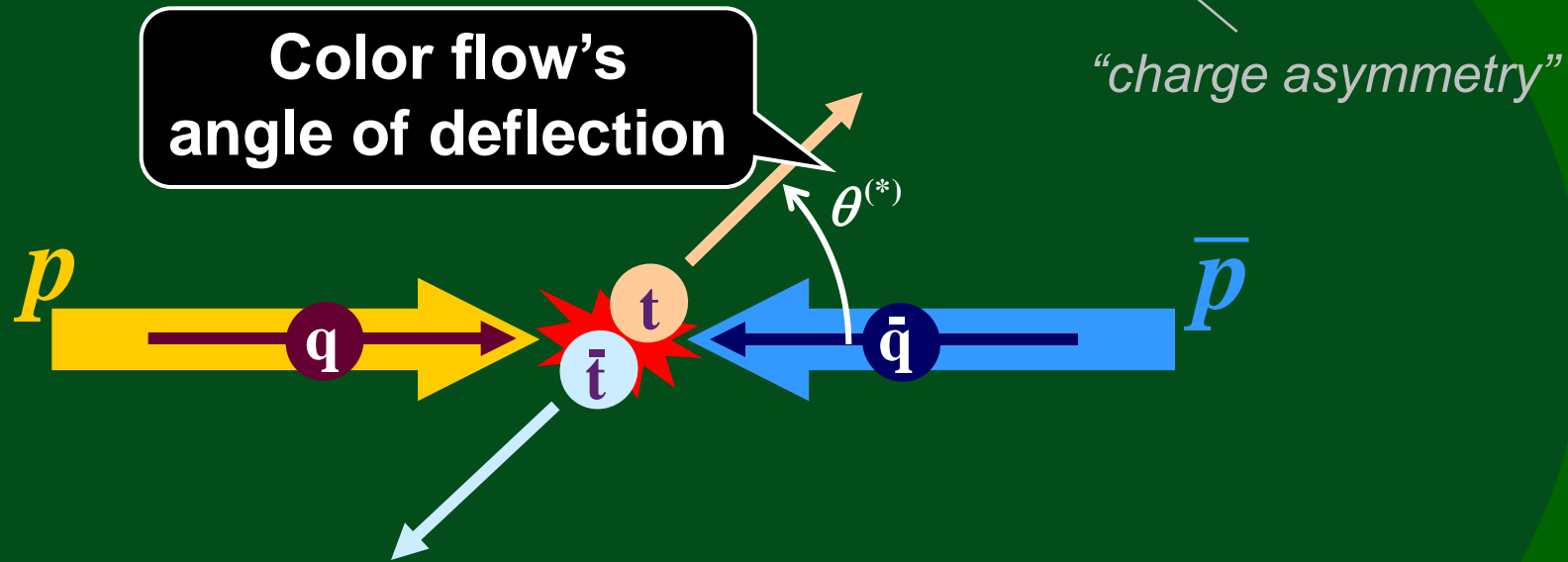
- at the Tevatron: $85\% \ q\bar{q} \rightarrow t\bar{t} + 15\% \ gg \rightarrow t\bar{t}$



SM motivations

It's not about the incoming protons

It's about the incoming quarks and their QCD charges

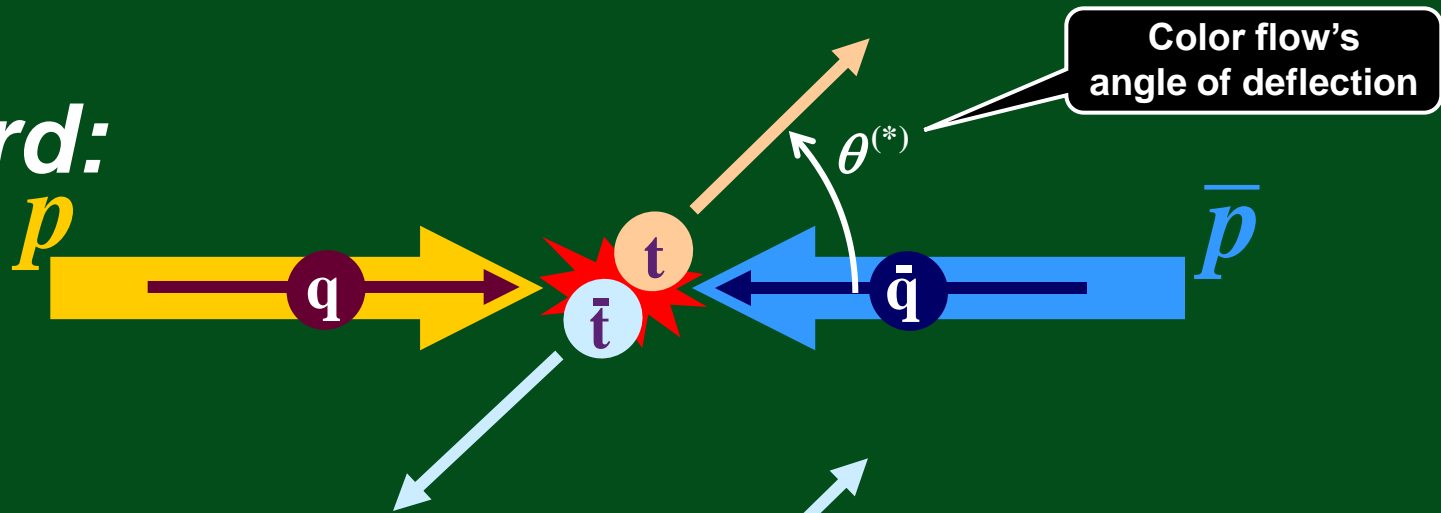


SM motivations

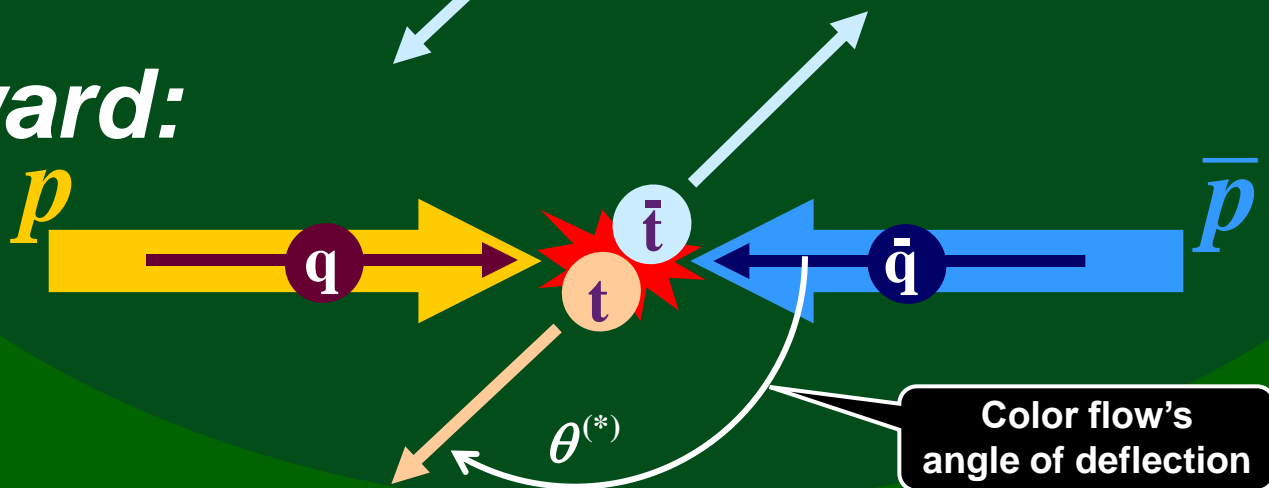
It's not about the incoming protons

It's about the incoming quarks and their QCD charges

Forward:

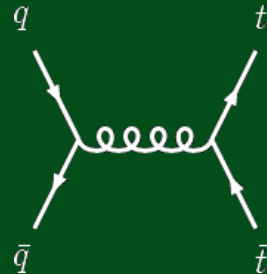


Backward:



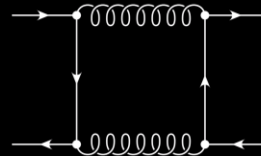
SM predictions

At order α_s^2 : no preference

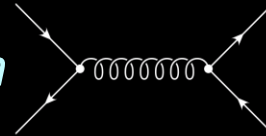


$$A_{FB}^{\alpha_s^2} = 0$$

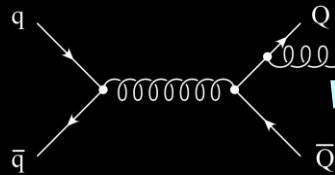
At order α_s^3 : *Interference terms*



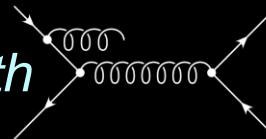
with



Enhances F



with



Enhances B

Kuhn and Rodrigo, PRL 81 (1998):

$$A_{FB}^{LO} = 5\%$$

- incl. flavor creation, etc.
- collision frame $\approx t\bar{t}$ frame

Ahrens et al., arXiv:1106.6051:

$$A_{FB}^{resum} = 7.3\%$$

- LO (i.e. α_s^3 / α_s^2) + NNLL
- $t\bar{t}$ frame (also in lab frame)

Hollik and Pagani, arXiv:1107.2606: $A_{FB}^{LO+EW} \cong 9.0\%$

- $\alpha_s + \alpha_{EW} + \alpha_s^2 / \alpha_{EW}^2$
- $t\bar{t}$ frame (also in lab frame)

SM motivations

1. “Retro” style: a test of the discrete symmetries of the strong force at high energies (is QCD really the theory of the strong force?)
2. Test of challenging SM calculations
 - this is also an argument against the measurement

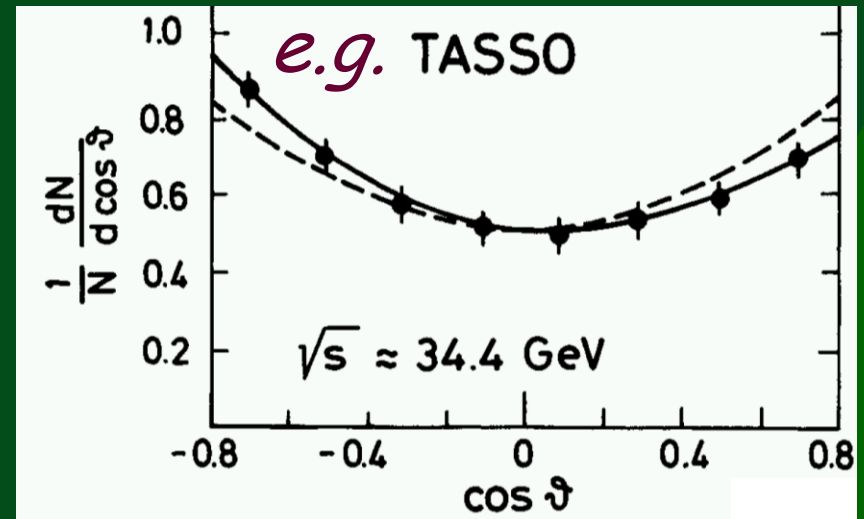
The above reasons got some of us into this measurement

But why are you listening to this talk?

SM motivations

1. “Retro” style: a test of the discrete symmetries of the strong force at high energies (is QCD really the theory of the strong force?)
2. Test of challenging SM calculations
 - this is also an argument against the measurement
3. Small SM predictions → can identify beyond the SM physics
 - Already happened for A_{FB} and EW physics in the 80s!
 - A_{FB} in $e^+e^- \rightarrow \mu^+\mu^-$
 - $E_{\text{c.m.}} = 35\text{ GeV}$
 - Indication for Z resonance

Adrian also reminded us of the LEP precedence – but little learned there



Inclusive A_{FB} in lepton+jets

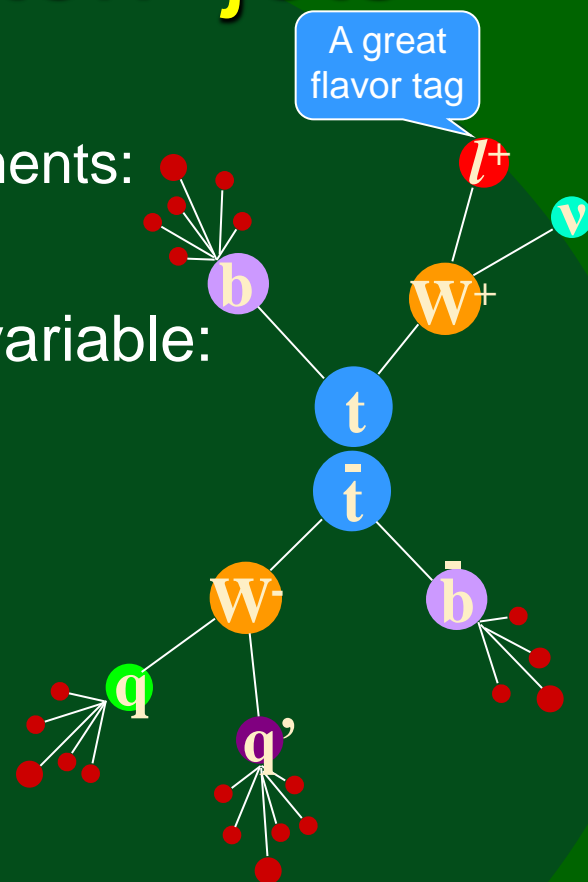
Most powerful channel: lepton (e/μ) + jets

Start with the (conceptually) simplest measurements:

Inclusive measurements with the angular variable:

$$\Delta y = y_t - y_{\bar{t}} = q_l (y_{t,\text{lep}} - y_{t,\text{had}})$$

- i.e. $t\bar{t}$ frame
 - Combines information from both top quarks
 - Invariant to boosts along the beam axis
- and so: $A_{FB} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$



Phys. Rev. D **83**,
(2011) 112003

$$\int \mathcal{L} dt = 5.3 \text{ fb}^{-1}$$

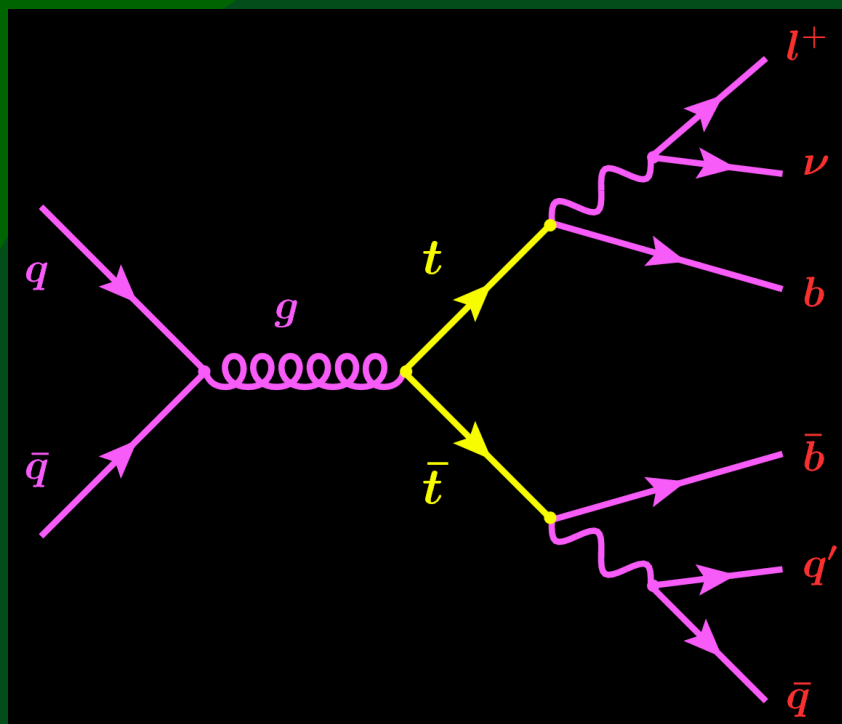


arXiv:1107.4995

Submitted to Phys. Rev. D

$$\int \mathcal{L} dt = 5.4 \text{ fb}^{-1}$$

Selection



Require:

- 1 lepton with $E_T \geq 20 \text{ GeV}$
 - CDF: $|\eta| < 1.1$
 - DØ: $|\eta_e| < 1.1, |\eta_\mu| < 2.0$
- p_T imbalance (MET) $> 20 \text{ GeV}$
- ≥ 4 jets with $E_T \geq 20 \text{ GeV}$
 - CDF: $|\eta| < 2.0$
 - DØ: $|\eta| < 2.5$
- ≥ 1 b -tagged jet

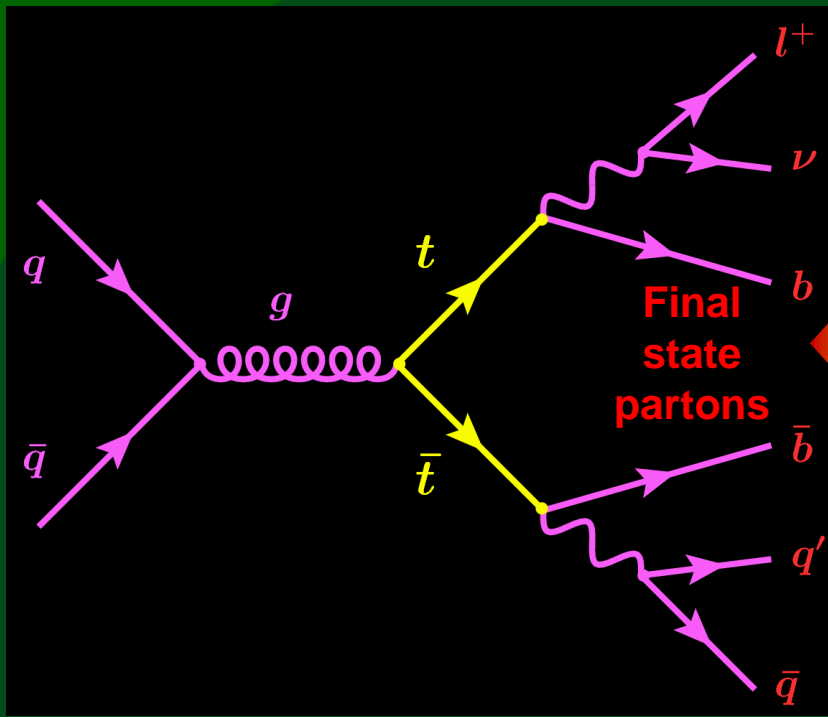


1260 events
22% background
977 est. signal

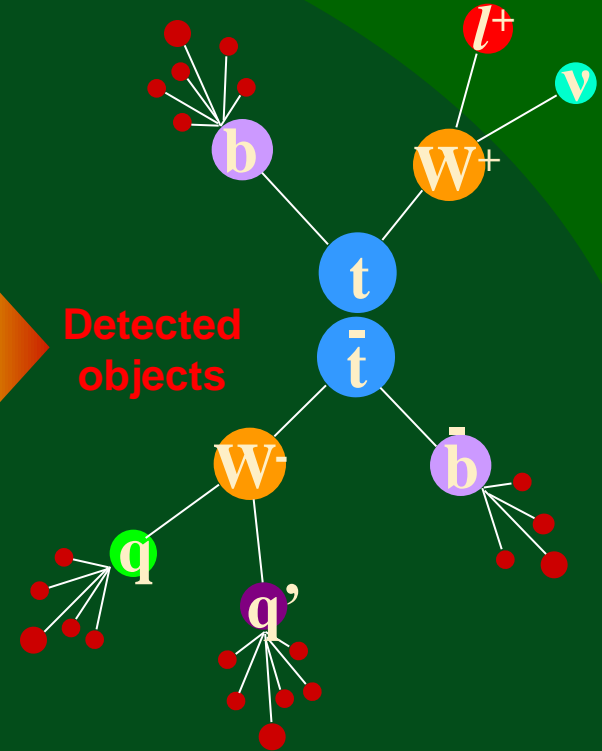


1581 events
29% background
1126 est. signal

Reconstruction



assign



Assign objects to final state partons using χ^2 test statistic that accounts for experimental resolutions, b -tags, $M_W=80.4\text{ GeV}$ & $m_t=170\text{ GeV}$



Varies object E in χ^2
 χ^2 includes Γ_W and Γ_t



Object E and direction varied and propagated into reconstruction ("kinematic fitter")

Assignment \rightarrow All final state 4-vectors available. In particular, Δy

Extracting detector-level A_{FB}

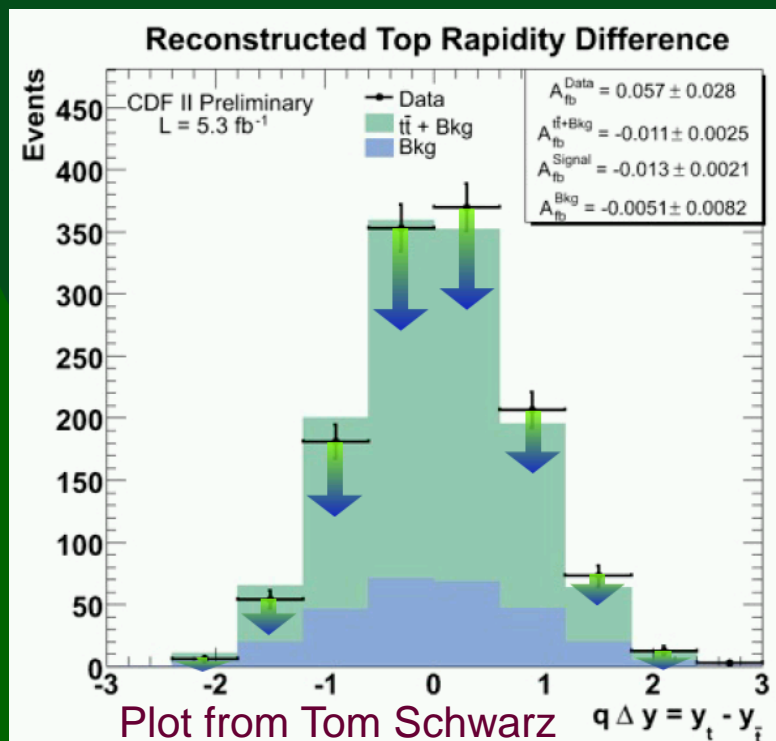


Subtract estimated background

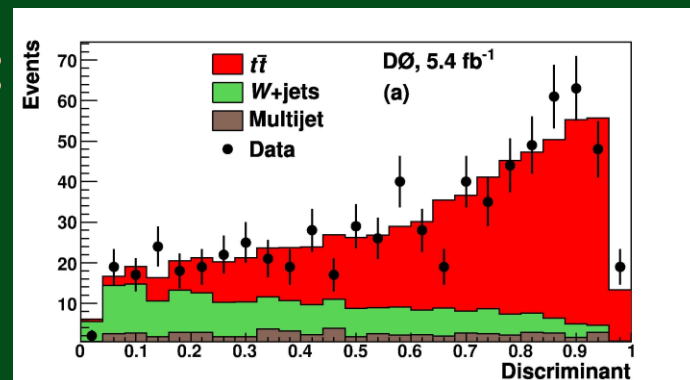
- Estimates from x-sec measurements
 - $W+jets$ estimated from $N_{pre-b-tag}$

Fit for sample composition and A_{FB}

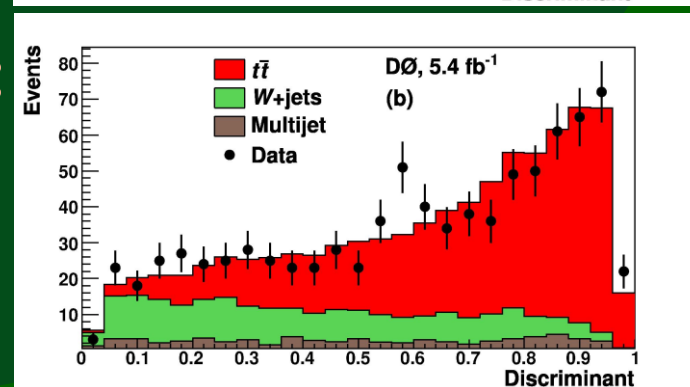
- Discriminant for $W+jets$ vs. signal



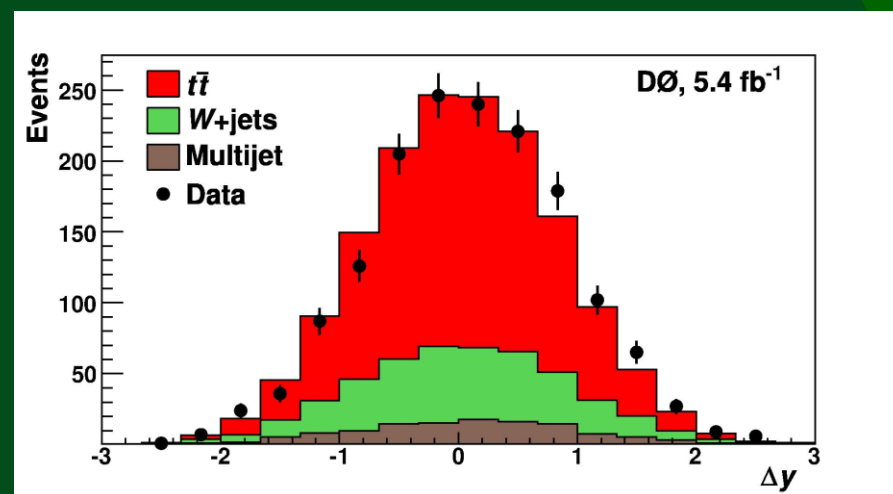
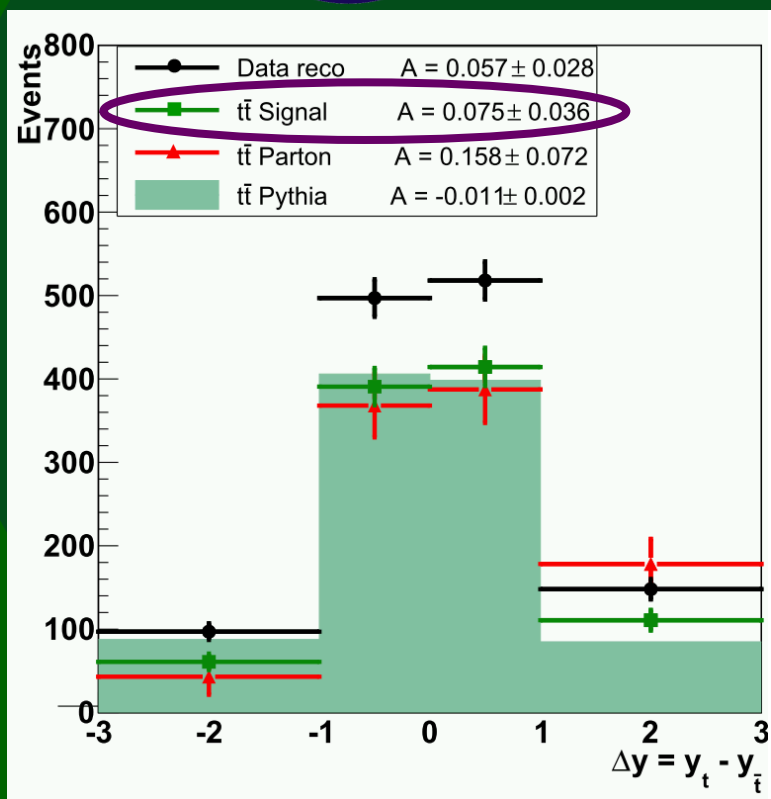
$\Delta y > 0$:



$\Delta y < 0$:



Detector-level A_{FB} s



	$l+\geq 4$ jets	$l+4$ jets	$l+\geq 5$ jets
$A_{FB}(\%)$	9.2 ± 3.7	12.2 ± 4.3	-3.0 ± 7.9
MC@NLO $A_{FB}(\%)$	2.4 ± 0.7	3.9 ± 0.8	-2.9 ± 1.1

Was central to previous DØ results

Inconvenient - can't compare directly to calculations

- but possible, see PRL **100**, 142002 (2008), and PRD **83**, (2011) 114027

Unfolding inclusive A_{FB} is easy

Measure a distribution:
(in N bins)



corrections

Some components well
measured, some not
→ N - dimensional info

*Typical unfolding problem:
how to summarize?*

*No problem:
 A_{FB} is the summary*

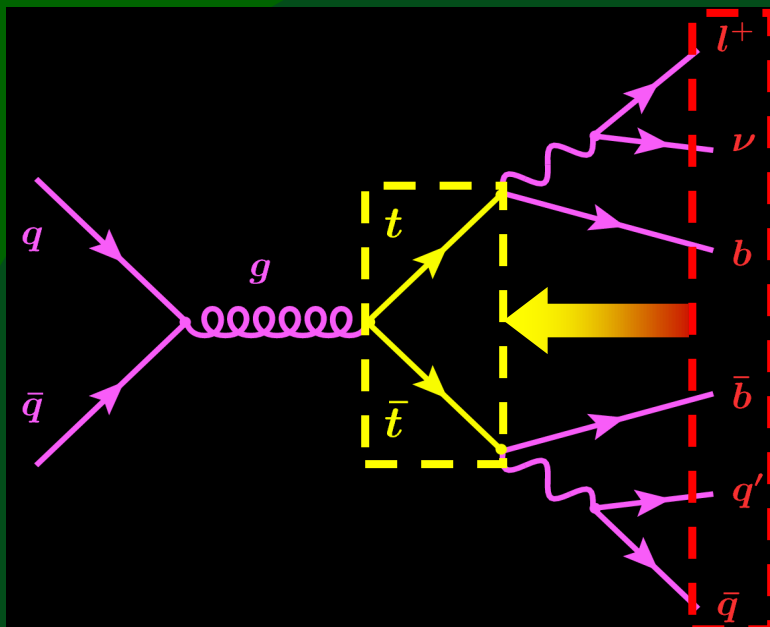
Can add regularization
to suppress fluctuations

A 2D plot

A_{FB}



Unfolding

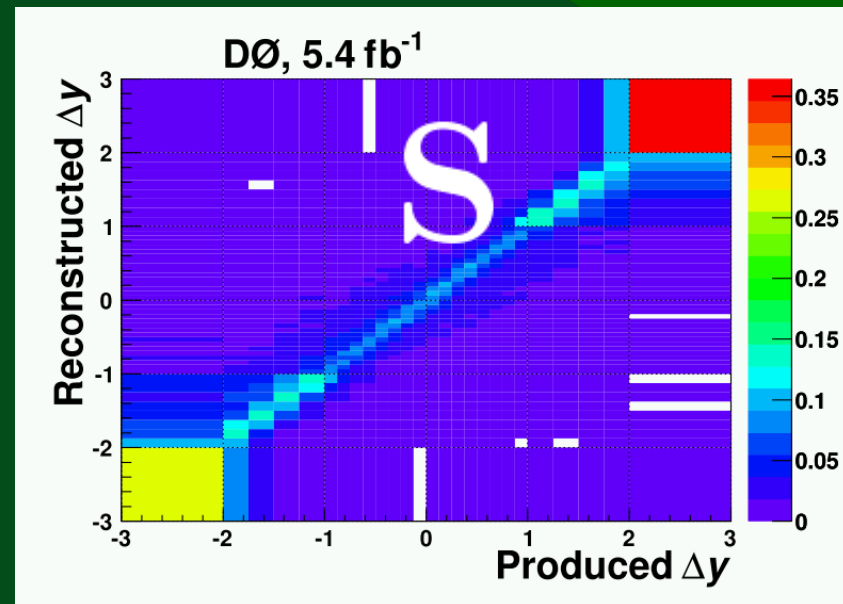


4 bin unfolding. Δy edges: -3, -1, 0, 1, 3

$$\vec{n}_{\text{parton}} = \mathbf{A}^{-1} \mathbf{S}^{-1} (\vec{n}_{\text{data}} - \vec{n}_{\text{bkg}})$$

**Acceptance
matrix
(diagonal)**

**Migration
matrix**



50 \rightarrow 26 bin regularized unfolding

- extended TUnfold for variable binning

Improves statistical strength

- expected (if BSM)
- and observed (1.9SD \rightarrow 2.4SD)



Fine-bin unfolding

Binning is crucial to unfolding (an implicit regularization)

- Narrow bins near $\Delta y=0$ boundary to fully describe migrations
- Wide bins at high $|\Delta y|$ due to limited MC statistics

Regularization term based on continuous curvature of density

- Curvature \rightarrow sum of absolute value of discrete 2nd derivative
- Density = diff. x-sec rather than bin counts \rightarrow need to account for bin widths

Regularization strength ***balances***

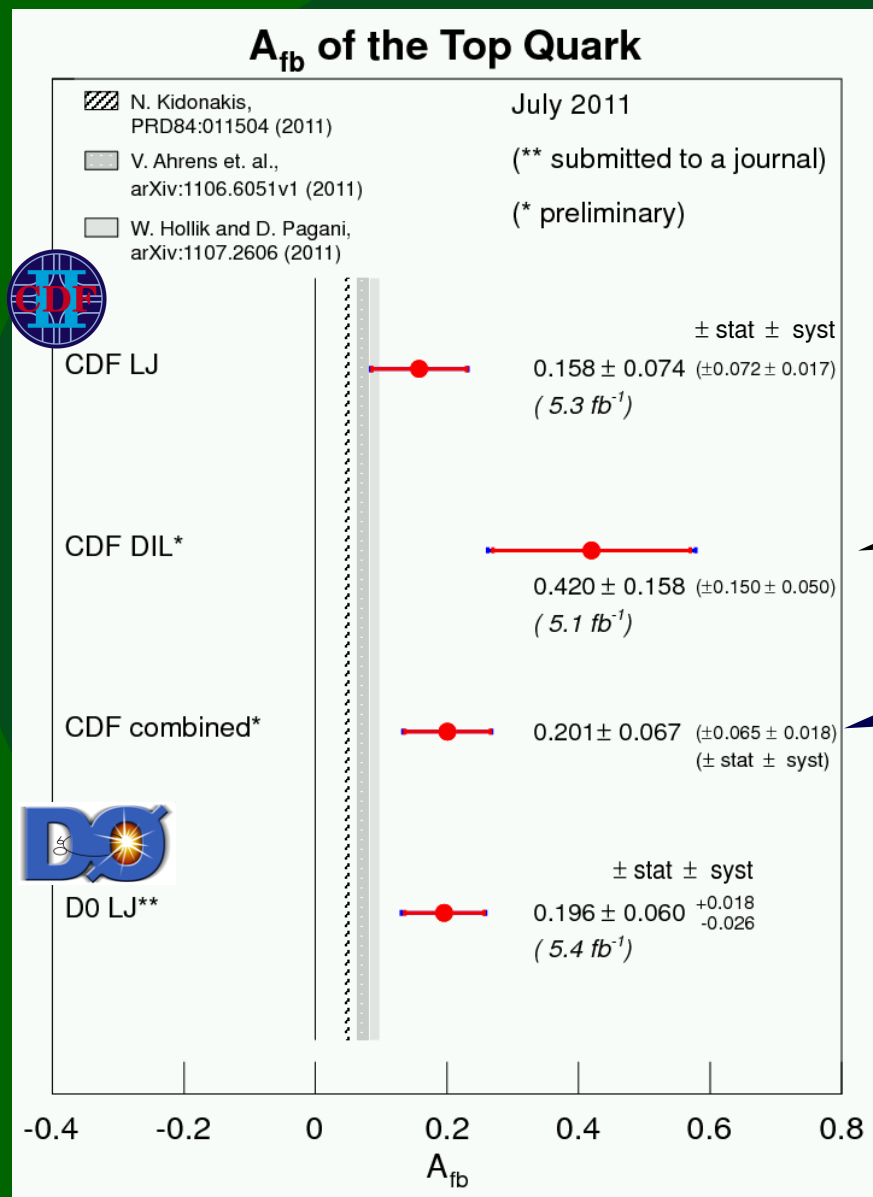
- statistical strength
- bias – we correct for bias on A_{FB} , but it's still an issue since...

Bias is model dependent

- Examines dozens of generator-level distributions (i.e. alternative models)
- Systematic uncertainties cover all realistic cases
- To invalidate systematic uncertainties: sharp bin-to-bin jumps.
 - 26 generator level bins...
 - s-channel narrow resonances have sharp edges – but already ruled out (Tuesday)

Production-level A_{FB} s

Inclusive, Δy -based A_{FB} s



Dileptons - In a few slides...

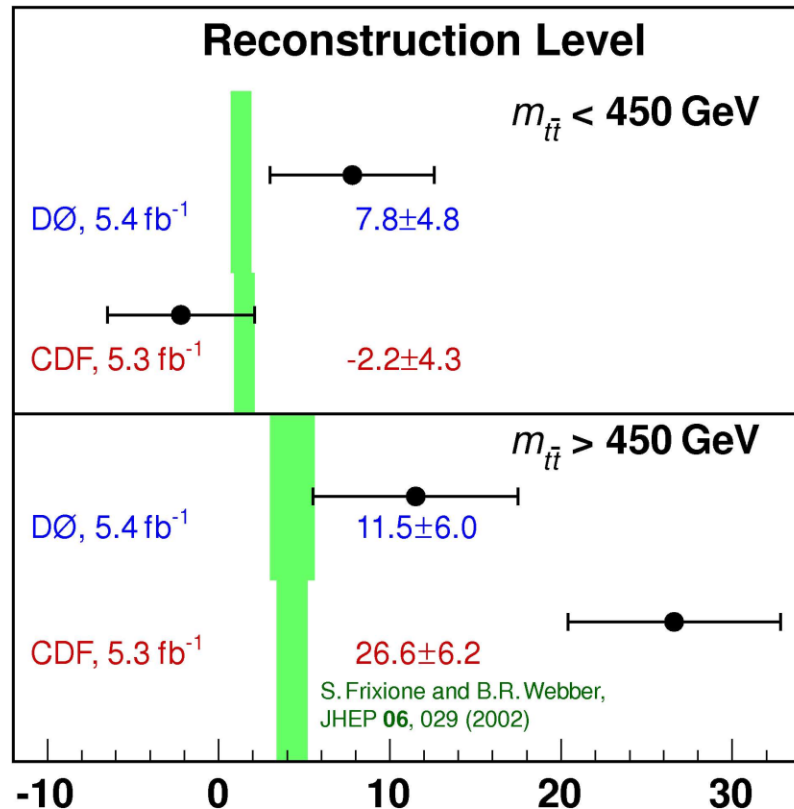
CDF Note #10584

Mass dependence – det. level

BSM contributions to AFB will change its dependence on $m_{t\bar{t}}$

- BSM contributions often through BSM+SM interference
- CDF introduced cut at $m_{t\bar{t}} = 450 \text{ GeV}$, cut value optimized on MC

Forward-Backward Top Asymmetry, %

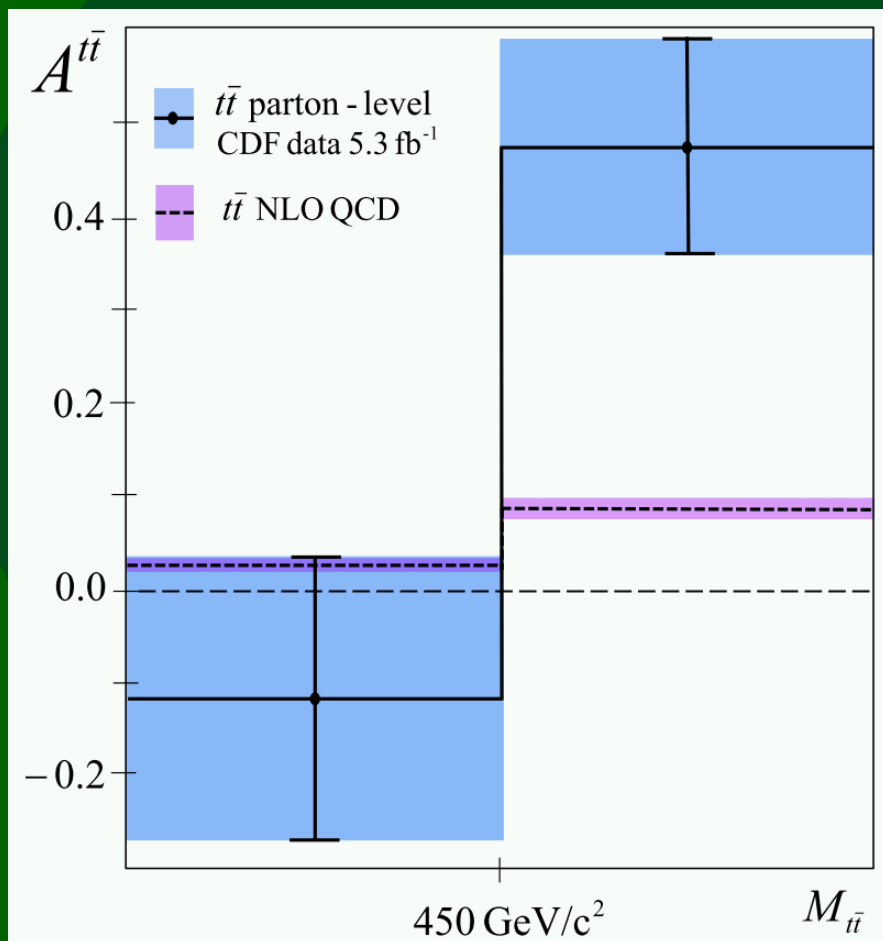


CDF di-lepton data also suggests a mass dependence:

$$\Delta A_{\text{FB}}^{\text{raw}} = (11 \pm 12)\%$$

Mass dependence – CDF prod.

Having observed a mass dependence, CDF reports also at production level. 4 bin unfolding



A 3σ discrepancy:

$$A_{\text{FB}} = (48 \pm 11 \text{ (total)})\%$$

vs.

$$A_{\text{FB}}^{\text{MCFM}} = (9 \pm 1)\%$$

→ lots excitement

and it's at high mass

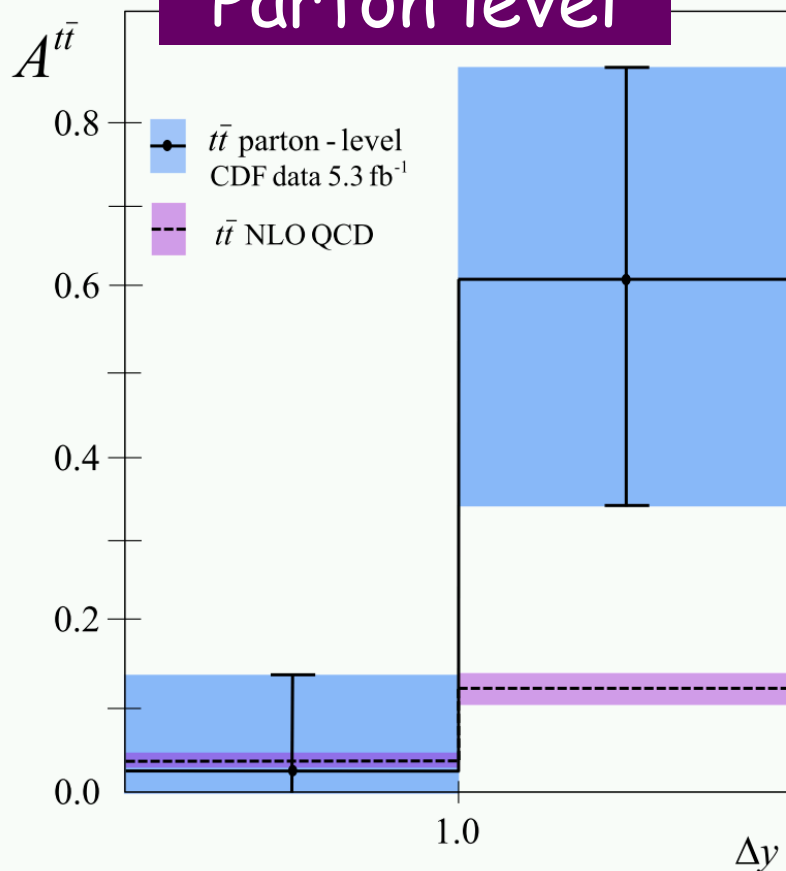
→ lots of BSM papers

Statistical significance at high mass 3.4 SD – not enhanced by unfolding

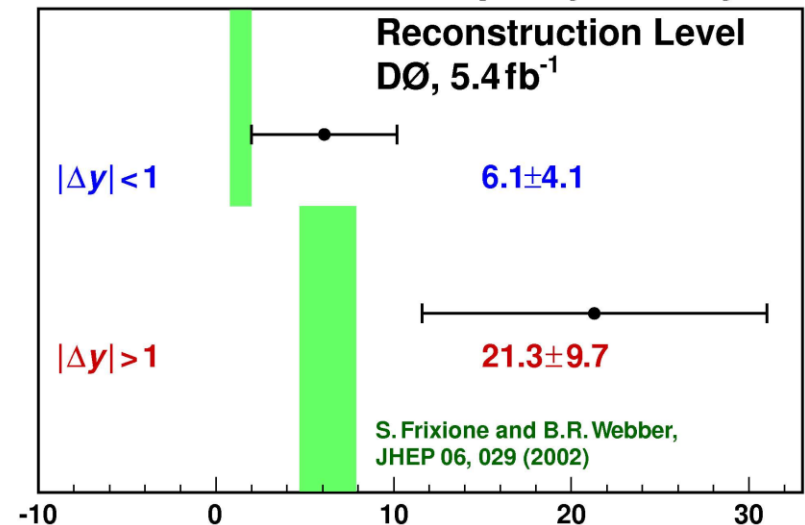
$|\Delta y|$ dependence



Parton level



Forward-Backward Top Asymmetry, %

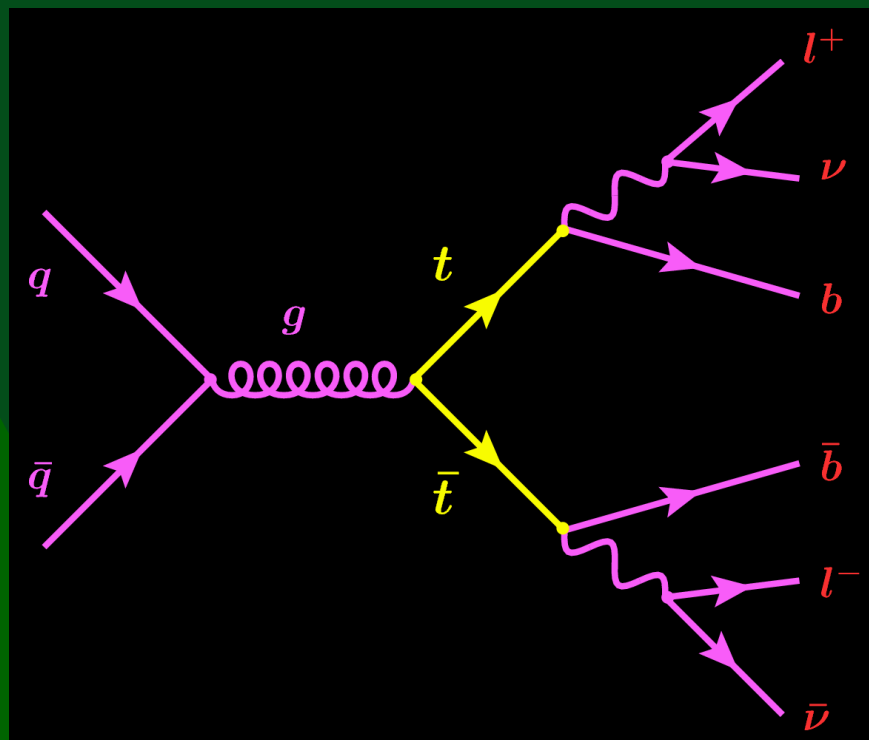


Di-lepton selection



CDF note 10436

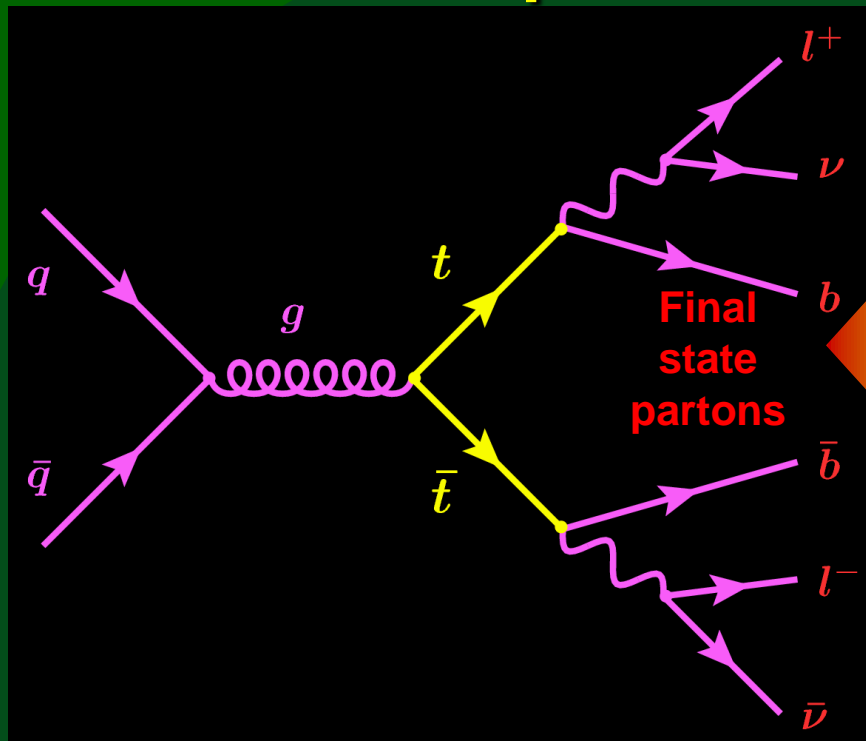
$$\int \mathcal{L} dt = 5.1 \text{ fb}^{-1}$$



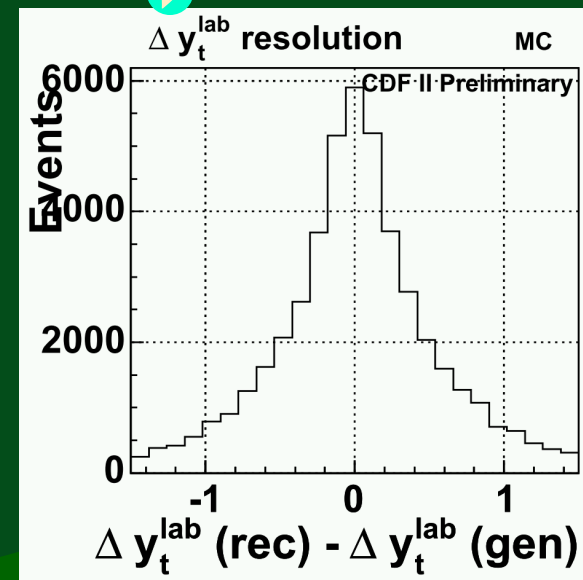
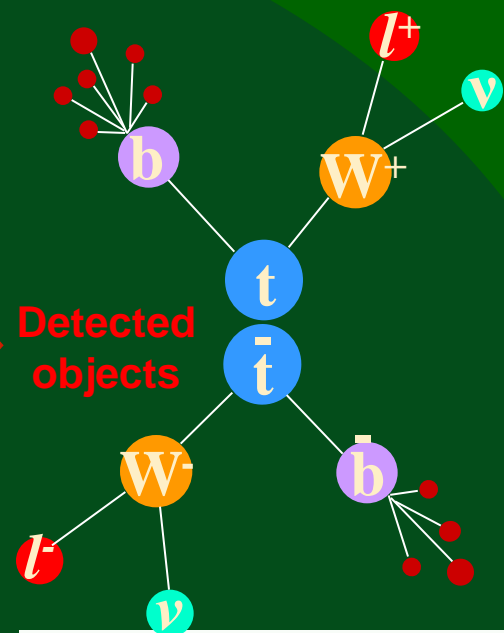
Require:

- 2 lepton with $E_T \geq 20 \text{ GeV}$,
 - $|\eta_e| < 1.1$ or $1.2 < |\eta_e| < 2.8$, $|\eta_\mu| < 1.1$
- p_T imbalance (MET) > **25 or 50** GeV
 - depending on angular separation
- ≥ 2 jets with $E_T \geq 15 \text{ GeV}$, $|\eta| < 2.5$
- $H_T > 200 \text{ GeV}$
 - scalar sum: lepton, jet E_T s + MET

Di-lepton reconstruction



assign



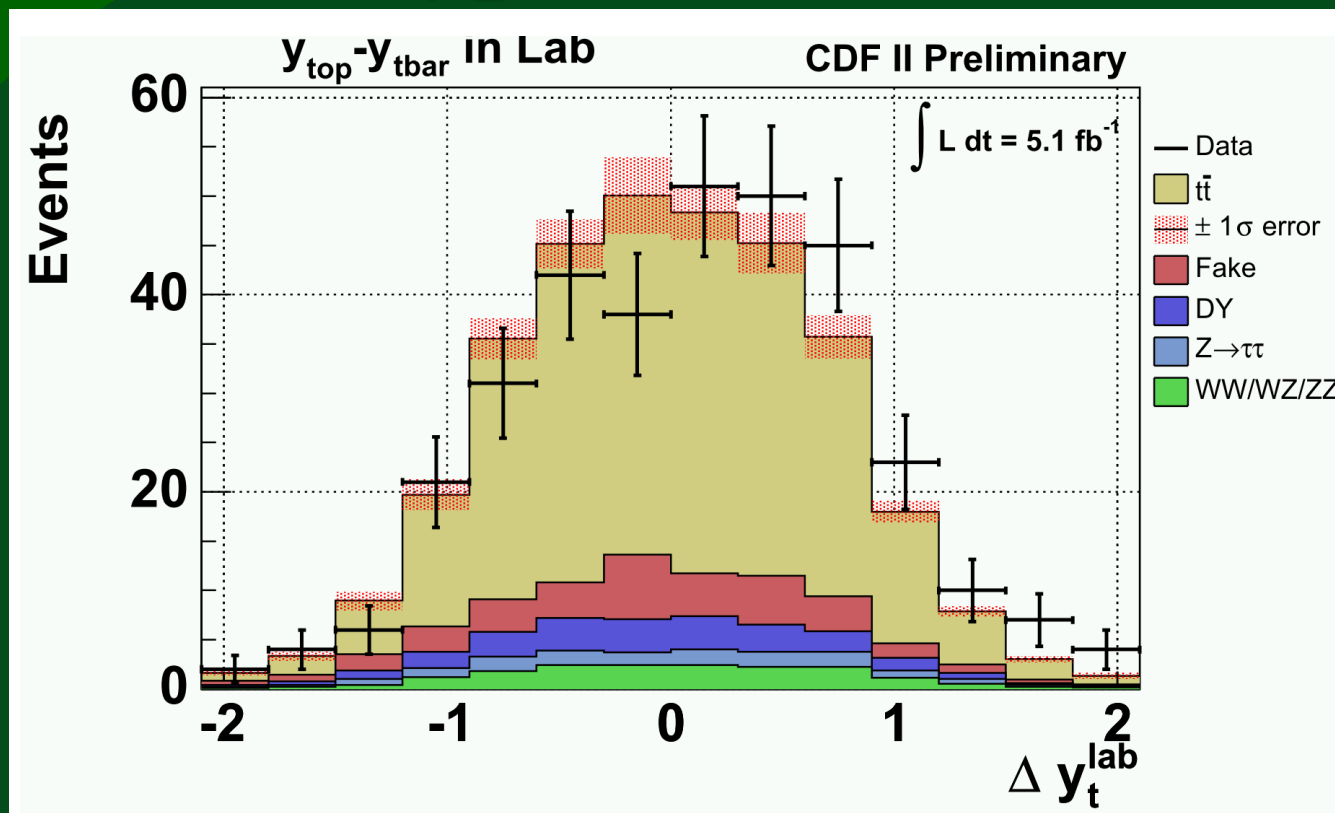
Again: kinematic fitting, χ^2 test statistic.

But fewer observables \rightarrow difficult reconstruction

\rightarrow also use a-priori distributions of $p_T^{t\bar{t}}$, $p_z^{t\bar{t}}$ and $m_{t\bar{t}}$

Excellent Δy reconstruction achieved!

A_{FB} in dileptons



A_{FB} extracted in two steps:

1. Background subtraction: $A_{FB}^{raw} = (14 \pm 5) \% \rightarrow A_{FB}^{sub} = (21 \pm 7) \%$
2. Assume A_{FB} is linear in Δy , to find $A_{FB} = (42 \pm 15 \text{ (stat)} \pm 4 \text{ (syst)}) \%$
 - Validated for Pythia, NLO QCD, axigluon models
 - 2.6σ from zero, 2.3σ from prediction ($A_{FB}=6\%$)

Lepton-based A_{FB} s

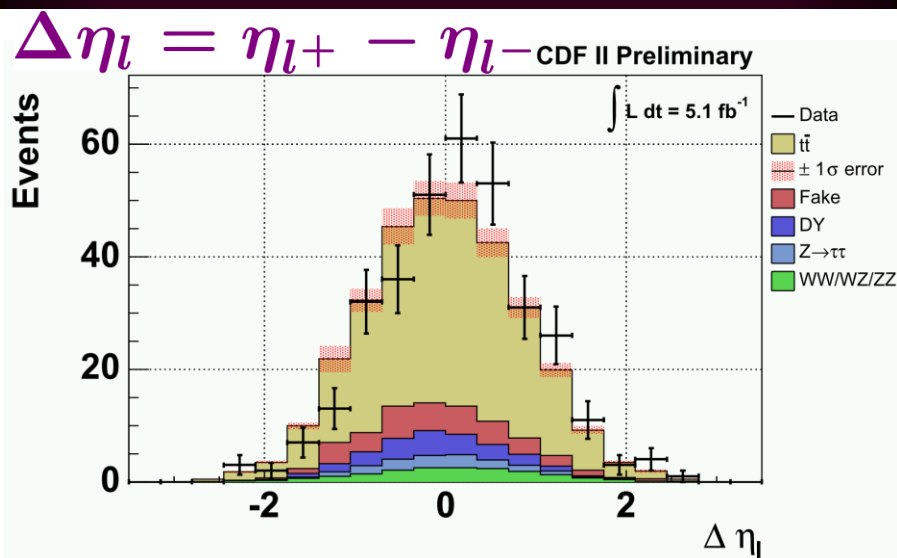
New angular variables \rightarrow new A_{FB} s

Lepton based \rightarrow Excellent resolution \rightarrow Simple unfolding & interpretation

- Sensitive to the top pair A_{FB} and their polarization, but less sensitive to θ^*



Di-lepton channel

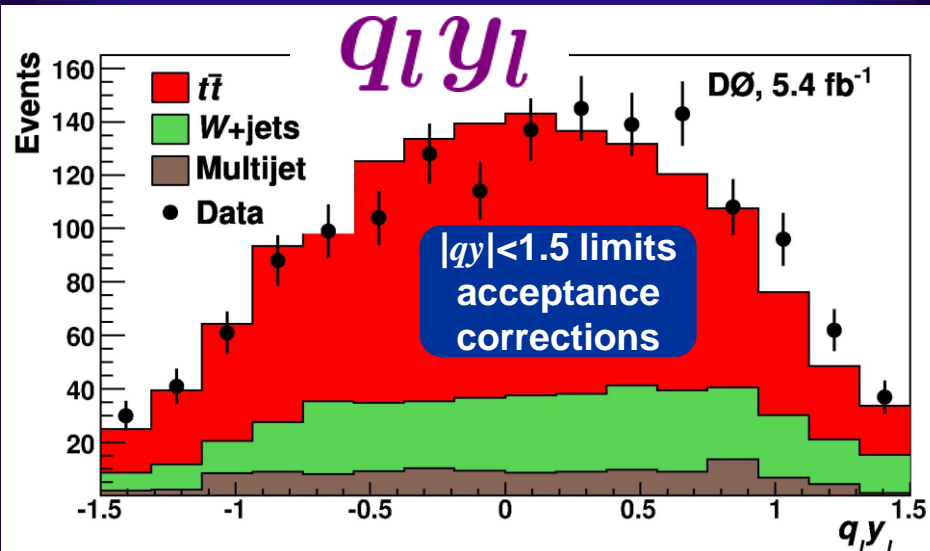


Almost the same numbers:

$$A_{FB}^{\text{raw}} = (14 \pm 5) \% \rightarrow A_{FB}^{\text{sub}} = (21 \pm 7) \%$$



$l+jets$ channel



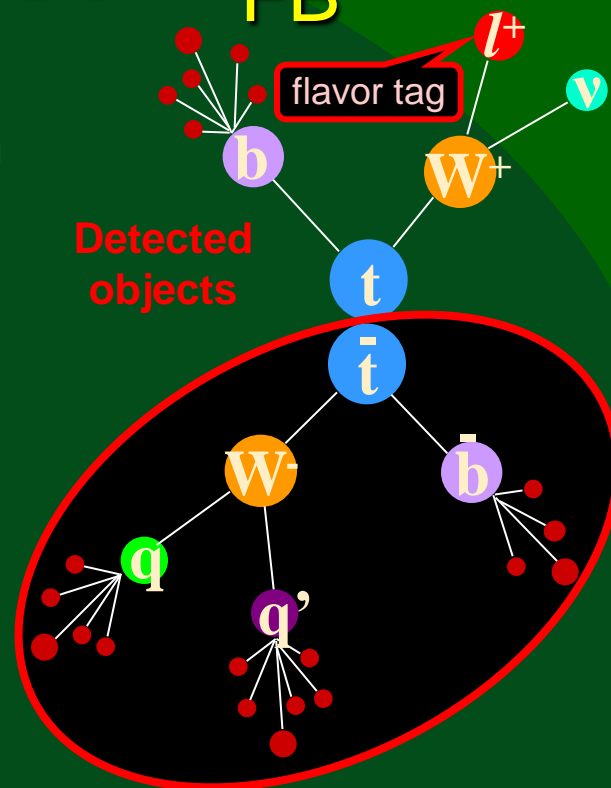
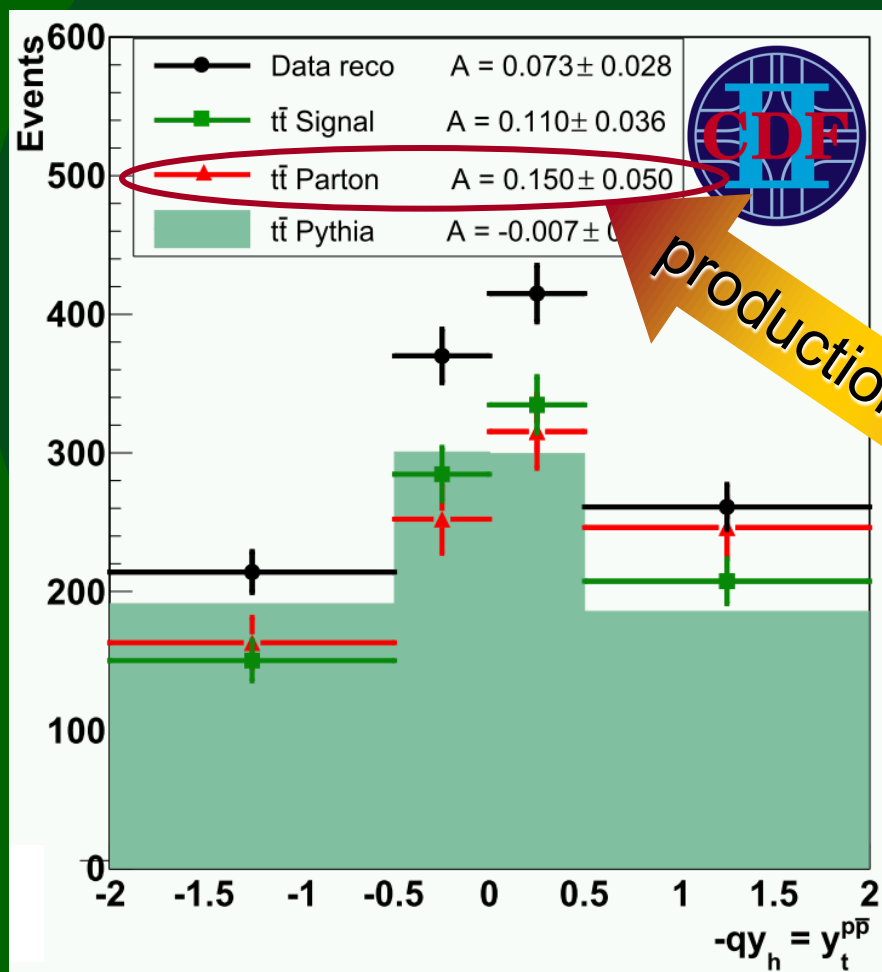
	$l+\geq 4$ jets	$l+4$ jets	$l+\geq 5$ jets
A_{FB}^l (%)	14.2 ± 3.8	15.9 ± 4.3	7.0 ± 8.0
MC@NLO A_{FB}^l (%)	0.8 ± 0.6	2.1 ± 0.6	-3.8 ± 1.2

$>3\sigma$ away from MC@NLO

Hadronic-top based A_{FB}

New angular variables \rightarrow new A_{FB} s

Use only the “hadronic” top \rightarrow Better resolution
 \rightarrow more stable unfolding



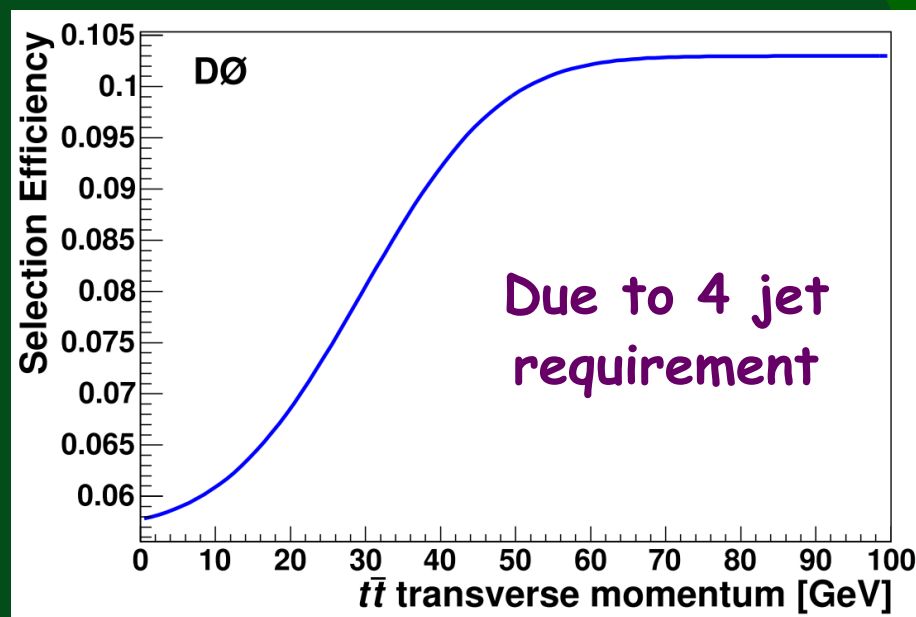
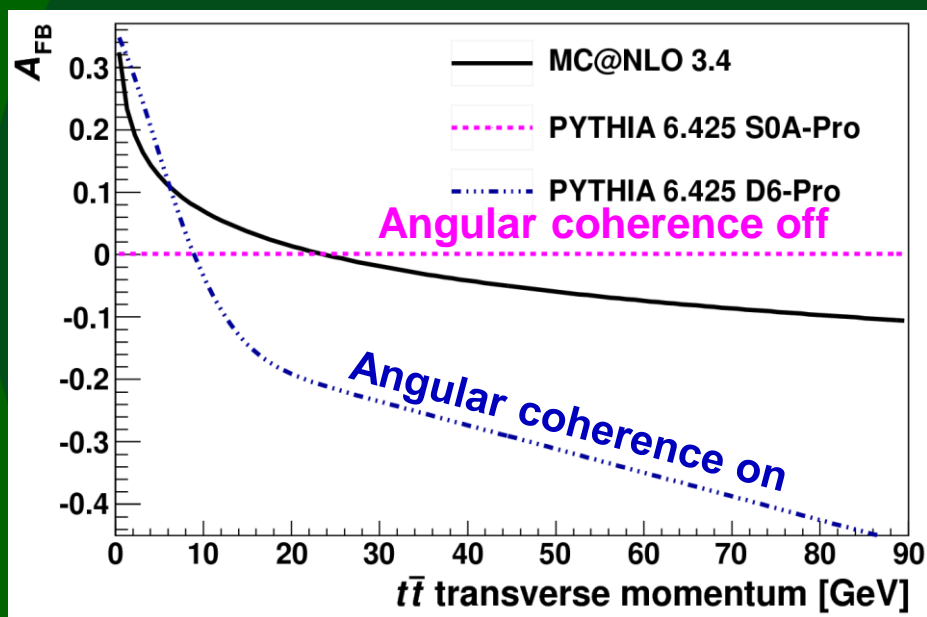
$$A_{FB}^{MCFM} = 3.8\%$$

- Sensitive to collision frame's boost
- Superior resolution compensates
- Observed less mass dependence

A related observable

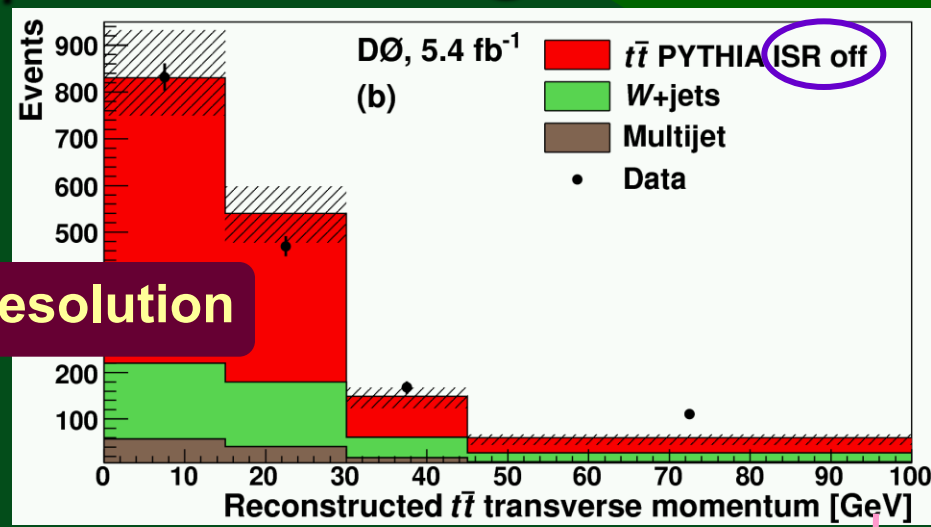
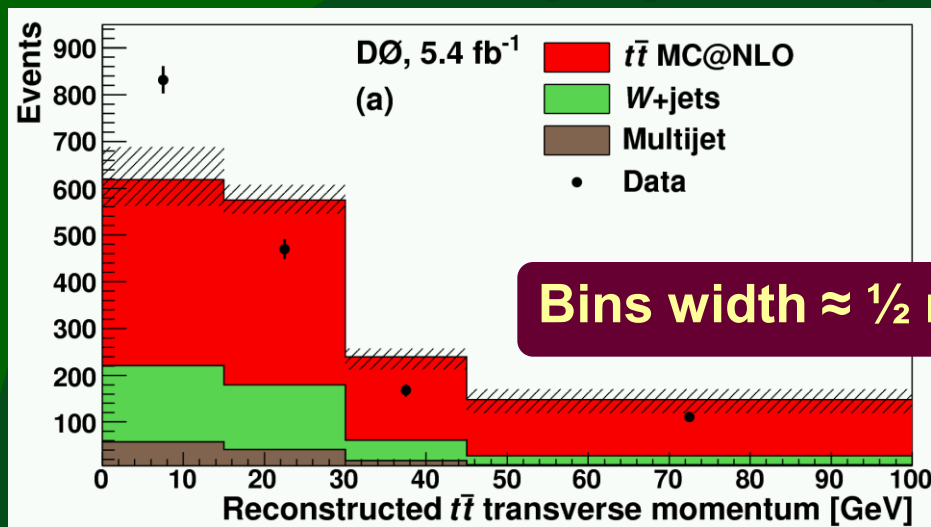


- Noted: $A_{\text{FB}} \leftrightarrow p_T^{t\bar{t}}$
- Is gluon radiation the same in forward and backward events?
 - experimental constraints are few and indirect



- If correlation exists, backward events selected more often than forward events
- One of the leading systematic uncertainties
 - newly identified \rightarrow conservative estimate by turning dependence off \rightarrow -1.6%(absolute)
 - all measurements are statistics dominated \rightarrow will not invalidate any measurement

Top pair p_T modeling

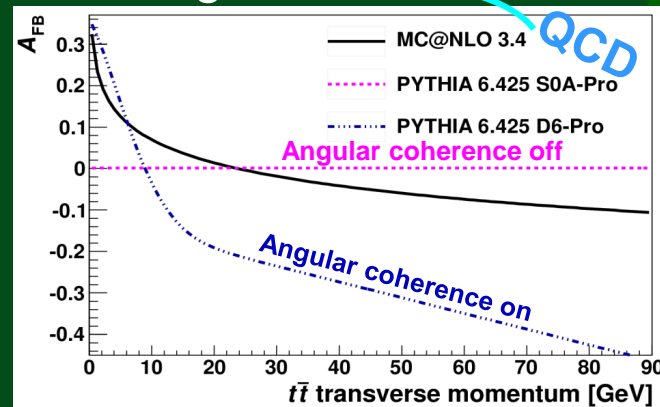


Bins width $\approx \frac{1}{2}$ resolution

- Drastic change needed to get simulation closer to data
 - top pair p_T badly modeled (A_{FB} measurements still OK – see prev. slide)
 - effect in the same direction as A_{FB} – hints at QCD origin?

- But: a check – *not a full measurement*

- reconstruction not tweaked for observable
 - very low resolution
- discriminant correlated with top pair p_T
- partial systematic uncertainties
- no unfolding



Calls for a dedicated measurement of top pair p_T

Conclusions

- Several “top forward backward asymmetries” measured
 - they are all very correlated
- Deviations from SM predictions of $\sim 2\text{--}3\sigma$
- Two $>3\sigma$ differences:
 - 1) CDF: $l+\text{jets}$, high mass, Δy -based
 - exciting as indicates BSM
 - but mass dependence is marginal in $D\bar{O}$ data
 - 2) $D\bar{O}$: $l+\text{jets}$, inclusive, lepton-based
 - but less sensitive to most BSM scenarios than Δy -based A_{FB}

Conclusions

- Several “top forward backward asymmetries” measured
 - they are all very correlated
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 - exciting as indicates BSM
 - but mass dependence is marginal in $D\bar{O}$ data
 - 2) $D\bar{O}$: $l+\text{jets}$, inclusive, lepton-based
 - but less sensitive to most BSM scenarios than Δy -based A_{FB}
- SM predictions creeping upwards?
 - combining CDF & $D\bar{O}$ on the back of an envelop:
tension with LO prediction $>3\sigma$, but with Hollik & Pagani $<3\sigma$

Homework assignment:

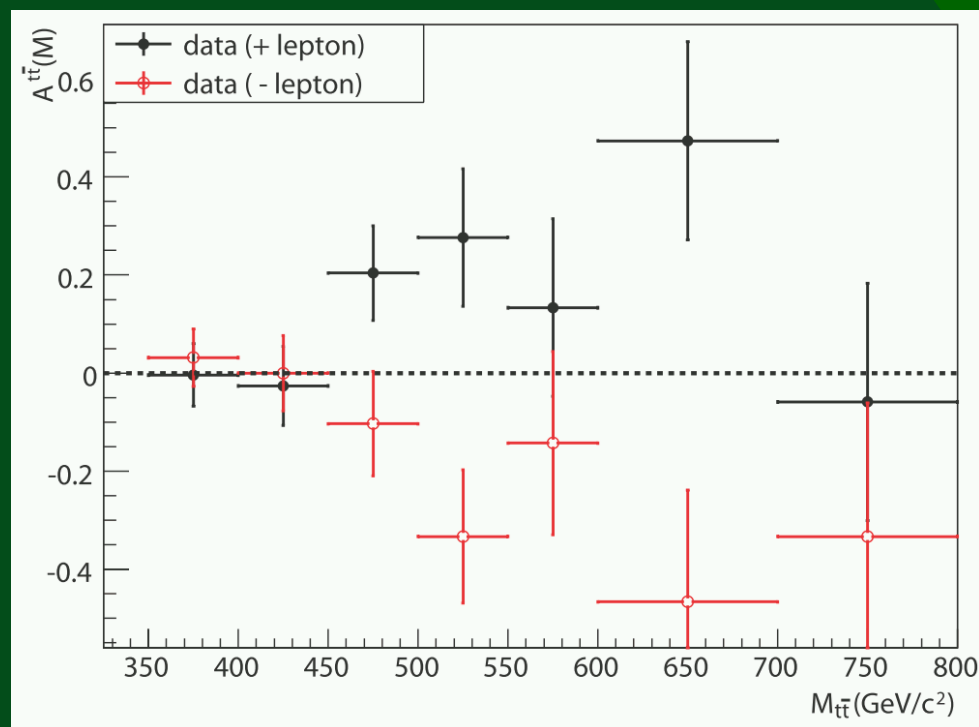
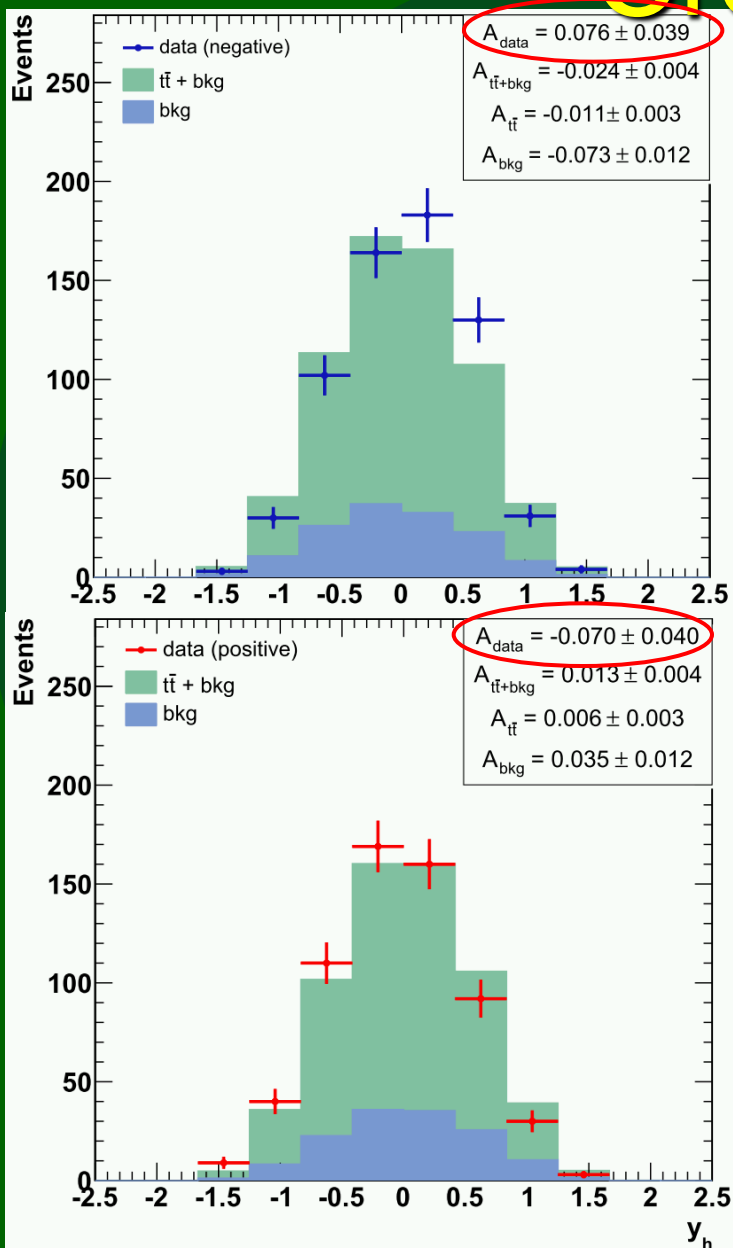
Cook up a BSM scenario where the CDF di-lepton result supports both 1&2

- More data on the way
 - More channels
 - Analysis improvements?
- ***Stay tuned!***

Back up slides

Cross checks

Should we combine A_{FB}^t and $A_{FB}^{\bar{t}}$?



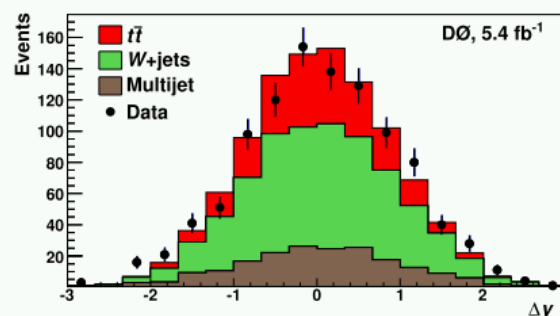
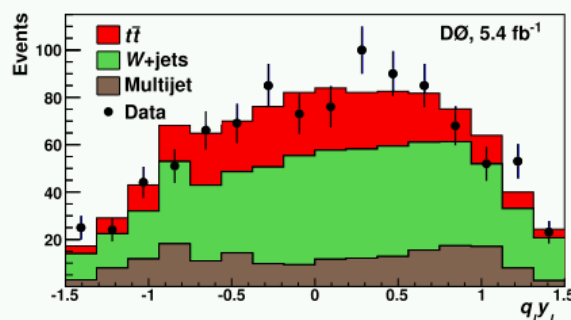
Black vs. red – a check of CP violation

- Should be opposite in this presentation

Cross checks

Cross checks

- Simultaneously measured A_{FB} for $t\bar{t}$ and W +jets
 - Also included events with 0 b-tags
 - Measured A_{FB} for W +jets in good agreement with simulation



- Checked A_{FB} by solenoid and toroid polarities
 - Found no significant dependence
- Checked A_{FB} by lepton charge
 - Found no significant dependence
- Good agreement between e +jets and μ +jets ←

CDF data (no bkg. sub.)

selection	$A^{t\bar{t}}$	$A^{\text{p}\bar{\text{p}}}$
inclusive	0.057 ± 0.028	0.073 ± 0.028
electrons	0.026 ± 0.037	0.053 ± 0.037
muons	0.105 ± 0.043	0.099 ± 0.043
single b -tags	0.058 ± 0.031	0.095 ± 0.032
double b -tags	0.053 ± 0.059	-0.004 ± 0.060



More on unfolding

Binning is crucial to unfolding (an implicit regularization)

- Narrow bins near $\Delta y=0$ boundary to fully describe migrations
- Wide bins at high $|\Delta y|$ due to limited MC statistics

Regularization term based on continuous curvature of density

- Curvature \rightarrow sum of absolute value of discrete 2nd derivative
- Density = diff. x-sec rather than bin counts \rightarrow need to account for bin widths
 - introduced functionality into TUnfold

Regularization strength ***balances***

- statistical strength
- bias – we correct for bias on A_{FB} , but it's still an issue since...

Bias is model dependent

- Examines dozens of generator-level distributions (i.e. alternative models)
- Systematic uncertainties cover all realistic cases
- To invalidate systematic uncertainties: sharp bin-to-bin jumps.
 - 26 generator level bins...
 - s-channel narrow resonances have sharp edges – but already rules out (Tuesday)

A_{FB} Tables

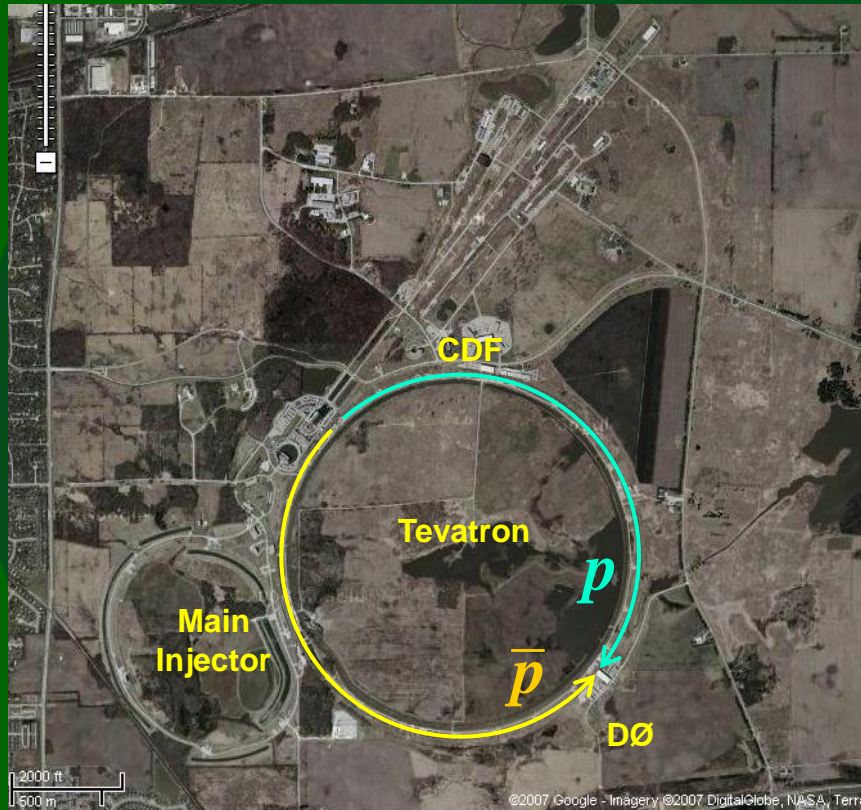


	$l+\geq 4$ jets	$e+\geq 4$ jets	$\mu+\geq 4$ jets	$l+4$ jets	$l+\geq 5$ jets
Raw $N_{\Delta y > 0}$	849	455	394	717	132
Raw $N_{\Delta y < 0}$	732	397	335	597	135
$N_{t\bar{t}}$	1126 ± 39	622 ± 28	502 ± 28	902 ± 36	218 ± 16
N_W	376 ± 39	173 ± 28	219 ± 27	346 ± 36	35 ± 16
N_{MJ}	79 ± 5	56 ± 3	8 ± 2	66 ± 4	13 ± 2
$A_{\text{FB}}(\%)$	9.2 ± 3.7	8.9 ± 5.0	9.1 ± 5.8	12.2 ± 4.3	-3.0 ± 7.9
MC@NLO $A_{\text{FB}}(\%)$	2.4 ± 0.7	2.4 ± 0.7	2.5 ± 0.9	3.9 ± 0.8	-2.9 ± 1.1

	$l+\geq 4$ jets	$e+\geq 4$ jets	$\mu+\geq 4$ jets	$l+4$ jets	$l+\geq 5$ jets
Raw $N_{q \cdot y_l > 0}$	867	485	382	730	137
Raw $N_{q \cdot y_l < 0}$	665	367	298	546	119
$A_{\text{FB}}^l(\%)$	14.2 ± 3.8	16.5 ± 4.9	9.8 ± 5.9	15.9 ± 4.3	7.0 ± 8.0
MC@NLO $A_{\text{FB}}^l(\%)$	0.8 ± 0.6	0.7 ± 0.6	1.0 ± 0.8	2.1 ± 0.6	-3.8 ± 1.2

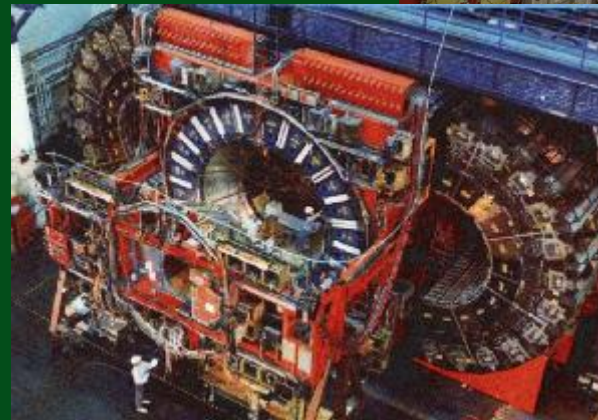
Experimental Apparatus

Fermilab Tevatron Collider



The detectors

Magnet polarities
regularly flipped



The collisions

- $p\bar{p}$
- $E_{c.m.} = 1.96\text{TeV}$

General purpose detectors

Top physics relies on tracking,
calorimetry and muon detectors.

Unfolding A_{FB} is easy

Starting at the end: can check whether the unfolding works well by examining several SM MCs and viable BSM scenarios.

- same wide-bin unfolding works for all viable models
- bias from regularized unfolding (a-priori “smoothing”) can be quantified

BTW: in both cases, narrow resonances would have spoiled everything.

Typical unfolding

How much distortion is acceptable?

Showing a distribution \rightarrow what bin errors?

- correlations are important
- statistical scatter vs. hypothesis testing

What additional information to supply?

Opinions differ.

I refer discussion to:

PHYSTAT 2011 Workshop at CERN, Geneva

17-20 January 2011

<http://indico.cern.ch/event/physstat2011>



Unfolding for A_{FB}

Compare to $\text{stat}(A_{FB})$

Not showing distribution

A_{FB} is a summary

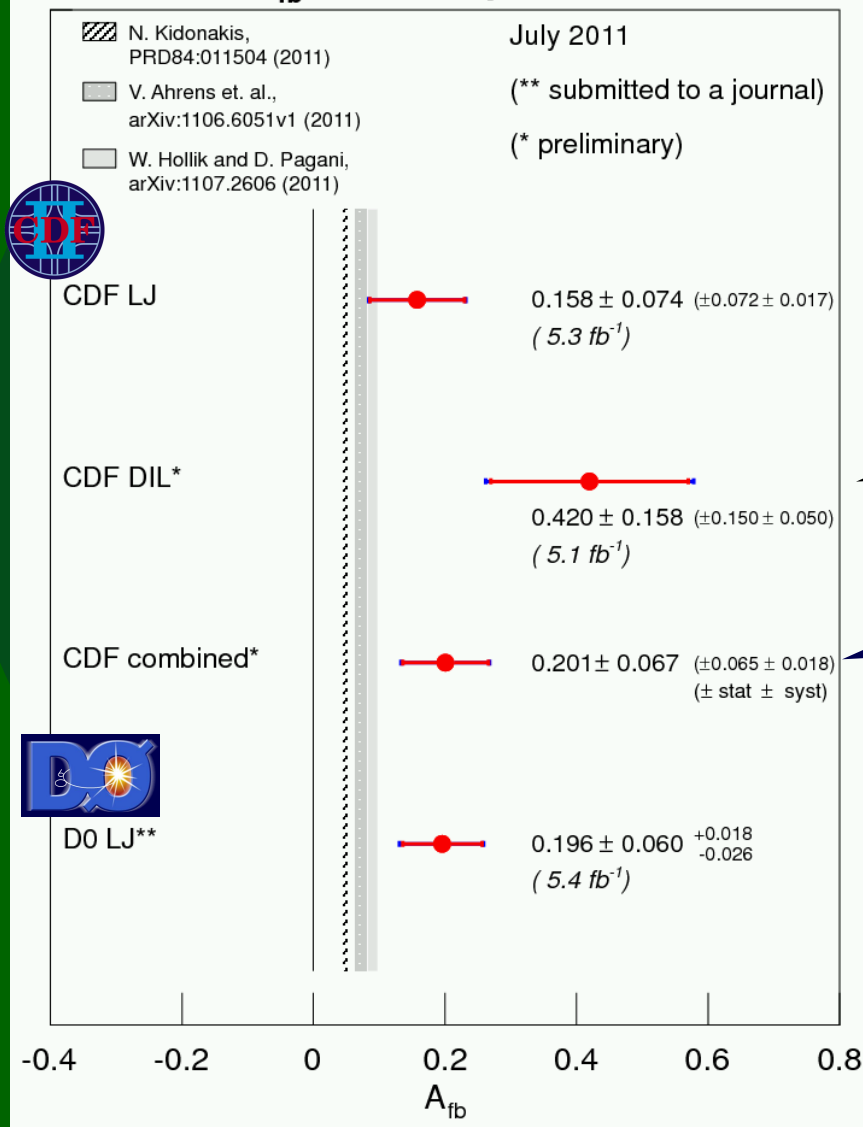
None needed



Details on DØ
unfolding in other
slide

Production-level A_{FB} s

A_{fb} of the Top Quark



Inclusive, Δy -based A_{FB} s

$$A_{FB} = (16 \pm 7.0 (\text{stat}) \pm 2 (\text{syst}))\%$$

Dileptons - In a few slides...

CDF Note #10584

$$A_{FB} = \left(19.6 \pm 6.0 (\text{stat})_{-2.6}^{+1.8} (\text{syst})\right)\%$$

Production-level A_{FB} s



$$A_{\text{FB}} = (16 \pm 7.0 (\text{stat}) \pm 2 (\text{syst}))\%$$



$$A_{\text{FB}} = \left(19.6 \pm 6.0 (\text{stat})_{-2.6}^{+1.8} (\text{syst}) \right)\%$$